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#### deepest\_valley 5.113

**DESCRIPTION LINKS AUTOMATON** 

Origin Derived from valley.

Constraint deepest\_valley(DEPTH, VARIABLES)

Arguments DEPTH : dvar

VARIABLES : collection(var-dvar)

Restriction required(VARIABLES, var)

> A variable  $V_k$  (1 < k < m) of the sequence of variables VARIABLES  $= V_1, \ldots, V_m$ is a valley if and only if there exists an i  $(1 < i \le k)$  such that  $V_{i-1} > V_i$  and  $V_i = V_{i+1} = \cdots = V_k$  and  $V_k < V_{k+1}$ . DEPTH is the minimum value of the valley variables. If no such variable exists DEPTH is equal to the default value MAXINT.

 $(2, \langle 5, 3, 4, 8, 8, 2, 7, 1 \rangle)$  $(7, \langle 1, 3, 4, 8, 8, 8, 7, 8 \rangle)$ 

> The first deepest\_valley constraint holds since 2 is the deepest valley of the sequence  $5\ 3\ 4\ 8\ 8\ 2\ 7\ 1$ .

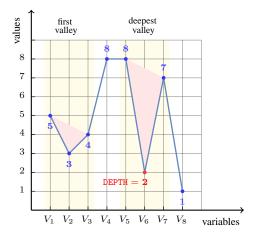


Figure 5.268: Illustration of the first example of the **Example** slot: a sequence of eight variables  $V_1$ ,  $V_2$ ,  $V_3$ ,  $V_4$ ,  $V_5$ ,  $V_6$ ,  $V_7$ ,  $V_8$  respectively fixed to values 5, 3, 4, 8, 8, 2, 7, 1 and its corresponding deepest valley of depth 2

