MAGNET – Mutable Arithmetic Expressions with Generators and Exceptions

1 INTRODUCTION

MAGNET is a toy language for the COSE212 course at Korea University. MAGNET stands for the **M**utable **A**rithmetic Expressions with **Gen**erators and **E**xceptions, and it supports the following features:

- undefined value (undefined):
- number values (0, 1, -1, 2, -2, 3, -3, ...)
- boolean values (true and false)
- arithmetic operators: negation (-), addition (+), subtraction (-), multiplication (*), division (/), and modulo (%)
- logical operators: conjunction (&&), disjunction (||), and negation (!)
- **comparison operators**: equality (== and !=) and relational (<, >, <=, and >=)
- mutable variable definitions (var) and identifier lookup (x)
- variable assignment (=) and sequences (;)
- augmented assignment (+=, -=, *=, /=, and %=) and increment/decrement (++ and --)
- conditionals (if-else), while loops (while), break (break), and continue (continue)
- first-class functions (=> or function)
- function applications and return (return)
- try-catch (try-catch) and throw (throw)
- generators (=>* or function*) and yield (yield)
- iterator next (_.next) and iterator result accessors (_.value and _.done)
- for-of loops (for-of)

This document is the specification of MAGNET. First, Section 2 describes the concrete syntax, and Section 3 describes the abstract syntax with the desugaring rules. Then, Section 4 describes the small-step operational (reduction) semantics of MAGNET.

2 CONCRETE SYNTAX

The concrete syntax of MAGNET is written in a variant of the extended Backus–Naur form (EBNF). The notation <nt> denotes a nonterminal, and "t" denotes a terminal. We use? to denote an optional element and + (or *) to denote one or more (or zero or more) repetitions of the preceding element. We use butnot to denote a set difference to exclude some strings from a producible set of strings. We omit some obvious terminals using the ellipsis (...) notation.

```
// expressions
<expr> ::= "undefined" | <number> | "true" | "false"
        // unary and binary operators
        | <uop> <expr> | <expr> <bop> <expr>
        // parentheses
        | "(" <expr> ")" | "{" <expr> "}"
        // mutable variable definitions
        "var" <id> "=" <expr> ";" <expr> | <id>
        // variable (augmented) assignment and sequence
        | <id> <aop> <expr> | <expr> ";" <expr>
        // increment and decrement
        // conditionals and loops
        | "if" "(" <expr> ")" <expr> "else" <expr>
        | "while" "(" <expr> ")" <expr>
        // first-class functions
        | <params> "=>" <expr> | "function" <params> "{" <expr> "}" <expr>
        // function applications and returns
        | <expr> "(" <expr> ")" | "return" <expr>
        // try-catch and throw
        | "try" <expr> "catch" "(" <id> ")" <expr> | "throw" <expr>
        // generators and yields
        <params> "=>" "*" <expr>
        | "function" "*" <params> "{" <expr> "}" <expr> | "yield" <expr>
        // iterator next and iterator result accessors
        | <expr> "." "next" "(" <expr>? ")"
        | <expr> "." "value" | <expr> "." "done"
// operators
<aop> ::= "=" | "+=" | "-=" | "*=" | "/=" | "%="
<uop> ::= "-" | "!"
<bop> ::= "+" | "-" | "*" | "/" | "%" | "&&" | "||"
       | "==" | "!=" | "<" | "<=" | ">" | ">="
// parameters
<params> ::= "(" ")" | "(" <id> ")" | "(" <id> ["," <id>]* ")"
```

The precedence and associativity of operators are defined as follows:

Description	Operator	Precedence	Associativity
Postfix Unary	++,,next,value,done	1	left
Prefix Unary	-, !, ++,	2	right
Multiplicative	*, /, %	3	left
Additive	+, -	4	
Relational	<, <=, >, >=	5	
Equality	==, !=	6	
Logical Conjunction	&&	7	
Logical Disjunction		8	
Assignment	=, +=, -=, *=, /=, %=, var	9	right
Sequence	;	10	left

