AE - Arithmetic Expressions

1 INTRODUCTION

AE is a toy language for the COSE212 course at Korea University. AE stands for a language of arithmetic expressions that supports the following features:

- integers
- basic arithmetic operators: addition (+) and multiplication (*)

This document is the specification of AE. First, Section 2 describes the concrete syntax, and Section 3 describes the abstract syntax. Then, Section 4 describes the big-step operational (natural) semantics of AE.

2 CONCRETE SYNTAX

The concrete syntax of AE is written in a variant of the extended Backus–Naur form (EBNF). The notation <nt> denotes a nonterminal, and "t" denotes a terminal. We use ? to denote an optional element, + to denote one or more repetitions of the preceding element, and * to denote zero or more repetitions of the preceding element.

```
<digit> ::= "0" | "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9"
<number> ::= "-"? <digit>+
<expr> ::= <number> | <expr> "+" <expr> | <expr> "*" <expr> | "(" <expr> ")"
```

The precedence and associativity of operators are defined as follows:

Operator	Associativity	Precedence
*	left	1
+	left	2

3 ABSTRACT SYNTAX

The abstract syntax of AE is defined as follows:

Expressions
$$e := n$$
 (Num) $\mid e + e$ (Add) $\mid e \times e$ (Mul)

where

Integers
$$n \in \mathbb{Z}$$
 (BigInt)

4 SEMANTICS

The big-step operational (natural) semantics of AE is defined as follows:

$$\begin{array}{c|c} & & & & \\ \hline \vdash e \Rightarrow n \\ \\ \text{Num} \ \hline \\ \vdash n \Rightarrow n \end{array} \qquad \text{Add} \ \frac{\vdash e_1 \Rightarrow n_1 \qquad \vdash e_2 \Rightarrow n_2}{\vdash e_1 + e_2 \Rightarrow n_1 + n_2} \qquad \text{Mul} \ \frac{\vdash e_1 \Rightarrow n_1 \qquad \vdash e_2 \Rightarrow n_2}{\vdash e_1 \times e_2 \Rightarrow n_1 \times n_2}$$