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## 5.42 atmost\_nvector

DESCRIPTION LINKS GRAPH

Origin Derived from nvector

Constraint atmost\_nvector(NVEC, VECTORS)

Arguments NVEC : dvar

VECTORS : collection(vec - VECTOR)

**Restrictions**  $|VECTOR| \ge 1$ 

NVEC \geq min(1, |VECTORS|)
required(VECTORS, vec)
same\_size(VECTORS, vec)

Purpose

The number of distinct tuples of values taken by the vectors of the collection VECTORS is less than or equal to NVEC. Two tuples of values  $\langle A_1, A_2, \ldots, A_m \rangle$  and  $\langle B_1, B_2, \ldots, B_m \rangle$  are distinct if and only if there exist an integer  $i \in [1, m]$  such that  $A_i \neq B_i$ .

Example

$$\left(\begin{array}{c} \text{vec} - \langle 5, 6 \rangle \,, \\ \text{vec} - \langle 5, 6 \rangle \,, \\ \text{vec} - \langle 9, 3 \rangle \,, \\ \text{vec} - \langle 5, 6 \rangle \,, \\ \text{vec} - \langle 5, 6 \rangle \,, \end{array}\right)$$

The atmost\_nvector constraint holds since the collection VECTORS involves at most 3 distinct tuples of values (i.e., in fact the 2 distinct tuples  $\langle 5, 6 \rangle$  and  $\langle 9, 3 \rangle$ ).

**Typical** 

```
\begin{split} |\text{VECTOR}| &> 1 \\ \text{NVEC} &> 1 \\ \text{NVEC} &< |\text{VECTORS}| \\ |\text{VECTORS}| &> 1 \end{split}
```

**Symmetries** 

- NVEC can be increased.
- Items of VECTORS are permutable.
- Items of VECTORS.vec are permutable (same permutation used).
- All occurrences of two distinct tuples of values of VECTORS.vec can be swapped; all occurrences of a tuple of values of VECTORS.vec can be renamed to any unused tuple of values.

Arg. properties

Contractible wrt. VECTORS.

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 $\textbf{Reformulation} \qquad \qquad \text{By introducing an extra variable NV} \in [0, |\texttt{VECTORS}|], \text{the atmost\_nvector}(\texttt{NV}, \texttt{VECTORS})$ 

constraint can be expressed in term of an nvector(NV, VECTORS) constraint and of an

inequality constraint NV  $\leq$  NVEC.

See also comparison swapped: atleast\_nvector.

implied by:  $nvector (\leq NVEC \ replaced \ by = NVEC)$ , ordered\_atmost\_nvector.

used in graph description: lex\_equal.

**Keywords characteristic of a constraint:** vector.

**constraint type:** counting constraint, value partitioning constraint. **final graph structure:** strongly connected component, equivalence.

modelling: number of distinct equivalence classes.

**problems:** domination.

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Arc input(s)	VECTORS
Arc generator	$CLIQUE \mapsto \texttt{collection}(\texttt{vectors1}, \texttt{vectors2})$
Arc arity	2
Arc constraint(s)	<pre>lex_equal(vectors1.vec, vectors2.vec)</pre>
<b>Graph property(ies)</b>	NSCC≤ NVEC
Graph class	EQUIVALENCE

## Graph model

Parts (A) and (B) of Figure 5.113 respectively show the initial and final graph associated with the **Example** slot. Since we use the **NSCC** graph property we show the different strongly connected components of the final graph. Each strongly connected component corresponds to a tuple of values that is assigned to some vectors of the VECTORS collection. The 2 following tuple of values  $\langle 5,6 \rangle$  and  $\langle 9,3 \rangle$  are used by the vectors of the VECTORS collection.

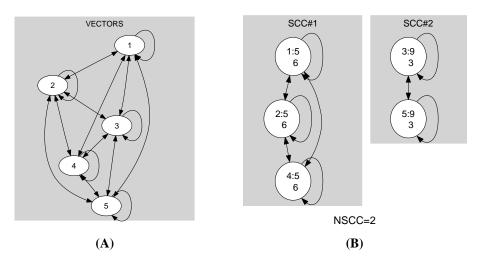


Figure 5.113: Initial and final graph of the atmost\_nvector constraint

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