

5.112 decreasing\_valley

DESCRIPTION

LINKS

AUTOMATON

Origin	Derived from <a href="#">valley</a> and <a href="#">decreasing</a> .
Constraint	<code>decreasing_valley(VARIABLES)</code>
Argument	<code>VARIABLES : collection(var-dvar)</code>
Restrictions	$ VARIABLES  > 0$ <code>required(VARIABLES, var)</code>
Purpose	<div>A variable <math>V_k</math> (<math>1 &lt; k &lt; m</math>) of the sequence of variables <math>VARIABLES = V_1, \dots, V_m</math> is a <i>valley</i> if and only if there exists an <math>i</math> (<math>1 &lt; i \leq k</math>) such that <math>V_{i-1} &gt; V_i</math> and <math>V_i = V_{i+1} = \dots = V_k</math> and <math>V_k &lt; V_{k+1}</math>. When considering all the valleys of the sequence <math>VARIABLES</math> from left to right enforce all valleys to be decreasing, i.e. the altitude of each valley is less than or equal to the altitude of its preceding valley when it exists.</div>
Example	<div><code>((1, 7, 6, 8, 3, 7, 3, 3, 5, 4))</code></div>

The `decreasing_valley` constraint holds since the sequence 1 7 **6** 8 **3** 7 **3** 3 5 2 contains three valleys, in bold, that are decreasing.

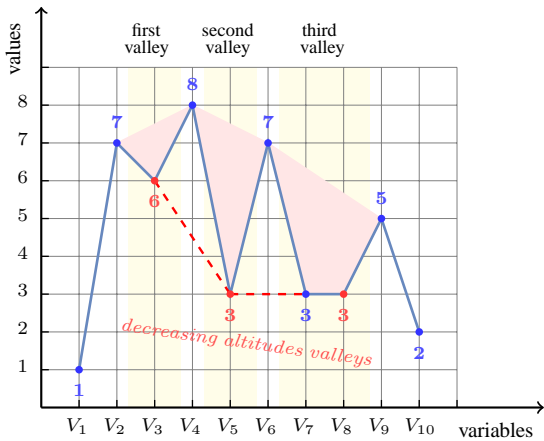


Figure 5.265: Illustration of the **Example** slot: a sequence of ten variables  $V_1, V_2, V_3, V_4, V_5, V_6, V_7, V_8, V_9, V_{10}$  respectively fixed to values 1, 7, 6, 8, 3, 7, 3, 3, 5, 2 and its corresponding three valleys, in red, respectively located at altitudes 6, 3 and 3

Typical

```
|VARIABLES| ≥ 7
range(VARIABLES.var) > 1
valley(VARIABLES.var) ≥ 3
```

Symmetry

One and the same constant can be added to the var attribute of all items of VARIABLES.

