

## I. Data Types

1. int

operator: **+**, **-**, **\***, **/**, **mod**  
 others: `abs`, `max_int`, `min_int`  
 note:  $5/2 = 2$

2. float

operator: **+**, **-**, **\***, **/**, **\*\***, `sqrt` (or `** 0.5`), `log` (`ln`), ...  
 note: `2.5 +. 2` will raise an error (it must be `2.`)

3. string

operator: **^** (concatenate)  
 note: string is surrounded with " ", char is surrounded with ' ' but char can only contain 1 character ('hi' will raise a syntax error)

4. bool

operator: **&&**, **||**, **not** (weird, it's **not** NOT !)  
 comparisons: `=`, `<>`, `<`, `<=`, `>`, `>=`

There are functions that help us convert any of those types to another type:

**type1\_of\_type2 v: type1 → type2 (change v from type2 to type1)**

example: `int_of_float 5.46 => int of 5.46 = 5`

note: there are only `bool_of_string` and `string_of_bool`, not `bool_of_int` or others

Other helpful functions:

`compare`: `'a → 'a → int` (compare x y return 0 if x is equal y, neg int if x < y, ...)

`min`: `'a → 'a → 'a`

`max`: `'a → 'a → 'a`

5. list (all elements in a list must be **same type**, separated by `;` inside `[]`)

operator: **x::lst** (unshift x to lst), **lst1@lst2** (concat lst1 & lst2)

note: if want to push x to lst, do `lst@[x]`

example: `1::2::[3;4;5];;`  $\Rightarrow$  `[1;2;3;4;5]`  
`[1;2]@[3;4;5];;`  $\Rightarrow$  `[1;2;3;4;5]`

6. tuple (elements in a tuple can be **different types**, separated by `,` inside `()`)

no operator since it is immutable

example: `([2;3;1], "hi", true) => int list * string * bool`

7. record (weird hash)

define: **type record\_name = {key\_1:val\_1; key\_2:val\_2; ...}**

get val: `record_name.key`

example: `type data = { month: string; day: int; year: int };;`  
`let today = { day=1; year=2023; month="mar"};;`  
`today.year;;` (\* 2023 \*)

note: notice the order does not matter but must be enough!

8. variant (enum)

define: **type variant\_name = Type\_1 of 'a | Type\_2 of 'b | ...**

important: `Type_1`, `Type_2`, ... **must be capitalized the first letter**

example: `type linked = Null | Item of string * linked;;`  
`let items = Item("banana", Item("apple", Null));;`

note: can be generic

`type 'a option = Some of 'a | None;;`

`let opt = Some 2;; => val opt: int option`

## II. Functions

1. anonymous function

example: `fun x y z -> x + y + z;;` (\* `int → int → int → int` \*)

2. 'normal' function

example: `let sum_1 x y z = x + y + z;;` (same type but now its name is `sum_1`)

or `let sum_2 = fun x y z -> x + y + z;;` (same idea but different :D)

`sum_1 1 2 3;; => 6`      `sum_2 1 2 3;; => 6`

3. recursive function (must have `rec` keyword)

example: `let rec fac n = if n = 1 then 1 else n * fac (n - 1);;` (\* `int → int` \*)

### III. More on `let`

#### 1. let bindings

a let binding is **not an expression** and just binds an expression to a variable.

example: `let a = 10;; (val a : int = 10)`

`let add a b = a + b;; (val add : int → int → int = <fun>)`

=> a or add can be re-used later.

note: we should consider **add** as a variable but its type is <fun> (function)

#### 2. let expressions

a let expression is like setting a local variable to be used in **another expression**.

example: `let a = 10 in`

`let add a b = a + b in (* a in this let is different from the earlier a *)`

`add 15 a;; (* output: 25 *)`

=> a can't be re-used later.

note: let expressions mostly make our code more readable

### IV. Pattern Matching

#### 0. Syntax

`match x with`

`| p1 -> e1 (* | is optional for this line *)`

`| p2 -> e2`

`...`

`| _ -> e3`

note: x, p1, p2 must be the same type

e1, e2, e3 must be the same type

\_ is wildcard, simply make our matching exhaustive (match all possible cases)

#### 1. int, float, string, char, or bool

nothing special, just like switch statement in other programming languages

#### 2. list

`match lst with`

`| [] -> e1 (* empty list *)`

`| h::[] -> e2 (* list with exactly 1 element *)`

`| h1::h2::[] -> e3 (* list with exactly 2 elements h1 and h2 *)`

`| h::t -> e4 (* list with more than 2 elements but h is the first element*)`

note: e1, e2, e3, e4 are the same type, the idea here is to extract values from list

#### 3. tuple

since length of tuple is fixed, be careful when matching it

example: `match tup with (x,y) -> x=y;;`

error-example: `match tup with`

`| (x,y) -> x + y`

`| (x,y,z) -> x + y + z;; (* don't do this *)`

valid-example: `match (1,2,3) with`

`| (2,_,a) -> a`

`| (1,2,a) -> a + 1 (* match here *)`

`| (_,_,a) -> a + 2;; (* output: 4 *)`

#### 4. record

`type data = { month: string; day: int; year: int };;`

`let today = { day=29; year=2023; month="feb"};;`

`match today with`

`| {day=4; month="jun"} -> "cool, my birthday"`

`| _ -> "sad, not my birthday";; (* output: "sad, not my birthday" *)`

#### 5. variant

`type linked = Null | Item of string * linked;;`

`let items = Item("banana", Item("apple", Null));;`

`let rec count_items items = match items with`

`| Null -> 0 (* base case *)`

`| Item(name, next) -> 1 + count_items next;;`

`count_items items;; (* output: 2 *)`

## V. Higher Order Functions

### 1. map

```
let rec map f l = match l with
| [] -> []
|h::t -> (f h)::(map f t);;
```

type: val map : ('a -> 'b) -> 'a list -> 'b list = <fun>

note: we use map() when the output is a list having the same length as input list

### 2. fold left

```
let rec fold_left f a lst = match lst with
| [] -> a
|h::t -> fold_left f (f a h) t;;
```

type: val fold\_left : ('a -> 'b -> 'a) -> 'a -> 'b list -> 'a = <fun>

note: 1. when the output of function is completely different from the input -> fold  
2. the type of a (accumulator) must be same as output type, also a base case  
3. the function we use for fold is on element inside lst, usually go with 1 or more restrict conditions, hardest part, try to find it.

example:

```
count_occ lst target
```

Type: 'a list -> 'a -> int

Description: returns how many elements in lst are equal to target.

=> analysis:

1. input type is 'a list, but output is int => use fold

2. what is type of a? => output type => int  
base case? => no occurrence => 0

3. what is a function we need?

=> we know: that fun is on every element in the list

=> we want: what is relation between that element and our concern?

=> we think: is it equal to target?

=> we do: if yes then increase accumulator by 1, if no then nothing happens

=> we implement: how can we write that fun? (\* it's fun but not fun :D \*)

=> final answer:

```
count_occ lst target = fold_left (fun a h -> if h = target then a + 1 else a) 0 lst;;
```

### 3. fold right

```
let rec fold_right f l a = match l with
| [] -> a
|h::t -> f h (fold_right f t a);;
```

technically, fold\_right is similar to fold\_left but we iterate each element from right to left instead of from left to right

note: the order of arguments is slightly different from fold\_left

\*Illustration of fold\_left and fold\_right

**fold\_left** f init [a;b;c] => f (f (f init a) b) c

**fold\_right** f [a;b;c] init => f a (f b (f c init))