## 5.142 element\_matrix

DESCRIPTION LINKS GRAPH AUTOMATON

Origin CHIP

Constraint element\_matrix(MAX\_I, MAX\_J, INDEX\_I, INDEX\_J, MATRIX, VALUE)

Synonyms elem\_matrix, matrix.

Arguments MAX\_I : int

MAX\_J : int INDEX\_I : dvar INDEX\_J : dvar

MATRIX : collection(i-int, j-int, v-int)

VALUE : dvar

Restrictions

$$\begin{split} \text{MAX\_I} &\geq 1 \\ \text{MAX\_J} &\geq 1 \\ \text{INDEX\_I} &\geq 1 \\ \text{INDEX\_J} &\leq \text{MAX\_I} \\ \text{INDEX\_J} &\leq \text{MAX\_J} \\ \text{required}(\text{MATRIX}, [\mathbf{i}, \mathbf{j}, \mathbf{v}]) \\ \text{increasing\_seq}(\text{MATRIX}, [\mathbf{i}, \mathbf{j}]) \\ \text{MATRIX}.\mathbf{i} &\geq 1 \\ \text{MATRIX}.\mathbf{i} &\leq \text{MAX\_I} \\ \text{MATRIX}.\mathbf{j} &\leq 1 \\ \text{MATRIX}.\mathbf{j} &\leq \text{MAX\_J} \\ |\text{MATRIX}| &= \text{MAX\_J} \\ |\text{MATRIX}| &= \text{MAX\_J} \\ \end{split}$$

**Purpose** 

The MATRIX collection corresponds to the two-dimensional matrix MATRIX[1..MAX\_I, 1..MAX\_J]. VALUE is equal to the entry MATRIX[INDEX\_I, INDEX\_J] of the previous matrix.

i-1 j-1 v-4, i-1 j-2 v-1, j - 3i-2j-3 $\mathtt{i}-2$ 4, 3, 1, 3,i-3j - 1i-3j-2 v-2,i-3j-3i-4j - 1j-2 v-0, i-4 $\mathtt{i}-4 \quad \mathtt{j}-3 \quad \mathtt{v}-6$ 

Example

20031101 1159

The element\_matrix constraint holds since its last argument VALUE = 7 is equal to the v attribute of the  $k^{th}$  item of the MATRIX collection such that MATRIX $[k].i = \mathtt{INDEX\_I} = 1$  and MATRIX $[k].j = \mathtt{INDEX\_J} = 3$ .

**Typical** 

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\begin{split} &\text{MAX\_I} > 1 \\ &\text{MAX\_J} > 1 \\ &| \text{MATRIX} | > 3 \\ &\text{maxval}(\text{MATRIX.i}) > 1 \\ &\text{maxval}(\text{MATRIX.j}) > 1 \\ &\text{range}(\text{MATRIX.v}) > 1 \end{split}
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**Symmetry** 

All occurrences of two distinct values in MATRIX.v or VALUE can be swapped; all occurrences of a value in MATRIX.v or VALUE can be renamed to any unused value.

Reformulation

The element\_matrix(MAX\_I, MAX\_J, INDEX\_I, INDEX\_J, MATRIX, VALUE) constraint can be expressed in term of MAX\_I element(INDEX\_J, LINE $_i$ , VAR $_i$ ) ( $i \in [1, MAX_I]$ ), where LINE $_i$  corresponds to the i-th line of the matrix MATRIX and of one element(INDEX\_I,  $\langle VAR_1, VAR_2, \ldots, VAR_{MAX_I} \rangle$ , VALUE) constraint.

If we consider the **Example** slot we get the following element constraints:

- element  $(3, \langle 4, 1, 7 \rangle, 7)$ ,
- element $(3, \langle 1, 0, 8 \rangle, 8)$ ,
- element $(3, \langle 3, 2, 1 \rangle, 1)$ ,
- element $(3, \langle 0, 0, 6 \rangle, 6)$ ,
- element $(1, \langle 7, 8, 1, 6 \rangle, 7)$ .

**Systems** 

nth in Choco, element in Gecode.

See also

common keyword: elem, element (array constraint).

Keywords

**characteristic of a constraint:** automaton, automaton without counters, reified automaton constraint, derived collection.

constraint arguments: ternary constraint.

 $\textbf{constraint network structure:} \ centered \ cyclic (3) \ constraint \ network (1).$ 

constraint type: data constraint.

filtering: arc-consistency.

modelling: array constraint, matrix.

## Graph model

Similar to the element constraint except that the arc constraint is updated according to the fact that we have a two-dimensional matrix.

Parts (A) and (B) of Figure 5.328 respectively show the initial and final graph associated with the **Example** slot. Since we use the **NARC** graph property, the unique arc of the final graph is stressed in bold.

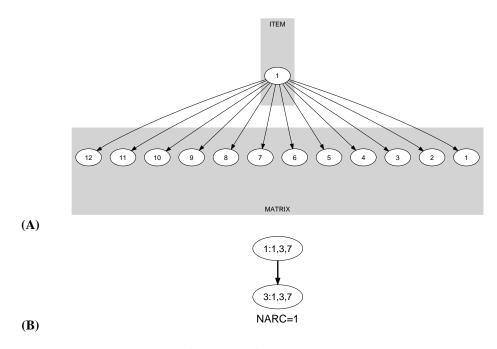


Figure 5.328: Initial and final graph of the element\_matrix constraint

## Signature

Because of the first condition of the arc constraint the final graph cannot have more than one arc. Therefore we can rewrite  $\mathbf{NARC}=1$  to  $\mathbf{NARC}\geq 1$  and simplify  $\overline{\mathbf{NARC}}$  to  $\overline{\mathbf{NARC}}$ .

20031101 1161

Automaton

Figure 5.329 depicts the automaton associated with the element\_matrix constraint. Let  $\mathbf{I}_k$ ,  $\mathbf{J}_k$  and  $\mathbf{V}_k$  respectively be the i, the j and the v  $k^{th}$  attributes of the MATRIX collection. To each sextuple (INDEX\_I, INDEX\_J, VALUE,  $\mathbf{I}_k$ ,  $\mathbf{J}_k$ ,  $\mathbf{V}_k$ ) corresponds a 0-1 signature variable  $S_k$  as well as the following signature constraint: ((INDEX\_I =  $\mathbf{I}_k$ )  $\wedge$  (INDEX\_J =  $\mathbf{J}_k$ )  $\wedge$  (VALUE =  $\mathbf{V}_k$ ))  $\Leftrightarrow S_k$ .

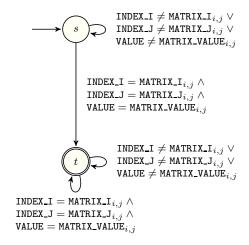


Figure 5.329: Automaton of the element\_matrix constraint

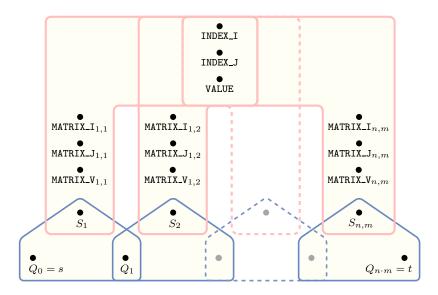


Figure 5.330: Hypergraph of the reformulation corresponding to the automaton of the element\_matrix constraint where n and m respectively stands for MAX\_I and MAX\_J