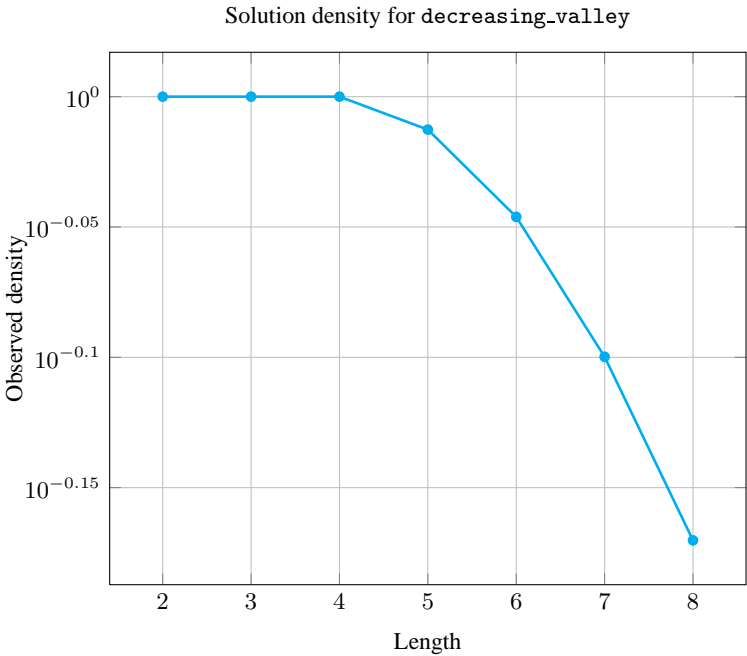
Arg. properties

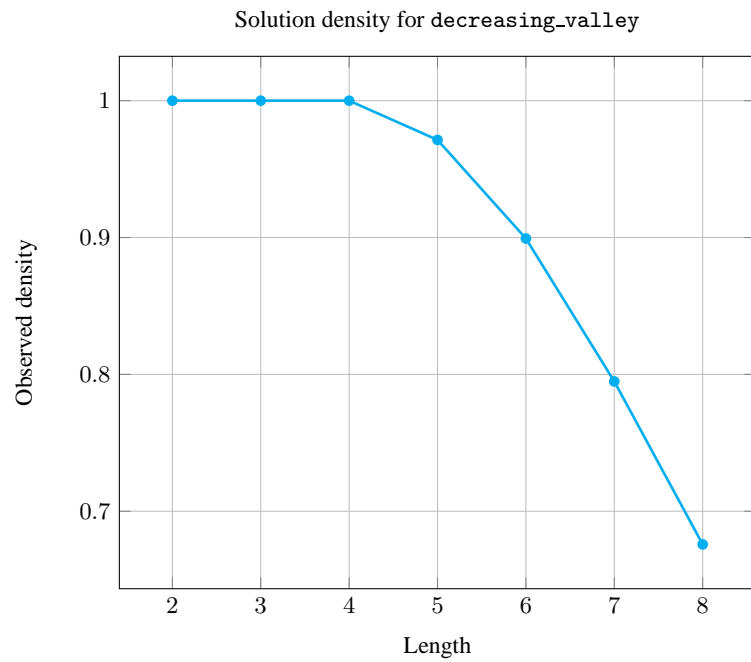
- Prefix-contractible wrt. VARIABLES.
- Suffix-contractible wrt. VARIABLES.

Counting

Length ( <i>n</i> )	2	3	4	5	6	7	8
Solutions	9	64	625	7553	105798	1666878	29090469

Number of solutions for decreasing\_valley: domains 0..*n*



**See also**

**implied by:** [all\\_equal\\_valley](#).

**related:** [increasing\\_valley](#), [valley](#).

**Keywords**

**characteristic of a constraint:** [automaton](#), [automaton with counters](#), [automaton with same input symbol](#).

**combinatorial object:** [sequence](#).

**constraint network structure:** [sliding cyclic\(1\) constraint network\(2\)](#).

**Cond. implications**

```
decreasing-valley(VARIABLES)
  with valley(VARIABLES.var) > 0
  implies not\_all\_equal(VARIABLES).
```

### Automaton

Figure 5.266 depicts the automaton associated with the `decreasing_valley` constraint. To each pair of consecutive variables  $(VAR_i, VAR_{i+1})$  of the collection `VARIABLES` corresponds a signature variable  $S_i$ . The following signature constraint links  $VAR_i$ ,  $VAR_{i+1}$  and  $S_i$ :  $(VAR_i < VAR_{i+1} \Leftrightarrow S_i = 0) \wedge (VAR_i = VAR_{i+1} \Leftrightarrow S_i = 1) \wedge (VAR_i > VAR_{i+1} \Leftrightarrow S_i = 2)$ .

#### STATES SEMANTICS

$s$	: initial stationary or increasing mode	$(\{=   >\}^*)$
$u$	: decreasing (before first potential valley) mode	$(< \{<   =\}^*)$
$v$	: increasing (after a valley) mode	$(> \{>   =\}^*)$
$w$	: decreasing (after a valley) mode	$(< \{<   =\}^*)$

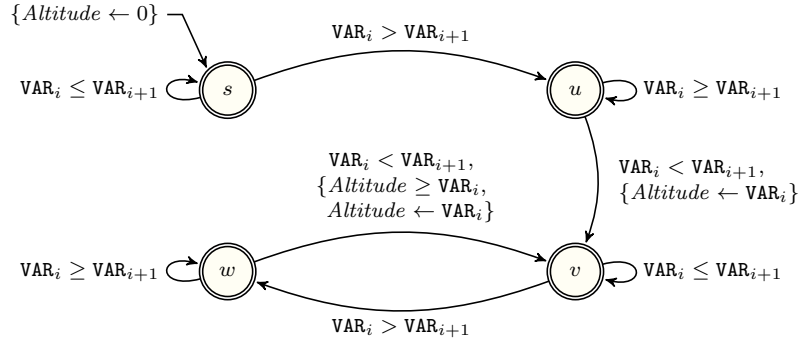


Figure 5.266: Automaton for the `decreasing_valley` constraint (note the conditional transition from state  $w$  to state  $v$  testing that the counter *Altitude* is greater than or equal to  $VAR_i$  for enforcing that all valleys from left to right are in decreasing altitude)

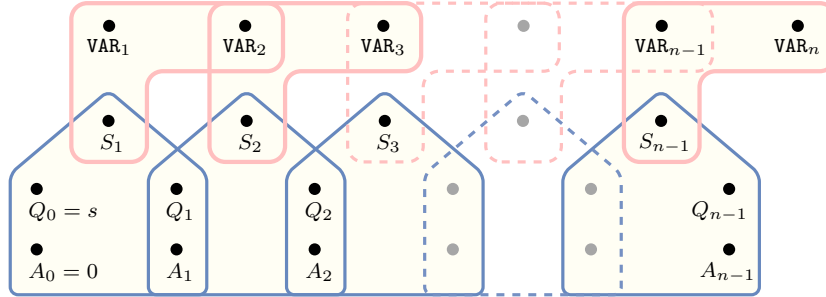


Figure 5.267: Hypergraph of the reformulation corresponding to the automaton of the `decreasing_valley` constraint where  $A_i$  stands for the value of the counter *Altitude* (since all states of the automaton are accepting there is no restriction on the last variable  $Q_{n-1}$ )