\overline{NSCC} , CLIQUE

5.38 atleast_nvector

DESCRIPTION LINKS GRAPH

Origin Derived from nvector

Constraint atleast_nvector(NVEC, VECTORS)

Type VECTOR : collection(var-dvar)

Arguments NVEC : dvar

VECTORS : collection(vec - VECTOR)

Restrictions

```
\begin{split} |\text{VECTOR}| &\geq 1 \\ \text{NVEC} &\geq 0 \\ \text{NVEC} &\leq |\text{VECTORS}| \\ \text{required}(\text{VECTORS}, \text{vec}) \\ \text{same\_size}(\text{VECTORS}, \text{vec}) \end{split}
```

Purpose

The number of distinct tuples of values taken by the vectors of the collection VECTORS is greater than or equal to NVEC. Two tuples of values $\langle A_1,A_2,\ldots,A_m\rangle$ and $\langle B_1,B_2,\ldots,B_m\rangle$ are distinct if and only if there exist an integer $i\in[1,m]$ such that $A_i\neq B_i$.

Example

$$\left(\begin{array}{c} \text{vec} - \langle 5, 6 \rangle\,, \\ \text{vec} - \langle 5, 6 \rangle\,, \\ 2, \left\langle\begin{array}{c} \text{vec} - \langle 9, 3 \rangle\,, \\ \text{vec} - \langle 5, 6 \rangle\,, \\ \text{vec} - \langle 9, 4 \rangle \end{array}\right)$$

The atleast_nvector constraint holds since the collection VECTORS involves at least 2 distinct tuples of values (i.e., in fact the 3 distinct tuples $\langle 5, 6 \rangle$, $\langle 9, 3 \rangle$ and $\langle 9, 4 \rangle$).

Typical

```
\begin{split} |\text{VECTOR}| &> 1 \\ \text{NVEC} &> 1 \\ \text{NVEC} &< |\text{VECTORS}| \\ |\text{VECTORS}| &> 1 \end{split}
```

Symmetries

- NVEC can be decreased to any value ≥ 0 .
- Items of VECTORS are permutable.
- Items of VECTORS.vec are permutable (same permutation used).
- All occurrences of two distinct tuples of values of VECTORS.vec can be swapped; all occurrences of a tuple of values of VECTORS.vec can be renamed to any unused tuple of values.

Arg. properties

Extensible wrt. VECTORS.

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Reformulation By introducing an extra variable NV $\in [0, |VECTORS|]$, the atleast_nvector(NV, VECTORS) constraint can be expressed in term of an

 $\frac{1}{\text{NVector}}$ (NV, VECTORS) constraint and of an inequality constraint NV \geq NVEC.

See also comparison swapped: atmost_nvector.

implied by: $nvector (\ge NVEC replaced by = NVEC)$, ordered_atleast_nvector.

used in graph description: lex_equal.

Keywords characteristic of a constraint: vector.

constraint type: counting constraint, value partitioning constraint.

final graph structure: strongly connected component, equivalence.

modelling: number of distinct equivalence classes.

problems: domination.

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 Arc input(s)
 VECTORS

 Arc generator
 CLIQUE→collection(vectors1, vectors2)

 Arc arity
 2

 Arc constraint(s)
 lex_equal(vectors1.vec, vectors2.vec)

 Graph property(ies)
 NSCC≥ NVEC

 Graph class
 EQUIVALENCE

Graph model

Parts (A) and (B) of Figure 5.107 respectively show the initial and final graph associated with the **Example** slot. Since we use the **NSCC** graph property we show the different strongly connected components of the final graph. Each strongly connected component corresponds to a tuple of values that is assigned to some vectors of the VECTORS collection. The 3 following tuple of values $\langle 5,6\rangle$, $\langle 9,3\rangle$ and $\langle 9,4\rangle$ are used by the vectors of the VECTORS collection.

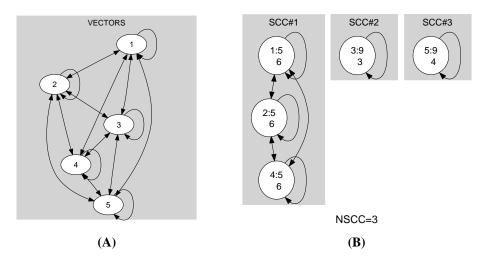


Figure 5.107: Initial and final graph of the atleast_nvector constraint

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