# **FVAE - VAE with First-Class Functions**

#### 1 INTRODUCTION

FVAE is a toy language for the COSE212 course at Korea University. FVAE stands for an extension of the VAE language with **first-class functions**, and it supports the following features:

- integers
- basic arithmetic operators: addition (+) and multiplication (\*)
- immutable variables (val)
- first-class functions (def)

This document is the specification of FVAE. First, Section 2 describes the concrete syntax, and Section 3 describes the abstract syntax. Then, Section 4 describes the big-step operational (natural) semantics of FVAE.

#### 2 CONCRETE SYNTAX

The concrete syntax of FVAE is written in a variant of the extended Backus–Naur form (EBNF). The notation <nt> denotes a nonterminal, and "t" denotes a terminal. We use? to denote an optional element and + (or \*) to denote one or more (or zero or more) repetitions of the preceding element. We use <a href="butnot">butnot</a> to denote a set difference to exclude some strings from a producible set of strings. We omit some obvious terminals using the ellipsis (...) notation.

The precedence and associativity of operators are defined as follows:

Operator	Associativity	Precedence
*	left	1
+	left	2

#### 3 ABSTRACT SYNTAX

The abstract syntax of FVAE is defined as follows:

where

Environments 
$$\sigma \in \mathbb{X} \xrightarrow{\text{fin}} \mathbb{V}$$
 (Env) Identifiers  $x \in \mathbb{X}$  (String)

### 4 SEMANTICS

The big-step operational (natural) semantics of FVAE is defined as follows:

## 4.1 Dynamic Scoping

The above semantics is defined with **static scoping** (or **lexical scoping**). We can augment it with **dynamic scoping** by changing the rule for function application as follows:

$$\operatorname{App} \frac{\sigma \vdash e_0 \Rightarrow \langle \lambda x. e_2, \sigma' \rangle \qquad \sigma \vdash e_1 \Rightarrow v_1 \qquad \sigma[x \mapsto v_1] \vdash e_2 \Rightarrow v_2}{\sigma \vdash e_0(e_1) \Rightarrow v_2}$$