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spont_decay_v2.py
                                 -- radioactive spontaneous decay -- applying a monte-carlo method
                                     by Kostas Tsachalinas, 2022
   - main idea based on listing #6.6 (p.282) of 'Computational Problems for Physics' book #
          but heavily modified and enriched, by using python's vectorizing techniques, making some calculations, as well as plotting output data, regression line and generated pseudo-randoms histogram
import numpy as np
import matplotlib.pyplot as plt import random
seed = 200
                                                   # set the seed of python's pseudo-randoms generator
random.seed(seed)
                                                   # probabilistic spontaneous decay rate parameter \lambda\colon # probability of a single atom decaying @ a certain time-step
lambda1 = 0.005
N = 100000
                                                   # initial number of radioactive atoms population
time max = 3000
                                                    # max number of mc-time steps for current simulation,
                                                    # -> max possible length of discrete-time vector
tV = np.linspace(0,time_max, time_max)  # create time-vector of successive points (start, end & number of points)  tV = tV.astype(int)  # convert to vector of integers, for discrete numbering m.c. steps in time-evolution loop
rem_atomsV = np.zeros(time_max)
                                                   # create vector of remaining atoms @ each t-step, of length time_max (init all vals to 0)
plot histogram = 1
                                                   # flag to/not-to plot histogram of [0,1) pseudo-randoms distribution
                                                  # this will take some time, depending on atoms number N ! # create & init vector for storing pseudo-randoms, of adequate size
if (plot histogram):
  rndV = np.zeros(int(N*time_max/10))
mc tries = 0
                                                   # monte-carlo tries number, init val
                                                   # current number of non-decayed atoms, fed as upper limit of (decaying) atoms sweeping loop # @ a given time-step (default: N, for time=0)
remaining atoms = N
rem_atomsV[0] = N
                                                   \# init: remaining atoms @ simulation start (t=0), stored @ vector
                                                   # time vector upper limit, to be used for calculations & plotting (default: time_max)
# init val of population zero-out time, exact val to be calculated later on..
# init val of current population distance from 50%, for half-life time estimation
t_end = time_max
zo_time = time_ma
zo_time = time_max
delta_from_half = 50.0
print(" time = 0 | non-decayed population :", N,"/",N,"atoms ( 100 % ) ") # print population initial condition
for time in tV[1:-1]:
                                                   # time evolution loop: current time taken out of mc-steps time vector tV (tV[0]=0)
     # At this mc time-step, some atoms of the remaining population may stochastically decay:
     for atom in range(1, remaining_atoms + 1):
          my_random = random.random()
mc_tries += 1
                                                                        \# get a pseudo-random float in [0,1) from python's pseudorandoms generator \# increase index of mc tries
          if (my_random < lambda1):</pre>
                                                                         # probabilistic rule for stochastic radioactive decay of a certain atom
                                                                        # -> revise non-decayed atoms population respectively
               remaining_atoms -= 1
          if (plot histogram):
                rndV[mc_tries] = my_random
                                                                        \ensuremath{\text{\#}} store this pseudo-random to vector, to do some graph later on
                                                                        # store current population number @ vector indexed by mc time-steps
     rem atomsV[time] = remaining atoms
     # Estimating half-life time, directly from simulation:
     tmp_delta_from_half = delta_from_half
                                                                        # store previous val, for comparing with current val
     rem perc = float(remaining atoms)*100.0/float(N) # percentage (%) of remaining over initial population
     delta from half = np.abs(rem perc - 50.0)
                                                                        # percentage distance from 50%
     if (delta_from_half < tmp_delta_from_half):</pre>
                                                                        # get an even better aproach to half-life time value
     half_life_time = time

#

formatted_perc ='{:.3}'.format(rem_perc)
mcc_tries_sci_not = '{:.4e}'.format(mc_tries)
                                                                # string format: set population percentage @ 3 decimal places
# string format: set monte-carlo tries number @ sci notation (4 decimal
print(" \ time = ",time," \ | \ non-decayed \ population : ",remaining\_atoms,"/",N, \ "atoms (", formatted\_perc ,"%) \ m.c. \\ tries : ",mc\_tries\_sci\_not)
     if (remaining atoms == 0):
        zo_time = time
                                                                        # population zero-out time
       break
 print("\n total monte-carlo tries involved :", mc_tries) \# all mc tries: (successful/unsuccessful) \\ print("\n half-life time = ",half_life_time, "mc time-steps (directly from simulation)") \\
# LINEAR REGRESSION:
if (zo_time < time_max):</pre>
     t_end = zo_time
                                                                   # to be used @ plotting time subvector
regr_last = 1500
                                                                   # upper limit index of acceptable x-axis data points, for linear regression
if (regr_last > zo_time):
