

5.182 in\_same\_partition

	DESCRIPTION	LINKS	GRAPH	AUTOMATON
Origin	Used for defining several entries of this catalog.			
Constraint	in_same_partition(VAR1, VAR2, PARTITIONS)			
Type	VALUES : collection(val-int)			
Arguments	VAR1 : dvar VAR2 : dvar PARTITIONS : collection(p - VALUES)			
Restrictions	VALUES  ≥ 1 required(VALUES, val) distinct(VALUES, val) required(PARTITIONS, p)  PARTITIONS  ≥ 2			
Purpose	Enforce VAR1 and VAR2 to be respectively assigned to values $v_1$ and $v_2$ that both belong to a same partition of the collection PARTITIONS.			
Example	$(6, 2, \langle p - \langle 1, 3 \rangle, p - \langle 4 \rangle, p - \langle 2, 6 \rangle \rangle)$			
	The in_same_partition constraint holds since its first and second arguments VAR1 = 6 and VAR2 = 2 both belong to the third partition $\langle 2, 6 \rangle$ of its third argument PARTITIONS.			
Typical	VAR1 ≠ VAR2			
Symmetries	<ul style="list-style-type: none"><li>Arguments are <a href="#">permutable</a> w.r.t. permutation (VAR1, VAR2) (PARTITIONS).</li><li>Items of PARTITIONS are <a href="#">permutable</a>.</li><li>Items of PARTITIONS.p are <a href="#">permutable</a>.</li></ul>			
Arg. properties	<a href="#">Extensible</a> wrt. PARTITIONS.			
Used in	alldifferent_partition, balance_partition, change_partition, common_partition, nclass, same_partition, soft_same_partition_var, soft_used_by_partition_var, used_by_partition.			
See also	common keyword: alldifferent_partition (partition), in (value constraint). used in graph description: in.			

**Keywords**

**characteristic of a constraint:** partition, automaton, automaton without counters, reified automaton constraint, derived collection.

**constraint arguments:** binary constraint.

**constraint network structure:** centered cyclic(2) constraint network(1).

**constraint type:** value constraint.

**filtering:** arc-consistency.

Derived Collection	$\text{col} \left( \begin{array}{c} \text{VARIABLES} - \text{collection}(\text{var} - \text{dvar}), \\ [\text{item}(\text{var} - \text{VAR1}), \text{item}(\text{var} - \text{VAR2})] \end{array} \right)$
Arc input(s)	VARIABLES PARTITIONS
Arc generator	<i>PRODUCT</i> $\mapsto$ collection(variables, partitions)
Arc arity	2
Arc constraint(s)	in(variables.var, partitions.p)
Graph property(ies)	<ul style="list-style-type: none"><li>• <u>NSOURCE</u> = 2</li><li>• <u>NSINK</u> = 1</li></ul>

Graph model

VAR1 and VAR2 are put together in the derived collection VARIABLES. Since both VAR1 and VAR2 should take their value in one of the partition depicted by the PARTITIONS collection, the final graph should have two sources corresponding respectively to VAR1 and VAR2. Since two, possibly distinct, values should be assigned to VAR1 and VAR2 and since these values belong to the same partition *p* the final graph should only have one sink. This sink corresponds in fact to partition *p*.

Parts (A) and (B) of Figure 5.424 respectively show the initial and final graph associated with the **Example** slot. Since we both use the **NSOURCE** and **NSINK** graph properties, the source and sink vertices of the final graph are shown with a double circle.

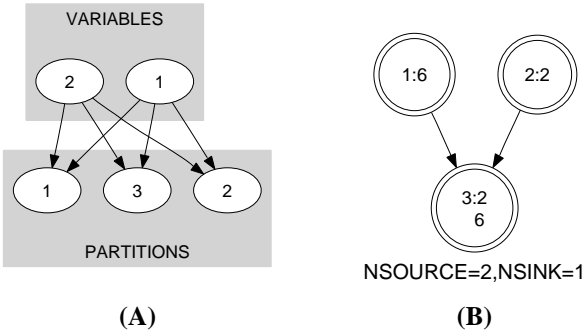


Figure 5.424: Initial and final graph of the *in.same.partition* constraint

Signature

Note that the sinks of the initial graph cannot become sources of the final graph since isolated vertices are eliminated from the final graph. Since the final graph contains two sources it also includes one arc between a source and a sink. Therefore the minimum number of sinks of the final graph is equal to one. So we can rewrite **NSINK** = 1 to **NSINK**  $\geq$  1 and simplify **NSINK** to **NSINK**.

**Automaton**

Figure 5.425 depicts the automaton associated with the `in_same_partition` constraint. Let  $\text{VALUES}_i$  be the  $p$  attribute of the  $i^{\text{th}}$  item of the `PARTITIONS` collection. To each triple  $(\text{VAR1}, \text{VAR2}, \text{VALUES}_i)$  corresponds a 0-1 signature variable  $S_i$  as well as the following signature constraint:  $((\text{VAR1} \in \text{VALUES}_i) \wedge (\text{VAR2} \in \text{VALUES}_i)) \Leftrightarrow S_i$ .

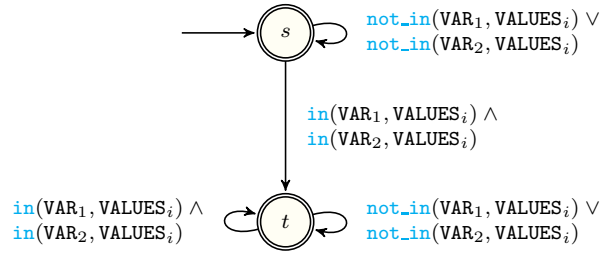


Figure 5.425: Automaton of the `in_same_partition` constraint

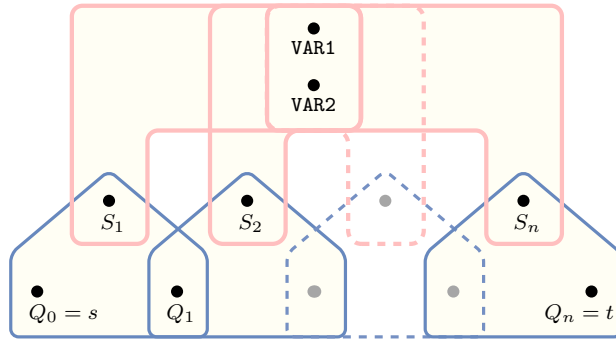


Figure 5.426: Hypergraph of the reformulation corresponding to the automaton of the `in_same_partition` constraint