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# 5.238 longest\_increasing\_sequence

#### DESCRIPTION LINKS AUTOMATON

Origin constraint on sequences

Constraint longest\_increasing\_sequence(L, VARIABLES)

Synonym size\_longest\_increasing\_sequence.

Arguments L : dvar

VARIABLES : collection(var-dvar)

**Restrictions**  $L \ge 0$ 

L <range(VARIABLES.var)
required(VARIABLES, var)</pre>

L is the largest difference between the first and the last value of the maximum increasing sequences of the collection VARIABLES.

A sequence of consecutive variables  $X_i, X_{i+1}, \ldots, X_j$   $(1 \le i \le j \le |VARIABLES|)$  of the collection of variables VARIABLES is a *maximum increasing sequence* if all the following conditions simultaneously apply:

- $X_i \leq X_{i+1} \leq \cdots \leq X_i$ ,
- $i = 1 \text{ or } X_{i-1} > X_i$ ,
- $i = |VARIABLES| \text{ or } X_j > X_{j+1}$ .

Example

**Purpose** 

 $(7, \langle 10, 8, 8, 6, 4, 9, 11, 8 \rangle)$  $(0, \langle 10, 8, 7, 5, 4, 3, 1, 0 \rangle)$ 

Figure 5.526 gives a graphical representation of the first example of the **Example** slot with its two maximum increasing sequences in red of respective size 0 and 7. The corresponding longest\_increasing\_sequence constraint holds since its first argument L is fixed to the maximum size 7.

Typical

$$\begin{split} \mathbf{L} &> 0 \\ |\mathtt{VARIABLES}| &> 1 \\ \mathtt{nval}(\mathtt{VARIABLES.var}) &> 2 \end{split}$$

**Symmetry** 

One and the same constant can be added to the var attribute of all items of VARIABLES.

Arg. properties

Functional dependency: L determined by VARIABLES.

Counting

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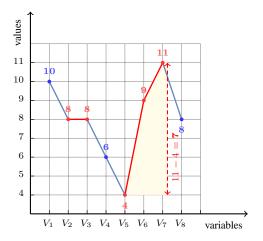
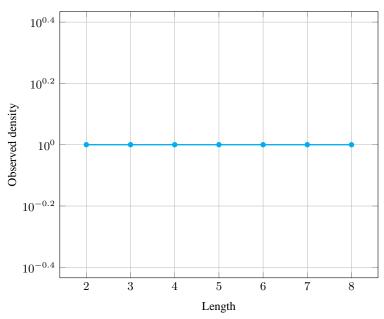


Figure 5.526: Illustration of the first example of the **Example** slot: a sequence of eight variables  $V_1$ ,  $V_2$ ,  $V_3$ ,  $V_4$ ,  $V_5$ ,  $V_6$ ,  $V_7$ ,  $V_8$  respectively fixed to values 10, 8, 8, 6, 4, 9, 11, 8 and its two maximum increasing sequences in red of respective size 8-8=0 and 11-4=7.

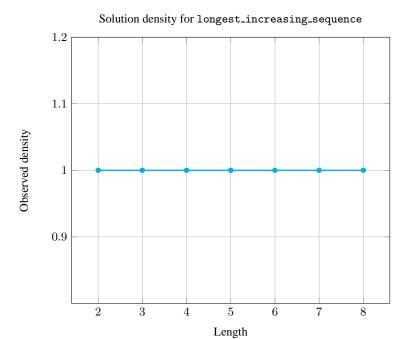
Length (n)	2	3	4	5	6	7	8
Solutions	9	64	625	7776	117649	2097152	43046721

Number of solutions for longest\_increasing\_sequence: domains 0..n

## $Solution\ density\ for\ {\tt longest\_increasing\_sequence}$



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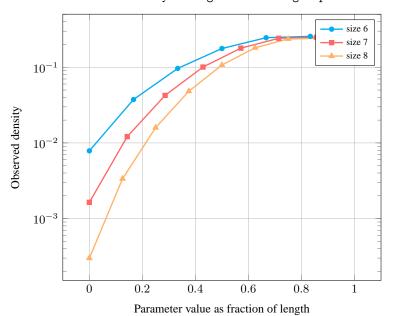


Length (n)		2	3	4	5	6	7	8
Total		9	64	625	7776	117649	2097152	43046721
Parameter value	0	6	20	70	252	924	3432	12870
	1	2	18	122	750	4412	25382	144314
	2	1	16	161	1398	11361	89132	685090
	3	-	10	162	1942	20816	211106	2074365
	4	-	-	110	2024	28930	375084	4603682
	5	-	-	-	1410	30134	506766	7792840
	6	-	-	-	-	21072	522648	10197174
	7	-	-	-	-	-	363602	10379696
	8	-	-	-	-	-	-	7156690

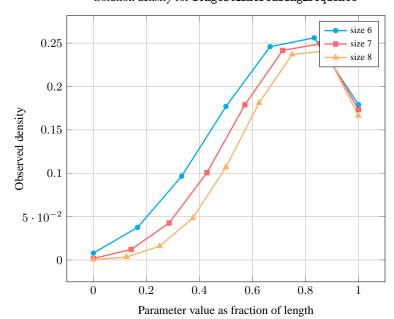
Solution count for longest\_increasing\_sequence: domains 0..n

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#### $Solution\ density\ for\ {\tt longest\_increasing\_sequence}$



### Solution density for longest\_increasing\_sequence



See also

common keyword:
min\_dist\_between\_inflexion(sequence).

longest\_decreasing\_sequence,

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**Keywords** characteristic of a constraint:

automaton,

automaton with counters,

automaton with same input symbol.

combinatorial object: sequence.

constraint arguments: reverse of a constraint, pure functional dependency.

filtering: glue matrix.

modelling: functional dependency.

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#### Automaton

Figure 5.527 depicts the automaton associated with the longest\_increasing\_sequence constraint.

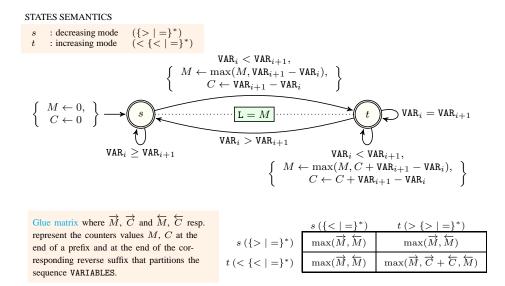


Figure 5.527: Automaton of the longest\_increasing\_sequence constraint and its glue matrix (note that the reverse of the longest\_increasing\_sequence constraint is the longest\_decreasing\_sequence constraint)

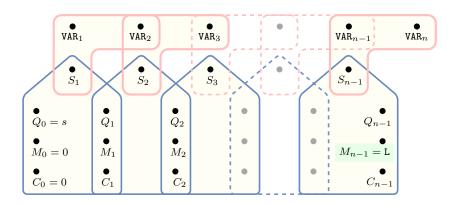


Figure 5.528: Hypergraph of the reformulation corresponding to the automaton of the longest\_increasing\_sequence constraint