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This document uses the slide template from the "Interactive Theorem Proving Course" by Thomas Tuerk (https://www.thomas-tuerk.de): https://github.com/thtuerk/ITP-course

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Interactive Theorem Proving and Program Verification Lecture 11

Pablo Buiras and Karl Palmskog



Academic Year 2019/20, Period 3-4

Based on slides by Thomas Tuerk



Part XX

HOL4 and ITPs in Research: an Overview



HOL4 and ITPs in Perspective



- this course only looks at the basics of ITP and HOL4
- thousands of researchers and engineers around the world use ITPs, and use is growing (mostly in Europe)
- ITPs can serve as platforms that connect programs, hardware, mathematical definitions, mathematical results
- many CS conferences and journals encourage use of ITPs; may become mandatory in the future

Proof Engineering



- developing large trustworthy systems using ITPs requires:
 - knowledge of strengths and limitations of selected ITP
 - good choice of underlying mathematical theories
 - careful selection of libraries and other tools
 - effective encodings of specifications and implementation
 - adequate development infrastructure and processes
 - **.** . . .
- the emerging field that considers these and related concerns holistically is called proof engineering
- see recent survey of proof engineering for program verification: https://arxiv.org/abs/2003.06458
- many concerns and ideas from software engineering apply—but generally unknown to what extent
- ITP languages tend to be nicely behaved and designed in comparison to many traditional programming languages

Strengths and Limitations of HOL4



- + based on classical higher order logic, a sweet spot between expressivity and ease of automation
- + trustworthy thanks to LCF approach
- + simple enough to understand easily
- + very easy to write custom proof tools, i. e. , own automation
- + reasonably fast and efficient
- + good automation
- + comprehensive bundled theories
- can't have types depend on term, e.g., R^n
- no organizational mechanisms such as type classes or modules
- no user interface (besides SML toplevel)
- no special proof language
- no IDE, very modest editor support
- modestly-sized ecosystem, hard to google questions



Strengths and Limitations of Coq



- + based on a constructive higher-order type theory
- logic is highly expressive (dependent types, universes, ...)
- trustworthy thanks to small type checker
- allows verified computation inside proofs (reflection)
- functions are computable by default
- + large ecosystem, relatively easy to google questions
- + supported by many graphical interfaces and IDEs
- tactic execution and proof checking can be slow (explicit proofs)
- low level of built-in automation (need many plugins)
- many separately developed incompatible "standard" libraries
- difficult to write custom proof tools besides using tactic language

See a more detailed comparison of Cog and HOL:

```
https://coq.discourse.group/t/
why-doesnt-coq-have-a-theorem-type-like-hol-light/532
```



Other ITPs



- HOL Light like HOL4, but implemented in OCaml
- Isabelle/HOL HOL logic with comprehensive automation, math proof language, advanced IDE, Archive of Formal Proofs
- Lean Coq-like type theory with classical logic and built-in automation
- Agda constructive Coq-like type theory
- ACL2 first-order logic with strong automation (idealized version formalised in HOL4, Milawa)
- NuPRL & RedPRL constructive extensional type theory

Definitions and theorem statements can often be directly transferred between systems, but proofs must typically be manually ported.



Learning and Reusing Libraries and Projects



- due to cost of using ITPs, important to avoid reinventing the wheel
- many CS applications already have several formalisations for a given ITP, but can still be inconvenient to "fit into" existing formalisation
- proper reuse of libraries may require careful study and experimentation
- there is probably no substitute for looking at lots of ITP code
- \bullet compare learning APIs in traditional programming languages such as Java and C++

HOL4 Theories I



Besides the basic libraries and theories that are required and loaded by hol, there are many more developments in HOL4's source directory.

- src/sort sorting lists
- src/string strings
- src/TeX exporting LaTeX code
- src/res_quan restricted quantifiers
- src/quotient quotient type package
- src/finite_map finite map theory
- src/bag bags a. k. a. multisets
- src/n-bit machine words

HOL4 Theories II



- src/ring reasoning about rings
- src/integer integers
- src/llists lazy lists
- src/path finite and infinite paths through a transition system
- src/patricia efficient finite map implementations using trees
- src/emit emitting SML and OCaml code
- src/search traversal of graphs that may contain cycles
- src/relation relations, including transition system bisimulations

HOL4 Theories III



- src/rational rational numbers
- src/real real numbers
- src/complex comples numbers
- src/HolQbf quantified boolean formulas
- src/HolSmt support for external SMT solvers
- src/float IEEE floating point numbers
- src/floating-point new version of IEEE floating point numbers
- src/probability probability theory
- src/temporal shallow embedding of temporal logic
- ...

HOL4 Selected Examples I



The directory examples hosts many theories and libraries as well. There is not always a clear distinction between an example and a development in src. However, in general examples are more specialised and often larger. They are not required to follow HOL4's coding style as much as developments in src.

