VAE - AE with Variables

1 INTRODUCTION

VAE is a toy language for the COSE212 course at Korea University. VAE stands for an extension of the AE language with **variables**, and it supports the following features:

- number (integer) values (0, 1, -1, 2, -2, 3, -3, ...)
- arithmetic operators: addition (+) and multiplication (*)
- immutable variable definitions (val)

This document is the specification of VAE. First, Section 2 describes the concrete syntax, and Section 3 describes the abstract syntax. Then, Section 4 describes the big-step operational (natural) semantics of VAE.

2 CONCRETE SYNTAX

The concrete syntax of VAE is written in a variant of the extended Backus-Naur form (EBNF). The notation <nt> denotes a nonterminal, and "t" denotes a terminal. We use ? to denote an optional element and + (or *) to denote one or more (or zero or more) repetitions of the preceding element. We use butnot to denote a set difference to exclude some strings from a producible set of strings. We omit some obvious terminals using the ellipsis (...) notation.

The precedence and associativity of operators are defined as follows:

Operator	Associativity	Precedence
*	left	1
+	left	2

3 ABSTRACT SYNTAX

The abstract syntax of VAE is defined as follows:

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Expressions \mathbb{E} \ni e := n (Num)

\begin{vmatrix} e + e & (\text{Add}) \\ | e * e & (\text{Mul}) \\ | val \ x = e; \ e & (\text{Val}) \end{vmatrix} where \begin{cases} \text{Numbers} & n \in \mathbb{Z} \\ \text{Identifiers} \end{cases} (String)
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4 SEMANTICS

We use the following notations in the semantics:

Environments
$$\sigma \in \mathbb{X} \xrightarrow{\text{fin}} \mathbb{Z}$$
 (Env)

The big-step operational (natural) semantics of VAE is defined as follows:

$$\operatorname{Num} \frac{}{ \vdash n \Rightarrow n} \operatorname{Add} \frac{\vdash e_1 \Rightarrow n_1 \qquad \vdash e_2 \Rightarrow n_2}{\vdash e_1 + e_2 \Rightarrow n_1 + n_2} \operatorname{Mul} \frac{\vdash e_1 \Rightarrow n_1 \qquad \vdash e_2 \Rightarrow n_2}{\vdash e_1 * e_2 \Rightarrow n_1 \times n_2}$$

$$\operatorname{Val} \frac{\sigma \vdash e_1 \Rightarrow n_1 \qquad \sigma[x \mapsto n_1] \vdash e_2 \Rightarrow n_2}{\sigma \vdash \operatorname{val} x = e_1; \ e_2 \Rightarrow n_2} \operatorname{Id} \frac{x \in \operatorname{Domain}(\sigma)}{\sigma \vdash x \Rightarrow \sigma(x)}$$