VAE - Arithmetic Expressions with Variables

1 INTRODUCTION

VAE is a toy language for the COSE212 course at Korea University. VAE stands for a language of arithmetic expressions with variables, and it supports the following features:

- integers
- basic arithmetic operators: addition (+) and multiplication (*)
- immutable variables (val)

This document is the specification of VAE. First, Section 2 describes the concrete syntax, and Section 3 describes the abstract syntax. Then, Section 4 describes the big-step operational (natural) semantics of VAE.

2 CONCRETE SYNTAX

The concrete syntax of VAE is written in a variant of the extended Backus–Naur form (EBNF). The notation <nt> denotes a nonterminal, and "t" denotes a terminal. We use ? to denote an optional element and + (or *) to denote one or more (or zero or more) repetitions of the preceding element. We use butnot to denote a set difference to exclude some strings from a producible set of strings. We omit some obvious terminals using the ellipsis (...) notation.

The precedence and associativity of operators are defined as follows:

Operator	Associativity	Precedence
*	left	1
+	left	2

3 ABSTRACT SYNTAX

The abstract syntax of VAE is defined as follows:

```
Expressions e := n
                                   (Num)
                                                     Environments \sigma \in \mathbb{X} \xrightarrow{\text{fin}} \mathbb{Z}
             |e+e|
                                   (Add)
                                                                                                 (Env)
             |e \times e|
                                   (Mul)
                                                     Integers
                                                                             n \in \mathbb{Z}
                                                                                                 (BigInt)
             | val x = e; e  (Val)
                                                     Identifiers
                                                                             x \in \mathbb{X}
                                                                                                 (String)
                                   (Id)
             |x|
```

4 SEMANTICS

The big-step operational (natural) semantics of VAE is defined as follows: