

## 5.213 $\text{k\_used\_by\_interval}$

	DESCRIPTION	LINKS	GRAPH
Origin	Derived from <a href="#">used_by_interval</a> and from <a href="#">k_used_by</a> .		
Constraint	$\text{k\_used\_by\_interval}(\text{SETS}, \text{SIZE\_INTERVAL})$		
Type	VARIABLES : <a href="#">collection</a> ( $\text{var} - \text{dvar}$ )		
Arguments	SETS : <a href="#">collection</a> ( $\text{set} - \text{VARIABLES}$ ) SIZE_INTERVAL : <a href="#">int</a>		
Restrictions	<a href="#">required</a> (VARIABLES, $\text{var}$ ) $ \text{VARIABLES}  \geq 1$ <a href="#">required</a> (SETS, $\text{set}$ ) $ \text{SETS}  > 1$ <a href="#">non_increasing_size</a> (SETS, $\text{set}$ ) $\text{SIZE\_INTERVAL} > 0$		
Purpose	Given $ \text{SETS} $ sets of domain variables, the $\text{k\_used\_by\_interval}$ constraint forces a <a href="#">used_by_interval</a> constraint between each pair of consecutive sets.		
Example	$(\langle \text{set} - \langle 1, 1, 1, 8, 6, 2 \rangle, \text{set} - \langle 1, 0, 7, 7 \rangle, \text{set} - \langle 1, 2 \rangle \rangle, 3)$		
	In the example, the second argument $\text{SIZE\_INTERVAL} = 3$ defines the following family of intervals $[3 \cdot k, 3 \cdot k + 2]$ , where $k$ is an integer. Consequently, the $\text{k\_used\_by\_interval}$ constraint holds since: <ul style="list-style-type: none"> <li>• The first collection of variables is assigned 4 values in the interval <math>[0, 2]</math> as well as 2 values in the interval <math>[6, 8]</math>, while the second collection of variables is assigned no more values in the previous two intervals.</li> <li>• The second collection of variables is assigned 2 values in the interval <math>[0, 2]</math> as well as 2 values in the interval <math>[6, 8]</math>, while the third collection of variables is assigned no more values in the previous two intervals.</li> </ul>		
Typical	$ \text{VARIABLES}  > 1$ $\text{SIZE\_INTERVAL} > 0$		
Symmetries	<ul style="list-style-type: none"> <li>• Items of SETS are <a href="#">permutable</a>.</li> <li>• Items of SETS.set are <a href="#">permutable</a>.</li> <li>• An occurrence of a value of SETS.set.var that belongs to the <math>k</math>-th interval, of size <math>\text{SIZE\_INTERVAL}</math>, can be <a href="#">replaced</a> by any other value of the same interval.</li> </ul>		
Arg. properties	<a href="#">Contractible</a> wrt. SETS.		

<b>See also</b>	<b>common keyword:</b> <code>k_used_by</code> ( <i>system of constraints</i> ). <b>implied by:</b> <code>k_same_interval</code> . <b>part of system of constraints:</b> <code>used_by_interval</code> . <b>used in graph description:</b> <code>used_by_interval</code> .
<b>Keywords</b>	<b>characteristic of a constraint:</b> sort based reformulation. <b>constraint type:</b> system of constraints, decomposition. <b>modelling:</b> inclusion, interval.

Arc input(s)	SETS
Arc generator	$\text{PATH} \mapsto \text{collection}(\text{set1}, \text{set2})$
Arc arity	2
Arc constraint(s)	$\text{used\_by\_interval}(\text{set1.set}, \text{set2.set}, \text{SIZE\_INTERVAL})$
Graph property(ies)	$\text{NARC} =  \text{SETS}  - 1$

**Graph model** Parts (A) and (B) of Figure 5.485 respectively show the initial and final graph associated with the **Example** slot. To each vertex corresponds a collection of variables, while to each arc corresponds a `used_by_interval` constraint.

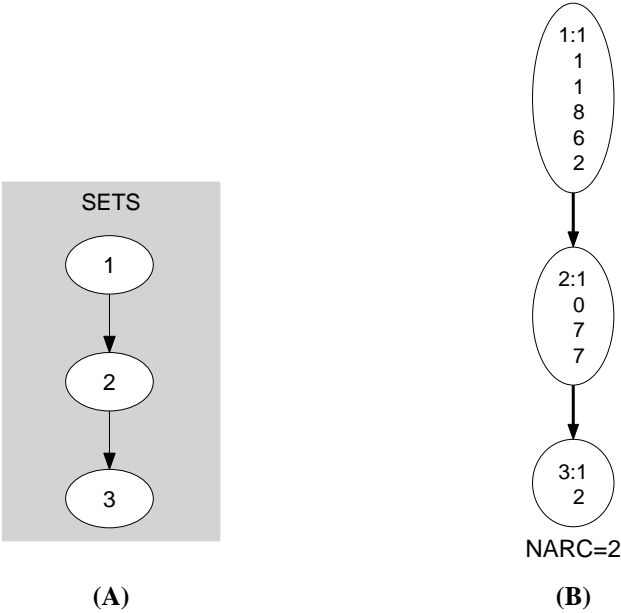


Figure 5.485: Initial and final graph of the `k.used_by_interval` constraint

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