# RFAE - FAE with Recursion and Conditionals

#### 1 INTRODUCTION

RFAE is a toy language for the COSE212 course at Korea University. RFAE stands for an extension of the FAE language with **recursion** and **conditionals**, and it supports the following features:

- integers
- arithmetic operators: negation (-), addition (+), subtraction (-), multiplication (\*), division (/), and modulo (%)
- first-class functions
- recursive functions (def)
- conditionals (if-else)
- boolean values (true and false)
- arithmetic comparison operators: equality (== and !=) and relational (<, >, <=, and >=)
- **logical operators**: conjunction (&&), disjunction (||), and negation (!)

This document is the specification of RFAE. First, Section 2 describes the concrete syntax, and Section 3 describes the abstract syntax with the desugaring rules. Then, Section 4 describes the big-step operational (natural) semantics of RFAE.

#### 2 CONCRETE SYNTAX

The concrete syntax of RFAE is written in a variant of the extended Backus–Naur form (EBNF). The notation <nt> denotes a nonterminal, and "t" denotes a terminal. We use? to denote an optional element and + (or \*) to denote one or more (or zero or more) repetitions of the preceding element. We use <a href="butnot">butnot</a> to denote a set difference to exclude some strings from a producible set of strings. We omit some obvious terminals using the ellipsis (...) notation.

```
// basic elements
<digit> ::= "0" | "1" | "2" | ... | "9"
<number> ::= "-"? <digit>+
<alphabet> ::= "A" | "B" | "C" | ... | "Z" | "a" | "b" | "c" | ... | "z"
<idstart> ::= <alphabet> | "_"
<idcont> ::= <alphabet> | "_" | <digit>
<keyword> ::= "true" | "false" | "def" | "if" | "else"
<id>
          ::= <idstart> <idcont>* butnot <keyword>
// expressions
          ::= <id> | <number> | "true" | "false"
<expr>
             | <uop> <expr> | <expr> <bop> <expr>
             | "(" <expr> ")" | "{" <expr> "}"
             | <id> "=>" <expr> | <expr> "(" <expr> ")"
             | "def" <id> "(" <id> ")" "=" <expr> ";" <expr>
             | "if" "(" <expr> ")" <expr> "else" <expr>
// operators
          ::= "-" | "!"
<qop>
<bop>
           ::= "+" | "-" | "*" | "%" | "&&" | "||"
             | "==" | "!=" | "<" | "<=" | ">" | ">="
```

The precedence and associativity of operators are defined as follows:

Description	Operator	Precedence	Associativity
Unary	-, !	1	right
Multiplicative	*, /, %	2	
Additive	+, -	3	
Relational	<, <=, >, >=	4	left
Equality	==, !=	5	
Logical Conjunction	&&	6	
Logical Disjunction	П	7	

## 3 ABSTRACT SYNTAX

The abstract syntax of RFAE is defined as follows:

Expressions 
$$\mathbb{E} \ni e := n$$
 (Num)  
 $\begin{vmatrix} b & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & &$ 

where

$$\begin{array}{ll} \text{Integers} & n \in \mathbb{Z} & \text{(BigInt)} \\ \text{Booleans} & b \in \mathbb{B} = \{ \text{true}, \text{false} \} & \text{(Boolean)} \\ \text{Identifiers} & x \in \mathbb{X} & \text{(String)} \\ \end{array}$$

The semantics of the remaining cases are defined with the following desugaring rules:

$$\begin{split} \mathcal{D} \llbracket - e \rrbracket &= \mathcal{D} \llbracket e \rrbracket * (-1) \\ \mathcal{D} \llbracket ! \ e \rrbracket &= \mathrm{if} \left( \mathcal{D} \llbracket e \rrbracket \right) \text{ false else true} \\ \mathcal{D} \llbracket e_1 - e_2 \rrbracket &= \mathcal{D} \llbracket e_1 \rrbracket + \mathcal{D} \llbracket - e_2 \rrbracket \\ \mathcal{D} \llbracket e_1 \& \& e_2 \rrbracket &= \mathrm{if} \left( \mathcal{D} \llbracket e_1 \rrbracket \right) \mathcal{D} \llbracket e_2 \rrbracket \text{ else false} \\ \mathcal{D} \llbracket e_1 \mid \mid \mid e_2 \rrbracket &= \mathrm{if} \left( \mathcal{D} \llbracket e_1 \rrbracket \right) \text{ true else } \mathcal{D} \llbracket e_2 \rrbracket \\ \end{split}$$

The omitted cases recursively apply the desugaring rule to sub-expressions.

### 4 **SEMANTICS**

We use the following notations in the semantics:

The big-step operational (natural) semantics of RFAE is defined as follows: