

5.291 **nvector**

	DESCRIPTION	LINKS	GRAPH
Origin	Introduced by G. Chabert as a generalisation of nvalue		
Constraint	<code>nvector(NVEC, VECTORS)</code>		
Synonyms	<code>nvectors</code> , <code>npoint</code> , <code>npoints</code> .		
Type	<code>VECTOR</code> : <code>collection</code> (<code>var-dvar</code>)		
Arguments	<code>NVEC</code> : <code>dvar</code> <code>VECTORS</code> : <code>collection</code> (<code>vec - VECTOR</code>)		
Restrictions	$ \text{VECTOR} \geq 1$ $NVEC \geq \min(1, \text{VECTORS})$ $NVEC \leq \text{VECTORS} $ <code>required</code> (<code>VECTORS</code> , <code>vec</code>) <code>same_size</code> (<code>VECTORS</code> , <code>vec</code>)		
Purpose	NVEC is the number of distinct tuples of values taken by the vectors of the collection VECTORS. Two tuples of values $\langle A_1, A_2, \dots, A_m \rangle$ and $\langle B_1, B_2, \dots, B_m \rangle$ are <i>distinct</i> if and only if there exist an integer $i \in [1, m]$ such that $A_i \neq B_i$.		
Example	<div>$\left(2, \left\langle \begin{array}{l} \text{vec} - \langle 5, 6 \rangle, \\ \text{vec} - \langle 5, 6 \rangle, \\ \text{vec} - \langle 9, 3 \rangle, \\ \text{vec} - \langle 5, 6 \rangle, \\ \text{vec} - \langle 9, 3 \rangle \end{array} \right\rangle \right)$</div> <p>The <code>nvector</code> constraint holds since its first argument $NVEC = 2$ is set to the number of distinct tuples of values (i.e., tuples $\langle 5, 6 \rangle$ and $\langle 9, 3 \rangle$) occurring within the collection VECTORS. Figure 5.623 depicts with a thick rectangle a possible initial domain for each of the five vectors and with a grey circle each tuple of values of the corresponding solution.</p>		
Typical	$ \text{VECTOR} > 1$ $NVEC > 1$ $NVEC < \text{VECTORS} $ $ \text{VECTORS} > 1$		
Symmetries	<ul style="list-style-type: none">Items of VECTORS are permutable.Items of VECTORS.vec are permutable (<i>same permutation used</i>).All occurrences of two distinct tuples of values of VECTORS.vec can be swapped; all occurrences of a tuple of values of VECTORS.vec can be renamed to any unused tuple of values.		

can be expressed in term of the constraint

`nvalue`(NVEC, $\langle D_1, D_2, \dots, D_n \rangle$).

Note that the previous reformulation does not work anymore if the variables have a continuous domain, or if an overflow occurs while propagating the equality constraint

$D_k = \sum_{1 \leq i \leq m} \left(\left(\prod_{i < j \leq m} \gamma_j \right) \cdot (C_{ki} - \alpha_i) \right)$ (i.e., the number of components m is too big).

When using this reformulation with respect to the **Example** slot we first introduce $D_1 = 1 \cdot 6 - 3 + (4 \cdot 5 - 20) = 3$, $D_2 = 1 \cdot 6 - 3 + (4 \cdot 5 - 20) = 3$, $D_3 = 1 \cdot 3 - 3 + (4 \cdot 9 - 20) = 16$, $D_4 = 1 \cdot 6 - 3 + (4 \cdot 5 - 20) = 3$, $D_5 = 1 \cdot 3 - 3 + (4 \cdot 9 - 20) = 16$ and then get the constraint `nvalue`(2, $\langle 3, 3, 16, 3, 16 \rangle$).

See also

common keyword: `lex_equal`, `ordered_atleast_nvector`, `ordered_atmost_nvector` (`vector`).

generalisation: `nvectors` (replace an equality with the number of distinct vectors by a comparison with the number of distinct `nvectors`).

implied by: `ordered_nvector`.

implies: `atleast_nvector` (= NVEC replaced by \geq NVEC), `atmost_nvector` (= NVEC replaced by \leq NVEC).

specialisation: `nvalue` (`vector` replaced by `variable`).

Keywords

application area: SLAM problem.

characteristic of a constraint: `vector`.

complexity: rectangle clique partition.

constraint arguments: pure functional dependency.

constraint type: counting constraint, value partitioning constraint.

final graph structure: strongly connected component, equivalence.

modelling: number of distinct equivalence classes, functional dependency.

problems: domination.

Arc input(s)	VECTORS
Arc generator	<code>CLIQUE</code> → <code>collection</code> (vectors1,vectors2)
Arc arity	2
Arc constraint(s)	<code>lex_equal</code> (vectors1.vec,vectors2.vec)
Graph property(ies)	<code>NSCC</code> = NVEC
Graph class	<code>EQUIVALENCE</code>

Graph model

Parts (A) and (B) of Figure 5.624 respectively show the initial and final graph associated with the **Example** slot. Since we use the `NSCC` graph property we show the different strongly connected components of the final graph. Each strongly connected component corresponds to a tuple of values that is assigned to some vectors of the `VECTORS` collection. The 2 following tuple of values $\langle 5, 6 \rangle$ and $\langle 9, 3 \rangle$ are used by the vectors of the `VECTORS` collection.

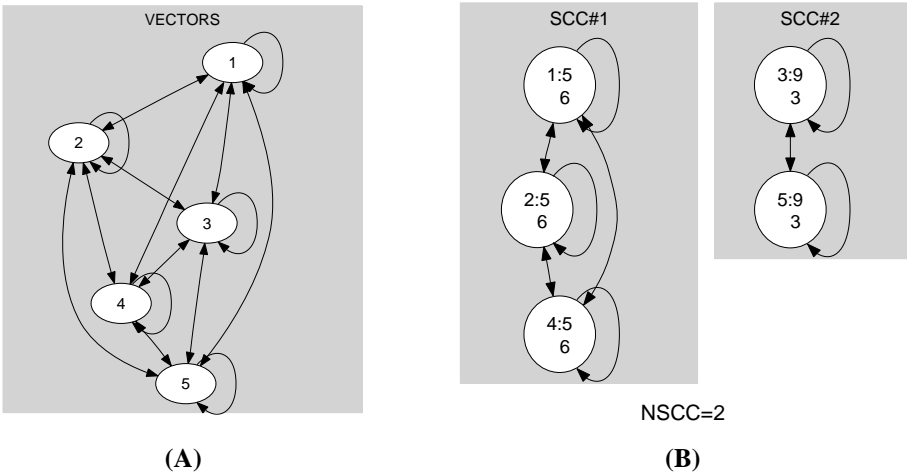


Figure 5.624: Initial and final graph of the `nvector` constraint