

The p4ott P4 Formalization

Anoud Alshnakat
Didrik Lundberg

June 14, 2021

This is a description of the `p4ott` formalization of P4, which includes a syntax and a strictly small-step style semantics. It is based on [the official P4 specification](#) and inspired by Core P4 [1].

`p4ott` is constructed using the `ott` tool. `ott` files can then be exported to \LaTeX commands (used in this document) as well as to the HOL4, Isabelle/HOL and Coq interactive theorem provers (of which only the first is currently supported).

1 Syntax

1.1 Types

x, f, msg	string
b	boolean
n_w	integer
i	natural number
m, n, o	indices

Figure 1: Variables

The variables shown in Figure 1 are standard designations for variables of [P4 base types](#) included in `p4ott`, plus the numerals i and the indices m, n, o which are not part of the P4 syntax, but used on a meta-level throughout this formalization. Depending on the context, strings are denoted with x (variable name), f (function or field name) or msg (error message). The integer n_w is a 64-bit word.

Types are sometimes explicitly referenced in the syntax, e.g. in declaration statements. The notation for this is shown in Figure 2. Subscript t is used to clarify the notation refers to a type, as opposed to a variable of that type. Instances of composite types also have names.

t	$::=$	types
		bool_t
		int_t

Figure 2: Types

1.2 Expressions

`p4ott` includes a subset of the full set of P4 expressions found in [Section 8](#) of the P4 specification, shown in [Figure 3](#).

e	$::=$	expression
	v	constant value
	x	variable name
	$\ominus e$	unary operation
	$e_1 \oplus e_2$	binary operation
	call $f(e_1, \dots, e_n)$	function call
	exec $stmt$	function execution
	(e)	

Figure 3: P4 Expressions

First, an expression can be a Boolean or an integer (collectively referred to as constant values v), or a string. There exist unary and binary arithmetic operations, where the semantics of the individual operations are defined on some subset of the constants¹. The function call is built from the function name f , and a list of arguments (expressions). In-progress execution of the body of a called function, **exec** $stmt$, is not a part of the P4 syntax, but is rather an artifact of our small-step semantics.

¹The concrete syntax of unary and binary operations is found in [Appendix A](#)

1.3 Statements

p4ott includes a subset of the full set of P4 statements found in [Section 11](#) of the P4 specification, shown in [Figure 4](#). They are mostly standard, apart from the following: the in-progress block is an artifact of our small-step semantics. The **verify** statement (here a statement and not an extern function as in [Section 12.7](#) of the P4 specification) can be found uniquely in a parser block. It asserts the expressions e and if it holds, does nothing. If e does not hold, it jumps to a rejecting parser state with error message being the result of evaluating e' . The **transition** statement continues execution at a new parser state p .

<i>stmt</i>	::=	statement
	\emptyset_{stmt}	empty statement
	$x := e$	assignment
	if e then stmt_1 else stmt_2	conditional
	decl $x\ t$	declaration
	$\{\text{stmt}\}$	block
	$[\text{stmt}]$	block in progress
	return e	return
	$\text{stmt}_1; \text{stmt}_2$	sequence
	verify $e\ e'$	verify
	transition p	transition

Figure 4: P4 Statements

1.4 Execution State

The P4 execution state is shown in Figure 5. Note that nothing like this is described in the P4 specification, so it is entirely an artifice of the `p4ott` implementation. In short, the execution state s is a tuple of the state memory σ and the state status t . The state memory σ consists of a tuple (ε, E) , where ε is a stack of scopes γ which hold the values of variables which are currently visible, and E holds variable mappings which belong to previous caller contexts.

