

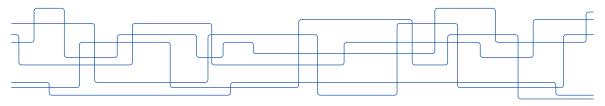


# Distributed Charging Coordination of Electric Trucks with Limited Charging Resources

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► Insufficient battery capacity – Range anxiety



Limited driving range (200-600 km)

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- Limited charging resources Long queuing time



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Limited number of charging ports

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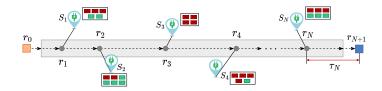
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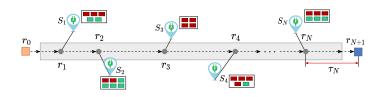
**Problem:** How to design reliable and efficient **charging strategy** for electric trucks so that trucks can complete delivery task while minimizing charging costs, subject to limited charging resources?

## Charging Problem: Route Model and Decision Variables



T. Bai, Y. Li, K. H. Johansson, and J. Mårtensson, "Rollout-based charging strategy for electric trucks with hours-of-service regulations". *IEEE Control Systems Letters*, 7, 2167-2172, 2023.

## Charging Problem: Route Model and Decision Variables



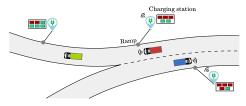
The decision variables are:

$$b_k \in \{0,1\}, t_k \in \Re_+, k=1,\ldots,N$$

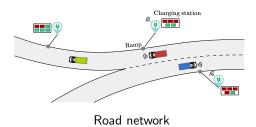
 $b_k$ : whether to charge at the station  $S_k$ 

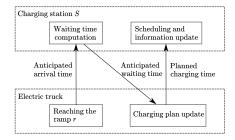
 $t_k$ : the planned charging time of the truck at  $S_k$  if  $b_k = 1$ 

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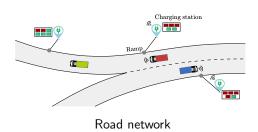


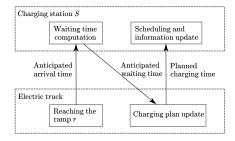
Road network





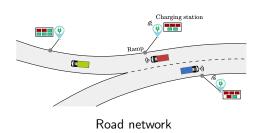
Station-truck coordination framework

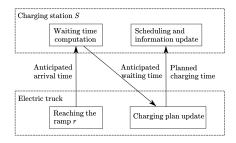




Station-truck coordination framework

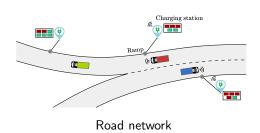
- Our framework highlights the following properties:
  - It is fully distributed and applies to cases where all parties do not belong to the same fleet

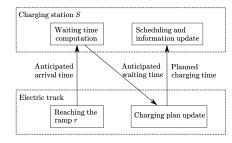




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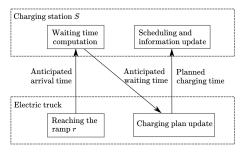




Station-truck coordination framework

- Our framework highlights the following properties:
  - It is fully distributed and applies to cases where all parties do not belong to the same fleet
  - It is light-weight, involving only simple information exchange between trucks and stations
  - It is adaptive, enabling changes in charging plans when needed via real-time computation

## Waiting Time Computation

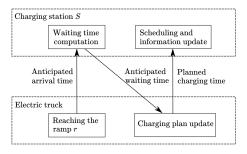


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$$\tilde{w} = \max\left\{\min_{c \in C}(a_c - \tilde{t}_a), 0\right\}$$

 $a_c$ : the earliest time from when the port  $c \in C$  becomes available onward  $\tilde{t}_a$ : the anticipated arrival time of a truck

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 $\blacktriangleright$  The station assigns the port c\* to the truck and update its information via

$$c^* \in \arg\min_{c \in C} a_c, \qquad a_{c*} = \tilde{t}_a + \tilde{w} + t$$

## Computing Charging Plan: Delivery Deadline

▶ Reaching the destination before the deadline is described by a soft constraint:

$$\Delta T_{k} = b_{k}(2d_{k} + t_{k} + \tilde{w}_{k}) + \sum_{\ell=k+1}^{N} b_{\ell}(2d_{\ell} + t_{\ell} + \hat{w}_{\ell}) + \sum_{\ell=k}^{N} \tau_{k} - T_{k},$$

 $\tilde{w}_k$ : the anticipated waiting time received from  $S_k$  when arriving  $r_k$ 

 $\hat{w}_{\ell}$ : the certain waiting time assumed at the subsequent station  $S_{\ell}$ ,  $\ell = k+1, \ldots, N$ 