- examples/balanced_bst finite maps via balanced trees
- examples/unification (nominal) unification
- examples/Crypto various block ciphers
- examples/elliptic elliptic curve cryptography
- examples/formal-languages regular and context free formal languages
- examples/computability basic computability theory



HOL4 Selected Examples II



- examples/set-theory axiomatic formalisation of set theory
- examples/lambda lambda calculus
- examples/ac12 connection to ACL2 prover
- examples/theorem-prover soundness proof of Milawa prover
- examples/PSL formalisation of PSL
- examples/HolBdd Binary Decision Diagrams
- examples/HolCheck basic model checker
- examples/temporal_deep deep embedding of temporal logics and automata

HOL4 Selected Examples III



- examples/pgcl formalisation of pGCL (the Probabilistic Guarded Command Language)
- examples/dev some hardware compilation
- examples/STE symbolic trajectory evalutation
- examples/separationLogic formalisation of separation logic
- examples/ARM formalisation of ARM architecture
- examples/13-machine-code I3 language
- examples/machine-code compilers and decompilers to machine-code
- . . .

Some Ongoing Research Projects Related to HOL4



- Rigorous Engineering of Mainstream Systems (REMS)
 - https://www.cl.cam.ac.uk/~pes20/rems/
 - ▶ NetSem, validated formalisation of the TCP/IP stack
 - ► SAIL language for defining Instruction-Set Architecture (ISA) models
- CakeML, including Candle, a verified HOL interactive theorem prover
- Formalisation of Network Interface Controllers
- HolBA and SCAM-V

HolBA



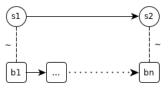
- Binary analysis platform in HOL4
- Toolkit to analyse and reason about low-level (assembly) code
- Relies on formal semantics of ISAs (ARM/Risc-V/etc)
- Binary Intermediate Representation (BIR)
 - Language designed to automate analysis
 - Formal semantics in HOL4
 - Similar to LLVM IR
- Program not in memory / Assertions
- Verified theories and proof producing analyses
 - Transpilation into BIR
 - Weakest precondition
 - Symbolic execution

HolBA Lifter (transpiler)



```
0: pop R1
4: push R1
\Downarrow
[0 \{ R1 := MEM[SP];
      SP := SP-4;
      PC := PC+4;
      JMP 4}]
[4 { MEM := MEM with [SP<-R1];
      SP := SP+4;
      PC := PC+4;
      JMP 8}]
```

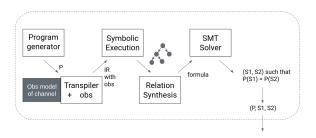
Simulation theorem:



SCAM-V: Side-channel abstract model validator



- Modern architectures are too complex to directly analyse side-channels
- Abstract models based on system-state observations
- Assumption: States with equivalent observations in the model are indistinguishable to the attacker on real hardware
- SCAM-V validates this by generating and testing states that are supposed to be indistinguishable.



Verification vs validation



- Verification: formally proving that the program satisfies its formal specification
- Validation: testing that the program satisfies its formal specification
- Validation cannot prove the absence of errors
- In most cases, verification is preferred, but it is much more costly
- Sometimes it's not possible, e.g. soundness of side-channel models with respect to microarchitecture
- Final decision sometimes boils down to risk assessment and resource allocation
- It is possible to mix and match depending on requirements, i.e. critical modules can be verified, while less critical ones can be validated

Some Ongoing Research in Proof Engineering



- improvements and extensions to portability tools such as Ott and Lem
- improvement and verification of incremental proof checking https://setoid.com/chip
- proof repair and proof transfer https://proofengineering.org
- mutation analysis of ITP theories to find weak specifications http://cozy.ece.utexas.edu/mcoq/
- learning and suggesting naming and formatting in ITP code

Trends in ITP for Research



- type theory ITPs heavily used programming languages research (POPL, PLDI)
- HOL-based ITPs often used in hardware-related research (FMCAD) and automated reasoning (IJCAR)
- lots of work on formalising mathematics, but ongoing debate which foundation and ITP should be used (CPP, ITP)
- ITP interface research may see a resurgence as ITPs go more mainstream
- bias towards "complete" formalisations for getting research published

Trends in Industrial Application of ITPs



- ITP verified cryptographic code included in Google Chrome
- seL4 and CompCert starting to get used in embedded systems
- Dune build system includes verified cycle checking code
- hardware designers and manufacturers look to apply formal verification (again?)

Challenges in Research Using ITPs



- working in a research group with knowledge of ITPs helps a lot, but documentation and resources for individual work are improving
- ITP experts may have unrealistically high expectations when reviewing applied work
- researchers without ITP expertise may underestimate effort and difference in trustworthiness
- personal experience: ITP community much friendlier to engineering research than the software engineering community is to ITP-based research