# Formelsammlung und Wertetabellen

# Statistische Verfahren in der Geographie

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#### **Inhaltsverzeichnis**

| Qu | ellen                    | 7 |
|----|--------------------------|---|
|    | $\chi^2$ -Verteilungen   | õ |
|    | F-Verteilungen           |   |
|    | t-Verteilungen           | 1 |
|    | Standardnormalverteilung | 3 |
|    | Formelsammlung           |   |
|    | Hinweise                 | 1 |

#### **Hinweise**

- Die im Folgenden dargestellten Informationen werden Ihnen so oder ähnlich auch in der Klausur zur Verfügung stehen.
- Bezeichnungen und Konventionen orientieren sich an Bortz und Schuster (2010), sind aber teilweise abweichend vereinfacht.
- Die Wertetabellen wurden mit den entsprechenden Funktionen in R (R Core Team 2018) automatisch generiert.

Stand: 21. Mai 2021 Seite 1/7

#### **Formelsammlung**

$$\bar{x} = \frac{\sum\limits_{i=1}^{n} x_{i}}{n}$$

$$t = \sqrt{n} \cdot \frac{\bar{x} - \mu_{0}}{s}$$

$$t = \frac{x_{1} - \bar{x}_{2}}{\sqrt{\frac{s_{1}^{2} + \nu_{2}^{2}}{s^{2}}}}$$

$$s_{2} = \frac{\sum\limits_{i=1}^{n} (x_{i} - \bar{x}) \cdot (y_{i} - \bar{y})}{n - 1}$$

$$s = \sqrt{s}$$

$$s_{xy} = \frac{\sum\limits_{i=1}^{n} (x_{i} - \bar{x}) \cdot (y_{i} - \bar{y})}{n - 1}$$

$$r = \frac{s_{xy}}{s_{x} \cdot s_{y}}$$

$$y = a + b \cdot x$$

$$v = \frac{s}{|\bar{x}|} \cdot 100\%$$

$$v = \frac{s}{|\bar{x}|} \cdot 100\%$$

$$z_{i} = \frac{x_{i} - \bar{x}}{s}$$

$$x_{i} = z_{i} \cdot s + \bar{x}$$

$$x_{i} = z_{i} \cdot s + \bar{x}$$

$$c_{i} = y_{i} - \hat{y}_{i}$$

$$m_{ij} = \frac{n_{i} \cdot n_{ij}}{n}$$

$$1 - \alpha = P(z_{\alpha/2} < z_{\mu} < z_{(1-\alpha/2)})$$

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$$

$$\frac{KIB}{2} = z_{(1-\alpha/2)} \cdot \sigma_{\bar{x}}$$

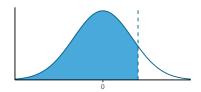
$$z = \sqrt{n} \cdot \frac{\bar{x} - \mu_{0}}{\sigma}$$

$$CI = \sqrt{\frac{\chi^{2}}{n \cdot (\min(k, \ell) - 1)}}$$

| Bestimmung der Freiheitsgrade für | Formel                            |
|-----------------------------------|-----------------------------------|
| 1-Stichproben- <i>t</i> -Test     | df = n - 1                        |
| 2-Stichproben- <i>t</i> -Test     | $df = 2 \cdot n - 2$              |
| F-Test                            | $df_1 = n_1 - 1;  df_2 = n_2 - 1$ |
| $\chi^2$ -Unabhängigkeitstest     | $df = (k-1) \cdot (\ell-1)$       |
| Eindimensionaler $\chi^2$ -Test   | df = k - 1                        |