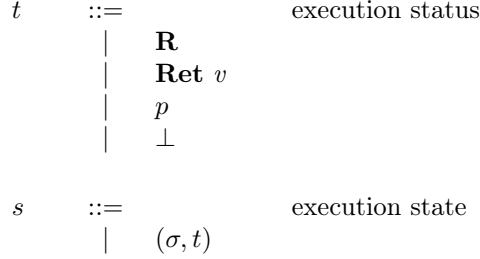


Figure 5: P4 Execution State

More formally, a scope $\gamma : X \hookrightarrow V$ is a partial function from variable names $x \in X$ to constant values $v \in V$. The following operations can be performed on γ :

- $\text{dom}(\gamma)$: Gets the domain of γ : obtains the set of variable names $x \in X$ which are mapped to values in γ .
- $(x \mapsto v) \gamma$: Updates a variable mapping in γ : yields the scope γ' , which is just γ where x instead maps to v . By writing $\forall i \leq n. (x_i \mapsto v_i) \gamma$ we extend this to lists of mappings from variable names to values.

A frame ε is a stack of scopes where the global scope γ_G is located at the bottom; that is, in location $\varepsilon[0]$. The current scope - that which was most recently entered by execution - is stored on the top of ε (note that this indexing is the reverse of what you would expect from a list). Whenever a new block (delineated by $\{\}$) is entered, a new fresh scope γ_\emptyset is pushed onto the frame ε . The following operations can be performed on a frame ε :

- $\gamma :: \varepsilon$: Pushes a scope γ on top of ε .
- $(i \mapsto \gamma) \varepsilon$: Updates the scope located at index i of ε by setting it to γ .

The call stack E is a stack of frames used whenever a function call occurs. When a function call is executed, the frame ε (minus the global scope γ_G) of the caller will be pushed onto E . When the callee function finishes execution and returns, ε will be popped from E and pushed onto a frame containing only γ_G . Note that this means that the same γ_G is kept throughout function calls, and updates to it are passed along accordingly. The following operations can be performed on E :

- $\varepsilon :: E$: Pushes a frame ε onto the call stack E .

The status **R** represents that the program is executing under regular circumstances. **Ret** v is used when the **return** statement returns a constant v at the end of a function call. The status p signifies transition to a new parser state inside the parser - a named state in the case of **Trans** x , or

a final state (p_{fin}) in the case of **Accept** or **Reject**. \perp represents a crash or undefined behaviour, for example caused by some badly-typed part of the program.

In addition to the above, there's also a function map F mapping function names to tuples of their bodies and argument names, a parser map P mapping parser state names to their bodies. These are assumed to be static, and are therefore not part of the execution state.

2 Semantics

2.1 Expressions

$$\begin{array}{c}
\boxed{[e](\sigma) \rightsquigarrow [e'](\sigma')} \quad \text{expression semantics} \\
\\
\begin{array}{c}
i = \max \{j. x \in \text{dom}(\varepsilon[j])\} \\
\gamma = \varepsilon[i] \\
v = \gamma(x) \\
\hline
[x](\varepsilon, E, \mathbf{R}) \rightsquigarrow [v](\varepsilon, E, \mathbf{R}) \quad \text{E_LOOKUP}
\end{array} \\
\\
\begin{array}{c}
(stmt, x_1, \dots, x_n) = F(f) \\
\gamma' = \forall i \leq n. (x_i \mapsto v_i) \gamma_\emptyset \\
\gamma = \varepsilon[0] \\
\varepsilon' = \gamma' :: [\gamma] \\
E' = \text{tl}(\varepsilon) :: E \\
\hline
[\text{call } f(v_1, \dots, v_n)](\varepsilon, E, \mathbf{R}) \rightsquigarrow [\text{exec } stmt](\varepsilon', E', \mathbf{R}) \quad \text{E_FUNC_CALL_NEWFRAME}
\end{array} \\
\\
\begin{array}{c}
[stmt](\sigma, \mathbf{R}) \rightarrow [stmt'](\sigma', \mathbf{R}) \\
\hline
[\text{exec } stmt](\sigma, \mathbf{R}) \rightsquigarrow [\text{exec } stmt'](\sigma', \mathbf{R}) \quad \text{E_FUNC_EXEC}
\end{array} \\
\\
\begin{array}{c}
\hline
[\text{exec } \emptyset_{\text{stmt}}](\sigma, \mathbf{Ret } v) \rightsquigarrow [v](\sigma', \mathbf{R}) \quad \text{E_FUNC_RET}
\end{array}
\end{array}$$

Figure 6: P4 Expression Evaluation Semantics

The semantics of expressions is shown in Figure 6²³.

