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Scaling complexity in soil carbon models

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$$\frac{dP}{dt} = \varepsilon f S \rightarrow S_{sol} \xrightarrow{ND}$$
$$\frac{dB}{dt} = \varepsilon v B S - h B$$
$$\frac{dS}{dt} = \frac{v' CE}{k_m' + C} - \frac{v B S}{k + B} - \frac{dP_s}{dt}$$
$$dC = I_c - \frac{v' CE}{k_m' + C} - \frac{dP_c}{dt}$$



@KatheMathBio



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Why is predicting atmospheric CO₂ levels hard?

Net Primary
Production
(NPP)

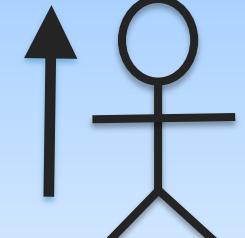
$56 \pm 8 \text{ Pg-C yr}^{-1}$



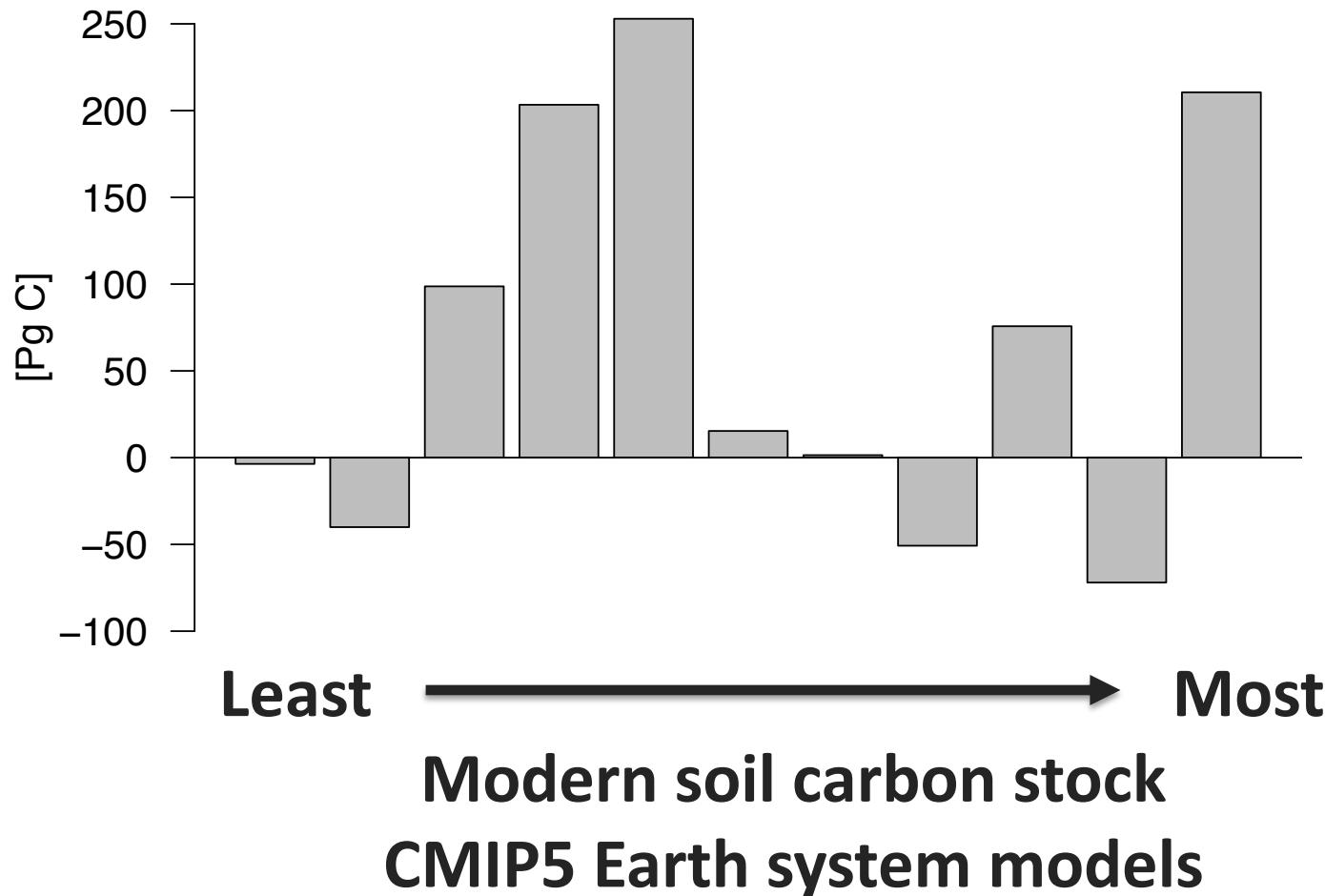
Heterotrophic
Respiration (R_h)
?? Pg-C yr⁻¹

Humans emit
8 to 10 Pg-C yr⁻¹

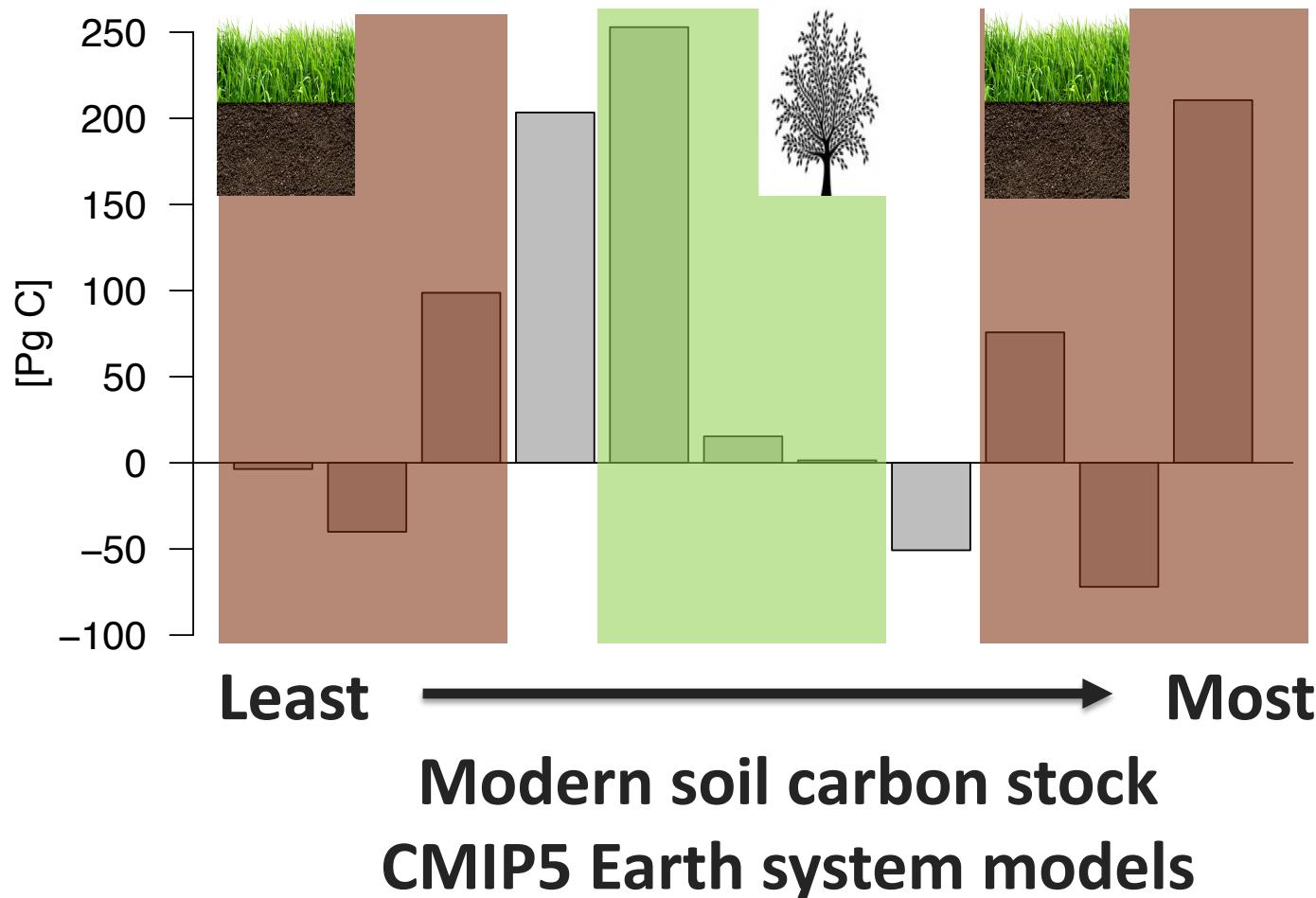
Net Ecosystem
Exchange (NEE)
1 to 4 Pg-C yr⁻¹



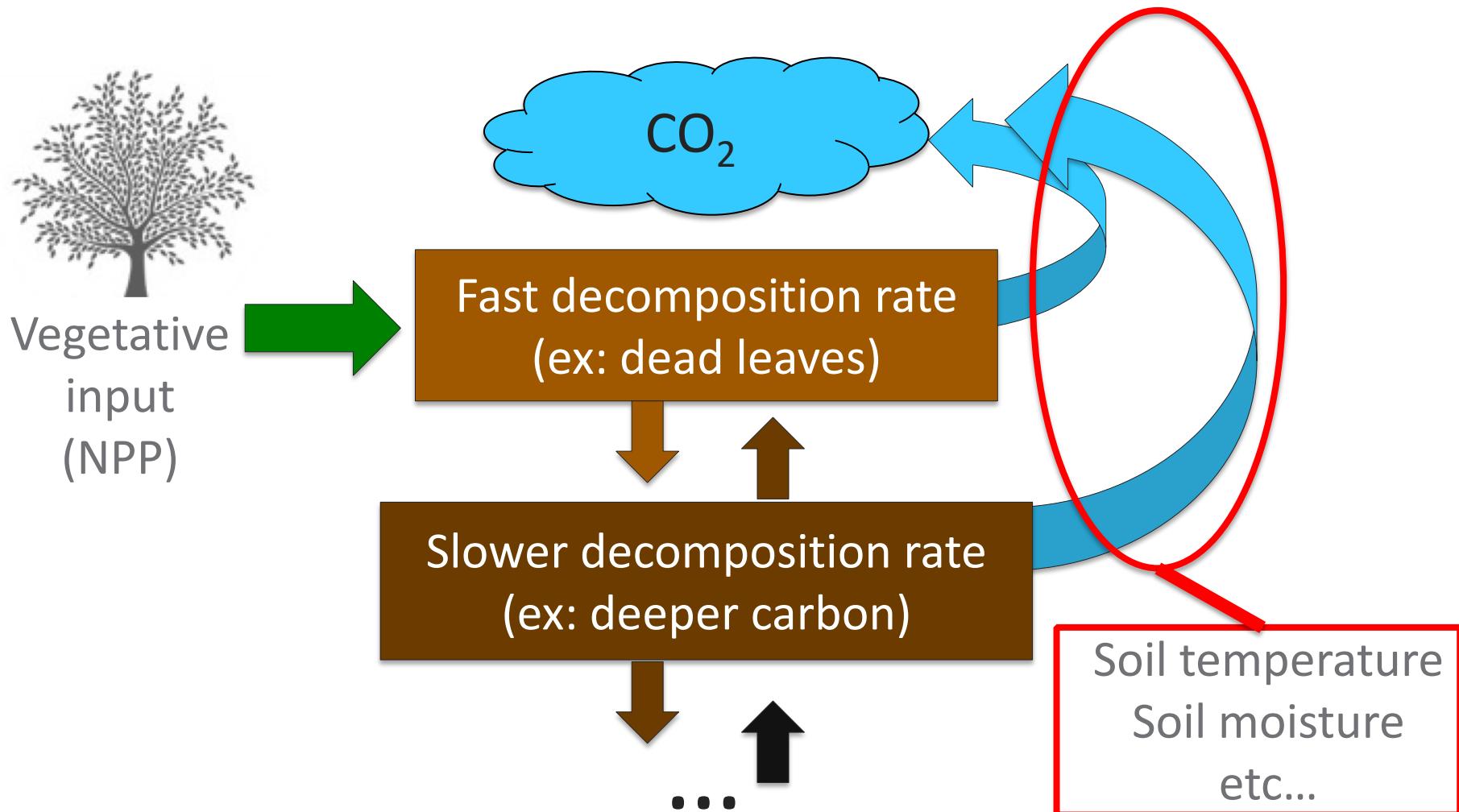
Change in soil carbon stock over the 21st century are very diverse



Modern benchmarks for global soil carbon and NPP do not constrain projections



Models can have different inputs, model structure, environmental drivers, and model parameters.