3 ABSTRACT SYNTAX

The abstract syntax of MAGNET is defined as follows:

```
Expressions \mathbb{E} \ni e ::= \text{undefined}
                                                        | if (e) e else e
                                      (EUndef)
                                                                               (EIf)
                                      (ENum)
                                                        | while (e) e
                                                                               (EWhile)
                                      (EBool)
                                                        break
                                                                               (EBreak)
                                                                               (EContinue)
                                      (Add)
                                                        continue
                       | e * e
                                      (Mul)
                                                        |\lambda(x,\ldots,x).e|
                                                                               (EFun)
                       |e|/e
                                      (EDiv)
                                                        |e(e,\ldots,e)|
                                                                               (EApp)
                       l e % e
                                      (EMod)
                                                        | return e
                                                                               (EReturn)
                       |e| == e
                                                        | try e catch (x) e
                                      (EEq)
                                                                              (ETry)
                       |e| < e
                                      (ELt)
                                                        | throw e
                                                                               (EThrow)
                                                        |\lambda*(x,\ldots,x).e|
                       | var x=e; e |
                                      (EVar)
                                                                               (EGen)
                                                        |e.next(e^?)|
                                                                               (EIterNext)
                                      (EId)
                                                        | yield e
                       |x=e|
                                      (EAssign)
                                                                               (EYield)
                       | e; e
                                                        |e.value|
                                                                               (EValueField)
                                      (ESeq)
                                                        |e.done|
                                                                               (EDoneField)
```

$$\text{where } \left\{ \begin{array}{ll} \text{Identifier} & x \in \mathbb{X} & (\texttt{String}) \\ \text{Number} & n \in \mathbb{Z} & (\texttt{BigInt}) \end{array} \right. \text{Boolean} \quad \mathbb{B} \ni b ::= \mathsf{true} \mid \mathsf{false} \quad (\mathsf{Boolean})$$

The semantics of the remaining cases are defined with the following desugaring rules:

```
 \mathcal{D} \llbracket -e \rrbracket = \mathcal{D} \llbracket e_1 \rrbracket * (-1) \qquad \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket e_1 - e_2 \rrbracket = \mathcal{D} \llbracket e_1 \rrbracket + \mathcal{D} \llbracket - e_2 \rrbracket \qquad \mathcal{D} \llbracket x - = e \rrbracket = x = x - \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket e_1 \& \& e_2 \rrbracket = \mathrm{if} \left( \mathcal{D} \llbracket e_1 \rrbracket \right) \mathcal{D} \llbracket e_2 \rrbracket \text{ else false } \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket e_1 \& \& e_2 \rrbracket = \mathrm{if} \left( \mathcal{D} \llbracket e_1 \rrbracket \right) \text{ true else } \mathcal{D} \llbracket e_2 \rrbracket \qquad \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket e_1 \& \& e_2 \rrbracket = \mathrm{if} \left( \mathcal{D} \llbracket e_1 \rrbracket \right) \text{ true else } \mathcal{D} \llbracket e_2 \rrbracket \qquad \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + x = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + x = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + x = e \rrbracket = x = x + \mathcal{D} \llbracket e \rrbracket \\ \mathcal{D} \llbracket x + x = e \rrbracket = x = x + x + \mathcal{
```

$$\mathcal{D}[\![\![\!]\!]\!] \text{for } (x \text{ of } e_1) e_2]\!] = \mathcal{D}\begin{bmatrix} \text{var } \underline{x_1} = e_1; \\ \text{var } \underline{x_2} = \underline{x_1}.\mathsf{next()}; \\ \text{while } (! \ \underline{x_2}.\mathsf{done}) \{ \\ \text{var } x = \underline{x_2}.\mathsf{value}; \\ e_2; \ \underline{x_2} = \underline{x_1}.\mathsf{next()} \end{bmatrix}$$

where $\underline{x_k}$ denotes a fresh temporary variable. All the omitted cases recursively apply the desugaring rule to their sub-expressions. For example, $\mathcal{D}[\![e_1 + e_2]\!] = \mathcal{D}[\![e_1]\!] + \mathcal{D}[\![e_2]\!]$.