Stand: 21. Mai 2021 Seite 2/7

### Standardnormalverteilung

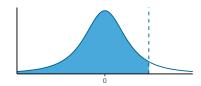


$$P(z \le -z_p) = 1 - P(z \le z_p)$$

|     | z (zweite Nachkommastelle) |        |        |        |        |        |        |        |        |        |  |  |  |  |
|-----|----------------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--|--|--|--|
| z   | 0,00                       | 0,01   | 0,02   | 0,03   | 0,04   | 0,05   | 0,06   | 0,07   | 0,08   | 0,09   |  |  |  |  |
| 0,0 | 0,5000                     | 0,5040 | 0,5080 | 0,5120 | 0,5160 | 0,5199 | 0,5239 | 0,5279 | 0,5319 | 0,5359 |  |  |  |  |
| 0,1 | 0,5398                     | 0,5438 | 0,5478 | 0,5517 | 0,5557 | 0,5596 | 0,5636 | 0,5675 | 0,5714 | 0,5753 |  |  |  |  |
| 0,2 | 0,5793                     | 0,5832 | 0,5871 | 0,5910 | 0,5948 | 0,5987 | 0,6026 | 0,6064 | 0,6103 | 0,6141 |  |  |  |  |
| 0,3 | 0,6179                     | 0,6217 | 0,6255 | 0,6293 | 0,6331 | 0,6368 | 0,6406 | 0,6443 | 0,6480 | 0,6517 |  |  |  |  |
| 0,4 | 0,6554                     | 0,6591 | 0,6628 | 0,6664 | 0,6700 | 0,6736 | 0,6772 | 0,6808 | 0,6844 | 0,6879 |  |  |  |  |
| 0,5 | 0,6915                     | 0,6950 | 0,6985 | 0,7019 | 0,7054 | 0,7088 | 0,7123 | 0,7157 | 0,7190 | 0,7224 |  |  |  |  |
| 0,6 | 0,7257                     | 0,7291 | 0,7324 | 0,7357 | 0,7389 | 0,7422 | 0,7454 | 0,7486 | 0,7517 | 0,7549 |  |  |  |  |
| 0,7 | 0,7580                     | 0,7611 | 0,7642 | 0,7673 | 0,7703 | 0,7734 | 0,7764 | 0,7794 | 0,7823 | 0,7852 |  |  |  |  |
| 0,8 | 0,7881                     | 0,7910 | 0,7939 | 0,7967 | 0,7995 | 0,8023 | 0,8051 | 0,8078 | 0,8106 | 0,8133 |  |  |  |  |
| 0,9 | 0,8159                     | 0,8186 | 0,8212 | 0,8238 | 0,8264 | 0,8289 | 0,8315 | 0,8340 | 0,8365 | 0,8389 |  |  |  |  |
| 1,0 | 0,8413                     | 0,8438 | 0,8461 | 0,8485 | 0,8508 | 0,8531 | 0,8554 | 0,8577 | 0,8599 | 0,8621 |  |  |  |  |
| 1,1 | 0,8643                     | 0,8665 | 0,8686 | 0,8708 | 0,8729 | 0,8749 | 0,8770 | 0,8790 | 0,8810 | 0,8830 |  |  |  |  |
| 1,2 | 0,8849                     | 0,8869 | 0,8888 | 0,8907 | 0,8925 | 0,8944 | 0,8962 | 0,8980 | 0,8997 | 0,9015 |  |  |  |  |
| 1,3 | 0,9032                     | 0,9049 | 0,9066 | 0,9082 | 0,9099 | 0,9115 | 0,9131 | 0,9147 | 0,9162 | 0,9177 |  |  |  |  |
| 1,4 | 0,9192                     | 0,9207 | 0,9222 | 0,9236 | 0,9251 | 0,9265 | 0,9279 | 0,9292 | 0,9306 | 0,9319 |  |  |  |  |
| 1,5 | 0,9332                     | 0,9345 | 0,9357 | 0,9370 | 0,9382 | 0,9394 | 0,9406 | 0,9418 | 0,9429 | 0,9441 |  |  |  |  |
| 1,6 | 0,9452                     | 0,9463 | 0,9474 | 0,9484 | 0,9495 | 0,9505 | 0,9515 | 0,9525 | 0,9535 | 0,9545 |  |  |  |  |
| 1,7 | 0,9554                     | 0,9564 | 0,9573 | 0,9582 | 0,9591 | 0,9599 | 0,9608 | 0,9616 | 0,9625 | 0,9633 |  |  |  |  |
| 1,8 | 0,9641                     | 0,9649 | 0,9656 | 0,9664 | 0,9671 | 0,9678 | 0,9686 | 0,9693 | 0,9699 | 0,9706 |  |  |  |  |
| 1,9 | 0,9713                     | 0,9719 | 0,9726 | 0,9732 | 0,9738 | 0,9744 | 0,9750 | 0,9756 | 0,9761 | 0,9767 |  |  |  |  |
| 2,0 | 0,9772                     | 0,9778 | 0,9783 | 0,9788 | 0,9793 | 0,9798 | 0,9803 | 0,9808 | 0,9812 | 0,9817 |  |  |  |  |
| 2,1 | 0,9821                     | 0,9826 | 0,9830 | 0,9834 | 0,9838 | 0,9842 | 0,9846 | 0,9850 | 0,9854 | 0,9857 |  |  |  |  |
| 2,2 | 0,9861                     | 0,9864 | 0,9868 | 0,9871 | 0,9875 | 0,9878 | 0,9881 | 0,9884 | 0,9887 | 0,9890 |  |  |  |  |
| 2,3 | 0,9893                     | 0,9896 | 0,9898 | 0,9901 | 0,9904 | 0,9906 | 0,9909 | 0,9911 | 0,9913 | 0,9916 |  |  |  |  |
| 2,4 | 0,9918                     | 0,9920 | 0,9922 | 0,9925 | 0,9927 | 0,9929 | 0,9931 | 0,9932 | 0,9934 | 0,9936 |  |  |  |  |
| 2,5 | 0,9938                     | 0,9940 | 0,9941 | 0,9943 | 0,9945 | 0,9946 | 0,9948 | 0,9949 | 0,9951 | 0,9952 |  |  |  |  |
| 2,6 | 0,9953                     | 0,9955 | 0,9956 | 0,9957 | 0,9959 | 0,9960 | 0,9961 | 0,9962 | 0,9963 | 0,9964 |  |  |  |  |
| 2,7 | 0,9965                     | 0,9966 | 0,9967 | 0,9968 | 0,9969 | 0,9970 | 0,9971 | 0,9972 | 0,9973 | 0,9974 |  |  |  |  |
| 2,8 | 0,9974                     | 0,9975 | 0,9976 | 0,9977 | 0,9977 | 0,9978 | 0,9979 | 0,9979 | 0,9980 | 0,9981 |  |  |  |  |
| 2,9 | 0,9981                     | 0,9982 | 0,9982 | 0,9983 | 0,9984 | 0,9984 | 0,9985 | 0,9985 | 0,9986 | 0,9986 |  |  |  |  |
| 3,0 | 0,9987                     | 0,9987 | 0,9987 | 0,9988 | 0,9988 | 0,9989 | 0,9989 | 0,9989 | 0,9990 | 0,9990 |  |  |  |  |