CENTURY: Parton et. al. 1987, 1988, 1992, 1993

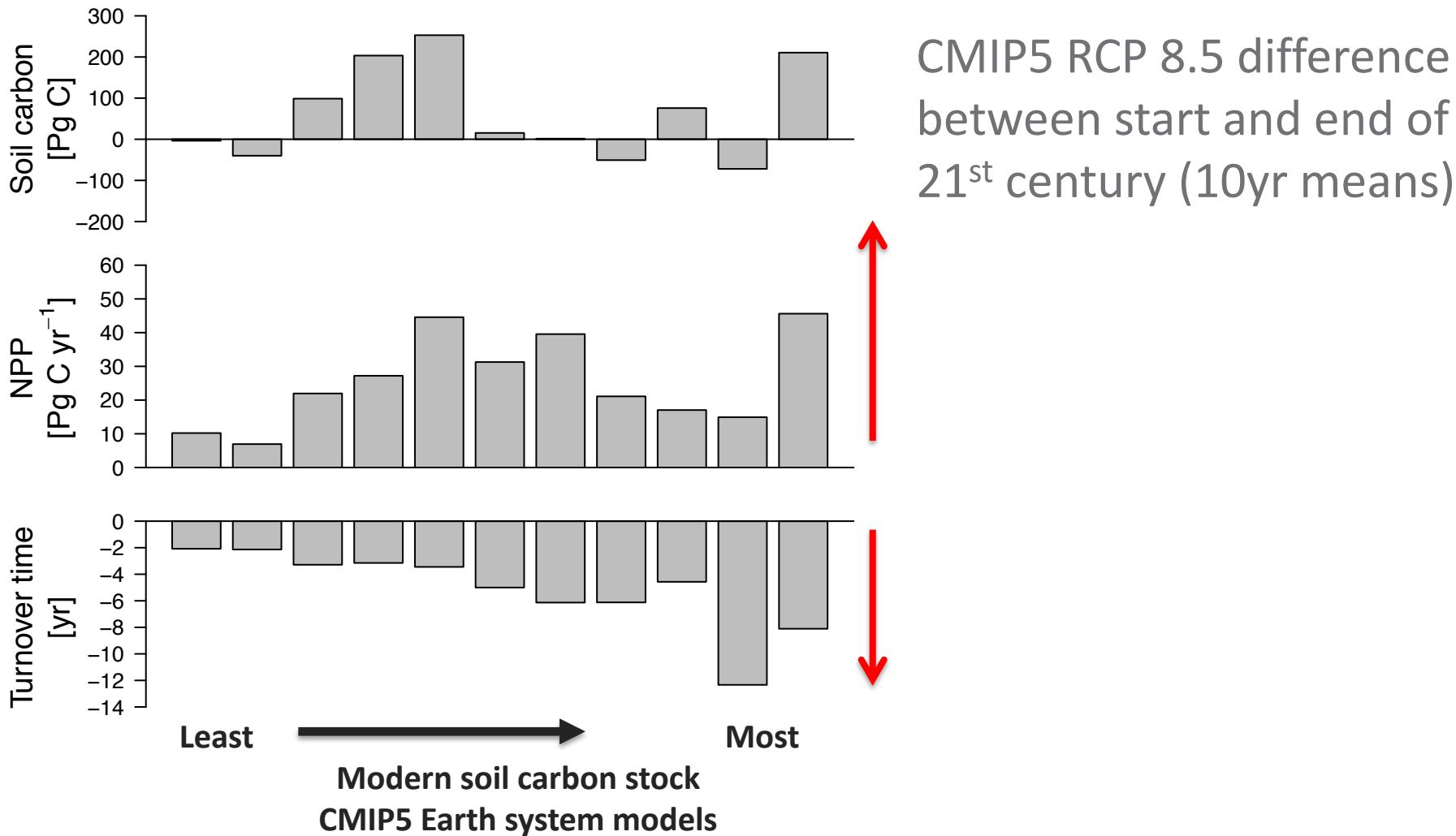
CLM: Oleson et. al. *Tech. description of vs 4.0 of CLM* 2010

Shifts in inputs and soil warming are the main drivers of soil carbon shifts.

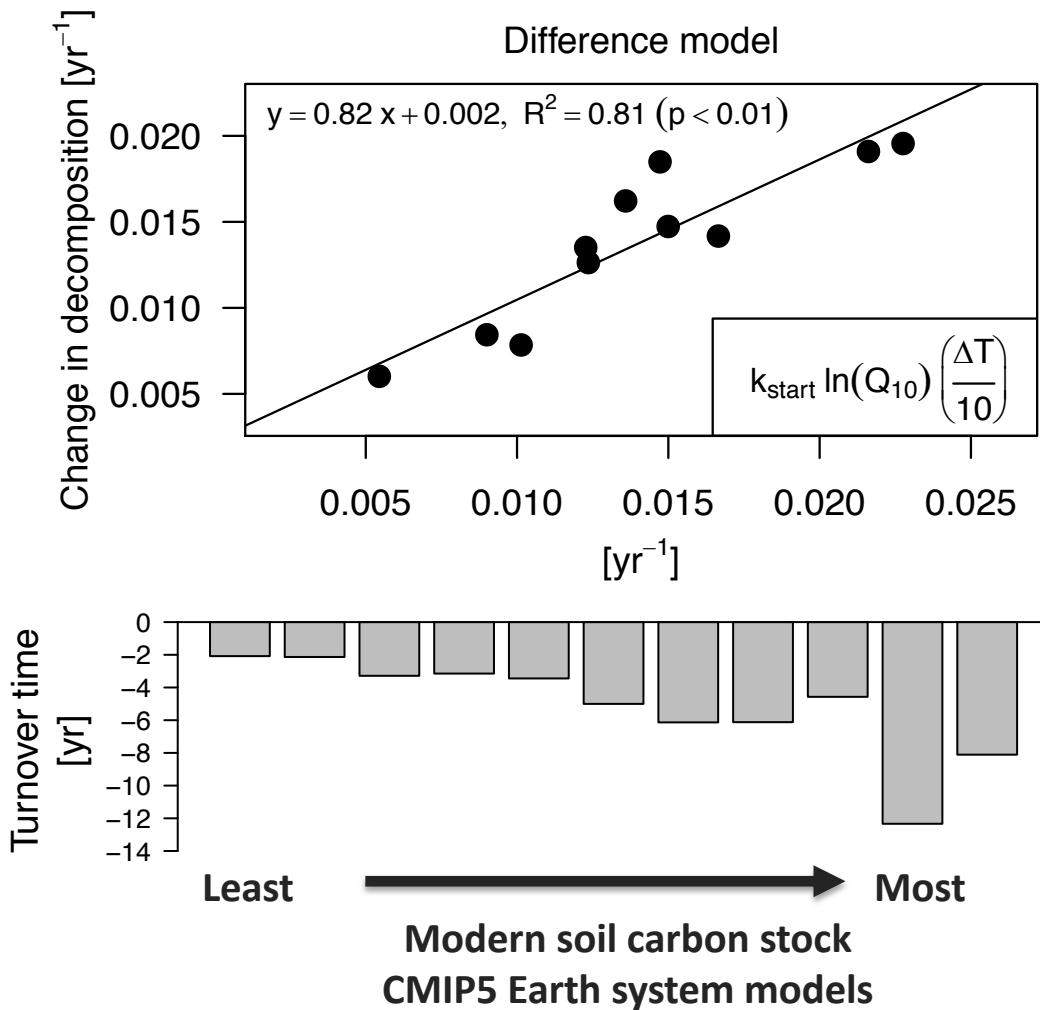


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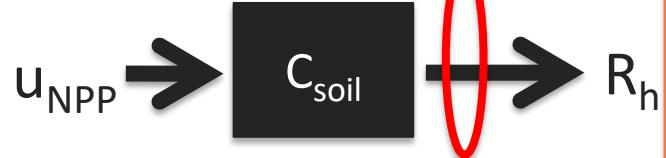


Parameterization and temperature explains differences in simulated decomposition rates.



CMIP5 RCP 8.5 difference
between start and end of
21st century (10yr means)

Reduced complexity model



$$R_h = C_{\text{soil}} k Q_{10}^{(T-15)/10}$$

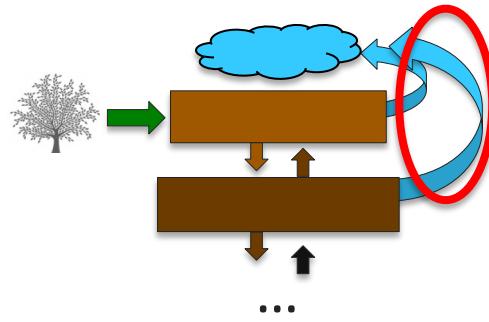
Intrinsic
decomposition
rate

Temperature
sensitivity



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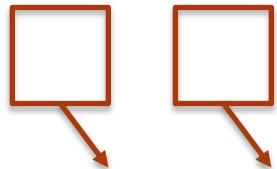


When can you use a one pool model for soils simulations?



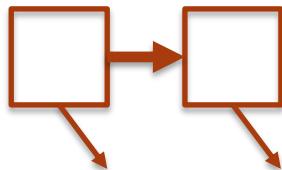
Soil carbon as a one pool model when inputs approximate outputs.

Independent



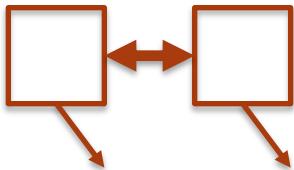
$$\frac{dC}{dt} = u(t)\mathbf{b} - \mathbf{KAC}(t)$$

Cascade



$$u(t) = kC$$

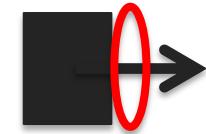
Feedback



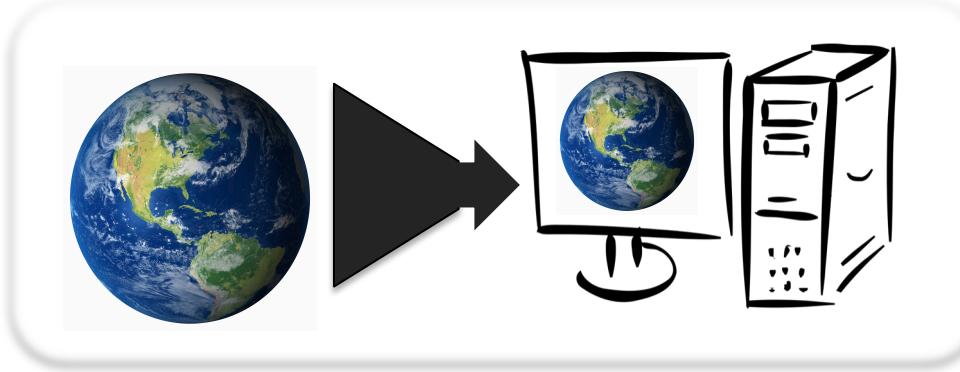
\mathbf{KA} is an M-matrix
Input approx. output

Reduced
Complexity

One pool



Using one pool models to “What If” Earth system model outputs without reruns.