In the E_LOOKUP rule, the first antecedent states that $i = \max \{j. x \in \text{dom}(\varepsilon[j])\}$, which ensures that the variable name x is evaluated in the uppermost (i.e. most recently entered) scope of ε where it can be found. This agrees with the description in Sections 6.8 and 10.2 of the P4 specification. The value of this variable is then resolved, and checked to be a constant.

The E_FUNC_CALL_NEWFRAME rule is used when all of the function arguments have been reduced to constants. The constants are assigned to their respective argument names in a fresh scope, after which this scope is put on top of the global scope γ_G in order to form the new current

²The semantics for reducing concrete arithmetic operations is standard and covers everything found in Appendix A

³Rules for reducing expressions in all contexts can be found in Appendix B

frame ε' . The old current frame ε (minus γ_G) is then saved on top of the call stack E to be used later when returning from the function call, and the function call statement is reduced to **exec** $stmt$ - in-progress execution of the function body $stmt$ (obtained from the function map F , which holds mappings between function names f and tuples of function bodies and lists of their argument names). Note that this rule also covers the case of a function call with no arguments. The E_FUNC_EXEC rule reduces the function body of in-progress execution with one statement reduction, and the E_FUNC_RET rule reduces finished (empty) in-progress execution with status **Return** e to e , provided e is a constant. This also changes the status to **Running**.

2.2 Statement Execution

The semantics of the statements is shown in Figures 8 and 7⁴.

$[stmt]s \rightarrow [stmt']s'$	statement semantics
---------------------------------	---------------------

$$\begin{array}{c}
i = \text{length}(\varepsilon) \\
\gamma = \varepsilon[i] \\
\varepsilon' = (i \mapsto (x \mapsto ?)\gamma)\varepsilon \\
\hline
[\mathbf{decl } x \ t](\varepsilon, E, \mathbf{R}) \rightarrow [\emptyset_{\text{stmt}}](\varepsilon', E, \mathbf{R}) \quad \text{STMT_DECL}
\end{array}$$

$$\begin{array}{c}
i = \max \{j. x \in \text{dom}(\varepsilon[j])\} \\
\gamma = \varepsilon[i] \\
\varepsilon' = (i \mapsto (x \mapsto v)\gamma)\varepsilon \\
\hline
[x := v](\varepsilon, E, \mathbf{R}) \rightarrow [\emptyset_{\text{stmt}}](\varepsilon', E, \mathbf{R}) \quad \text{STMT_ASS_V}
\end{array}$$

$$\begin{array}{c}
\gamma = \varepsilon[0] \\
\varepsilon' :: E' = E \\
\varepsilon'' = (\varepsilon') + +([\gamma]) \\
\hline
[\mathbf{return } v](\varepsilon, E, \mathbf{R}) \rightarrow [\emptyset_{\text{stmt}}](\varepsilon'', E', \mathbf{Ret } v) \quad \text{STMT_RET}
\end{array}$$

$$\begin{array}{c}
\hline
[\mathbf{if true then } stmt_1 \mathbf{ else } stmt_2](\sigma, \mathbf{R}) \rightarrow [stmt_1](\sigma, \mathbf{R}) \quad \text{STMT_COND2}
\end{array}$$

$$\begin{array}{c}
\hline
[\mathbf{if false then } stmt_1 \mathbf{ else } stmt_2](\sigma, \mathbf{R}) \rightarrow [stmt_2](\sigma, \mathbf{R}) \quad \text{STMT_COND3}
\end{array}$$

Figure 7: P4 Statement Execution Semantics

The STMT_DECL is used to reduce the **decl** statement, which has the effect of declaring variable mappings in the current (topmost) scope. The newly declared variable is given an uninitialized value, denoted by ?.

