# KFAE - FAE with First-Class Continuations

### 1 INTRODUCTION

KFAE is a toy language for the COSE212 course at Korea University. KFAE stands for the KFAE language with the **first-class continuations**, and it supports the following features:

- number (integer) values (0, 1, -1, 2, -2, 3, -3, ...)
- arithmetic operators: addition (+) and multiplication (\*)
- immutable variable definitions (val)
- first-class functions (=>)
- first-class continuations (vcc)

This document is the specification of KFAE. First, Section 2 describes the concrete syntax, and Section 3 describes the abstract syntax with the desugaring rules. Then, Section 4 describes the small-step operational (reduction) semantics of KFAE.

#### 2 CONCRETE SYNTAX

The concrete syntax of KFAE is written in a variant of the extended Backus–Naur form (EBNF). The notation <nt> denotes a nonterminal, and "t" denotes a terminal. We use ? to denote an optional element and + (or \*) to denote one or more (or zero or more) repetitions of the preceding element. We use <a href="button">butnot</a> to denote a set difference to exclude some strings from a producible set of strings. We omit some obvious terminals using the ellipsis (...) notation.

The precedence and associativity of operators are defined as follows:

Operator	Associativity	Precedence
*	left	2
+	left	1

#### 3 ABSTRACT SYNTAX

The abstract syntax of KFAE is defined as follows:

Expressions 
$$\mathbb{E} \ni e := n$$
 (Num)  
 $| e + e$  (Add)  
 $| e * e$  (Mul)  
 $| x$  (Id) where  $| \lambda x.e$  (Fun)  
 $| e(e)$  (App)  
 $| \text{vcc } x; \ e$  (Vcc)

The semantics of the remaining cases are defined with the following desugaring rules:

$$\mathcal{D}[\![\mathsf{val}\ x = e_1;\ e_2]\!] = (\lambda x. \mathcal{D}[\![e_2]\!])(\mathcal{D}[\![e_1]\!])$$

The omitted cases recursively apply the desugaring rule to sub-expressions.

## 4 SEMANTICS

We use the following notations in the semantics:

The small-step operational (reduction) semantics of KFAE is defined as follows:

where  $\rightarrow^*$  is the reflexive-transitive closure of  $\rightarrow$  and denotes the repeated reduction:

$$\langle \kappa \mid \mid s \rangle \rightarrow^* \langle \kappa \mid \mid s \rangle$$

$$\frac{\langle \kappa \mid \mid s \rangle \rightarrow^* \langle \kappa' \mid \mid s' \rangle \qquad \langle \kappa' \mid \mid s' \rangle \rightarrow \langle \kappa'' \mid \mid s'' \rangle}{\langle \kappa \mid \mid s \rangle \rightarrow^* \langle \kappa'' \mid \mid s'' \rangle}$$

The evaluation result of an expression e is the value v if

$$\langle (\varnothing \vdash e) :: \Box \mid \mid \blacksquare \rangle \to^* \langle \Box \mid \mid v :: \blacksquare \rangle$$