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Typical
                        |VARIABLES| > 2
                        range(VARIABLES.var) > 2
                        valley(VARIABLES.var) > 0
```

**Purpose** 

**Example** 

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Symmetry

Items of VARIABLES can be reversed.

Arg. properties

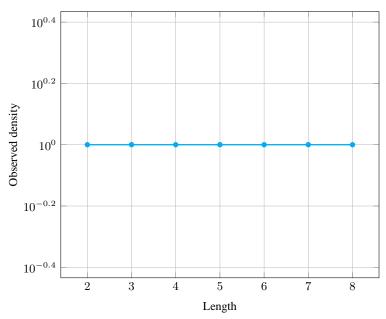
Functional dependency: DEPTH determined by VARIABLES.

# Counting

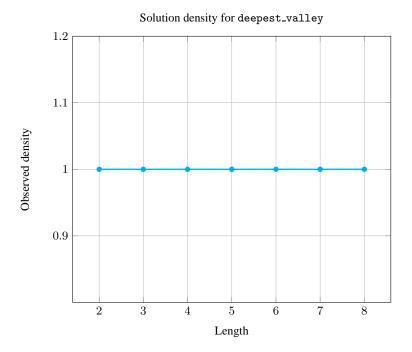
Length (n)	2	3	4	5	6	7	8
Solutions	9	64	625	7776	117649	2097152	43046721

Number of solutions for deepest\_valley: domains 0..n

Solution density for deepest\_valley



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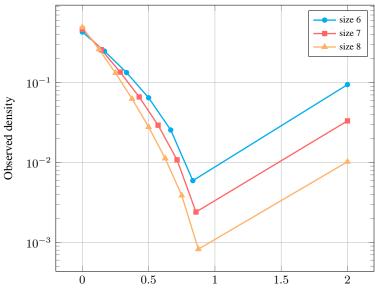


Length (n)			3	4	5	6	7	8
Total		9	64	625	7776	117649	2097152	43046721
Parameter value	0	-	9	176	2900	50472	976227	21133632
	1	-	4	99	1712	29125	540576	11233250
	2	-	1	44	900	15680	283250	5665896
	3	-	-	11	380	7587	138544	2693425
	4	-	-	-	92	3000	61389	1195056
	5	-	-	-	-	697	22632	484020
	6	-	-	-	-	-	5036	166208
	7	-	-	-	-	-	-	35443
	1000000	9	50	295	1792	11088	69498	439791

Solution count for deepest\_valley: domains 0..n

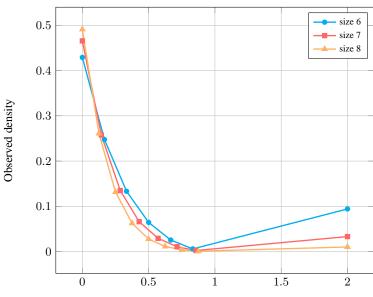
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## Solution density for deepest\_valley



Parameter value as fraction of length

## Solution density for deepest\_valley



Parameter value as fraction of length

See also

common keyword: highest\_peak, valley (sequence).
implies: between\_min\_max.

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Keywords

**characteristic of a constraint:** maxint, automaton, automaton with counters, automaton with same input symbol.

combinatorial object: sequence.

constraint arguments: reverse of a constraint, pure functional dependency.

constraint network structure: sliding cyclic(1) constraint network(2).

filtering: glue matrix.

modelling: functional dependency.

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Automaton

 $\mathtt{VAR}_i = \mathtt{VAR}_{i+1}$ 

Figure 5.269 depicts the automaton associated with the deepest\_valley constraint. To each pair of consecutive variables (VAR $_i$ , VAR $_{i+1}$ ) of the collection VARIABLES corresponds a signature variable  $S_i$ . The following signature constraint links VAR $_i$ , VAR $_{i+1}$  and  $S_i$ :

$$\begin{array}{lll} \mathtt{VAR}_i &< \mathtt{VAR}_{i+1} \Leftrightarrow S_i = 0 \ \land \ \mathtt{VAR}_i &= \mathtt{VAR}_{i+1} \Leftrightarrow S_i = 1 \ \land \ \mathtt{VAR}_i \ > \mathtt{VAR}_{i+1} \Leftrightarrow S_i = 2. \end{array}$$

#### STATES SEMANTICS : stationary/increasing mode : decreasing mode Glue matrix where $\overrightarrow{C}$ and $\overleftarrow{C}$ resp. represent the counters values C at the end of a $\{C \leftarrow \mathsf{maxint}\}$ prefix and at the end of the corresponding reverse suffix that partitions the sequence VARIABLES; $\overrightarrow{X}$ denotes the last variable of the prefix. $VAR_i = VAR_{i+1}$ $\min(\overrightarrow{C}, \overleftarrow{C})$ $\min(\overrightarrow{C}, \overleftarrow{C})$ $\mathtt{VAR}_i < \mathtt{VAR}_{i+1},$ $VAR_i > VAR_{i+1}$ $\{C \leftarrow \min(C, \mathtt{VAR}_i)\}$ $\min(\overrightarrow{C}, \overleftarrow{C})$ $\min(\overrightarrow{C}, \overrightarrow{X}, \overleftarrow{C})$ u

Figure 5.269: Automaton of the deepest\_valley constraint and its glue matrix (state s means that we are in *increasing* or *stationary* mode, state u means that we are in *decreasing* mode, a new valley is detected each time we switch from decreasing to increasing mode and the counter C is updated accordingly); maxint is the largest integer that can be represented on a machine

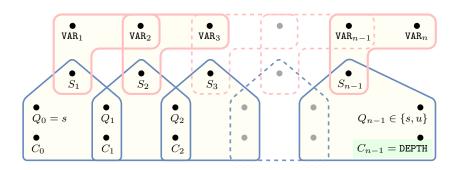


Figure 5.270: Hypergraph of the reformulation corresponding to the automaton of the deepest\_valley constraint ( $C_0$  is set to maxint the largest integer that can be represented on a machine)