Stand: 21. Mai 2021 Seite 3/7

### $t ext{-}Verteilungen$

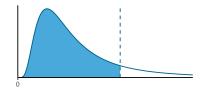


$$P(t \le -t_p) = 1 - P(t \le t_p)$$

|            |                |                |                |                |                |                |                | F              | läche          |                |                |                |                  |                  |                  |
|------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|----------------|------------------|------------------|------------------|
| df         | 0,55           | 0,6            | 0,65           | 0,7            | 0,75           | 0,8            | 0,85           | 0,9            | 0,95           | 0,975          | 0,99           | 0,995          | 0,999            | 0,9995           | 0,9999           |
| 1          | 0,158          | 0,325          | 0,510          | 0,727          | 1,000          | 1,376          | 1,963          | 3,078          | 6,314          | 12,706         | 31,821         | 63,657         | 318,309          | 636,619          | 3183,099         |
| 2          | 0,142<br>0,137 | 0,289<br>0,277 | 0,445<br>0,424 | 0,617<br>0,584 | 0,816<br>0,765 | 1,061<br>0,978 | 1,386<br>1,250 | 1,886<br>1,638 | 2,920<br>2,353 | 4,303<br>3,182 | 6,965<br>4,541 | 9,925<br>5,841 | 22,327<br>10,215 | 31,599<br>12,924 | 70,700<br>22,204 |
| 4          | 0,134          | 0,271          | 0,424          | 0,569          | 0,763          | 0,941          | 1,190          | 1,533          | 2,333          | 2,776          | 3,747          | 4,604          | 7,173            | 8,610            | 13,034           |
| 5          | 0,132          | 0,267          | 0,408          | 0,559          | 0,727          | 0,920          | 1,156          | 1,476          | 2,015          | 2,571          | 3,365          | 4,032          | 5,893            | 6,869            | 9,678            |
| 6          | 0,131          | 0,265          | 0,404          | 0,553          | 0,718          | 0,906          | 1,134          | 1,440          | 1,943          | 2,447          | 3,143          | 3,707          | 5,208            | 5,959            | 8,025            |
| 7<br>8     | 0,130<br>0,130 | 0,263<br>0,262 | 0,402<br>0,399 | 0,549<br>0,546 | 0,711<br>0,706 | 0,896<br>0,889 | 1,119<br>1,108 | 1,415<br>1,397 | 1,895<br>1,860 | 2,365<br>2,306 | 2,998<br>2,896 | 3,499<br>3,355 | 4,785<br>4,501   | 5,408<br>5,041   | 7,063<br>6,442   |
| 9          | 0,130          | 0,262          | 0,398          | 0,543          | 0,700          | 0,883          | 1,100          | 1,383          | 1,833          | 2,360          | 2,830          | 3,250          | 4,297            | 4,781            | 6,010            |
| 10         | 0,129          | 0,260          | 0,397          | 0,542          | 0,700          | 0,879          | 1,093          | 1,372          | 1,812          | 2,228          | 2,764          | 3,169          | 4,144            | 4,587            | 5,694            |
| 11         | 0,129          | 0,260          | 0,396          | 0,540          | 0,697          | 0,876          | 1,088          | 1,363          | 1,796          | 2,201          | 2,718          | 3,106          | 4,025            | 4,437            | 5,453            |
| 12         | 0,128          | 0,259          | 0,395          | 0,539          | 0,695          | 0,873          | 1,083          | 1,356          | 1,782          | 2,179          | 2,681          | 3,055          | 3,930            | 4,318            | 5,263            |
| 13         | 0,128          | 0,259          | 0,394          | 0,538          | 0,694          | 0,870          | 1,079          | 1,350          | 1,771          | 2,160          | 2,650          | 3,012          | 3,852            | 4,221            | 5,111            |
| 14<br>15   | 0,128          | 0,258          | 0,393          | 0,537          | 0,692          | 0,868          | 1,076          | 1,345          | 1,761          | 2,145          | 2,624          | 2,977          | 3,787            | 4,140            | 4,985            |
|            | 0,128<br>0,128 | 0,258<br>0,258 | 0,393          | 0,536<br>0,535 | 0,691          | 0,866<br>0,865 | 1,074          | 1,341          | 1,753<br>1,746 | 2,131          | 2,602<br>2,583 | 2,947          | 3,733            | 4,073            | 4,880            |
| 16<br>17   | 0,128          | 0,258          | 0,392          | 0,535          | 0,689          | 0,863          | 1,071<br>1,069 | 1,337<br>1,333 | 1,740          | 2,120<br>2,110 | 2,563          | 2,921<br>2,898 | 3,686<br>3,646   | 4,015<br>3,965   | 4,791<br>4,714   |
| 18         | 0,127          | 0,257          | 0,392          | 0,534          | 0,688          | 0,862          | 1,067          | 1,330          | 1,734          | 2,110          | 2,552          | 2,878          | 3,610            | 3,922            | 4,648            |
| 19         | 0,127          | 0,257          | 0,391          | 0,533          | 0,688          | 0,861          | 1,066          | 1,328          | 1,729          | 2,093          | 2,539          | 2,861          | 3,579            | 3,883            | 4,590            |
| 20         | 0,127          | 0,257          | 0,391          | 0,533          | 0,687          | 0,860          | 1,064          | 1,325          | 1,725          | 2,086          | 2,528          | 2,845          | 3,552            | 3,850            | 4,539            |
| 25         | 0,127          | 0,256          | 0,390          | 0,531          | 0,684          | 0,856          | 1,058          | 1,316          | 1,708          | 2,060          | 2,485          | 2,787          | 3,450            | 3,725            | 4,352            |
