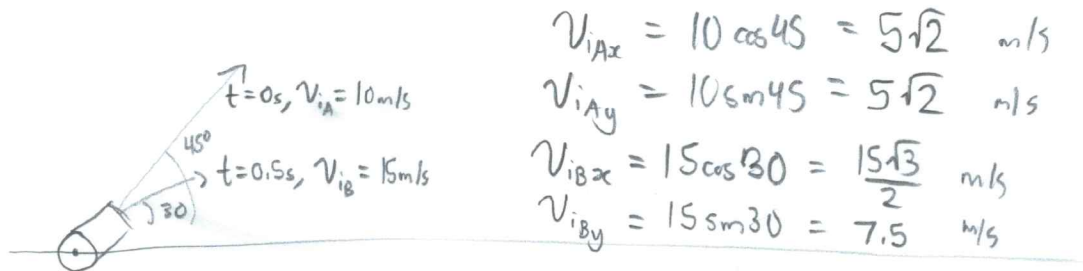


Marks by feel. Multiple approaches. This is probably the simplest.

## Question 2

A cannon on infinitely flat ground is going to fire 2 balls. At time  $t = 0$  seconds, ball A is fired with a speed of  $10\text{m/s}$  [ $45^\circ$  above horizontal]. At time  $t = 0.5$  seconds, ball B is fired with a speed of  $15\text{m/s}$  [ $30^\circ$  above horizontal]. Show whether or not the two balls ever collide in mid-air.

Briefly explain what you are doing/finding at each significant step so that I can understand what's going on when I mark this.[6]



$$v_{iAx} = 10 \cos 45 = 5\sqrt{2} \text{ m/s}$$

$$v_{iAy} = 10 \sin 45 = 5\sqrt{2} \text{ m/s}$$

$$v_{iBx} = 15 \cos 30 = \frac{15\sqrt{3}}{2} \text{ m/s}$$

$$v_{iBy} = 15 \sin 30 = 7.5 \text{ m/s}$$

First we will see where A is after 0.5secs, in the x.

$$\text{Find } d_{Ax(0.5s)} = v_{iAx} \cos 45^\circ \Delta t = 10 \cos 45 (0.5) = \frac{5\sqrt{2}}{2} \text{ m}$$

$$d_{Ay(0.5s)} = v_{iAy} \sin 45^\circ \Delta t = 10 \sin 45 (0.5) = \frac{5\sqrt{2}}{2} \text{ m}$$

Now we can see if these balls collide in the x.

In the x

$$\begin{aligned} & \text{B} \rightarrow \frac{5\sqrt{2}}{2} \text{ m} \quad \text{A} \rightarrow \quad \Rightarrow d_{Bx} = d_{Ax} + \frac{5\sqrt{2}}{2} \\ & \Rightarrow \frac{15\sqrt{3}}{2} \Delta t = 5\sqrt{2} \Delta t + \frac{5\sqrt{2}}{2} \\ & \Rightarrow 5.919 \Delta t = \frac{5\sqrt{2}}{2} \Rightarrow \Delta t_{\text{needed for x collision}} = 0.597 \text{ s} \end{aligned}$$

Note this is after  $t = 0.5\text{s}$ .

So this is technically at  $t = 1.097\text{s}$ .

In the y

We have the  $\Delta t$  needed for the x to collide, Just sub this into the y distances for A and B and see if they collide at the same y height. So  $t = 1.097\text{s}$ .

$$\Delta d_{Ay(1.097s)} = v_{iAy} \Delta t + \frac{1}{2} a \Delta t^2 = 13.654 \text{ m}$$

$$\Delta d_{By(0.597s)} = v_{iBy} \Delta t + \frac{1}{2} a \Delta t^2 = 7.209 \text{ m}$$

$\Delta d_{Ay} \neq \Delta d_{By}$ ,  
thus no collision ever.