\overline{NARC} , PATH

5.210 k_same_partition

DESCRIPTION LINKS GRAPH

Origin

Derived from same_partition and from k_same.

Constraint

k_same_partition(SETS, PARTITIONS)

Types

VARIABLES : collection(var-dvar)
VALUES : collection(val-int)

Arguments

SETS : collection(set - VARIABLES)
PARTITIONS : collection(p - VALUES)

Restrictions

```
\begin{array}{l} \textbf{required}(\texttt{VARIABLES}, \texttt{var}) \\ | \texttt{VARIABLES}| \geq 1 \\ | \texttt{VALUES}| \geq 1 \\ | \textbf{required}(\texttt{VALUES}, \texttt{val}) \\ | \textbf{distinct}(\texttt{VALUES}, \texttt{val}) \\ | \textbf{required}(\texttt{SETS}, \texttt{set}) \\ | \texttt{SETS}| > 1 \\ | \textbf{same\_size}(\texttt{SETS}, \texttt{set}) \\ | \textbf{required}(\texttt{PARTITIONS}, \texttt{p}) \\ | \texttt{PARTITIONS}| \geq 2 \end{array}
```

Purpose

Given a collection of |SETS| sets, each containing the same number of domain variables, the k_same_partition constraint forces a same_partition constraint between each pair of consecutive sets.

Example

```
\left(\begin{array}{c} \left\langle\begin{array}{c} \mathtt{set} - \left\langle1, 2, 6, 3, 1, 2\right\rangle, \\ \mathtt{set} - \left\langle6, 6, 2, 3, 1, 3\right\rangle, \\ \mathtt{set} - \left\langle2, 2, 2, 1, 1, 1\right\rangle \end{array}\right), \\ \left\langle\mathtt{p} - \left\langle1, 3\right\rangle, \mathtt{p} - \left\langle4\right\rangle, \mathtt{p} - \left\langle2, 6\right\rangle\right\rangle \end{array}\right)
```

The first argument SETS of the k_same_partition constraint corresponds to 3 collections of variables, while the second argument PARTITIONS defines the 3 sets of values $\{1,3\},\{4\}$ and $\{2,6\}$. The k_same_partition constraint holds since:

- The first and second collections of variables are assigned 3 values in the $\{1,3\}$ as well as 3 values in $\{2,6\}$.
- The second and third collections of variables are also assigned 3 values in the {1,3} as well as 3 values in {2,6}.

Typical

|VARIABLES| > 1

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Symmetries

- Items of SETS are permutable.
- Items of SETS.set are permutable.
- Items of PARTITIONS are permutable.
- Items of PARTITIONS.p are permutable.

• An occurrence of a value of SETS.set.var can be replaced by any other value that also belongs to the same partition of PARTITIONS.

Arg. properties

Contractible wrt. SETS.

See also common keyword: k_same (system of constraints).

implies: k_used_by_partition.

part of system of constraints: same_partition.
used in graph description: same_partition.

Keywords characteristic of a constraint: sort based reformulation, partition.

combinatorial object: permutation.

constraint type: system of constraints, decomposition.

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Arc input(s)	SETS
Arc generator	$PATH \mapsto collection(set1, set2)$
Arc arity	2
Arc constraint(s)	<pre>same_partition(set1.set, set2.set, PARTITIONS)</pre>
Graph property(ies)	NARC = SETS - 1

Graph model

Parts (A) and (B) of Figure 5.464 respectively show the initial and final graph associated with the **Example** slot. To each vertex corresponds a collection of variables, while to each arc corresponds a same_partition constraint.

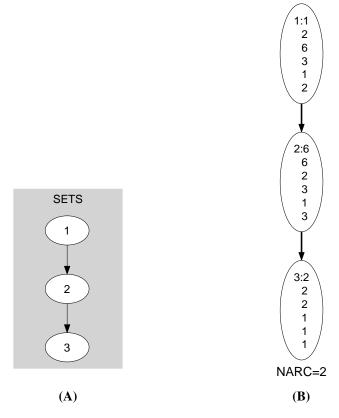


Figure 5.464: Initial and final graph of the k_same_partition constraint

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