1662 <u>ORDER</u>, CLIQUE

5.251 maximum_modulo

DESCRIPTION LINKS GRAPH

Origin Derived from maximum.

Constraint maximum_modulo(MAX, VARIABLES, M)

Arguments MAX : dvar

VARIABLES : collection(var-dvar)

M : int

Restrictions |VARIABLES| > 0

M > 0

required(VARIABLES, var)

Purpose MAX is a maximum value of the collection of domain variables VARIABLES according to

the following partial ordering: $(X \mod M) < (Y \mod M)$.

Example (5, (9, 1, 7, 6, 5), 3)

The maximum_modulo constraint holds since its first argument MAX is set to value 5, where $5 \bmod 3 = 2$ is greater than or equal to all the expressions $9 \bmod 3 = 0$,

 $1 \mod 3 = 1$, $7 \mod 3 = 1$ and $6 \mod 3 = 0$.

Typical M > 1

M <maxval(VARIABLES.var)</pre>

 $|{\tt VARIABLES}| > 1$

 ${\tt range}({\tt VARIABLES.var}) > 1$

Symmetry Items of VARIABLES are permutable.

Arg. properties

Functional dependency: MAX determined by VARIABLES and M.

See also comparison swapped: minimum_modulo.

specialisation: maximum (variable mod constant replaced by variable).

Keywords characteristic of a constraint: modulo, maximum.

 ${\color{red} \textbf{constraint arguments:}} \ \textbf{pure functional dependency.}$

constraint type: order constraint.
modelling: functional dependency.

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Arc input(s) VARIABLES

Arc generator CLIQUE → collection (variables1, variables2)

Arc arity 2

Arc constraint(s) V ( variables1.key = variables2.key, variables1.var mod M > variables2.var mod M )

Graph property(ies) ORDER(0, MININT, var) = MAX
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Graph model

Parts (A) and (B) of Figure 5.546 respectively show the initial and final graph associated with the **Example** slot. Since we use the **ORDER** graph property, the vertex of rank 0 (without considering the loops) of the final graph is outlined with a thick circle.

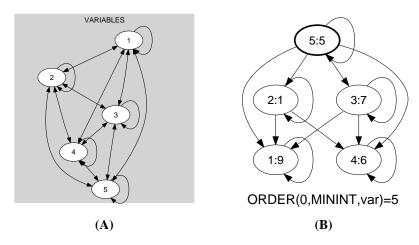


Figure 5.546: Initial and final graph of the maximum_modulo constraint