| 30         | 0,127          | 0,256          | 0,389          | 0,530          | 0,683          | 0,854          | 1,055          | 1,310          | 1,697          | 2,042          | 2,457          | 2,750          | 3,385            | 3,646            | 4,234            |
| 35<br>40   | 0,127<br>0,126 | 0,255<br>0,255 | 0,388<br>0,388 | 0,529<br>0,529 | 0,682<br>0,681 | 0,852<br>0,851 | 1,052          | 1,306<br>1,303 | 1,690          | 2,030<br>2,021 | 2,438<br>2,423 | 2,724<br>2,704 | 3,340            | 3,591            | 4,153<br>4,094   |
| 45         | 0,126          | 0,255          | 0,388          | 0,528          | 0,680          | 0,851          | 1,050<br>1,049 | 1,303          | 1,684<br>1,679 | 2,021          | 2,423          | 2,690          | 3,307<br>3,281   | 3,551<br>3,520   | 4,049            |
| 50         | 0,126          | 0,255          | 0,388          | 0,528          | 0,679          | 0,849          | 1,047          | 1,299          | 1,676          | 2,009          | 2,403          | 2,678          | 3,261            | 3,496            | 4,014            |
| 55         | 0,126          | 0,255          | 0,387          | 0,527          | 0,679          | 0,848          | 1,046          | 1,297          | 1,673          | 2,004          | 2,396          | 2,668          | 3,245            | 3,476            | 3,986            |
| 60         | 0,126          | 0,254          | 0,387          | 0,527          | 0,679          | 0,848          | 1,045          | 1,296          | 1,671          | 2,000          | 2,390          | 2,660          | 3,232            | 3,460            | 3,962            |
| 65         | 0,126          | 0,254          | 0,387          | 0,527          | 0,678          | 0,847          | 1,045          | 1,295          | 1,669          | 1,997          | 2,385          | 2,654          | 3,220            | 3,447            | 3,942            |
| 70         | 0,126          | 0,254          | 0,387          | 0,527          | 0,678          | 0,847          | 1,044          | 1,294          | 1,667          | 1,994          | 2,381          | 2,648          | 3,211            | 3,435            | 3,926            |
| 75         | 0,126          | 0,254          | 0,387          | 0,527          | 0,678          | 0,846          | 1,044          | 1,293          | 1,665          | 1,992          | 2,377          | 2,643          | 3,202            | 3,425            | 3,911            |
| 80<br>90   | 0,126<br>0,126 | 0,254<br>0,254 | 0,387<br>0,387 | 0,526<br>0,526 | 0,678<br>0,677 | 0,846<br>0,846 | 1,043<br>1,042 | 1,292<br>1,291 | 1,664<br>1,662 | 1,990<br>1,987 | 2,374<br>2,368 | 2,639<br>2,632 | 3,195<br>3,183   | 3,416            | 3,899<br>3,878   |
| 100        | 0,126          | 0,254          | 0,386          | 0,526          | 0,677          | 0,845          | 1,042          | 1,291          | 1,660          | 1,984          | 2,364          | 2,632          | 3,174            | 3,402<br>3,390   | 3,862            |
| 110        | 0,126          | 0,254          | 0,386          | 0,526          | 0,677          | 0,845          | 1,041          | 1,289          | 1,659          | 1,982          | 2,361          | 2,621          | 3,166            | 3,381            | 3,848            |
| 120        | 0,126          | 0,254          | 0,386          | 0,526          | 0,677          | 0,845          | 1,041          | 1,289          | 1,658          | 1,980          | 2,358          | 2,617          | 3,160            | 3,373            | 3,837            |
| 130        | 0,126          | 0,254          | 0,386          | 0,526          | 0,676          | 0,844          | 1,041          | 1,288          | 1,657          | 1,978          | 2,355          | 2,614          | 3,154            | 3,367            | 3,828            |
| 140        | 0,126          | 0,254          | 0,386          | 0,526          | 0,676          | 0,844          | 1,040          | 1,288          | 1,656          | 1,977          | 2,353          | 2,611          | 3,149            | 3,361            | 3,820            |
| 150        | 0,126          | 0,254<br>0,254 | 0,386          | 0,526<br>0,525 | 0,676<br>0,676 | 0,844<br>0,843 | 1,040          | 1,287<br>1,286 | 1,655          | 1,976          | 2,351          | 2,609          | 3,145            | 3,357            | 3,813            |
| 200        | 0,126          | •              | 0,386          |                | •              | •              | 1,039          |                | 1,653          | 1,972          | 2,345          | 2,601          | 3,131            | 3,340            | 3,789            |
| 300        | 0,126          | 0,254          | 0,386          | 0,525          | 0,675          | 0,843          | 1,038          | 1,284          | 1,650          | 1,968          | 2,339          | 2,592          | 3,118            | 3,323            | 3,765            |
| 400<br>500 | 0,126<br>0,126 | 0,254<br>0,253 | 0,386<br>0,386 | 0,525<br>0,525 | 0,675<br>0,675 | 0,843<br>0,842 | 1,038<br>1,038 | 1,284<br>1,283 | 1,649<br>1,648 | 1,966<br>1,965 | 2,336<br>2,334 | 2,588<br>2,586 | 3,111<br>3,107   | 3,315<br>3,310   | 3,754<br>3,747   |
| z          | 0,126          | 0,253          | 0,385          | 0,524          | 0,674          | 0,842          | 1,036          | 1,282          | 1,645          | 1,960          | 2,334          | 2,576          | 3,090            | 3,291            | 3,719            |
| ~          | 0,220          | 0,200          | 5,505          | J,J_ 1         | 5,511          | 0,012          | _,,555         | -,             | -,5 15         | _,500          | _,525          | _,5.5          | 2,000            | ٠,٢٥١            |                  |