The STMT_ASS_V rule handles the assignment statement. In general, the variables that the program can assign values to are in the global scope γ_G or the current frame, thus we need to look up mappings in the current frame ε , but never in E . So the antecedent $i = \max\{j. x \in \text{dom}(\varepsilon[j])\}$ obtains the index i of the uppermost (i.e. most recently entered) scope in the current frame ε containing the variable. In the last antecedent, $(x \mapsto v)\gamma$ updates the mapping of the variable name x to the new value (constant v) in the proper scope, that indeed lies in the current frame. The reduction results in the empty statement and an updated current frame.

Once the expression in the **return** statement has been reduced to a constant, the rule STMT_RET can be applied. The global scope γ_G is always stored at the bottom (index zero) in the stack of scopes, i.e. $\varepsilon[0]$. It is fetched and concatenated with the frame of the most recent caller that is stored on top of the call stack E . Thus, this concatenation will yield a new frame ε that has the same shape as the one before the function being called (of course before reaching the **return** statement some variable mappings in the global scope γ_G could have been changed during function

⁴Rules for reducing expressions in all contexts are found in Appendix B

evaluation). The status is also changed to **Return** v which allows for applying `E_FUNC_RET`.

The `STMT_COND2` and `STMT_COND3` rules are the standard ones for conditional statements.

$$\boxed{[stmt]s \rightarrow [stmt']s'} \quad \text{statement semantics}$$

$$\frac{[stmt_1](\sigma, \mathbf{R}) \rightarrow [stmt'_1](\sigma', \mathbf{R})}{[stmt_1; stmt_2](\sigma, \mathbf{R}) \rightarrow [stmt'_1; stmt_2](\sigma', \mathbf{R})} \quad \text{STMT_SEQ1}$$

$$\frac{}{[\emptyset_{\text{stmt}}; stmt](\sigma, \mathbf{R}) \rightarrow [stmt](\sigma, \mathbf{R})} \quad \text{STMT_SEQ2}$$

$$\frac{[stmt_1](\sigma, \mathbf{R}) \rightarrow [stmt'_1](\sigma', \mathbf{Ret } v)}{[stmt_1; stmt_2](\sigma, \mathbf{R}) \rightarrow [\emptyset_{\text{stmt}}](\sigma', \mathbf{Ret } v)} \quad \text{STMT_SEQ3}$$

$$\frac{\varepsilon' = \gamma_{\emptyset} :: \varepsilon}{[\{stmt\}](\varepsilon, E), \mathbf{R}) \rightarrow [[stmt]](\varepsilon', E), \mathbf{R})} \quad \text{STMT_BLOCK_ENTER}$$

$$\frac{[stmt](\sigma, \mathbf{R}) \rightarrow [stmt'](\sigma', \mathbf{R})}{[[stmt]](\sigma, \mathbf{R}) \rightarrow [[stmt']](\sigma', \mathbf{R})} \quad \text{STMT_BLOCK_EXEC}$$

$$\frac{\varepsilon' = \text{tl}(\varepsilon)}{[[\emptyset_{\text{stmt}}]](\varepsilon, E), \mathbf{R}) \rightarrow [\emptyset_{\text{stmt}}](\varepsilon', E), \mathbf{R})} \quad \text{STMT_BLOCK_EXIT}$$

Figure 8: P4 Statement Execution Semantics: Structural Rules

The `STMT_SEQ1` and `STMT_SEQ2` rules are pretty standard. The `STMT_SEQ3` rule is used in the situation when the **return** statement does not occur at the end of the the function body. The next statement to reduce will be empty and the status will be changed to **Return**, which is handled by `STMT_RET`.