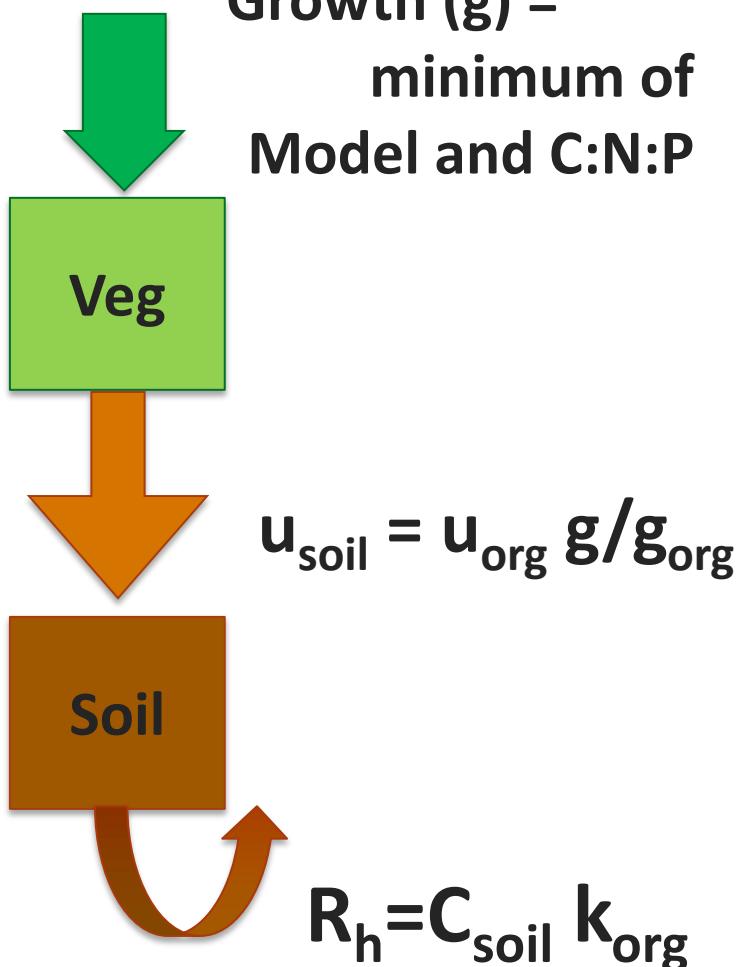


What if...

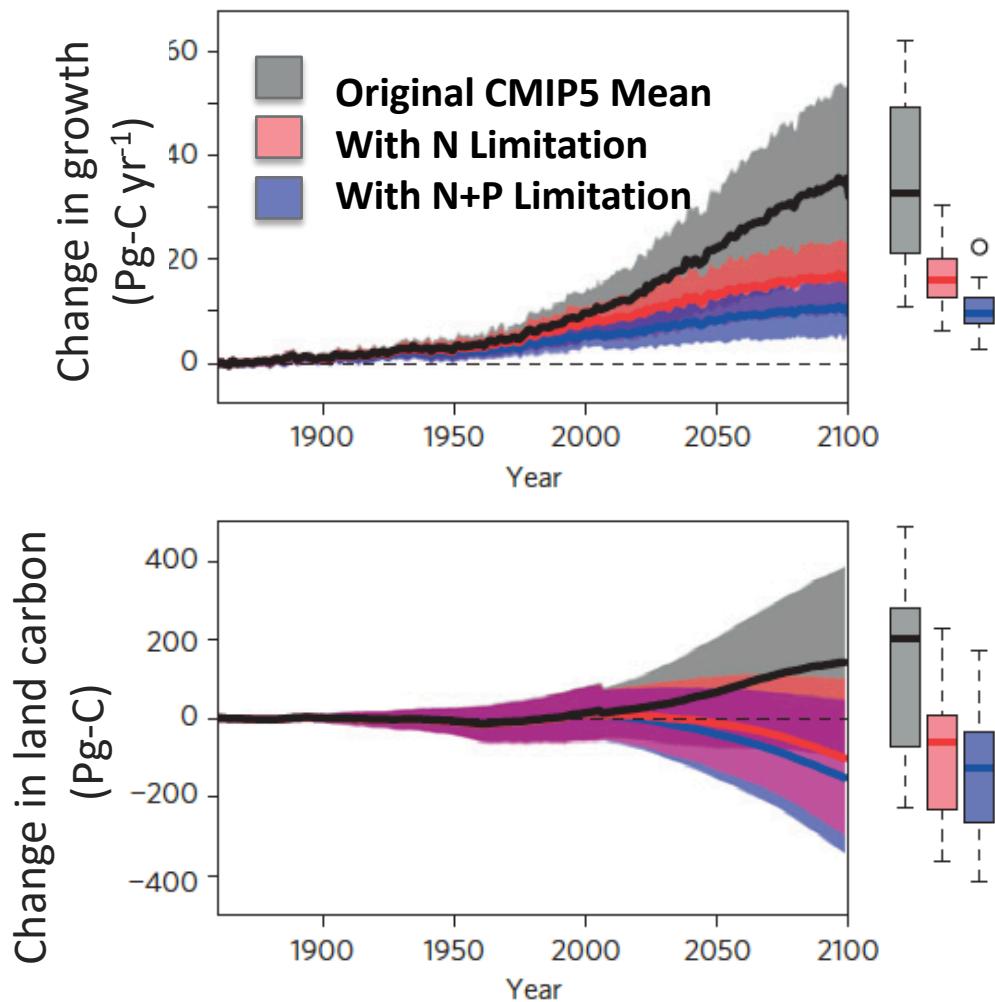
... plant productivity was limited by C:N:P?

... temperature sensitivity of soil decay was uncertain?

Nutrient limited plants lowers land carbon estimates in Earth system models.



Growth (g) =
minimum of
Model and C:N:P



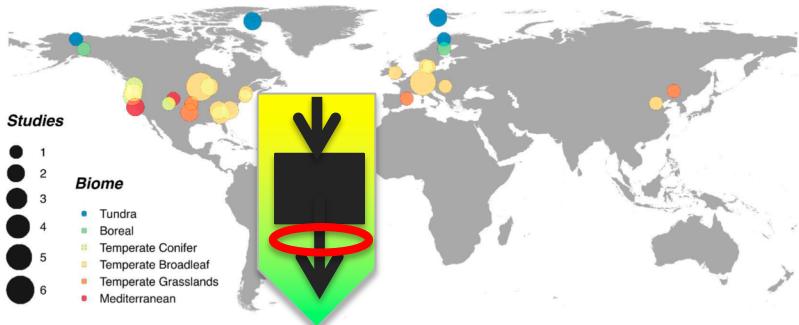
Soil carbon uncertainty from temperature response under estimated in Earth system models.



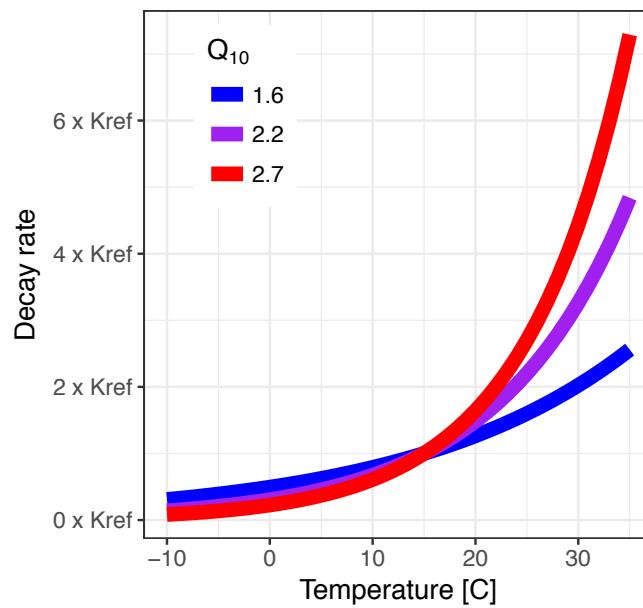
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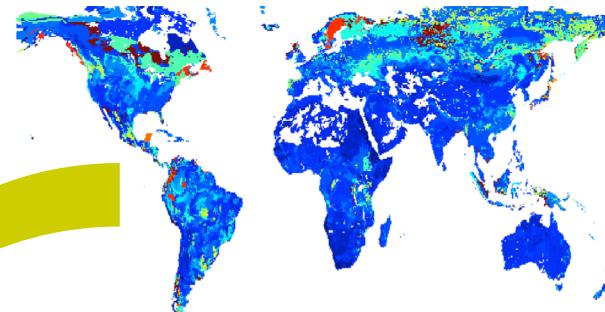
36 field warming experiments