Stand: 21. Mai 2021 Seite 4/7

### $F ext{-} ext{Verteilungen}$



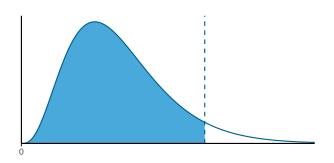
$$F_{\mathit{df}_1;\mathit{df}_2;\alpha} = \frac{1}{F_{\mathit{df}_2;\mathit{df}_1;(1-\alpha)}}$$

#### Alle Werte für Flächenanteil 0,95

|        | $d\!f_1$ |        |        |        |        |        |        |        |        |        |        |        |        |        |
|--------|----------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| $df_2$ | 1        | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | 10     | 15     | 20     | 50     | 100    |
| 1      | 161,45   | 199,50 | 215,71 | 224,58 | 230,16 | 233,99 | 236,77 | 238,88 | 240,54 | 241,88 | 245,95 | 248,01 | 251,77 | 253,04 |
| 2      | 18,51    | 19,00  | 19,16  | 19,25  | 19,30  | 19,33  | 19,35  | 19,37  | 19,38  | 19,40  | 19,43  | 19,45  | 19,48  | 19,49  |
| 3      | 10,13    | 9,55   | 9,28   | 9,12   | 9,01   | 8,94   | 8,89   | 8,85   | 8,81   | 8,79   | 8,70   | 8,66   | 8,58   | 8,55   |
| 4      | 7,71     | 6,94   | 6,59   | 6,39   | 6,26   | 6,16   | 6,09   | 6,04   | 6,00   | 5,96   | 5,86   | 5,80   | 5,70   | 5,66   |
| 5      | 6,61     | 5,79   | 5,41   | 5,19   | 5,05   | 4,95   | 4,88   | 4,82   | 4,77   | 4,74   | 4,62   | 4,56   | 4,44   | 4,41   |
| 6      | 5,99     | 5,14   | 4,76   | 4,53   | 4,39   | 4,28   | 4,21   | 4,15   | 4,10   | 4,06   | 3,94   | 3,87   | 3,75   | 3,71   |
| 7      | 5,59     | 4,74   | 4,35   | 4,12   | 3,97   | 3,87   | 3,79   | 3,73   | 3,68   | 3,64   | 3,51   | 3,44   | 3,32   | 3,27   |
| 8      | 5,32     | 4,46   | 4,07   | 3,84   | 3,69   | 3,58   | 3,50   | 3,44   | 3,39   | 3,35   | 3,22   | 3,15   | 3,02   | 2,97   |
| 9      | 5,12     | 4,26   | 3,86   | 3,63   | 3,48   | 3,37   | 3,29   | 3,23   | 3,18   | 3,14   | 3,01   | 2,94   | 2,80   | 2,76   |
| 10     | 4,96     | 4,10   | 3,71   | 3,48   | 3,33   | 3,22   | 3,14   | 3,07   | 3,02   | 2,98   | 2,85   | 2,77   | 2,64   | 2,59   |
| 11     | 4,84     | 3,98   | 3,59   | 3,36   | 3,20   | 3,09   | 3,01   | 2,95   | 2,90   | 2,85   | 2,72   | 2,65   | 2,51   | 2,46   |
| 12     | 4,75     | 3,89   | 3,49   | 3,26   | 3,11   | 3,00   | 2,91   | 2,85   | 2,80   | 2,75   | 2,62   | 2,54   | 2,40   | 2,35   |
| 13     | 4,67     | 3,81   | 3,41   | 3,18   | 3,03   | 2,92   | 2,83   | 2,77   | 2,71   | 2,67   | 2,53   | 2,46   | 2,31   | 2,26   |
| 14     | 4,60     | 3,74   | 3,34   | 3,11   | 2,96   | 2,85   | 2,76   | 2,70   | 2,65   | 2,60   | 2,46   | 2,39   | 2,24   | 2,19   |
| 15     | 4,54     | 3,68   | 3,29   | 3,06   | 2,90   | 2,79   | 2,71   | 2,64   | 2,59   | 2,54   | 2,40   | 2,33   | 2,18   | 2,12   |
| 16     | 4,49     | 3,63   | 3,24   | 3,01   | 2,85   | 2,74   | 2,66   | 2,59   | 2,54   | 2,49   | 2,35   | 2,28   | 2,12   | 2,07   |
| 17     | 4,45     | 3,59   | 3,20   | 2,96   | 2,81   | 2,70   | 2,61   | 2,55   | 2,49   | 2,45   | 2,31   | 2,23   | 2,08   | 2,02   |
| 18     | 4,41     | 3,55   | 3,16   | 2,93   | 2,77   | 2,66   | 2,58   | 2,51   | 2,46   | 2,41   | 2,27   | 2,19   | 2,04   | 1,98   |
