## 5.308 ordered\_atmost\_nvector

DESCRIPTION	LINKS	GRAPH
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Origin

Conjoin atmost\_nvector and lex\_chain\_lesseq.

Constraint

ordered\_atmost\_nvector(NVEC, VECTORS)

**Synonyms** 

ordered\_atmost\_nvectors, ordered\_atmost\_npoint, ordered\_atmost\_npoints.

Type

VECTOR : collection(var-dvar)

Arguments

NVEC : dvar
VECTORS : collection(vec - VECTOR)

Restrictions

```
\begin{split} |\texttt{VECTOR}| &\geq 1 \\ \texttt{NVEC} &\geq \texttt{min}(1, |\texttt{VECTORS}|) \\ \texttt{required}(\texttt{VECTORS}, \texttt{vec}) \\ \texttt{same\_size}(\texttt{VECTORS}, \texttt{vec}) \end{split}
```

Enforces the following two conditions:

- 1. The number of distinct tuples of values taken by the vectors of the collection VECTORS is less than or equal to NVEC. Two tuples of values  $\langle A_1, A_2, \dots, A_m \rangle$  and  $\langle B_1, B_2, \dots, B_m \rangle$  are *distinct* if and only if there exist an integer  $i \in [1, m]$  such that  $A_i \neq B_i$ .
- 2. For each pair of consecutive vectors  $\operatorname{VECTOR}_i$  and  $\operatorname{VECTOR}_{i+1}$  of the  $\operatorname{VECTORS}$  collection we have that  $\operatorname{VECTOR}_i$  is lexicographically less than or equal to  $\operatorname{VECTOR}_{i+1}$ . Given two vectors,  $\vec{X}$  and  $\vec{Y}$  of n components,  $\langle X_0, \ldots, X_{n-1} \rangle$  and  $\langle Y_0, \ldots, Y_{n-1} \rangle$ ,  $\vec{X}$  is lexicographically less than or equal to  $\vec{Y}$  if and only if n=0 or  $X_0 < Y_0$  or  $X_0 = Y_0$  and  $\langle X_1, \ldots, X_{n-1} \rangle$  is lexicographically less than or equal to  $\langle Y_1, \ldots, Y_{n-1} \rangle$ .

Purpose

 $\left(\begin{array}{c} \mathtt{vec} - \langle 5, 6 \rangle \,, \\ \mathtt{vec} - \langle 9, 3 \rangle \,, \end{array}\right)$ 

 $vec - \langle 9, 3 \rangle$ 

Example

The ordered\_atmost\_nvector constraint holds since:

- 1. The collection VECTORS involves at most 3 distinct tuples of values (i.e., in fact the 2 distinct tuples (5,6) and (9,3)).
- $2. \ \ The \ vectors \ of \ the \ collection \ \ VECTORS \ are \ sorted \ in \ increasing \ lexicographical \ order.$

**Typical** 

```
\begin{split} |\text{VECTOR}| &> 1 \\ \text{NVEC} &> 1 \\ \text{NVEC} &< |\text{VECTORS}| \\ |\text{VECTORS}| &> 1 \end{split}
```

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Symmetry NVEC can be increased.

Arg. properties

Contractible wrt. VECTORS.

Reformulation The ordered\_atmost\_nvector constraint can be reformulated as a conjunction of a

atmost\_nvector and a lex\_chain\_lesseq constraints.

See also common keyword: nvector (vector).

comparison swapped: ordered\_atleast\_nvector.

implied by: ordered\_nvector ( $\leq$  NVEC replaced by = NVEC).

implies: atmost\_nvector, lex\_chain\_lesseq(NVEC of constraint

ordered\_atmost\_nvector removed).

used in graph description: lex\_less, lex\_lesseq.

**Keywords characteristic of a constraint:** vector.

constraint type: counting constraint, order constraint.

**symmetry:** symmetry.

Arc input(s)	VECTORS
Arc generator	$PATH \mapsto collection(vectors1, vectors2)$
Arc arity	2
Arc constraint(s)	${\tt lex\_lesseq}({\tt vectors1.vec}, {\tt vectors2.vec})$
<b>Graph property(ies)</b>	NARC =  VECTORS  - 1
Arc input(s)	VECTORS
Arc input(s) Arc generator	VECTORS  PATH → collection(vectors1, vectors2)
•	
Arc generator	$PATH \mapsto collection(vectors1, vectors2)$

## **Graph model**

Parts (A) and (B) of Figure 5.646 respectively show the initial and final graph of the second graph constraint associated with the **Example** slot. Since we use the **NCC** graph property in this second graph constraint, we show the different connected components of the final graph. Each strongly connected component corresponds to a tuple of values that is assigned to some vectors of the VECTORS collection. The 2 following tuple of values  $\langle 5,6 \rangle$  and  $\langle 9,3 \rangle$  are used by the vectors of the VECTORS collection.

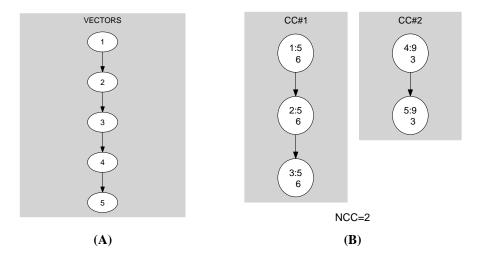


Figure 5.646: Initial and final graph of the ordered\_atmost\_nvector constraint

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