1644 PREDEFINED

## 5.248 max\_occ\_of\_tuples\_of\_values

## **DESCRIPTION**

LINKS

Origin

Design.

Constraint

max\_occ\_of\_tuples\_of\_values(MAX, K, VECTORS)

Type

VECTOR : collection(var-dvar)

Arguments

MAX : int K : int

VECTORS : collection(vec - VECTOR)

Restrictions

```
required(VECTOR, var)
|VECTOR| > 2
strictly_increasing(VECTOR)
MAX > 1
K > 2
K < |VECTOR|
required(VECTORS, vec)
|VECTORS| > 1
same_size(VECTORS, vec)
```

Purpose

MAX is equal to the maximum number of occurrences of identical vectors derived from the vectors VECTORS in the following way. To each vector  $\langle v_1, v_2, \ldots, v_m \rangle$  (with  $v_1 < v_2 \wedge \cdots \wedge v_{m-1} < v_m$ ) of VECTORS we generate all vectors  $\langle u_1, u_2, \ldots, u_K \rangle$  such that  $u_1 = v_{i_1}, u_2 = v_{i_2}, \ldots, u_K = v_{i_K}$  (with  $1 \le i_1 < i_2 < \cdots < i_K \le m$ ).

Example

```
\left(\begin{array}{c} \mathtt{vec} - \langle 1,2,4\rangle\,,\\ \mathtt{vec} - \langle 2,3,5\rangle\,,\\ \mathtt{vec} - \langle 3,4,6\rangle\,,\\ 1,2,\left\langle\begin{array}{c} \mathtt{vec} - \langle 4,5,7\rangle\,,\\ \mathtt{vec} - \langle 1,5,6\rangle\,,\\ \mathtt{vec} - \langle 2,6,7\rangle\,,\\ \mathtt{vec} - \langle 1,3,7\rangle \end{array}\right)
```

Given the seven vectors of the example we respectively generate:

- the pairs  $\langle 1, 2 \rangle$ ,  $\langle 1, 4 \rangle$  and  $\langle 2, 4 \rangle$  from the triple  $\langle 1, 2, 4 \rangle$ ,
- the pairs  $\langle 2, 3 \rangle$ ,  $\langle 2, 5 \rangle$  and  $\langle 3, 5 \rangle$  from the triple  $\langle 2, 3, 5 \rangle$ ,
- the pairs  $\langle 3, 4 \rangle$ ,  $\langle 3, 6 \rangle$  and  $\langle 4, 6 \rangle$  from the triple  $\langle 3, 4, 6 \rangle$ ,
- the pairs  $\langle 4, 5 \rangle$ ,  $\langle 4, 7 \rangle$  and  $\langle 5, 7 \rangle$  from the triple  $\langle 4, 5, 7 \rangle$ ,
- the pairs  $\langle 1, 5 \rangle$ ,  $\langle 1, 6 \rangle$  and  $\langle 5, 6 \rangle$  from the triple  $\langle 1, 5, 6 \rangle$ ,
- the pairs  $\langle 2, 6 \rangle$ ,  $\langle 2, 7 \rangle$  and  $\langle 6, 7 \rangle$  from the triple  $\langle 2, 6, 7 \rangle$ ,

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• the pairs  $\langle 1, 3 \rangle$ ,  $\langle 1, 7 \rangle$  and  $\langle 3, 7 \rangle$  from the triple  $\langle 1, 3, 7 \rangle$ .

Putting these pairs together, we get the set of pairs  $\{\langle 1,2\rangle,\langle 1,3\rangle,\langle 1,4\rangle,\langle 1,5\rangle,\langle 1,6\rangle,\langle 1,7\rangle,\langle 2,3\rangle,\langle 2,4\rangle,\langle 2,5\rangle,\langle 2,6\rangle,\langle 2,7\rangle,\langle 3,4\rangle,\langle 3,5\rangle,\langle 3,6\rangle,\langle 3,7\rangle,\langle 4,5\rangle,\langle 4,6\rangle,\langle 4,7\rangle,\langle 5,6\rangle,\langle 5,7\rangle,\langle 6,7\rangle\}$ . The max\_occ\_of\_tuples\_of\_values constraint holds since the components of the original seven vectors are strictly increasing, and since MAX is set to one and all the generated pairs are distinct.

**Typical** 

```
\begin{aligned} \text{MAX} &\leq 2 \\ |\text{VECTOR}| &< \text{K} + 5 \\ \text{K} &= 2 \vee \text{K} + 1 = |\text{VECTOR}| \\ |\text{VECTORS}| &> 2 \end{aligned}
```

Arg. properties

- Functional dependency: MAX determined by K and VECTORS.
- Contractible wrt. VECTORS when MAX = 1.

Usage

This constraint occurs in balanced block design problems [207, 262] such as Steiner or Kirkman triples.

See also

common keyword: max\_occ\_of\_consecutive\_tuples\_of\_values,
max\_occ\_of\_sorted\_tuples\_of\_values(vector).
implies: max\_occ\_of\_sorted\_tuples\_of\_values.

Keywords

characteristic of a constraint: vector
modelling: functional dependency