| 19     | 4,38     | 3,52   | 3,13   | 2,90   | 2,74   | 2,63   | 2,54   | 2,48   | 2,42   | 2,38   | 2,23   | 2,16   | 2,00   | 1,94   |
| 20     | 4,35     | 3,49   | 3,10   | 2,87   | 2,71   | 2,60   | 2,51   | 2,45   | 2,39   | 2,35   | 2,20   | 2,12   | 1,97   | 1,91   |
| 25     | 4,24     | 3,39   | 2,99   | 2,76   | 2,60   | 2,49   | 2,40   | 2,34   | 2,28   | 2,24   | 2,09   | 2,01   | 1,84   | 1,78   |
| 30     | 4,17     | 3,32   | 2,92   | 2,69   | 2,53   | 2,42   | 2,33   | 2,27   | 2,21   | 2,16   | 2,01   | 1,93   | 1,76   | 1,70   |
| 35     | 4,12     | 3,27   | 2,87   | 2,64   | 2,49   | 2,37   | 2,29   | 2,22   | 2,16   | 2,11   | 1,96   | 1,88   | 1,70   | 1,63   |
| 40     | 4,08     | 3,23   | 2,84   | 2,61   | 2,45   | 2,34   | 2,25   | 2,18   | 2,12   | 2,08   | 1,92   | 1,84   | 1,66   | 1,59   |
| 45     | 4,06     | 3,20   | 2,81   | 2,58   | 2,42   | 2,31   | 2,22   | 2,15   | 2,10   | 2,05   | 1,89   | 1,81   | 1,63   | 1,55   |
| 50     | 4,03     | 3,18   | 2,79   | 2,56   | 2,40   | 2,29   | 2,20   | 2,13   | 2,07   | 2,03   | 1,87   | 1,78   | 1,60   | 1,52   |
| 60     | 4,00     | 3,15   | 2,76   | 2,53   | 2,37   | 2,25   | 2,17   | 2,10   | 2,04   | 1,99   | 1,84   | 1,75   | 1,56   | 1,48   |
| 70     | 3,98     | 3,13   | 2,74   | 2,50   | 2,35   | 2,23   | 2,14   | 2,07   | 2,02   | 1,97   | 1,81   | 1,72   | 1,53   | 1,45   |
| 80     | 3,96     | 3,11   | 2,72   | 2,49   | 2,33   | 2,21   | 2,13   | 2,06   | 2,00   | 1,95   | 1,79   | 1,70   | 1,51   | 1,43   |
| 90     | 3,95     | 3,10   | 2,71   | 2,47   | 2,32   | 2,20   | 2,11   | 2,04   | 1,99   | 1,94   | 1,78   | 1,69   | 1,49   | 1,41   |
| 100    | 3,94     | 3,09   | 2,70   | 2,46   | 2,31   | 2,19   | 2,10   | 2,03   | 1,97   | 1,93   | 1,77   | 1,68   | 1,48   | 1,39   |
| 110    | 3,93     | 3,08   | 2,69   | 2,45   | 2,30   | 2,18   | 2,09   | 2,02   | 1,97   | 1,92   | 1,76   | 1,67   | 1,47   | 1,38   |
| 120    | 3,92     | 3,07   | 2,68   | 2,45   | 2,29   | 2,18   | 2,09   | 2,02   | 1,96   | 1,91   | 1,75   | 1,66   | 1,46   | 1,37   |
| 130    | 3,91     | 3,07   | 2,67   | 2,44   | 2,28   | 2,17   | 2,08   | 2,01   | 1,95   | 1,90   | 1,74   | 1,65   | 1,45   | 1,36   |
| 140    | 3,91     | 3,06   | 2,67   | 2,44   | 2,28   | 2,16   | 2,08   | 2,01   | 1,95   | 1,90   | 1,74   | 1,65   | 1,44   | 1,35   |
| 150    | 3,90     | 3,06   | 2,66   | 2,43   | 2,27   | 2,16   | 2,07   | 2,00   | 1,94   | 1,89   | 1,73   | 1,64   | 1,44   | 1,34   |
| 200    | 3,89     | 3,04   | 2,65   | 2,42   | 2,26   | 2,14   | 2,06   | 1,98   | 1,93   | 1,88   | 1,72   | 1,62   | 1,41   | 1,32   |
| 300    | 3,87     | 3,03   | 2,63   | 2,40   | 2,24   | 2,13   | 2,04   | 1,97   | 1,91   | 1,86   | 1,70   | 1,61   | 1,39   | 1,30   |
| 400    | 3,86     | 3,02   | 2,63   | 2,39   | 2,24   | 2,12   | 2,03   | 1,96   | 1,90   | 1,85   | 1,69   | 1,60   | 1,38   | 1,28   |
| 500    | 3,86     | 3,01   | 2,62   | 2,39   | 2,23   | 2,12   | 2,03   | 1,96   | 1,90   | 1,85   | 1,69   | 1,59   | 1,38   | 1,28   |
| 1000   | 3,85     | 3,00   | 2,61   | 2,38   | 2,22   | 2,11   | 2,02   | 1,95   | 1,89   | 1,84   | 1,68   | 1,58   | 1,36   | 1,26   |