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 $\rightarrow \Delta T_k > 0$ : indicates the **violation** of the delivery deadline

## Computing Charging Plan: Optimization Problem

▶ The charging problem upon reaching  $r_k$  is cast as:

$$\min_{\{(b_\ell,t_\ell)\}_{\ell=k}^N} \kappa \left( b_k \left( 2d_k + t_k + \tilde{w}_k \right) + \sum_{\ell=k+1}^N b_\ell \left( 2d_\ell + t_\ell + \hat{w}_\ell \right) \right) + \sum_{\ell=k}^N \epsilon_\ell b_\ell t_\ell + \max \left\{ \rho \Delta T_k, 0 \right\}$$

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s.t. 
$$b_k \in \{0,1\}, t_k \in \Re_+, k=1,\ldots,N,$$
 (1)

$$e_1 = e_{\mathsf{ini}} - \bar{P}\tau_0, \tag{2}$$

$$e_{k+1} = e_k + b_k \Delta e_k - \bar{P}(2b_k d_k + \tau_k), \quad k = 1, ..., N,$$
 (3)

$$e_k \ge e_s + \bar{P}d_k, \quad k=1,\ldots,N,$$
 (4)

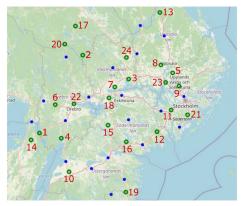
$$e_{N+1} \ge e_s, \tag{5}$$

$$\Delta e_k = t_k \min \{ P_k, P_{\max} \}, \quad k = 1, \dots, N, \tag{6}$$

$$0 \le \Delta e_k \le e_f - (e_k - \bar{P}d_k), \quad k = 1, \dots, N, \tag{7}$$

$$\Delta T_k = b_k (2d_k + t_k + \tilde{w}_k) + \sum_{\ell=k+1}^{N} b_\ell (2d_\ell + t_\ell + \hat{w}_\ell) + \sum_{\ell=k}^{N} \tau_k - T_k$$
 (8)

## Simulation – Parameter settings

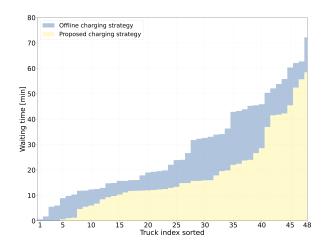


The road network and charging stations

- 150 trucks, 24 charging stations, 3 charging ports per station
- Start times are randomly determined between 08:00-10:00 a.m.
- Random initial battery with feasibility guarantee
- Routes are pre-planned using data from OpenStreetMap
- Parameters related to trucks are set using the data latest published by Scania

# Simulation – Evaluation Results (1)

► Real waiting times of individual trucks



Total waiting time:

- Offline strategy: 22.67 hours

- Proposed strategy: 14.30 hours

# Simulation – Evaluation Results (2)

► Charging and waiting times at each station



- Alleviate charging congestion by reducing average waiting time from 10.9 to 6.9 minutes

## Simulation – Evaluation Results (2)

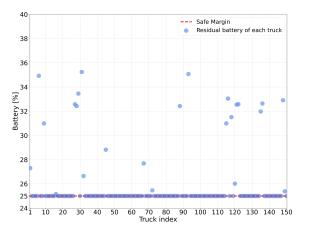
Charging and waiting times at each station



- Alleviate charging congestion by reducing average waiting time from 10.9 to 6.9 minutes
- Our method may result in longer waiting times for some trucks due to characteristic diversity

# Simulation – Evaluation Results (3)

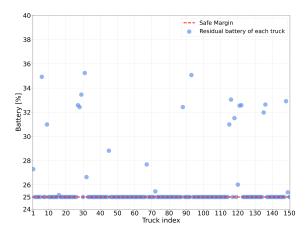
► Trucks' residual batteries upon reaching destinations



- Most trucks complete their delivery missions while consuming all the usable batteries

## Simulation – Evaluation Results (3)

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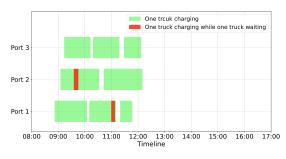
- Most trucks complete their delivery missions while consuming all the usable batteries
- Note: our method can be easily modified to meet higher battery requirements at destinations

# Simulation – Evaluation Results (4)

► Charging ports assignment at two stations ("first-arrive, first-served" rule)



Charging time scheduling at Station 12



Charging time scheduling at Station 22

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  - It requires simple information exchange
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  - It enables re-planning by trucks
- ▶ Simulation studies show our approach outperforms the offline strategy by large margins.
- ► Future research will focus on developing data-driven schemes for waiting time estimations at future stations, as well as single-carrier charging planning.

