

## 5.234 `lex_lesseq_allperm`

	DESCRIPTION	LINKS
Origin	Inspired by [168]	
Constraint	<code>lex_lesseq_allperm(VECTOR1, VECTOR2)</code>	
Synonym	<code>leximin.</code>	
Arguments	VECTOR1 : <code>collection</code> ( <code>var-dvar</code> ) VECTOR2 : <code>collection</code> ( <code>var-dvar</code> )	
Restrictions	<code>required</code> (VECTOR1, var) <code>required</code> (VECTOR2, var) $ \text{VECTOR1}  =  \text{VECTOR2} $	
Purpose	VECTOR1 is <i>lexicographically less than or equal to</i> all permutations of VECTOR2. Given two vectors, $\vec{X}$ and $\vec{Y}$ of $n$ components, $\langle X_0, \dots, X_{n-1} \rangle$ and $\langle Y_0, \dots, Y_{n-1} \rangle$ , $\vec{X}$ is <i>lexicographically less than or equal to</i> $\vec{Y}$ if and only if $n = 0$ or $X_0 < Y_0$ or $X_0 = Y_0$ and $\langle X_1, \dots, X_{n-1} \rangle$ is <i>lexicographically less than or equal to</i> $\langle Y_1, \dots, Y_{n-1} \rangle$ .	
Example	$((\langle 1, 2, 3 \rangle), \langle 3, 1, 2 \rangle)$ <p>The <code>lex_lesseq_allperm</code> constraint holds since vector <math>\langle 1, 2, 3 \rangle</math> is lexicographically less than or equal to all the permutations of vector <math>\langle 3, 1, 2 \rangle</math> (i.e., <math>\langle 1, 2, 3 \rangle</math>, <math>\langle 1, 3, 2 \rangle</math>, <math>\langle 2, 1, 3 \rangle</math>, <math>\langle 2, 3, 1 \rangle</math>, <math>\langle 3, 1, 2 \rangle</math>, <math>\langle 3, 2, 1 \rangle</math>).</p>	
Typical	$ \text{VECTOR1}  > 1$	
Symmetry	All occurrences of two distinct values in <code>VECTOR1.var</code> or <code>VECTOR2.var</code> can be <code>swapped</code> ; all occurrences of a value in <code>VECTOR1.var</code> or <code>VECTOR2.var</code> can be <code>renamed</code> to any unused value.	
Arg. properties	<code>Suffix-contractible</code> wrt. VECTOR1 and VECTOR2 ( <i>remove items from same position</i> ).	
Remark	The <code>lex_lesseq_allperm(VECTOR1, VECTOR2)</code> can be reformulated as the conjunction <code>sort</code> (VECTOR2, VECTOR), <code>lex_lesseq</code> (VECTOR1, VECTOR).	
Systems	<code>leximin</code> in <b>Choco</b> .	
Used in	<code>allperm</code> .	
See also	<b>common keyword:</b> <code>allperm</code> ( <i>matrix symmetry, lexicographic order</i> ). <b>implies:</b> <code>lex_lesseq</code> . <b>system of constraints:</b> <code>allperm</code> .	

**Keywords**

**characteristic of a constraint:** vector.

**constraint type:** predefined constraint, order constraint.

**symmetry:** symmetry, matrix symmetry, lexicographic order.