The `{ }` brackets indicate a block, while the `[]` brackets indicate a block in progress of being executed. The `STMT_BLOCK_ENTER` rule is used to enter a block, which entails a new empty scope γ_{\emptyset} being pushed onto the current frame ε , and then the `{ }` brackets are switched to the in-progress ones `[]` to signify that the block is currently being executed. The `STMT_BLOCK_EXEC` rule simply describes small-step reduction of the block contents, and the `STMT_BLOCK_EXIT` rule is used in the case where the end of a block is reached, i.e. whenever a block contains only an empty statement: it pops the scope corresponding to the block (the most recent one) from the frame ε .

2.3 Parser

The parser is a part of the P4 language which is generally used to parse packets from bit-string representations to structures of parsed headers, described in [Section 13](#) of the P4 specification. It can be thought of as describing a state machine with three unique states: a *start* state, an **Accept** state and a **Reject** *msg* state. A parser state p (including *start*, but not the abstract final states of **Accept** and **Reject** *msg*) consists of a list of statements to be executed, with a transition statement

at the end which decides the parser state to jump to next.

$$\boxed{[stmt]s \rightarrow [stmt']s'} \quad \text{statement semantics}$$

$$\frac{}{[\mathbf{verify\ true\ (errmsg\ x)}](\sigma, \mathbf{R}) \rightarrow [\emptyset_{\text{stmt}}](\sigma', \mathbf{R})} \quad \text{STMT_VERIFY_3}$$

$$\frac{}{[\mathbf{verify\ false\ (errmsg\ x)}](\sigma, \mathbf{R}) \rightarrow [\emptyset_{\text{stmt}}](\sigma', \mathbf{Reject\ x})} \quad \text{STMT_VERIFY_4}$$

$$\frac{}{[\mathbf{transition\ p}](\sigma, \mathbf{R}) \rightarrow [\emptyset_{\text{stmt}}](\sigma, p)} \quad \text{STMT_TRANSITION}$$

Figure 9: P4 Parser-Specific Statement Execution Semantics

The parser-specific statement semantics is shown in Figure 9. The STMT_VERIFY_3 and STMT_VERIFY_4 rules describe the semantics of **verify**, the expressions having been reduced to values. If the condition holds, the reduction is to the empty statement (i.e. nothing happens and execution continues). If the condition does not hold, reduction is also to the empty statement, but state status is set to **Reject** x . The STMT_TRANSITION rule describes reduction of the **transition** statement, whose only effect on the state is to set status to p (the PARS_STATE or PARS_T_FIN rules can then be used next)

$$\boxed{[stmt]s \longrightarrow [stmt']s'} \quad \text{parser semantics}$$

$$\frac{[stmt](\sigma, \mathbf{R}) \rightarrow [stmt'](\sigma', \mathbf{R})}{[stmt](\sigma, \mathbf{R}) \longrightarrow [stmt'](\sigma', \mathbf{R})} \quad \text{PARS_STMT}$$

$$\frac{[stmt](\sigma, \mathbf{R}) \rightarrow [stmt'](\sigma', \mathbf{Trans\ x}) \quad stmt'' = P(x)}{[stmt](\sigma, \mathbf{R}) \longrightarrow [stmt''](\sigma', \mathbf{R})} \quad \text{PARS_STATE}$$

$$\boxed{[stmt]s \longrightarrow s'} \quad \text{parser semantics, final step}$$

$$\frac{[stmt](\sigma, \mathbf{R}) \rightarrow [stmt'](\sigma, p_{\text{fin}})}{[stmt](\sigma, \mathbf{R}) \longrightarrow (\sigma, p_{\text{fin}})} \quad \text{PARS_T_FIN}$$

$$\frac{[stmt](\sigma, \mathbf{R}) \rightarrow [\emptyset_{\text{stmt}}](\sigma', \mathbf{R}) \quad x = \text{ParserStateEnd}}{[stmt](\sigma, \mathbf{R}) \longrightarrow (\sigma', \mathbf{Reject\ x})} \quad \text{PARS_T_EMPTY}$$

Figure 10: Parser Execution Semantics

The parser state machine semantics is shown in Figure 10. Note the separate judgment form for the final step of the parser, which goes to a state with status **Accept** or **Reject** (representing the abstract accepting and rejecting states).

