# CS294 DeepRL Notes

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- reward function r(s, a) tells which actions/states are better
- Markov chain
  - $-M = \{S, T\}$ , where S = state space, T = transition operator (conditional probabilities to transition between states)
  - $-\mu_{t+1} = T\mu_t$ , where  $\mu_t$  is vector where  $\mu_{t,i} = p(s_t = i)$ ,  $T_{i,j} = p(s_{t+1} = i|s_t = j)$ : transition from one vector to next
- Markov Decision Process
  - $-M = \{S, A, T, r\}$ , adding action space and reward function
  - similar formulas,  $\mu_{t,j}=p(s_t=j), \xi_{t,k}=p(a_t=k), T_{i,j,k}=p(s_{t+1}=i|s_t=j,a_t=k)$ , so  $\mu_{t,i}=\sum_{j,k}T_{i,j,k}\mu_{t,j}\xi_{t,k}$  (non-vectorized)
  - partially observed MDP:  $M = \{S, A, T, O, \epsilon, r\}$  added O = observation space,  $\epsilon =$  emission probability  $(p(o_t|s_t))$
- Goal of RL
  - trying to learn  $\theta$  in  $\pi_{\theta}(a|s)$ , which can be represented as a neural network
  - can write probability of getting a SEQUENCE of states/actions:  $p_{\theta}(s_1, a_1, ..., s_T, a_T) = p(s_1) \Pi_{t=1}^T \pi_{\theta}(a_t | s_t) p(s_{t+1} | s_t, a_t)$  (getting the correct action \* getting the correct next state)
    - \* the terms in the product follow Markov chain given a "state" of (s,a)
    - \*  $p((s_{t+1}, a_{t+1})|(s_t, a_t)) = p(s_{t+1}|s_t, a_t)\pi_{\theta}(s_t, a_t))$  follows Markov's rule
  - GOAL:  $\theta^* = argmax_{\theta} E_{r \sim p_{\theta}(r)} [\sum_t r(s_t, a_t)]$  (the arguments that get the highest expectation of rewards given the possible sequences of states/actions)
    - \* equivalent:  $\theta^* = argmax_{\theta}1/T \sum_{t=1}^{T} E_{(s_t, a_t) \sim p_{\theta}(s_t, a_t)}[r(s_t, a_t)]$ , useful to find stationary distribution
    - \* Conditional expectations

- $\sum_{t=1}^{T} E_{(s_t,a_t) \sim p_{\theta}(s_t,a_t)}[r(s_t,a_t)] = E_{s_1 \sim p(s_1)}[E_{a_1 \sim \pi(a_1|s_1)}[r(s_1,a_1) + E_{s_2 \sim p(s_2|s_1,a_1)}[E_{a_2 \sim \pi(a_2|s_2)}[r(s_2,a_2) + \dots]|s_1,a_1]|s_1]]$
- · Define  $Q(s_1, a_1)$  s.t. this evaluates to  $E_{s_1 \sim p(s_1)}[E_{a_1 \sim \pi(a_1|s_1)}[Q(s_1, a_1)|s_1]]$ , we can easily modify the policy  $\pi_{\theta}(a_1|s_1)$  if we know  $Q(s_1, a_1)$
- \* Q-function
  - ·  $Q^{\pi}(s_t, a_t) = \sum_{t'=t}^{T} E_{\pi_{\theta}}[r(s_{t'}, a_{t'})|s_t, a_t]$ : total reward from taking  $a_t$  at  $s_t$  if you follow the policy
- $* \ \ Value-function$ 
  - ·  $V^{\pi}(s_t) = \sum_{t'=t}^{T} E_{\pi_{\theta}}[r(s_{t'}, a_{t'})|s_t]$ : total reward from  $s_t$  if you follow the policy
  - $\cdot V^{\pi}(s_t) = E_{a_t \sim \pi_{\theta}(a_t|s_t)[Q^{\pi}(s_t, a_t)]}$
  - · RL Objective can be written as  $E_{s_1 \sim p(s_1)}[V^{\pi}(s_1)]$
- \* Using Q and Value-functions
  - · can improve  $\pi$  if we know  $\pi$  and Q(s,a) by setting  $\pi'(a|s)=1$  if  $a=argmax_aQ^{\pi}(s,a)$
  - · can compute gradients to improve prob of getting a better than average a: if  $Q^{\pi}(s,a) > V^{\pi}(s)$ , modify  $\pi(a|s)$  to increase probability of a
- anatomy of RL algorithm
  - \* run policy to generate samples
    - · bottleneck is get real-time samples if not simulator
  - \* fit model/estimate returns
    - · bottleneck is if model-based, getting a function to predict next state is hard
  - \* use to improve policy