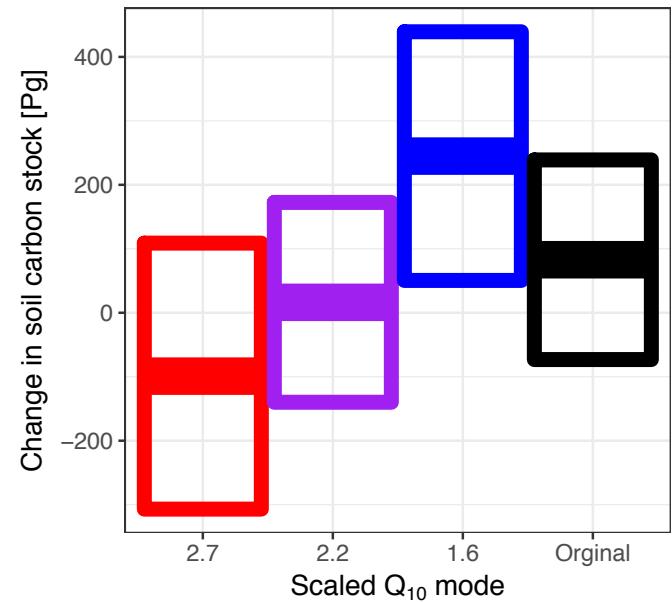
Field temperature sensitivity



20 Earth system models (CMIP5)



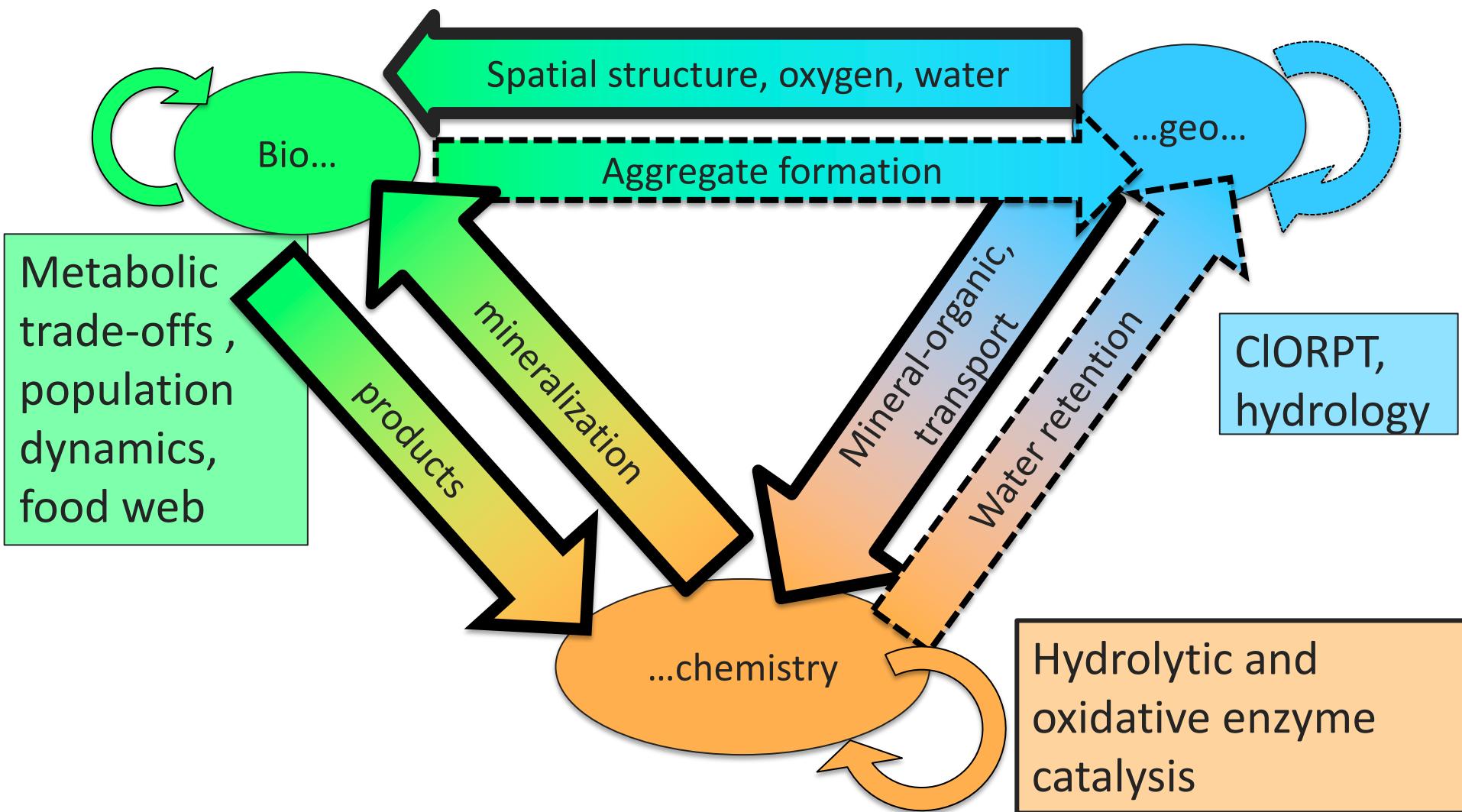
Soil carbon loss with modified Q_{10}



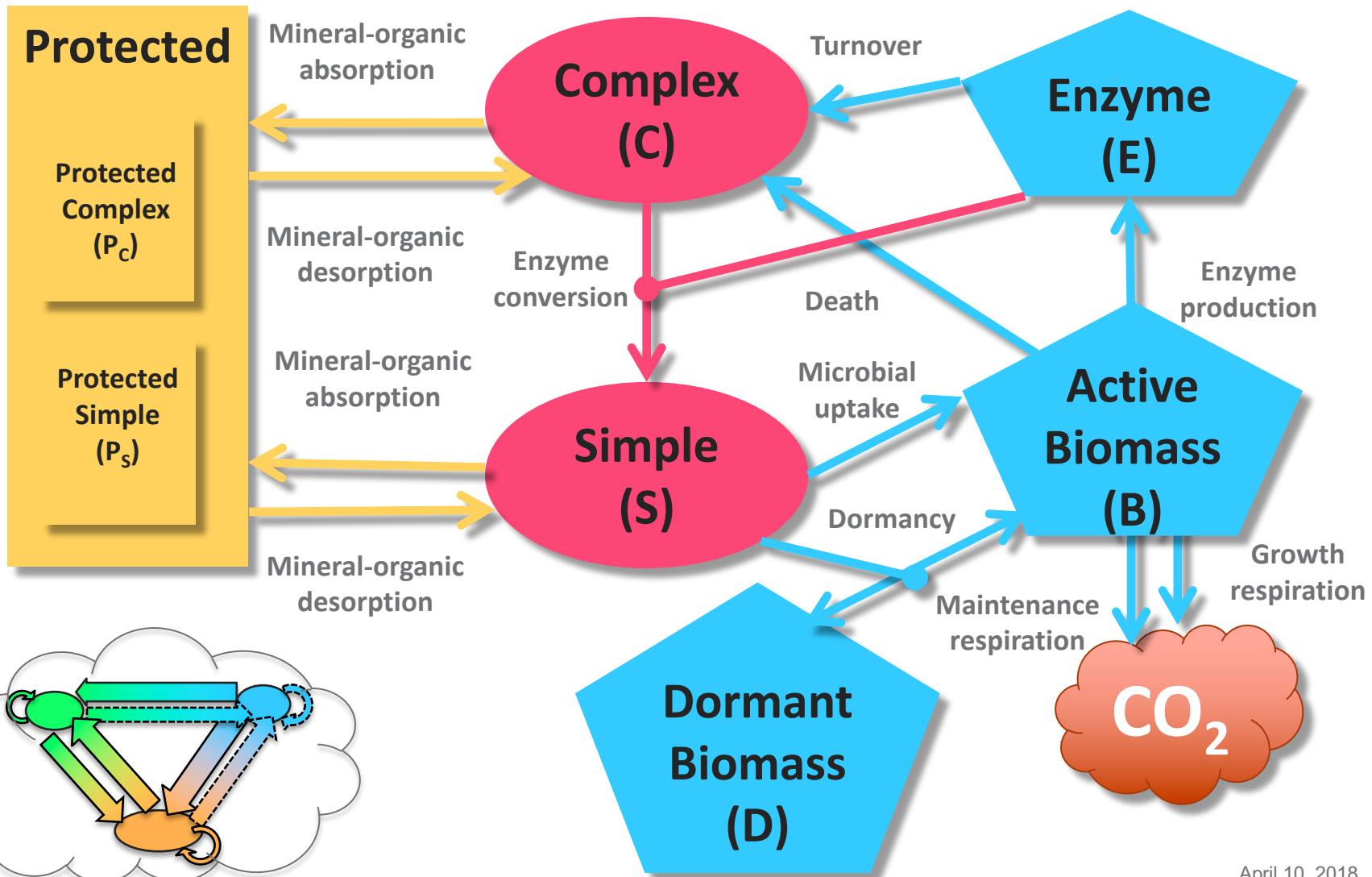
Crowther, Todd-Brown, et al. *Nature*. 2017

Todd-Brown, Zheng, Crowther, *Biogeosciences* (in review)

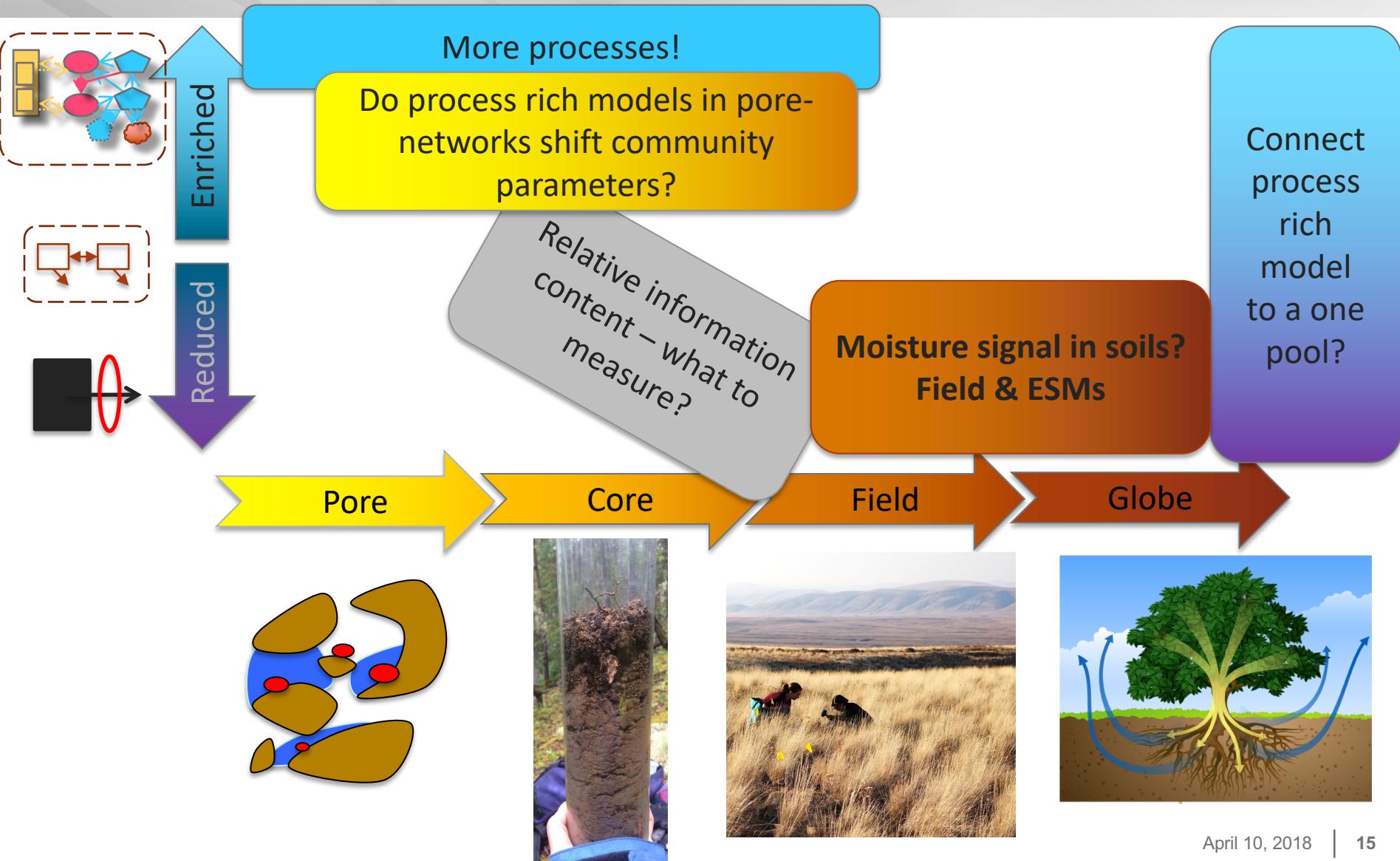
Soil carbon dynamics governed by biological, chemical and geophysical processes.



New models try to capture more explicit process complexity with wider data potential.

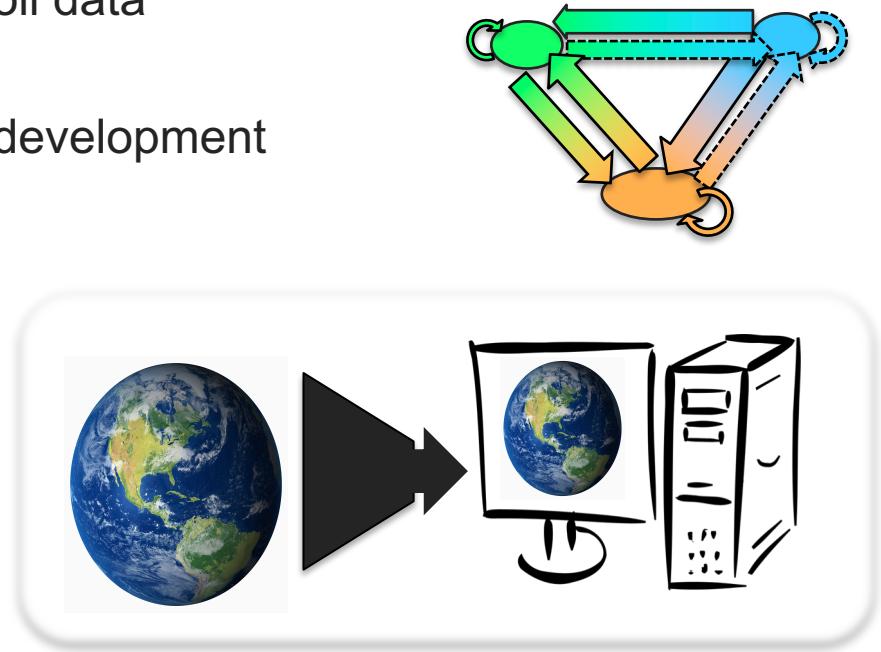


Future work integrating data and models across complexity in soils.



