

5.146 elements

	DESCRIPTION	LINKS	GRAPH
Origin	Derived from <a href="#">element</a> .		
Constraint	<code>elements(ITEMS, TABLE)</code>		
Arguments	ITEMS : <code>collection(index=<a href="#">dvar</a>, value=<a href="#">dvar</a>)</code> TABLE : <code>collection(index=<a href="#">int</a>, value=<a href="#">dvar</a>)</code>		
Restrictions	<code>required(ITEMS, [index, value])</code> <code>ITEMS.index ≥ 1</code> <code>ITEMS.index ≤  TABLE </code> <code>required(TABLE, [index, value])</code> <code>TABLE.index ≥ 1</code> <code>TABLE.index ≤  TABLE </code> <code>distinct(TABLE, index)</code>		
Purpose	All the items of ITEMS should be equal to one of the entries of the table TABLE.		
Example	<div><math display="block">\left( \begin{array}{l} \langle \text{index} - 4 \text{ value} - 9, \text{index} - 1 \text{ value} - 6 \rangle, \\ \left\langle \begin{array}{ll} \text{index} - 1 &amp; \text{value} - 6, \\ \text{index} - 2 &amp; \text{value} - 9, \\ \text{index} - 3 &amp; \text{value} - 2, \\ \text{index} - 4 &amp; \text{value} - 9 \end{array} \right\rangle \end{array} \right)</math></div> <p>The <code>elements</code> constraint holds since each item of its first argument ITEMS corresponds to an item of the TABLE collection: the first item <code>⟨index - 4 value - 9⟩</code> of ITEMS corresponds to the fourth item of TABLE, while the second item <code>⟨index - 1 value - 6⟩</code> of ITEMS corresponds to the first item of TABLE.</p>		
Typical	<code> ITEMS  &gt; 1</code> <code><a href="#">range</a>(ITEMS.index) &gt; 1</code> <code> TABLE  &gt; 1</code> <code><a href="#">range</a>(TABLE.value) &gt; 1</code>		
Symmetries	<ul style="list-style-type: none"><li>• Items of ITEMS are <a href="#">permutable</a>.</li><li>• Items of TABLE are <a href="#">permutable</a>.</li><li>• All occurrences of two distinct values in ITEMS.value or TABLE.value can be <a href="#">swapped</a>; all occurrences of a value in ITEMS.value or TABLE.value can be <a href="#">renamed</a> to any unused value.</li></ul>		
Arg. properties	<a href="#">Functional dependency</a> : ITEMS.value determined by ITEMS.index and TABLE.		

<b>Usage</b>	Used for replacing several <code>element</code> constraints sharing exactly the same table by a single constraint.
<b>Reformulation</b>	<p>The <code>elements(&lt;index - <math>I_1</math> value - <math>V_1</math>, index - <math>I_2</math> value - <math>V_2</math>, ..., index - <math>I_{ ITEMS }</math> value - <math>V_{ ITEMS }</math>&gt;, TABLE)</code> constraint can be expressed in term of a conjunction of <math> ITEMS </math> <code>elem</code> constraints of the form:</p> <pre> elem(&lt;index - <math>I_1</math> value - <math>V_1</math>&gt;, TABLE), elem(&lt;index - <math>I_2</math> value - <math>V_2</math>&gt;, TABLE), ... elem(&lt;index - <math>I_{ ITEMS }</math> value - <math>V_{ ITEMS }</math>&gt;, TABLE).</pre>
<b>See also</b>	<p><b>implied by:</b> <code>elem</code>, <code>elements_alldifferent</code>.</p> <p><b>part of system of constraints:</b> <code>elem</code>, <code>element</code>.</p>
<b>Keywords</b>	<p><b>constraint arguments:</b> pure functional dependency.</p> <p><b>constraint type:</b> data constraint, system of constraints.</p> <p><b>filtering:</b> arc-consistency.</p> <p><b>modelling:</b> table, shared table, functional dependency.</p>
<b>Cond. implications</b>	<pre> elements(ITEMS, TABLE)   with distinct(ITEMS, index)   and TABLE.value ≥ 0   implies bin_packing_capa(TABLE, ITEMS).</pre>

Arc input(s)	ITEMS TABLE
Arc generator	<i>PRODUCT</i> $\mapsto$ <i>collection</i> (items, table)
Arc arity	2
Arc constraint(s)	<ul style="list-style-type: none"><li>• items.index = table.index</li><li>• items.value = table.value</li></ul>
Graph property(ies)	<u>NARC</u> =  ITEMS

**Graph model** Parts (A) and (B) of Figure 5.337 respectively show the initial and final graph associated with the **Example** slot. Since we use the **NARC** graph property, the arcs of the final graph are stressed in bold.

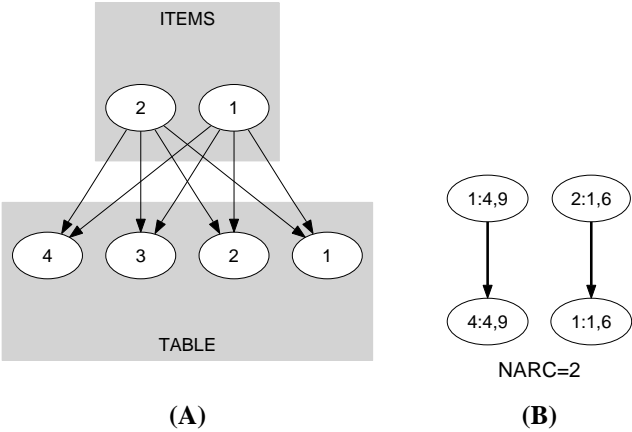


Figure 5.337: Initial and final graph of the `elements` constraint

**Signature** Since all the `index` attributes of `TABLE` collection are distinct and because of the first condition `items.index = table.index` of the arc constraint, a source vertex of the final graph can have at most one successor. Therefore `|ITEMS|` is the maximum number of arcs of the final graph and we can rewrite `NARC = |ITEMS|` to `NARC ≥ |ITEMS|`. So we can simplify NARC to NARC.

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