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- More general analysis, assuming states in same distribution as training set  $p_{train}(s)$  follow  $\pi_{\theta}(a \neq \pi^*(s)|s) \leq \epsilon$ 
  - when  $p_{train}(s) \neq p_{\theta}(s)$ 
    - \*  $p_{\theta}(s) = (1 \epsilon)^t p_{train}(s_t) + (1 (1 \epsilon)^t) p_{mistake}(s_t)$
    - \* or,  $|p_{\theta}(s_t) p_{train}(s_t)| = (1 (1 \epsilon)^t)|p_{mistake}(s_t) p_{train}(s_t)| \le 2 * (1 (1 \epsilon)^t)$  (summing over all states, which is why it's 2)
    - \* since  $(1 \epsilon)^t \le 1 \epsilon t$  (by algebraic trick),  $|p_{\theta}(s_t) p_{train}(s_t)| \le 2\epsilon t$
    - \* therefore,  $\sum_t E_{p_{\theta}(s_t)}[c_t] = \sum_t \sum_{s_t} p_{\theta}(s_t) c_t(s_t) \leq \sum_t \sum_{s_t} p_{train}(s_t) c_t(s_t) + |p_{\theta}(s_t) p_{\theta}(s_t)| c_{max} \leq \sum_t \epsilon + 2\epsilon t \leq \epsilon T + 2\epsilon T^2$ , or  $O(\epsilon T^2)$

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- $\pi_{\theta}(a_t|o_t) = \pi_{\theta}(a_t|s_t)$  when world is fully observed, but not realistic
- $s_{t+1}$  independent of  $s_t, a_t$  (previous states won't help determining future states), but the same cannot be said for  $o_{t+1}$  and its relationship to  $o_t$ 
  - this makes sense because of what state means (whole world, including vectors for speed, etc.)

### • Imitation Learning

- interesting example with three different examples, approximates policy better since has samples outside of norm to correct for drift
- training perfect policy is hard, so maybe change data to closely match  $p_{\pi_{\theta}}$ : DAgger (Dataset Aggregation)
  - \* repeatedly add data by running policy but asking human to label with correct action, then retrain using this new policy to explore the entire space
  - \* assumption that humans can pick good actions
- Why fail fit the expert?
  - \* Non-Markovian behavior (e.g. humans look at previous previous states instead of just previous)
    - · can train on RNN or something using whole history
  - \* Multimodal behavior (e.g. humans are very complicated, can behave differently for same situation due to whatever constants)
    - $\cdot$  can output mixture of gaussians
    - · can use latent variable models
    - · can use autoregressive discretization

#### • Rewards/Costs

- -r(s,a) = reward function (negative cost function)
- For imitation learning,  $r(s, a) = \log p(a = \pi^*(s)|s)$  is good candidate, where asterisk is the master policy
  - \* other is c(s, a) = 0 if  $a = \pi^*(s)$ , 1 otherwise
  - \* analysis
    - · assume  $\pi_{\theta}(a \neq \pi^*(s)|s) \leq \epsilon$  for all  $s \in D_{train}$
    - ·  $E[\sum_t c(s_t, a_t)] \le \epsilon T + (1 \epsilon)(\epsilon(T 1) + ...)$ , or T terms, each  $O(\epsilon T)$ , so  $O(\epsilon T^2)$  total cost
    - · for DAgger,  $E[\sum_t c(s_t, a_t)] \leq \epsilon T$

# 4 8/22

- Decisions  $\leftrightarrow$  observations, rewards
- Deep models allow solve reinforcement learning algos from end to end
- Interesting car jam situation with autonomous car
- Basic reinforcement learning = maximizing rewards but not enough to generalize to situations in real world
  - Learn from demonstrations
  - Observing the world
  - Learn from other tasks (transfer learning), inferring intentions
- Predicting what actions will do, or planning actions
- General learning in the future, have learning algorithm(s) for all situations
  - What must this single algorithm do
    - \* Interpret rich sensory inputs
    - \* Choose complex actions
  - Deep = interpret, reinforcement learning = complex actions
- Brain actually seems to work like deep reinforcement learning (deep learning and reinforcement learning), like basal ganglia = reward function
- NOW: deep rl great in simple rules, learn simple skills, learn from imitation
- CHALLENGING: humans learn much faster, humans can do transfer learning (OPEN PROBLEM), not clear what reward function should be, not clear what role of prediction should be
- thought: human main purpose is to sustain life, it may be beneficial for the reward function to be "negative" in the sense that any move that isn't optimal causes neurons in the neural net to be removed at random, this actually mimics real life when neurons are being pared during development
  - the objective would be to keep as many neurons as possible
  - if mistakes are made, then the neural net would become smaller but more specialized for the task at hand
  - if we start with a really large neural net (babies have really large brains), we won't run into having a neural net that cannot generalize to the problem at hand
  - couple this with prediction