Mathematical and informatics bridging soil observation and Earth system models at UL

- ▶ Undergraduate and graduate research projects
 - Aggregation and harmonization of soil data
 - Model-data integration
 - Model evaluation, comparison, and development
- ▶ Coursework offering
 - Data management and informatics
 - Soil biogeochemistry
 - Earth system science
 - Applied model development
- ▶ Targeted funders
 - NERC: soil security, critical zone research, math and informatics for ‘omics, Earth system modeling strategy
 - EPSRC: continuum mathematics, mathematical biology, non-linear systems
 - EU-collaborators and US-collaborators (NSF, DOE)



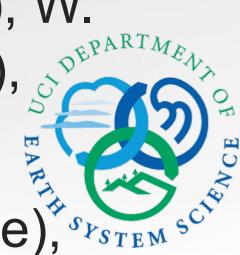


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Acknowledgements

- ▶ ESM SOC analysis: James Randerson (UCI), Steven Allison (UCI), W. Mac Post (ORNL), Charles Tarnocai (AAFC), E. Ted Schuur (NAU), and CMIP5 modelers (9 institutes)
- ▶ ESM post-hoc analysis: Tom Crowther (NIOO), Mark Bradford (Yale), Will Wieder (NCAR), Cory Cleveland (U Montana), Bin Zheng (PNNL), and data providers (40 institutes)
- ▶ Process explicit models: Vanessa Bailey (PNNL), Nancy Hess (PNNL), Tim Scheibe (PNNL), Jeremy Zucker (PNNL), Peyton Smith (PNNL), Matthew Smith (Microsoft), Josh Schimel (UCSB), Melanie Mayes (ORNL), Julie Jastrow (ANL), Stefano Manzoni (Stockholm U), Jennifer Talbot (BU)



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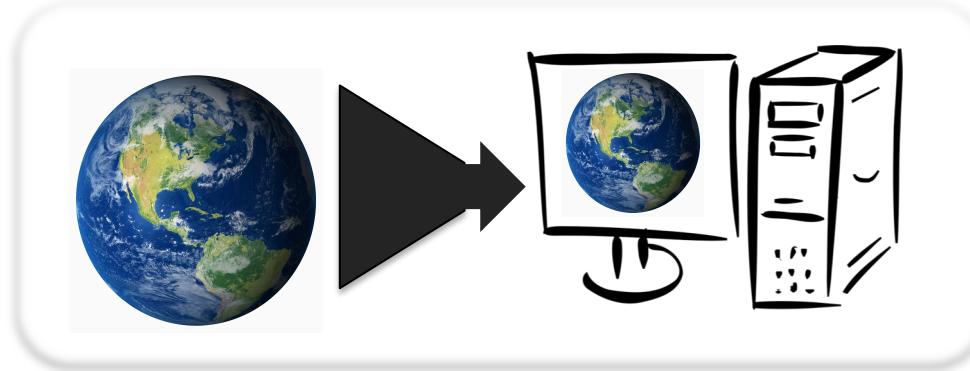
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Scaling complexity in soil carbon models

Predictions of future soil carbon stock in Earth system models



Reducing model complexity

Mathematical cleverness

Model-data integration

Enriching model complexity

Refine assumptions

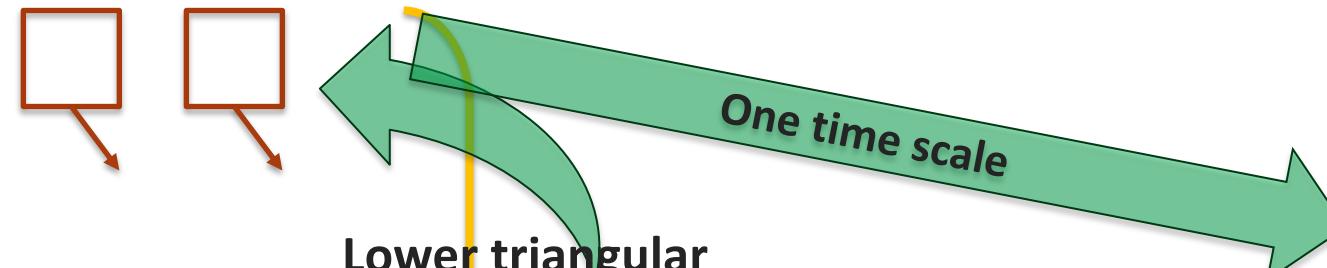
New experimental opportunities

Complexity in space-time

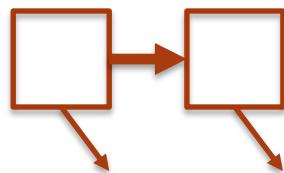
Soil carbon as a one pool model when inputs approximate outputs or (in some cases) single timescale.

Independent

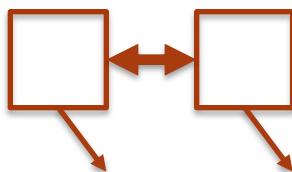
$$\frac{dC}{dt} = u(t)\mathbf{b} - KAC(t)$$



Cascade



Feedback



Lower triangular
is a diagonalizable
matrix

KA is an M-matrix
Input approx. output

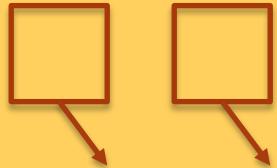
Reduced
Complexity
One pool



Soil carbon models fall into three classes; independent, cascade, and feedback.

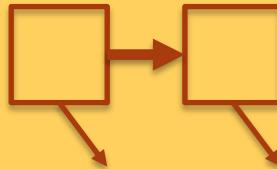
Independent

Diagonal matrix



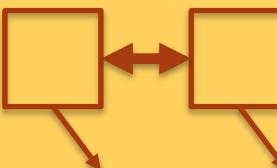
Cascade

Lower triangular matrix



Feedback

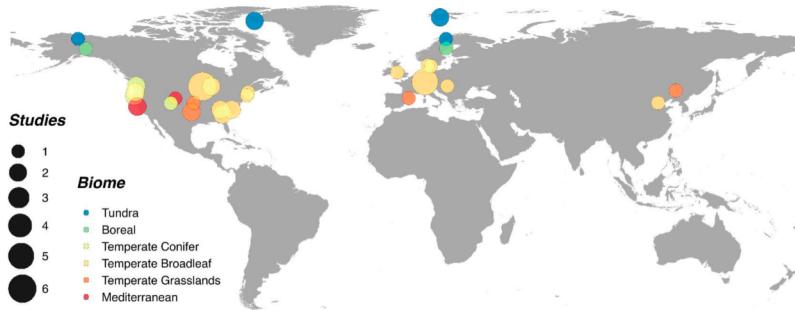
Dense matrix



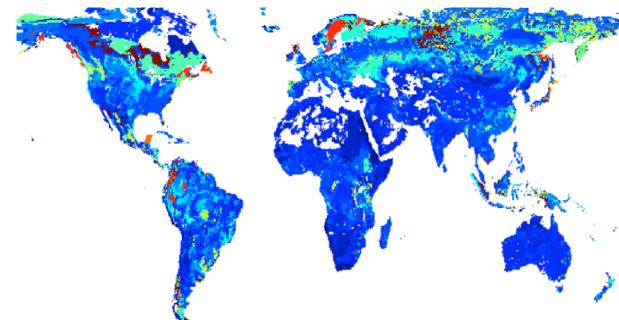
$$\frac{dC}{dt} = u(t)b - KAC(t)$$

Derive field Q_{10} from soil carbon, shift ESM Q_{10} , and recalculate new SOC shift.

