1968 AUTOMATON

## 5.318 pattern

DESCRIPTION LINKS AUTOMATON

Origin [83]

Constraint pattern(VARIABLES, PATTERNS)

Type PATTERN : collection(var-int)

Arguments VARIABLES : collection(var-dvar)
PATTERNS : collection(pat - PATTERN)

Restrictions required(PATTERN, var)

$$\begin{split} & \texttt{PATTERN.var} \geq 0 \\ & \texttt{change}(0, \texttt{PATTERN}, =) \\ & | \texttt{PATTERN}| > 1 \\ & \texttt{required}(\texttt{VARIABLES}, \texttt{var}) \end{split}$$

 $\frac{\texttt{required}(\texttt{PATTERNS}, \texttt{pat})}{|\texttt{PATTERNS}| > 0}$ 

same\_size(PATTERNS, pat)

We quote the definition from the original article [83, page 157] introducing the pattern constraint:

"We call a k-pattern (k > 1) any sequence of k elements such that no two successive elements have the same value. Consider a set  $V = \{v_1, v_2, \ldots, v_m\}$  and a sequence  $\mathbf{s} = s_1 \ s_2 \ \ldots \ s_n$  of elements of V. In this context, a stretch is a maximum subsequence of variables of  $\mathbf{s}$  which all have the same value. Consider now the sequence  $v_{i_1} \ v_{i_2} \ \ldots \ v_{i_l}$  of the types of the successive stretches that appear in  $\mathbf{s}$ . Let P be a set of k-patterns.  $\mathbf{s}$  satisfies P if and only if every subsequence of k elements in  $v_{i_1} \ v_{i_2} \ \ldots, v_{i_l}$  belongs to P."

Purpose

Example

```
\left(\begin{array}{c} \left\langle 1,1,2,2,2,1,3,3\right\rangle,\\ \left\langle \mathtt{pat} - \left\langle 1,2,1\right\rangle, \mathtt{pat} - \left\langle 1,2,3\right\rangle, \mathtt{pat} - \left\langle 2,1,3\right\rangle \right) \end{array}\right)
```

The pattern constraint holds since, as depicted by Figure 5.660, all its sequences of three consecutive stretches correspond to one of the 3-patterns given in the PATTERNS collection.

**Typical** 

```
\begin{aligned} |\mathtt{VARIABLES}| &> 2 \\ \mathtt{range}(\mathtt{VARIABLES.var}) &> 1 \end{aligned}
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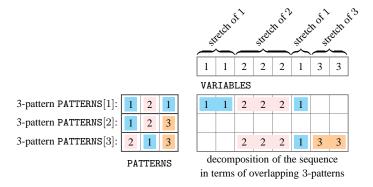


Figure 5.660: The sequence of the **Example** slot, its four stretches and the corresponding two 3-patterns  $1\ 2\ 1$  and  $2\ 1\ 3$ 

## **Symmetries**

- Items of PATTERNS are permutable.
- Items of VARIABLES and PATTERNS.pat are simultaneously reversable.
- All occurrences of two distinct tuples of values in VARIABLES.var or PATTERNS.pat.var can be swapped; all occurrences of a tuple of values in VARIABLES.var or PATTERNS.pat.var can be renamed to any unused tuple of values.

## Arg. properties

- Prefix-contractible wrt. VARIABLES.
- Suffix-contractible wrt. VARIABLES.

Usage

The pattern constraint was originally introduced within the context of staff scheduling. In this context, the value of the  $i^{th}$  variable of the VARIABLES collection corresponds to the type of shift performed by a person on the  $i^{th}$  day. A stretch is a maximum sequence of consecutive variables that are all assigned to the same value. The pattern constraint imposes that each sequence of k consecutive stretches belongs to a given list of patterns.

Remark

A generalisation of the pattern constraint to the regular constraint enforcing the fact that a sequence of variables corresponds to a regular expression is presented in [306].

See also

common keyword: group(timetabling constraint),
sliding\_distribution(sliding sequence constraint),
stretch\_circuit, stretch\_path(sliding sequence constraint, timetabling constraint),
stretch\_path\_partition(sliding sequence constraint).

Keywords

characteristic of a constraint: automaton, automaton without counters, reified automaton constraint.constraint network structure: Berge-acyclic constraint network.

**constraint type:** timetabling constraint, sliding sequence constraint.

filtering: arc-consistency.

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Automaton

Taking advantage that all k-patterns have the same length k, it is straightforward to construct an automaton that only accepts solutions of the pattern constraint. Figure 5.661 depicts the automaton associated with the pattern constraint of the **Example** slot. The construction can be done in three steps:

- First, build a prefix tree of all the k-patterns. In the context of our example, this gives
  all arcs of Figure 5.661, except self loops and the arc from s<sub>3</sub> to s<sub>7</sub>.
- Second, find out the transitions that exit a leave of the tree. For this purpose we remove the first symbol of the corresponding k-pattern, add at the end of the remaining k-pattern a symbol corresponding to a stretch value, and check whether the new pattern belongs or not to the set of k-patterns of the pattern constraint. When the new pattern belongs to the set of k-patterns we add a corresponding transition. For instance, in the context of our example, consider the leave s<sub>3</sub> that is associated with the 3-pattern 1, 2, 1. We remove the first symbol 1 and get 2, 1. We then try to successively add the stretch values 1, 2 and 3 to the end of 2, 1 and check if the corresponding patterns 2, 1, 1, 2, 1, 2 and 2, 1, 3 belong or not to our set of 3-patterns. Since only 2, 1, 3 is a 3-pattern we add a new transition between the corresponding leaves of the prefix tree (i.e., a transition from s<sub>3</sub> to s<sub>7</sub>).
- Third, in order to take into account that each value of a k-pattern corresponds in fact to a given stretch value (i.e., several consecutive values that are assigned the same value), we add a self loop to all non-source states with a transition label that corresponds to the transition label of their entering arc.

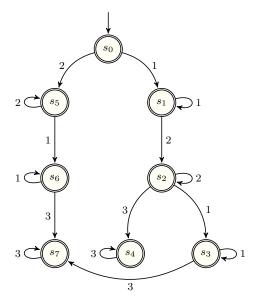


Figure 5.661: Automaton of the pattern constraint of the **Example** slot

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