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# 5.329 proper\_circuit

### **DESCRIPTION**

### **LINKS**

Origin Derived from circuit

Constraint proper\_circuit(NODES)

Synonym circuit.

Argument NODES : collection(index-int, succ-dvar)

 $\textbf{Restrictions} \hspace{1.5cm} |\mathtt{NODES}| > 1$ 

required(NODES, [index, succ])

 ${\tt NODES.index} \geq 1$ 

 $\mathtt{NODES.index} \leq |\mathtt{NODES}|$ 

distinct(NODES, index)

 $\mathtt{NODES.succ} \geq 1$ 

 $\mathtt{NODES.succ} \leq |\mathtt{NODES}|$ 

Purpose

Enforce to cover a digraph G described by the NODES collection with one circuit visiting once a subset of the vertices of G.

Example

```
\left(\begin{array}{ccc} \operatorname{index} - 1 & \operatorname{succ} - 2, \\ \operatorname{index} - 2 & \operatorname{succ} - 3, \\ \operatorname{index} - 3 & \operatorname{succ} - 1, \\ \operatorname{index} - 4 & \operatorname{succ} - 4 \end{array}\right)
```

The proper\_circuit constraint holds since its NODES argument depicts the following circuit visiting successively the vertices  $1,\ 2,\ 3$  and 1 (i.e., node 4 is not visited).

Typical

|NODES| > 2

Symmetry

Items of NODES are permutable.

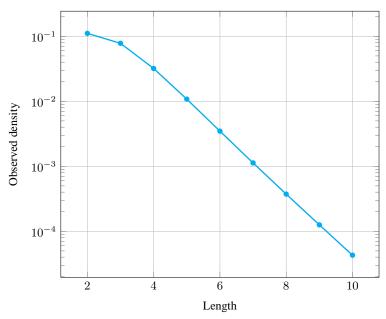
**Counting** 

Length (n)	2	3	4	5	6	7	8	9	10
Solutions	1	5	20	84	409	2365	16064	125664	1112073

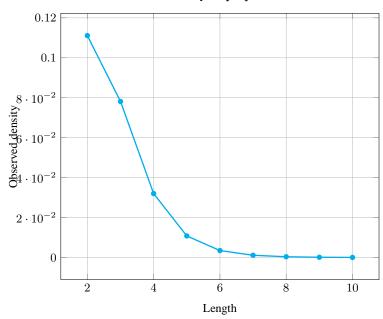
Number of solutions for proper\_circuit: domains 0..n

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# Solution density for proper\_circuit



# Solution density for $proper\_circuit$



See also

common keyword: alldifferent (permutation), circuit (permutation, one\_succ),
path(graph partitioning constraint, one\_succ).
implied by: circuit.

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implies: permutation, twin.

implies (items to collection): lex\_alldifferent.

Keywords combinatorial object: permutation.

constraint type: graph constraint, graph partitioning constraint.

filtering: DFS-bottleneck.

final graph structure: circuit, one\_succ.

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