36 field warming experiments

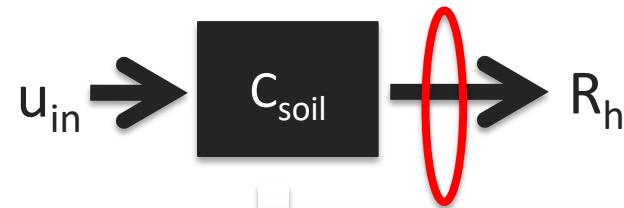


20 Earth system models (CMIP5)



Crowther, Todd-Brown, et al. *Nature*. 2017

Reduced complexity model at quasi-steady state



$$u_{in} = C_{soil} k Q_{10}^{(T-15)/10}$$

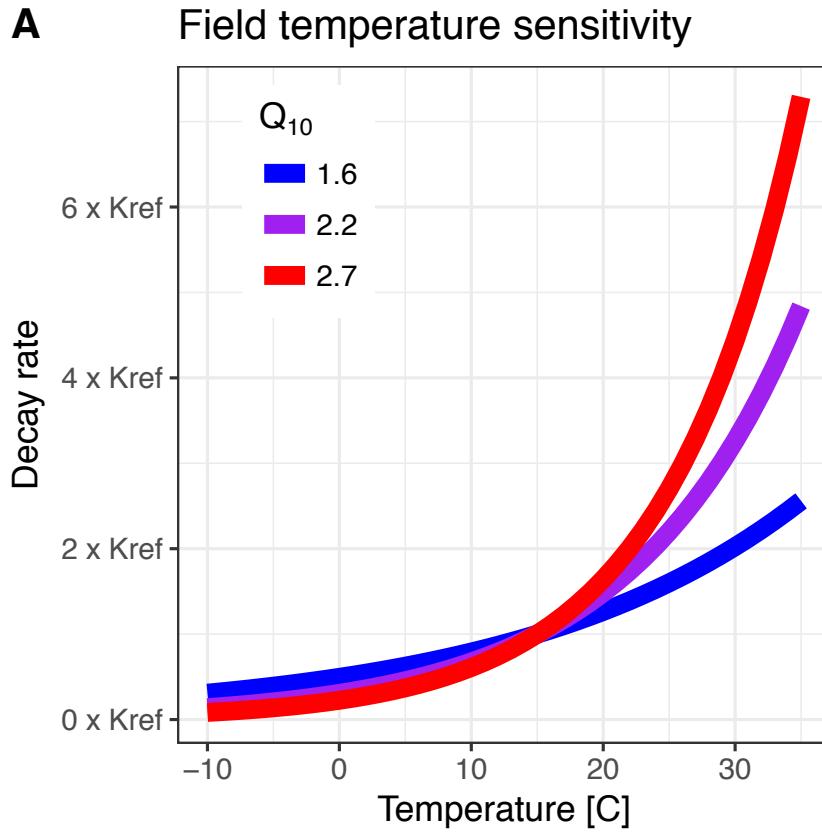
Intrinsic
decomposition rate

Temperature
sensitivity

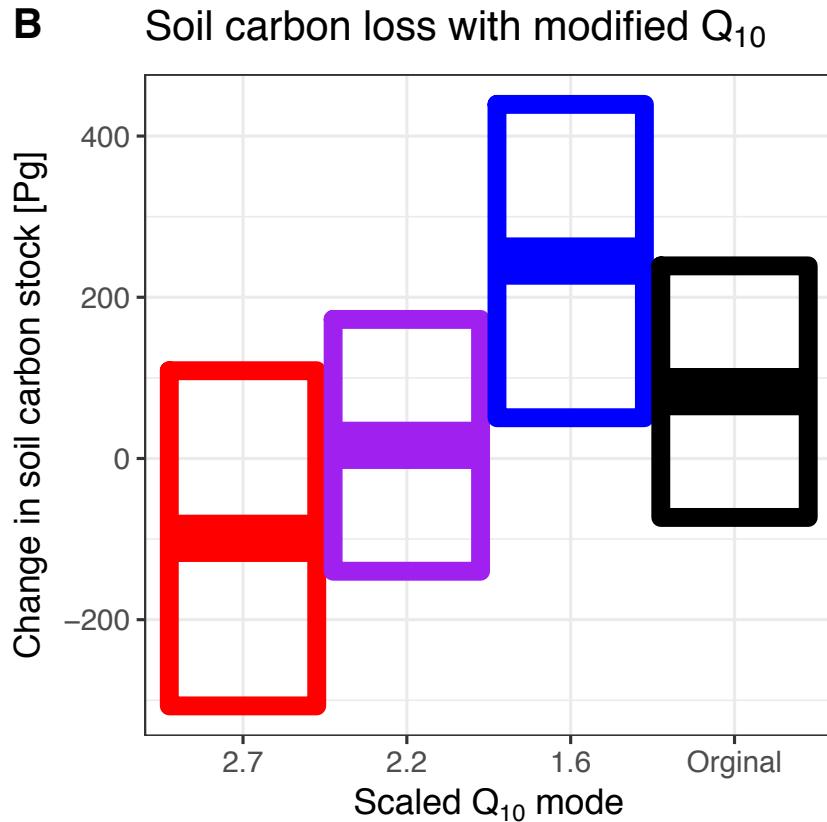
Todd-Brown, Zheng, Crowther, *Biogeosciences* (in submission)

Data- Q_{10} uncertainty led to high ESM-dSOC variation.

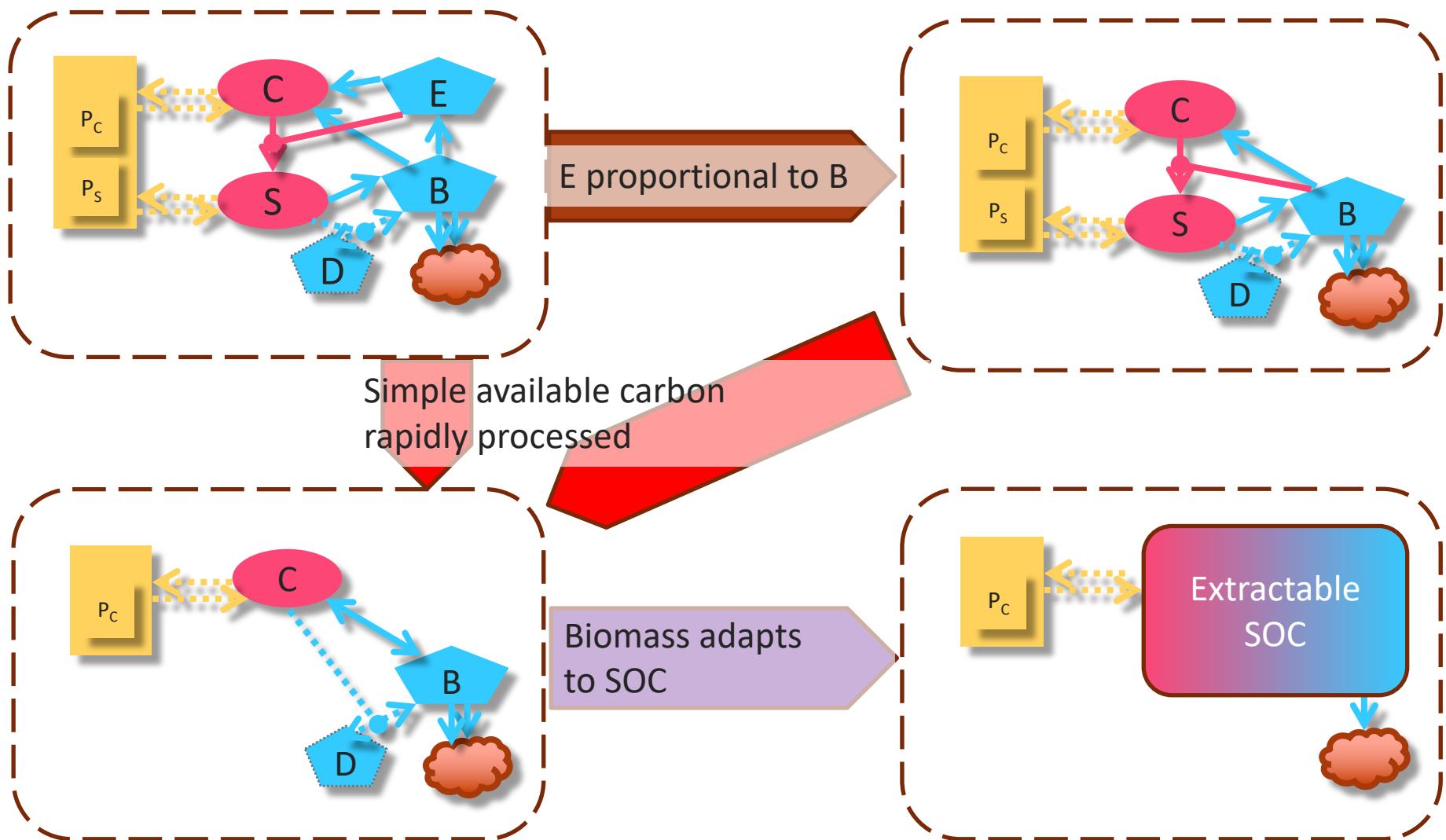
A



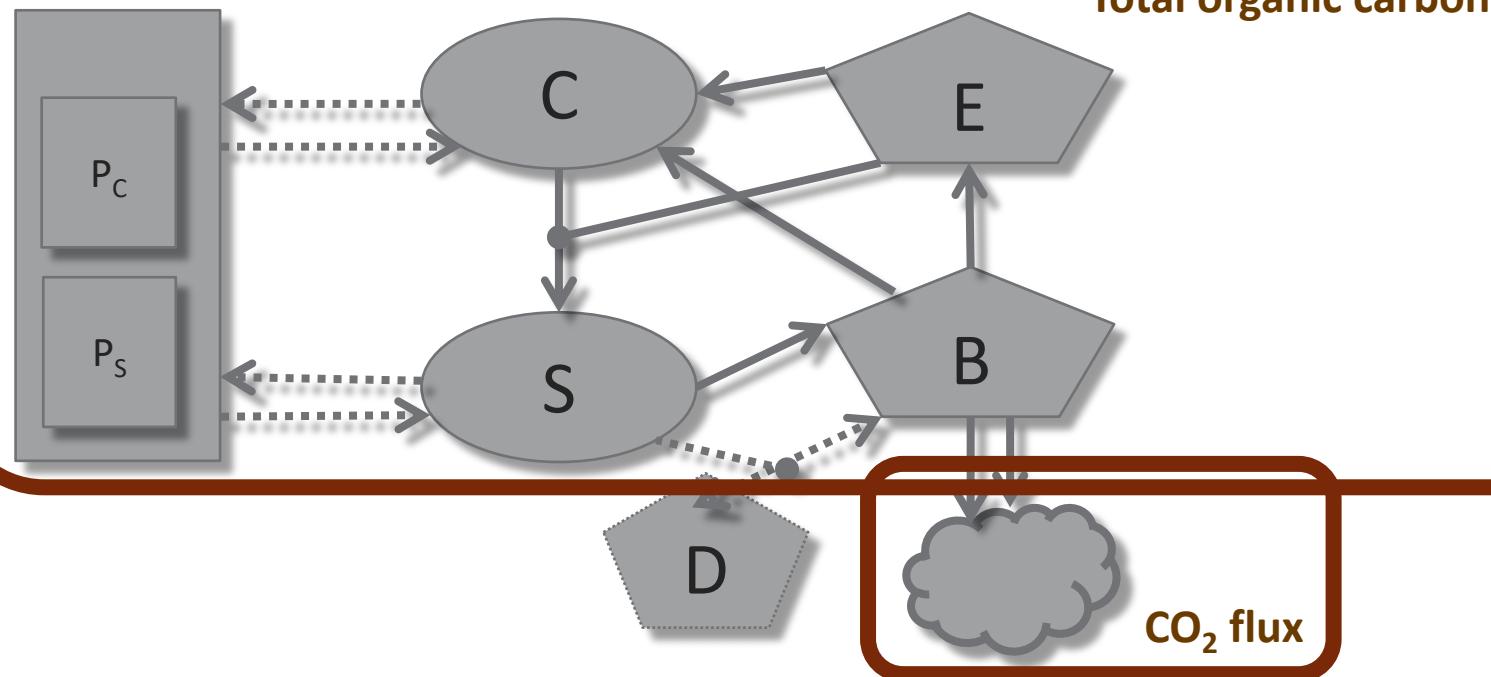
B



A reasonable set of assumptions linking process-rich and reduced complexity:



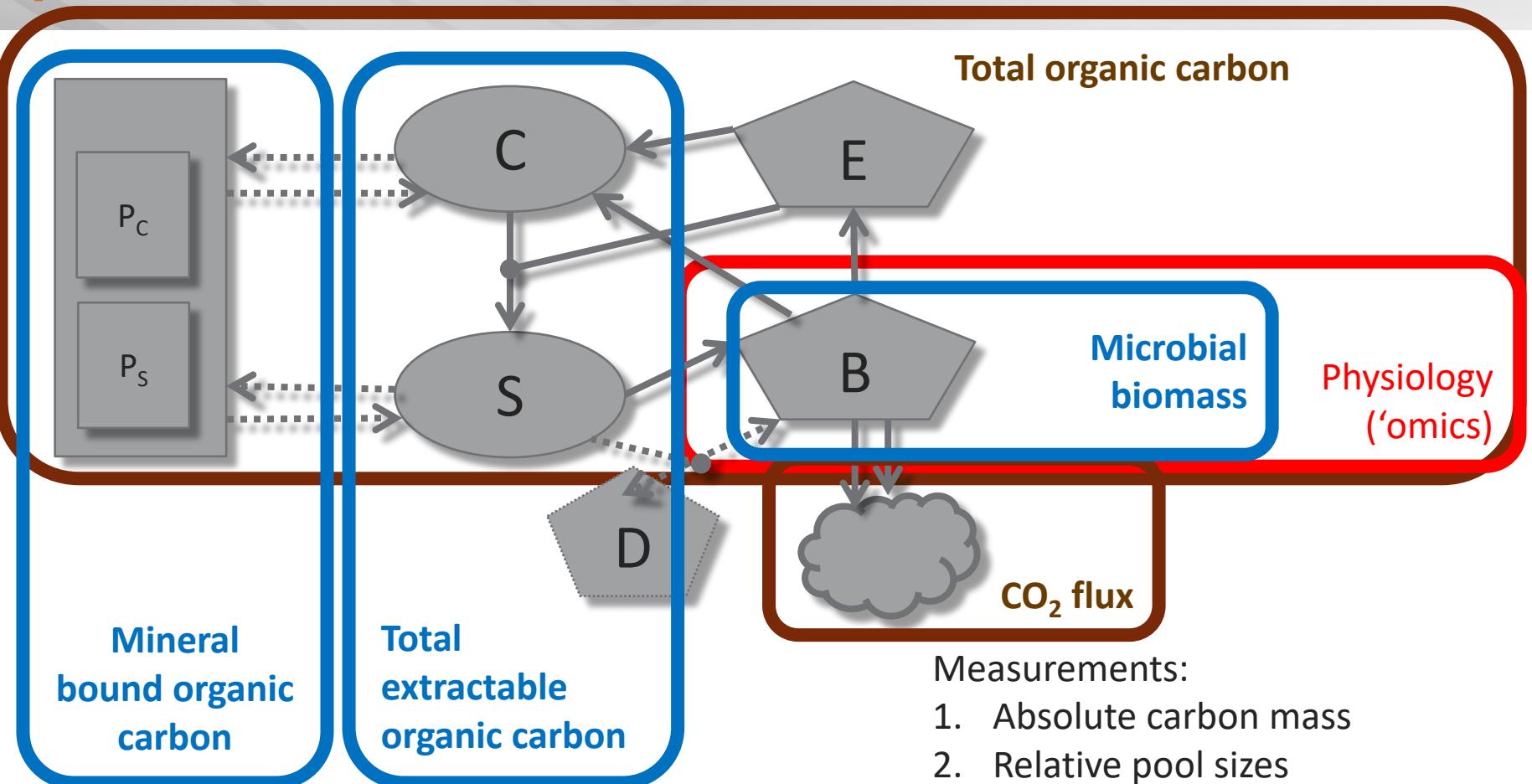
The promise of data integration in process-rich models.