    regr_last = zo_time - 1
                                                                   # just as not to assume more input data than actual ones!
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log_rem_atomsV = np.log(rem_atomsV[:regr_last])
                                                                              # transform y-axis vals to log scale
# Fit chosen data by linear regression polynomial:
# slope, intercept = np.polyfit(xV, yV, n)
a, b = np.polyfit(tV[:regr_last], log_rem_atomsV, 1)
                                                                              # here, degree of polynomial n = 1 (least-squares line)
 print("\n regression line slope :", a,"\n actual decay-rate constant :", lambda1,"(time-step^-1)\n rel. error : ", np.abs( (np.abs(a)-lambda1)*100.0/lambda1),"%\n" ) 
# this figure, (#1), will overlay both mc-simulation data & respective regression line:
fig1 = plt.figure()
plt.yscale('log')
                                                                          # setting log scale @ y-axis (semi-log diagram)
                                                                          \# create regression line points vector and exponentiate, \# so as regression line will emerge @ semi-log diagram
yyV = np.exp(a * tV[:t_end-1] + b)
# Regression line points scatterplot (plot up to t_end-1, to avoid plotting log[n=0] @ t_end): plt.scatter(tV[:t_end-1], yyV, color='gray', marker='.',label='L-S linear regression line')
# Remaining atoms data vs. mc-time scatterplot:
plt.scatter(tV[:t_end-1], rem_atomsV[:t_end-1], color='red', marker='.',label='Monte-Carlo simulation')
 plt.grid(color='gray', linestyle='--', linewidth=2) \\ plt.title('Radioactive spontaneous decay monte-carlo simulation\n(regression line slope: %f)'%a) \\ plt.xlabe1('Time (MC steps)') \\ plt.ylabe1('Non-decayed atoms population, N(t)') 
plt.legend()
  this figure, (#2), will plot a frequencies histogram of all randoms used, to verify their unifom distribution in [0,1):
if (plot_histogram):
rnd_effV = rndV[:mc_tries]  # use mc-tries number indexing subvector up to population zero-out (effective randoms vector)
   fig2 = plt.figure()
   #n, bins, patches = plt.hist(xV, bins='auto')
plt.hist(rnd_effV, bins='auto')
   plt.grid(axis='y') # set grid on y-axis
plt.xlabe1('pseudo-random float in [0,1)')
plt.ylabe1('counts')
plt.title('%s uniformly-distributed pseudo-randoms freq. histogram,\nused @ this monte-carlo simulation'%mc_tries_sci_not)
   # this (optional) figure, (#3), will plot a scatterplot of all [0,1) pseudo-randoms used vs. their indices # Notice: Big data -> very slow! Use only @ small initial atoms population N!
   plot_rnd_scattterp1 = 0
if (plot_rnd_scattterp1):
     fig3 = plt.figure()
      rnd_indexV= np.arange(1,len(rnd_effV)+1)
     plt.scatter(rnd_indexV, rnd_effV,marker='.')
     plt.grid(axis='x')  # set grid on x-axis
plt.grid(axis='y')  # set grid on y-axis
plt.xlabel('pseudo-random index #')
plt.ylabel('pseudo-random float')
plt.title('%s uniformly-distributed pseudo-randoms scatterplot,\nused @ this monte-carlo simulation'%mc_tries_sci_not)
plt.show() # show all created figures. User must close all figure windows, so as this program will terminate !
print(" -- Program end --\n")
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