Stand: 21. Mai 2021 Seite 5/7

## $\chi^2$ -Verteilungen



|     |         |         |         |         |         | Fläche  |         |         |         |         |         |
|-----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| df  | 0,6     | 0,7     | 0,8     | 0,85    | 0,9     | 0,95    | 0,975   | 0,99    | 0,995   | 0,999   | 0,9995  |
| 1   | 0,708   | 1,074   | 1,642   | 2,072   | 2,706   | 3,841   | 5,024   | 6,635   | 7,879   | 10,828  | 12,116  |
| 2   | 1,833   | 2,408   | 3,219   | 3,794   | 4,605   | 5,991   | 7,378   | 9,210   | 10,597  | 13,816  | 15,202  |
| 3   | 2,946   | 3,665   | 4,642   | 5,317   | 6,251   | 7,815   | 9,348   | 11,345  | 12,838  | 16,266  | 17,730  |
| 4   | 4,045   | 4,878   | 5,989   | 6,745   | 7,779   | 9,488   | 11,143  | 13,277  | 14,860  | 18,467  | 19,997  |
| 5   | 5,132   | 6,064   | 7,289   | 8,115   | 9,236   | 11,070  | 12,833  | 15,086  | 16,750  | 20,515  | 22,105  |
| 6   | 6,211   | 7,231   | 8,558   | 9,446   | 10,645  | 12,592  | 14,449  | 16,812  | 18,548  | 22,458  | 24,103  |
| 7   | 7,283   | 8,383   | 9,803   | 10,748  | 12,017  | 14,067  | 16,013  | 18,475  | 20,278  | 24,322  | 26,018  |
| 8   | 8,351   | 9,524   | 11,030  | 12,027  | 13,362  | 15,507  | 17,535  | 20,090  | 21,955  | 26,124  | 27,868  |
| 9   | 9,414   | 10,656  | 12,242  | 13,288  | 14,684  | 16,919  | 19,023  | 21,666  | 23,589  | 27,877  | 29,666  |
| 10  | 10,473  | 11,781  | 13,442  | 14,534  | 15,987  | 18,307  | 20,483  | 23,209  | 25,188  | 29,588  | 31,420  |
| 11  | 11,530  | 12,899  | 14,631  | 15,767  | 17,275  | 19,675  | 21,920  | 24,725  | 26,757  | 31,264  | 33,137  |
| 12  | 12,584  | 14,011  | 15,812  | 16,989  | 18,549  | 21,026  | 23,337  | 26,217  | 28,300  | 32,909  | 34,821  |
| 13  | 13,636  | 15,119  | 16,985  | 18,202  | 19,812  | 22,362  | 24,736  | 27,688  | 29,819  | 34,528  | 36,478  |
| 14  | 14,685  | 16,222  | 18,151  | 19,406  | 21,064  | 23,685  | 26,119  | 29,141  | 31,319  | 36,123  | 38,109  |
| 15  | 15,733  | 17,322  | 19,311  | 20,603  | 22,307  | 24,996  | 27,488  | 30,578  | 32,801  | 37,697  | 39,719  |
| 16  | 16,780  | 18,418  | 20,465  | 21,793  | 23,542  | 26,296  | 28,845  | 32,000  | 34,267  | 39,252  | 41,308  |
| 17  | 17,824  | 19,511  | 21,615  | 22,977  | 24,769  | 27,587  | 30,191  | 33,409  | 35,718  | 40,790  | 42,879  |
| 18  | 18,868  | 20,601  | 22,760  | 24,155  | 25,989  | 28,869  | 31,526  | 34,805  | 37,156  | 42,312  | 44,434  |
| 19  | 19,910  | 21,689  | 23,900  | 25,329  | 27,204  | 30,144  | 32,852  | 36,191  | 38,582  | 43,820  | 45,973  |