Measurements:

1. Absolute carbon mass
- 2.
- 3.
4. Carbon pool age
- 5.

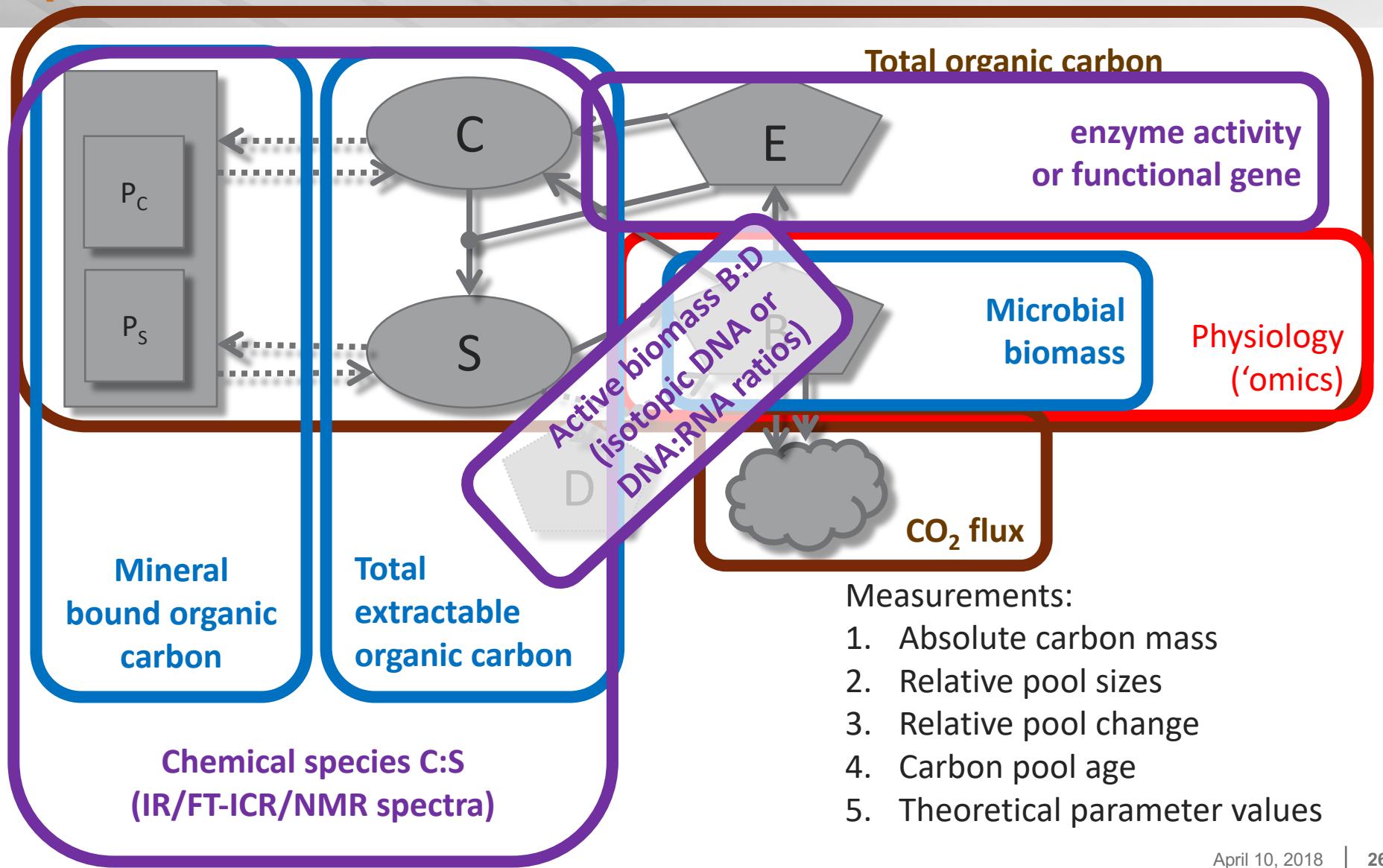
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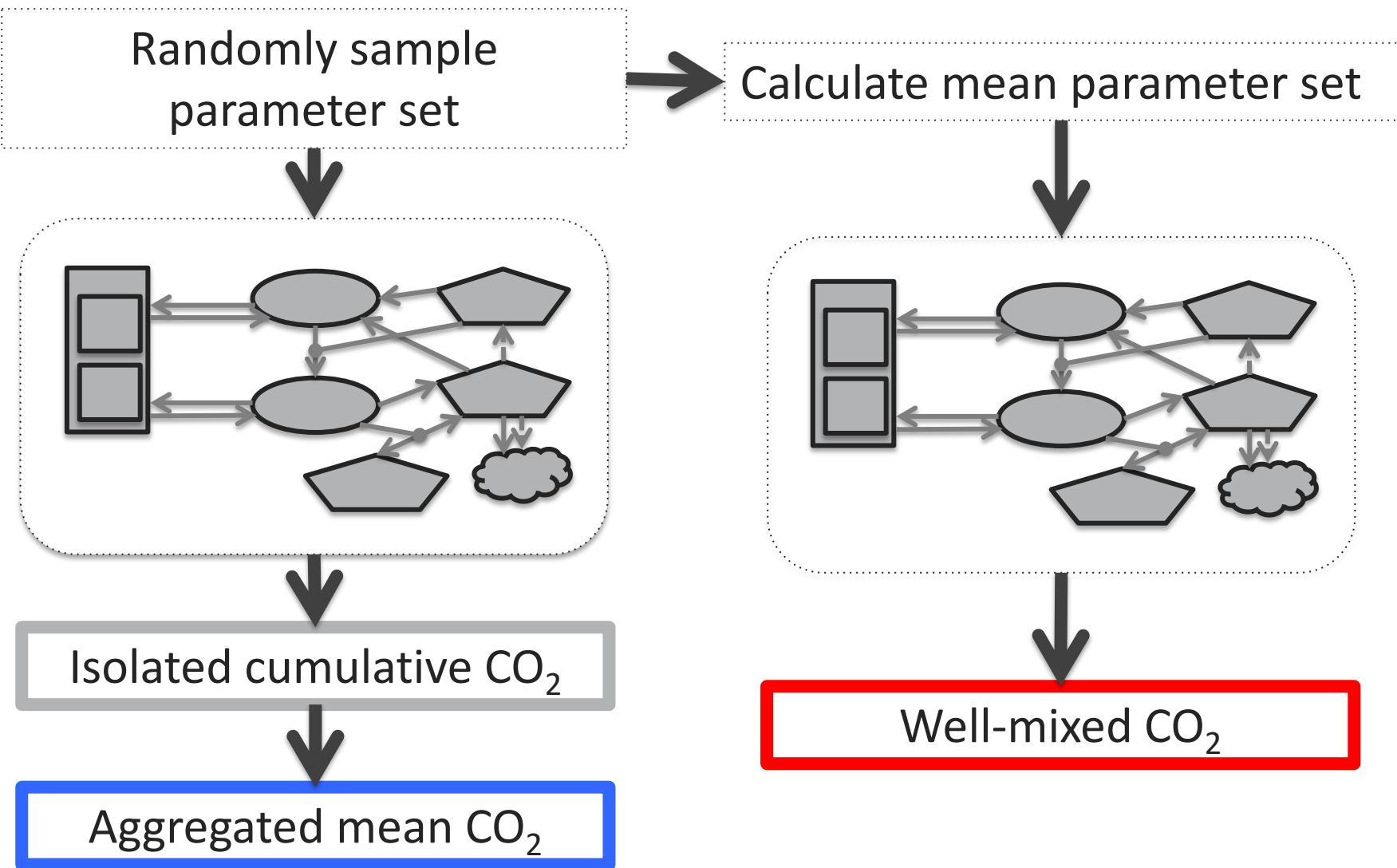
Measurements:

1. Absolute carbon mass
2. Relative pool sizes
3. Relative pool change
4. Carbon pool age
5. Theoretical parameter values

