\overline{NARC} , PATH_N

5.347 size_max_seq_alldifferent

DESCRIPTION LINKS GRAPH

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Constraint size_max_seq_alldifferent(SIZE, VARIABLES)

 ${\bf Synonyms} \\ {\bf size_maximal_sequence_alldiff}, \\ {\bf size_maximal_sequence_alldistinct}, \\$

size_maximal_sequence_alldifferent.

Arguments SIZE : dvar

VARIABLES : collection(var-dvar)

Restrictions SIZE > 0

 $\begin{aligned} \mathtt{SIZE} &\leq |\mathtt{VARIABLES}| \\ & \underline{\mathtt{required}}(\mathtt{VARIABLES}, \mathtt{var}) \end{aligned}$

Purpose SIZE is the size of the maximal sequence (among all possible sequences of consecutive variables of the collection VARIABLES) for which the alldifferent constraint holds.

Example

```
 \begin{array}{c} (4,\langle 2,2,4,5,2,7,4\rangle) \\ (1,\langle 2,2,2,2,2,2,2\rangle) \\ (2,\langle 2,2,4,4,4,7,4\rangle) \\ (7,\langle 2,0,4,6,5,7,3\rangle) \end{array}
```

The first size_max_seq_alldifferent constraint holds since the constraint alldifferent($\langle var - 4, var - 5, var - 2, var - 7 \rangle$) holds and since the following three constraints do not hold:

- alldifferent($\langle var 2, var 2, var 4, var 5, var 2 \rangle$),
- alldifferent($\langle var 2, var 4, var 5, var 2, var 7 \rangle$),
- alldifferent($\langle var 4, var 5, var 2, var 7, var 4 \rangle$).

Typical

```
\begin{split} & \texttt{SIZE} > 2 \\ & \texttt{SIZE} < |\texttt{VARIABLES}| \\ & \texttt{range}(\texttt{VARIABLES.var}) > 1 \end{split}
```

Symmetry

One and the same constant can be added to the var attribute of all items of VARIABLES.

Arg. properties

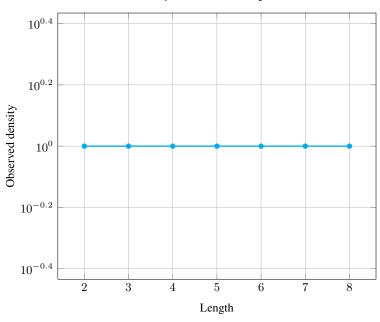
Functional dependency: SIZE determined by VARIABLES.

Counting

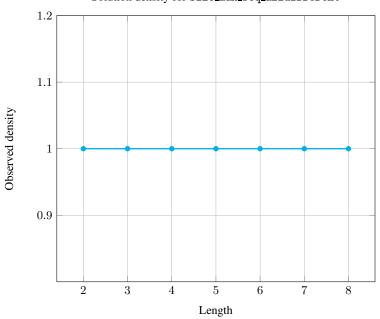
Length (n)	2	3	4	5	6	7	8
Solutions	9	64	625	7776	117649	2097152	43046721

Number of solutions for ${\tt size_max_seq_alldifferent:}\ domains\ 0..n$

 $Solution\ density\ for\ {\tt size_max_seq_alldifferent}$



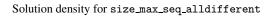
Solution density for ${\tt size_max_seq_alldifferent}$

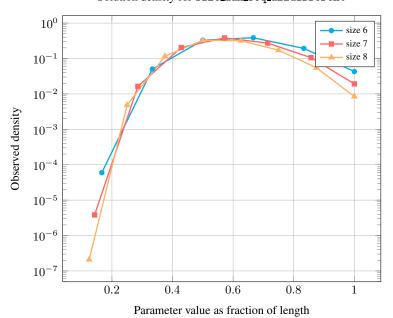


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Length (n)		2	3	4	5	6	7	8
Total		9	64	625	7776	117649	2097152	43046721
Parameter value	1	3	4	5	6	7	8	9
	2	6	36	200	1050	5922	34104	208224
	3	-	24	300	3480	38640	428400	4981032
	4	-	-	120	2520	45360	801360	14028336
	5	-	-	-	720	22680	571200	13728960
	6	-	-	-	-	5040	221760	7378560
	7	-	-	-	-	-	40320	2358720
	8	-	-	-	-	-		362880

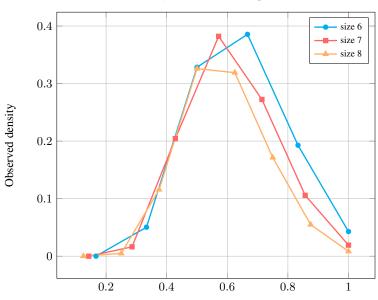
Solution count for size_max_seq_alldifferent: domains 0..n





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Solution density for ${\tt size_max_seq_alldifferent}$



Parameter value as fraction of length

See also

common keyword: alldifferent, open_alldifferent,
size_max_starting_seq_alldifferent(all different, disequality).
implies: atleast_nvalue.

Keywords

characteristic of a constraint: all different, disequality, hypergraph.
combinatorial object: sequence
constraint arguments: pure functional dependency
constraint type: sliding sequence constraint, conditional constraint.
modelling: functional dependency.

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Arc input(s) VARIABLES

Arc generator $PATH_N \mapsto collection$

Arc arity *

Arc constraint(s) alldifferent(collection)

Graph property(ies) NARC= SIZE

Graph model

Note that this is an example of global constraint where the arc constraints do not have the same arity. However they correspond to the same type of constraint.

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