| 20  | 20,951  | 22,775  | 25,038  | 26,498  | 28,412  | 31,410  | 34,170  | 37,566  | 39,997  | 45,315  | 47,498  |
| 25  | 26,143  | 28,172  | 30,675  | 32,282  | 34,382  | 37,652  | 40,646  | 44,314  | 46,928  | 52,620  | 54,947  |
| 30  | 31,316  | 33,530  | 36,250  | 37,990  | 40,256  | 43,773  | 46,979  | 50,892  | 53,672  | 59,703  | 62,162  |
| 35  | 36,475  | 38,859  | 41,778  | 43,640  | 46,059  | 49,802  | 53,203  | 57,342  | 60,275  | 66,619  | 69,199  |
| 40  | 41,622  | 44,165  | 47,269  | 49,244  | 51,805  | 55,758  | 59,342  | 63,691  | 66,766  | 73,402  | 76,095  |
| 45  | 46,761  | 49,452  | 52,729  | 54,810  | 57,505  | 61,656  | 65,410  | 69,957  | 73,166  | 80,077  | 82,876  |
| 50  | 51,892  | 54,723  | 58,164  | 60,346  | 63,167  | 67,505  | 71,420  | 76,154  | 79,490  | 86,661  | 89,561  |
| 60  | 62,135  | 65,227  | 68,972  | 71,341  | 74,397  | 79,082  | 83,298  | 88,379  | 91,952  | 99,607  | 102,695 |
| 70  | 72,358  | 75,689  | 79,715  | 82,255  | 85,527  | 90,531  | 95,023  | 100,425 | 104,215 | 112,317 | 115,578 |
| 80  | 82,566  | 86,120  | 90,405  | 93,106  | 96,578  | 101,879 | 106,629 | 112,329 | 116,321 | 124,839 | 128,261 |
| 90  | 92,761  | 96,524  | 101,054 | 103,904 | 107,565 | 113,145 | 118,136 | 124,116 | 128,299 | 137,208 | 140,782 |
| 100 | 102,946 | 106,906 | 111,667 | 114,659 | 118,498 | 124,342 | 129,561 | 135,807 | 140,169 | 149,449 | 153,167 |
| 110 | 113,121 | 117,269 | 122,250 | 125,376 | 129,385 | 135,480 | 140,917 | 147,414 | 151,948 | 161,581 | 165,435 |
| 120 | 123,289 | 127,616 | 132,806 | 136,062 | 140,233 | 146,567 | 152,211 | 158,950 | 163,648 | 173,617 | 177,603 |
| 130 | 133,450 | 137,949 | 143,340 | 146,719 | 151,045 | 157,610 | 163,453 | 170,423 | 175,278 | 185,571 | 189,682 |
| 140 | 143,604 | 148,269 | 153,854 | 157,352 | 161,827 | 168,613 | 174,648 | 181,840 | 186,847 | 197,451 | 201,683 |
| 150 | 153,753 | 158,577 | 164,349 | 167,962 | 172,581 | 179,581 | 185,800 | 193,208 | 198,360 | 209,265 | 213,613 |
| 200 | 204,434 | 209,985 | 216,609 | 220,744 | 226,021 | 233,994 | 241,058 | 249,445 | 255,264 | 267,541 | 272,423 |
| 300 | 305,574 | 312,346 | 320,397 | 325,409 | 331,789 | 341,395 | 349,874 | 359,906 | 366,844 | 381,425 | 387,203 |
| 400 | 406,535 | 414,335 | 423,590 | 429,340 | 436,649 | 447,632 | 457,305 | 468,724 | 476,606 | 493,132 | 499,666 |
| 500 | 507,382 | 516,087 | 526,401 | 532,803 | 540,930 | 553,127 | 563,852 | 576,493 | 585,207 | 603,446 | 610,648 |

Stand: 21. Mai 2021 Seite 6/7

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Stand: 21. Mai 2021 Seite 7/7