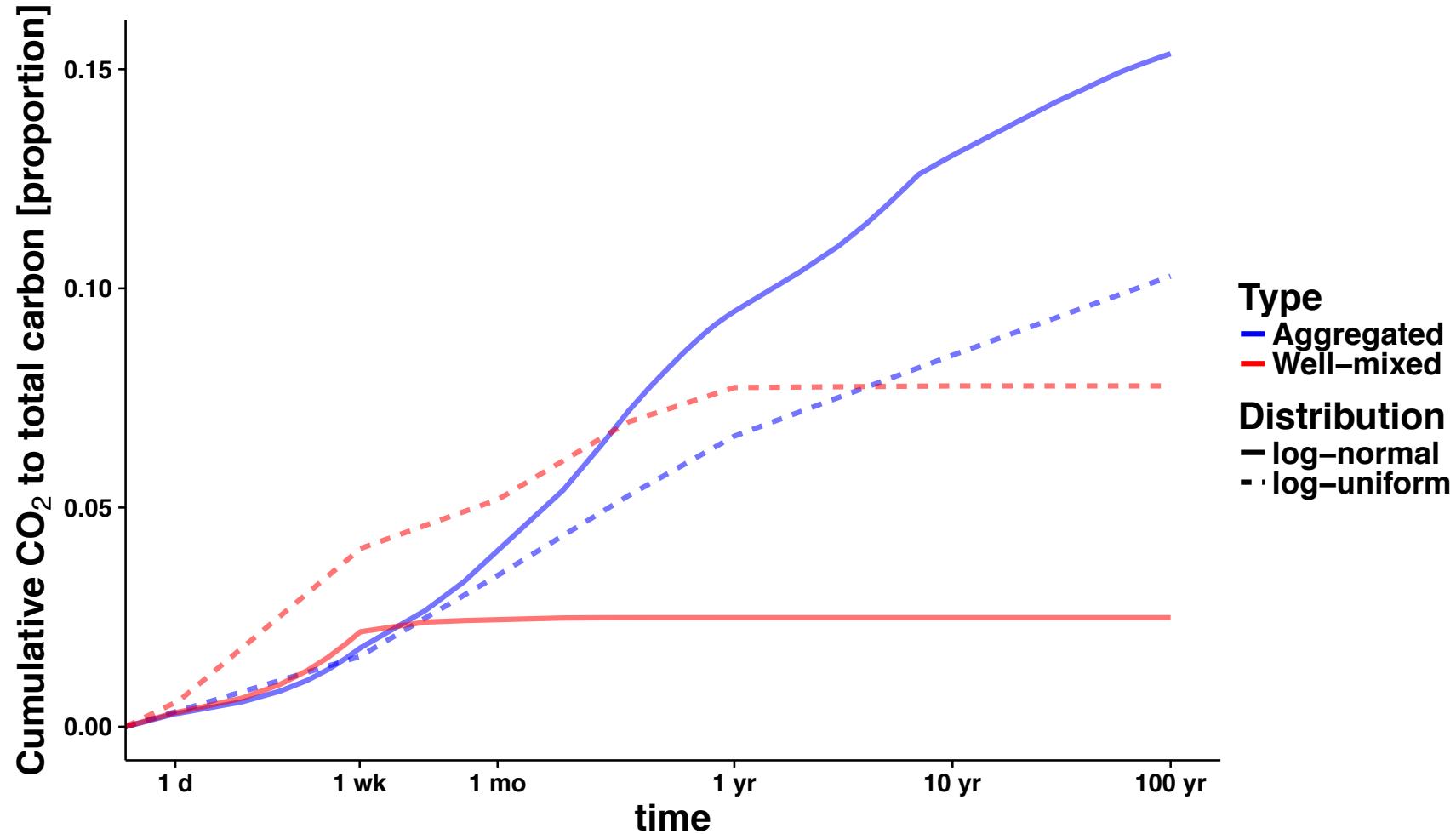
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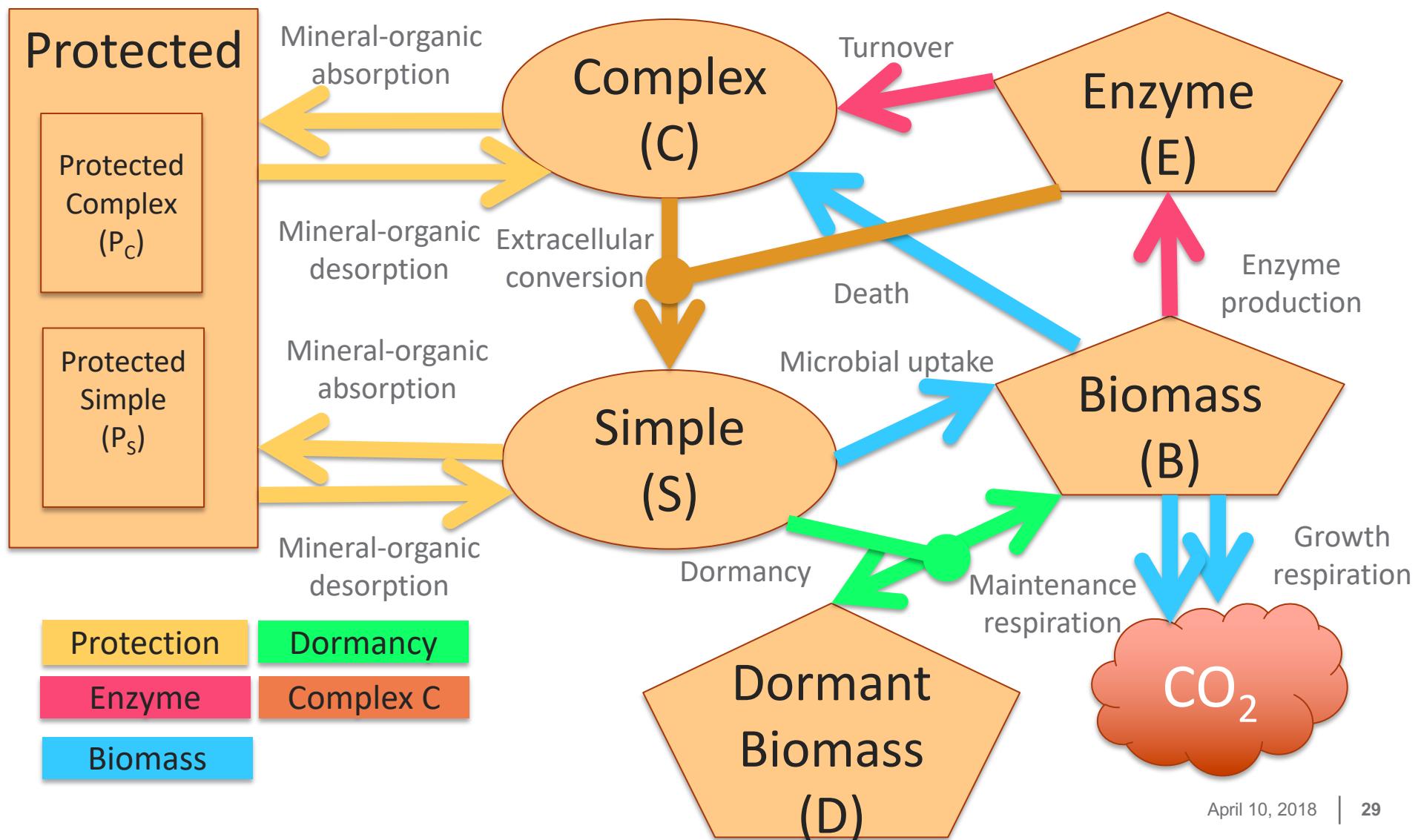
Well-mixed vs aggregated isolated pores simulations...



Measuring means is not enough, parameter distribution also matters.



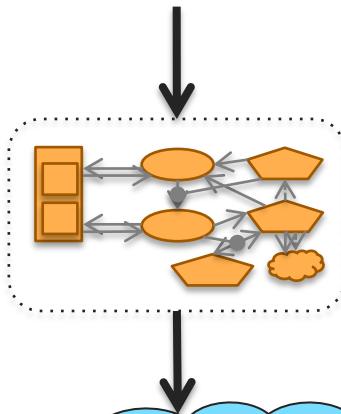
Just Another Microbial (JAM) model integrates biotic and abiotic processes



Sensitivity of cumulative CO₂ to parameter perturbations...

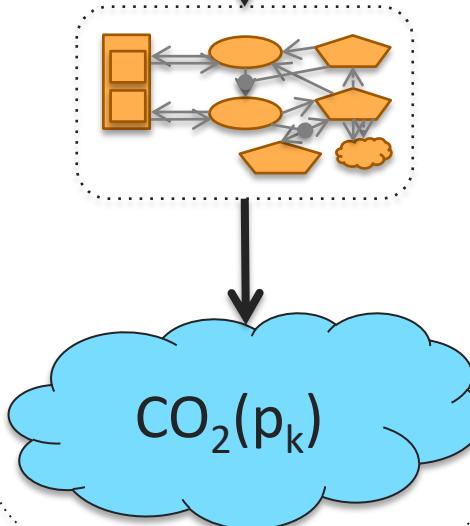
Perturbed parameter set

$$p_i = (p_1 + \varepsilon, \dots, p_{23})$$



Parameter set

$$p_k = (p_1, \dots, p_{23})$$



CO₂ response to perturbation

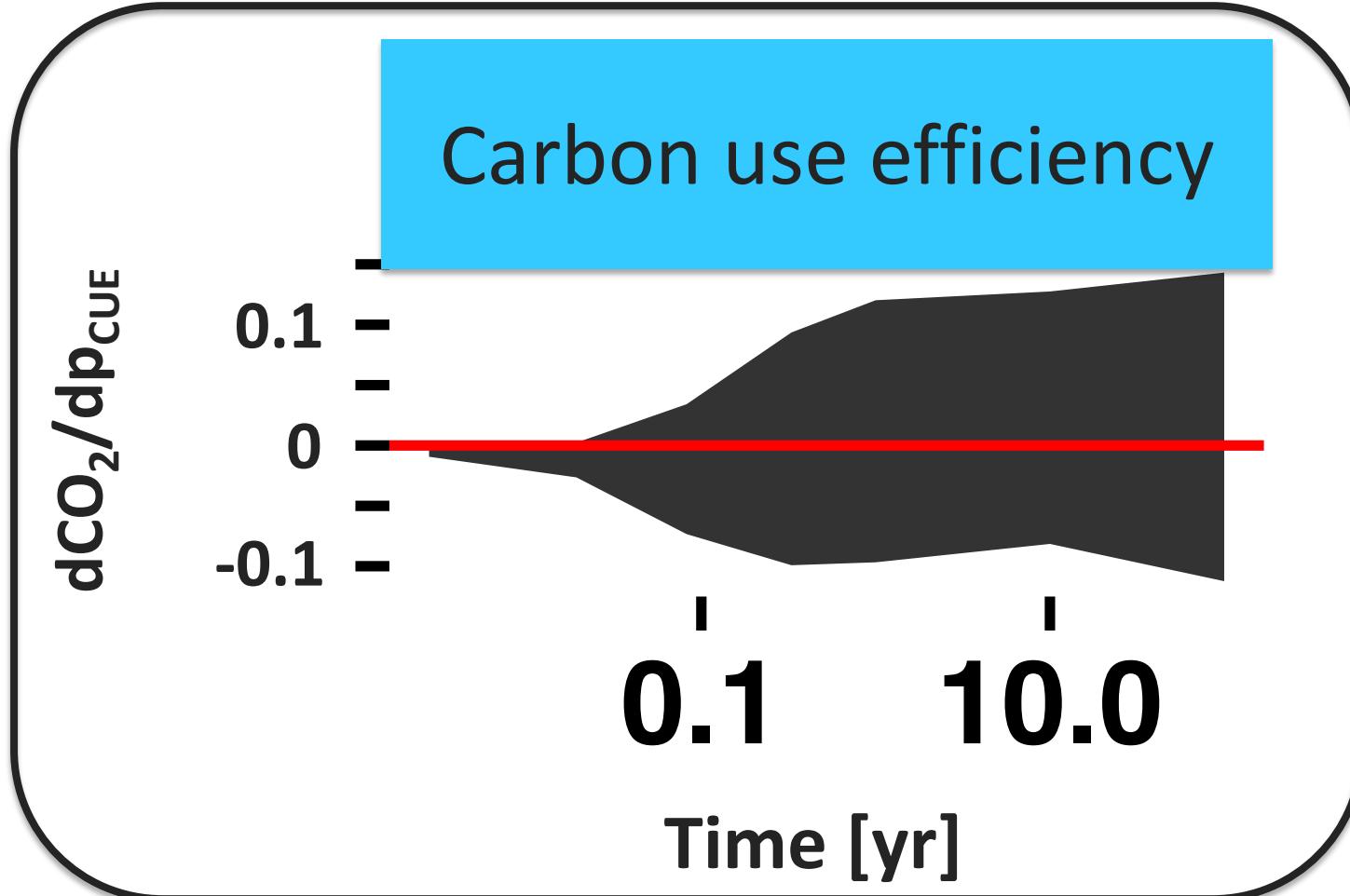
$$\frac{dCO_2}{dp_1} =$$

$$= \frac{[C_{CO_2}(p_i) - C_{CO_2}(p_k)] / \sum_i C_i}{\varepsilon / p_1 \text{ range}}$$

1 unit = a parameter shift over the parameter range
drives 100% increase in cumulative CO₂

Direction of effect of parameter on CO₂ depends on other parameters (e.g. CUE).

Sensitivity of cumulative CO₂ to parameter perturbation (95% CI)



Biological parameters are good targets for 'easy' model improvements.

Sensitivity of cumulative CO₂ to parameter perturbation (95% CI)