The PARS_STMT rule performs a single small-step reduction of the current statement (the body of the current parser state), while the PARS_STATE rule governs transition to the next parser state: if the current statement $stmt$ is reduced to $stmt'$ with the status being **Trans** x , the next statement

is the body of the parser state with name x , obtained from the map P from parser state names to parser bodies.

The `PARS_T_FIN` rule says that when reduction using the statement semantics of the current statement results in a status with a final parser state p_{fin} , this is also set as the status in the parser semantics. The `PARS_T_EMPTY` rule covers the special case when the statement semantics runs out of statements in a parser state, in which case the status is set to **Reject** `ParserStateEnd`.

2.4 Control Blocks

The control block is a part of the P4 language which is generally used to decide which actions to take (typically forwarding) based on the metadata (headers) which was extracted by the parser, as described in [Section 12](#) of the P4 specification. The two main components of a control block is the match-action table and the actions themselves. Note that part of the functionality is separated into the control plane, which is interfaced with here using the `ctrl(table_name, v, m_kind)` function that takes a table name, constant value and matching kind and obtains an action name f and a list of function arguments v_1, \dots, v_n . Actions can be thought of roughly as functions with no return values. The action can be called implicitly from the match-action process (i.e. in the table application), or explicitly from another action or a control block, as described in [Section 13.1.1](#) of the P4 specification.

The `APPLY_TABLE_E` rule performs small-step evaluation of the header expression used for the matching.

The `APPLY_TABLE_V` looks up the table name in the table name map, then uses the result together with the header to be looked up to obtain an action (together with action arguments) from the control plane.

$$\frac{[e](\sigma) \rightsquigarrow [e'](\sigma')}{[\text{apply } table_name \ e](\sigma) \rightarrow [\text{apply } table_name \ e'](\sigma')} \text{ APPLY_TABLE_E}$$

$$\frac{\begin{array}{l} t_map(table_name) = (e', m_kind) \\ ctrl(table_name, v, m_kind) = (f, v_1, \dots, v_n) \end{array}}{[\text{apply } table_name \ v](\sigma) \rightarrow [\text{call } f(v_1, \dots, v_n)](\sigma')} \text{ APPLY_TABLE_V}$$

Figure 11: Match-Action Semantics

References

- [1] Ryan Doenges et al. “Petr4: formal foundations for p4 data planes”. In: *Proceedings of the ACM on Programming Languages* 5.POPL (2021), pp. 1–32.

A Concrete Syntax of Operations

\ominus	$::=$	
		!
		\neg
		$-$
		$+$
		boolean negation
		bitwise complement
		signed negation
		unary plus

Figure 12: P4 Unary Operations

The unary expressions included are shown in Figure 12. These include all of the unary operations in P4. Boolean negation is only defined on Booleans, the other operations have their standard meanings (note that [unary plus is a no-op](#)).

\oplus	$::=$		
		\times	multiplication
		$/$	division
		mod	modulo
		$+$	addition
		$-$	subtraction
		\ll	left-shift
		\gg	right-shift
		\leq	less or equal
		\geq	greater or equal
		$<$	less
		$>$	greater
		\neq	not equal
		$=$	equal
		$\&$	bitwise and
		$\underline{\vee}$	bitwise xor
		$ $	bitwise or
		\wedge	binary and
		\vee	binary or

Figure 13: P4 Binary Operations

The binary expressions included are shown in Figure 12. These include all of the binary operations in P4.

B Semantics of Expression Reduction

This appendix describes semantics for reducing expressions in certain contexts. The expression semantics are shown in Figure 14. The statement semantics are shown in Figure 15.

The `E_FUNC_CALL_ARGS` rule reduces the leftmost function argument which has yet to be reduced to a constant with one expression evaluation step. The first two antecedents divide the list of arguments into two sub-lists, where the prefix must contain all constants. The head of the suffix is then reduced with one step, after which the corresponding index in the original list of arguments is update with the resulting expression.

