# VAE - AE with Variables

## 1 INTRODUCTION

VAE is a toy language for the COSE212 course at Korea University. VAE stands for an extension of the AE language with **variables**, and it supports the following features:

- integers
- basic arithmetic operators: addition (+) and multiplication (\*)
- immutable variables (val)

This document is the specification of VAE. First, Section 2 describes the concrete syntax, and Section 3 describes the abstract syntax. Then, Section 4 describes the big-step operational (natural) semantics of VAE

#### 2 CONCRETE SYNTAX

The concrete syntax of VAE is written in a variant of the extended Backus-Naur form (EBNF). The notation <nt> denotes a nonterminal, and "t" denotes a terminal. We use ? to denote an optional element and + (or \*) to denote one or more (or zero or more) repetitions of the preceding element. We use <a href="butnot">butnot</a> to denote a set difference to exclude some strings from a producible set of strings. We omit some obvious terminals using the ellipsis (...) notation.

The precedence and associativity of operators are defined as follows:

Operator	Associativity	Precedence
*	left	1
+	left	2

## 3 ABSTRACT SYNTAX

The abstract syntax of VAE is defined as follows:

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Expressions e := n (Num)

\begin{vmatrix} e + e & (Add) \\ e \times e & (Mul) \\ val \ x = e; \ e & (Val) \end{vmatrix} where \begin{vmatrix} Integers & n \in \mathbb{Z} & (BigInt) \\ Identifiers & x \in \mathbb{X} & (String) \end{vmatrix}
```

# 4 **SEMANTICS**

We use the following notations in the semantics:

Environments 
$$\sigma \in \mathbb{X} \xrightarrow{\text{fin}} \mathbb{Z}$$
 (Env)

The big-step operational (natural) semantics of VAE is defined as follows:

$$\sigma \vdash e \Rightarrow n$$

$$\operatorname{Num} \frac{\sigma \vdash n \Rightarrow n}{\sigma \vdash n \Rightarrow n} \qquad \operatorname{Add} \frac{\sigma \vdash e_1 \Rightarrow n_1 \qquad \sigma \vdash e_2 \Rightarrow n_2}{\sigma \vdash e_1 + e_2 \Rightarrow n_1 + n_2} \qquad \operatorname{Mul} \frac{\sigma \vdash e_1 \Rightarrow n_1 \qquad \sigma \vdash e_2 \Rightarrow n_2}{\sigma \vdash e_1 \times e_2 \Rightarrow n_1 \times n_2}$$

$$\operatorname{Val} \frac{\sigma \vdash e_1 \Rightarrow n_1 \qquad \sigma[x \mapsto n_1] \vdash e_2 \Rightarrow n_2}{\sigma \vdash \operatorname{val} x = e_1; \ e_2 \Rightarrow n_2} \qquad \operatorname{Id} \frac{x \in \operatorname{Domain}(\sigma)}{\sigma \vdash x \Rightarrow \sigma(x)}$$