## **5.31** arith

DESCRIPTION LINKS GRAPH AUTOMATON

**Origin** Used in the definition of several automata

Constraint arith(VARIABLES, RELOP, VALUE)

Synonym rel.

Arguments VARIABLES : collection(var-dvar)

RELOP : atom VALUE : int

Restrictions required (VARIABLES, var)

 $RELOP \in [=, \neq, <, \geq, >, \leq]$ 

Purpose Enforce for all variables var of the VARIABLES collection to have var RELOP VALUE.

Example  $(\langle 4, 5, 7, 4, 5 \rangle, \langle, 9)$ 

The arith constraint holds since all values of the collection  $\langle 4,5,7,4,5 \rangle$  are strictly less than 9.

Typical |VARIABLES| > 1 $RELOP \in [=]$ 

Symmetries • Items of VARIABLES are permutable.

 An occurrence of a value of VARIABLES.var can be replaced by any value of VARIABLES.var.

Arg. properties

Contractible wrt. VARIABLES.

Systems eq in Choco, neq in Choco, geq in Choco, gt in Choco, leq in Choco, lt in Choco, rel in Gecode,  $\#_{\hat{i}}$  in SICStus,  $\#=_{\hat{i}}$  in SICStus,  $\#_{\hat{c}}$  in SICStus,  $\#_{\hat{c}$ 

SICStus, # "=in SICStus.

Used in arith\_sliding.

See also common keyword: among, count (value constraint).

 ${\bf generalisation: arith\_or} \ ({\tt variable \ RELOP \ VALUE} \ replaced \ by \ {\tt variable \ RELOP \ VALUE}$ 

 $\lor$  variable RELOP VALUE).

 $system\ of\ constraints:\ {\tt arith\_sliding}.$ 

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Keywords characteristic of a constraint: automaton, automaton without counters,

reified automaton constraint.

constraint network structure: Berge-acyclic constraint network.

constraint type: decomposition, value constraint.

**filtering:** arc-consistency. **modelling:** domain definition.

 $\textbf{Cond. implications} \qquad \texttt{arith}(\texttt{VARIABLES}, \texttt{RELOP}, \texttt{VALUE})$ 

with RELOP  $\in$  [<]

 $\begin{array}{ll} \text{and} & \texttt{minval}(\texttt{VARIABLES.var}) \geq 0 \\ \textbf{implies} & \texttt{range\_ctr}(\texttt{VARIABLES}, \texttt{CTR}, \texttt{R}) \end{array}$ 

when  $CTR \in [<]$ .

 Arc input(s)
 VARIABLES

 Arc generator
 SELF → collection(variables)

 Arc arity
 1

 Arc constraint(s)
 variables.var RELOP VALUE

 Graph property(ies)
 NARC= |VARIABLES|

**Graph model** 

Parts (A) and (B) of Figure 5.72 respectively show the initial and final graph associated with the **Example** slot. Since we use the **NARC** graph property, the loops of the final graph are stressed in bold.

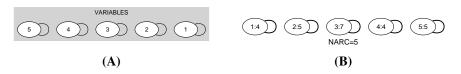


Figure 5.72: Initial and final graph of the arith constraint

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Automaton

Figure 5.73 depicts the automaton associated with the arith constraint. To each variable VAR $_i$  of the collection VARIABLES corresponds a 0-1 signature variable  $S_i$ . The following signature constraint links VAR $_i$  and  $S_i$ : VAR $_i$  RELOP VALUE  $\Leftrightarrow S_i$ . The automaton enforces for each variable VAR $_i$  the condition VAR $_i$  RELOP VALUE.



Figure 5.73: Automaton of the arith constraint

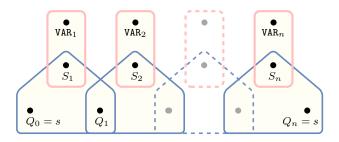


Figure 5.74: Hypergraph of the reformulation corresponding to the automaton of the arith constraint