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5.87 consecutive_groups_of_ones

DESCRIPTION

LINKS

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Origin

Derived from group

Constraint

 ${\tt consecutive_groups_of_ones}({\tt GROUP_SIZES}, {\tt VARIABLES})$

Arguments

```
GROUP_SIZES : collection(nb-int)
VARIABLES : collection(var-dvar)
```

Restrictions

```
\begin{array}{l} \textbf{required}(\texttt{GROUP\_SIZES}, \texttt{nb}) \\ | \texttt{GROUP\_SIZES}| \geq 1 \\ | \texttt{GROUP\_SIZES.nb} \geq 1 \\ | \texttt{GROUP\_SIZES.nb} \leq | \texttt{VARIABLES}| \\ | \textbf{required}(\texttt{VARIABLES}, \texttt{var}) \\ | \texttt{VARIABLES}| \geq 2 * | \texttt{GROUP\_SIZES}| - 1 \\ | \texttt{VARIABLES}| \geq \texttt{sum}(\texttt{GROUP\_SIZES.nb}) + | \texttt{GROUP\_SIZES}| - 1 \\ | \texttt{VARIABLES}. \texttt{var} \geq 0 \\ | \texttt{VARIABLES.var} \leq 1 \end{array}
```

In order to define the meaning of the consecutive_groups_of_ones constraint, we first introduce the notions of *stretch* and *span*. Let n be the number of variables of the collection VARIABLES and let m be the number of items of the collection GROUP_SIZES. Let X_i, \ldots, X_j $(1 \le i \le j \le n)$ be consecutive variables of the collection of variables VARIABLES such that the following conditions apply:

• All variables X_i, \ldots, X_i are assigned value 1,

• $i = 1 \text{ or } X_{i-1} \neq 1$,

• $j = n \text{ or } X_{j+1} \neq 1.$

We call such a set of variables a *stretch*. The *span* of the stretch is equal to j - i + 1. We now define the condition enforced by the consecutive_groups_of_ones constraint.

All variables of the VARIABLES collection should be assigned value 0 or 1. In addition there is |GROUP_SIZES| successive stretches of respective span GROUP_SIZES[1].nb, GROUP_SIZES[2].nb,..., GROUP_SIZES[m].nb.

Example

```
(\langle 2, 1 \rangle, \langle 1, 1, 0, 0, 0, 1, 0 \rangle)
```

The consecutive_groups_of_ones constraint holds since the sequence $1\ 1\ 0\ 0\ 0\ 1\ 0$ contains a first stretch (i.e., a maximum sequence of 1) of span 2 and a second stretch of span 1.

Typical

```
\begin{aligned} |\mathtt{VARIABLES}| &> 1 \\ \mathtt{range}(\mathtt{VARIABLES.var}) &> 1 \end{aligned}
```

Symmetry

Items of GROUP_SIZES and VARIABLES are simultaneously reversable.

Purpose

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Usage The consecutive_groups_of_ones constraint can be used in order to model the

logigraphe problem.

See also root concept: group.

Keywords characteristic of a constraint: automaton, automaton without counters,

reified automaton constraint.

constraint network structure: Berge-acyclic constraint network.

filtering: arc-consistency.

modelling exercises: logigraphe.

puzzles: logigraphe.

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Automaton

Figure 5.215 depicts the automaton associated with the consecutive_groups_of_ones constraint. To each variable VAR_i of the collection VARIABLES corresponds a signature variable that is equal to VAR_i . There is no signature constraint.

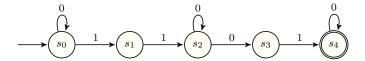


Figure 5.215: Non deterministic automaton of the consecutive_groups_of_ones constraint of the **Example** slot (a stretch of two 1 followed by a stretch of a single 1)



Figure 5.216: Hypergraph of the reformulation corresponding to the automaton of the consecutive_groups_of_ones constraint of the **Example** slot

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