8.1 of the P4 specification states that expressions are evaluated left-to-right. Accordingly, the rules for binary operations - `E_BINOP1` and `E_BINOP2` - are split up so that reduction of the second operand requires that the first operand has been completely reduced to a constant. This is trivial for unary operations (`E_UNOP`).

$$\boxed{[e](\sigma) \rightsquigarrow [e'](\sigma')} \quad \text{expression semantics}$$

$$\begin{array}{l}
e_list' + e_list'' = e_1, \dots, e_n \\
\text{is_consts } e_list' \\
e = \text{hd } e_list'' \\
[e](\sigma, \mathbf{R}) \rightsquigarrow [e'](\sigma', \mathbf{R}) \\
i = \text{len } e_list' \\
e'_1, \dots, e'_m = (i \mapsto e')(e_1, \dots, e_n) \\
\hline
[\text{call } f(e_1, \dots, e_n)](\sigma, \mathbf{R}) \rightsquigarrow [\text{call } f(e'_1, \dots, e'_m)](\sigma, \mathbf{R}) \quad \text{E_FUNC_CALL_ARGS}
\end{array}$$

$$\frac{[e](\sigma, \mathbf{R}) \rightsquigarrow [e'](\sigma', \mathbf{R})}{[\ominus e](\sigma, \mathbf{R}) \rightsquigarrow [\ominus e'](\sigma', \mathbf{R})} \quad \text{E_UNOP_ARG}$$

$$\frac{[e](\sigma, \mathbf{R}) \rightsquigarrow [e'](\sigma', \mathbf{R})}{[e \oplus e'](\sigma, \mathbf{R}) \rightsquigarrow [e' \oplus e'](\sigma', \mathbf{R})} \quad \text{E_BINOP_ARG1}$$

$$\frac{[e'](\sigma, \mathbf{R}) \rightsquigarrow [e'](\sigma', \mathbf{R})}{[v \oplus e'](\sigma, \mathbf{R}) \rightsquigarrow [e \oplus e'](\sigma', \mathbf{R})} \quad \text{E_BINOP_ARG2}$$

Figure 14: P4 Expression Evaluation Semantics

$$\boxed{[stmt]s \rightarrow [stmt']s'} \quad \text{statement semantics}$$

$$\frac{[e](\sigma, \mathbf{R}) \rightsquigarrow [e'](\sigma', \mathbf{R})}{[\text{return } e](\sigma, \mathbf{R}) \rightarrow [\text{return } e'](\sigma', \mathbf{R})} \quad \text{STMT_RET_E}$$

$$\frac{[e](\sigma, \mathbf{R}) \rightsquigarrow [e'](\sigma', \mathbf{R})}{[x := e](\sigma, \mathbf{R}) \rightarrow [x := e'](\sigma', \mathbf{R})} \quad \text{STMT_ASS_E}$$

$$\frac{[e](\sigma, \mathbf{R}) \rightsquigarrow [e'](\sigma', \mathbf{R})}{[\text{if } e \text{ then } stmt_1 \text{ else } stmt_2](\sigma, \mathbf{R}) \rightarrow [\text{if } e' \text{ then } stmt_1 \text{ else } stmt_2](\sigma', \mathbf{R})} \quad \text{STMT_COND_E}$$

$$\frac{[e](\sigma, \mathbf{R}) \rightsquigarrow [e'](\sigma', \mathbf{R})}{[\text{verify } e \ e'](\sigma, \mathbf{R}) \rightarrow [\text{verify } e' \ e'](\sigma', \mathbf{R})} \quad \text{STMT_VERIFY_E1}$$

$$\frac{[e](\sigma, \mathbf{R}) \rightsquigarrow [e'](\sigma', \mathbf{R})}{[\text{verify } b \ e](\sigma, \mathbf{R}) \rightarrow [\text{verify } b \ e'](\sigma', \mathbf{R})} \quad \text{STMT_VERIFY_E2}$$

Figure 15: P4 Statement Execution Semantics