4 SEMANTICS

We use the following notations in the semantics:

```
\langle \kappa \mid \mid s \mid \mid H \mid \mid M \rangle \in \mathbb{K} \times \mathbb{S} \times \mathbb{H} \times \mathbb{M} (State)
                   Continuations
                                                               \kappa \in \mathbb{K}
                                                                                                (Cont)
                                                               \kappa ::= \Box \mid i :: \kappa
Instructions i \in \mathbb{I}
                                                            (Inst)
                    i := (\sigma \vdash e)
                                                            (IEval)
                                                                                    |jmp-if[\psi]|
                                                                                                         (IJmpIf)
                         (+)
                                                            (IAdd)
                                                                                    | jmp[c]
                                                                                                          (IJmp)
                         |(*)
                                                                                    | call[n]
                                                                                                          (ICall)
                                                            (IMul)
                         +(/)
                                                            (IDiv)
                                                                                    return
                                                                                                          (IReturn)
                          (%)
                                                            (IMod)
                                                                                    next
                                                                                                          (INext)
                          | (==)
                                                            (IEq)
                                                                                    |yield
                                                                                                          (IYield)
                          (<)
                                                            (ILt)
                                                                                    | value
                                                                                                          (IValueField)
                          | def[x,...,x][\sigma \vdash e]
                                                            (IDef)
                                                                                    done
                                                                                                          (IDoneField)
                          |write[a]
                                                            (IWrite)
                                                                                    pop
                                                                                                          (IPop)
                                   Value Stacks s \in \mathbb{S}
                                                                                (Stack)
                                                        s := \blacksquare \mid v :: s
   Values v \in \mathbb{V}
                                                   (Value)
                v := undefined
                                                   (UndefV)
                                                                           |\langle \kappa || s || H \rangle
                                                                                                             (ContV)
                     \mid n \mid
                                                   (NumV)
                                                                           |\langle \lambda *(x,\ldots,x).e,\sigma \rangle|
                                                                                                             (GenV)
                                                                           | iter[a]
                                                   (BoolV)
                                                                                                             (IterV)
                      |\langle \lambda(x,\ldots,x).e,\sigma\rangle|
                                                                                                            (ResultV)
                                                  (CloV)
                                                                           | \{ value : v, done : b \} 
                           Control Handlers H \in \mathbb{H} = \mathbb{C} \xrightarrow{\text{fin}} \Psi (Handler)
        Control Operators
                                     c \in \mathbb{C}
                                                              (Control)
                                                              (Return)
                                     c := return
                                                                                          | throw
                                                                                                       (Throw)
                                                              (Break)
                                                                                          | throw
                                                                                                       (Finally)
                                           break
                                           | continue (Continue)
                                                                                          |yield
                Continuation Values \psi, \langle \kappa \mid \mid s \mid \mid H \rangle \in \Psi = \mathbb{K} \times \mathbb{S} \times \mathbb{H} (KValue)
                                                                M \in \mathbb{M} = \mathbb{A} \xrightarrow{\text{fin}} \mathbb{V}
                                                                                                  (Mem)
                Memories
                                                                 \sigma \in \mathbb{X} \xrightarrow{\text{fin}} \mathbb{A}
                Environments
                                                                                                  (Env)
                Addresses
                                                                  a \in \mathbb{A}
                                                                                                  (Addr)
```

The small-step operational (reduction) semantics of MAGNET is defined in the following form of the reduction relation (\rightarrow) :

$$| \langle \kappa || s || H || M \rangle \rightarrow \langle \kappa || s || H || M \rangle$$

4.1 Reduction Relations for IEval

```
EUndef \langle (\sigma \vdash \mathsf{undefined}) :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle \rightarrow \langle \kappa \mid \mid \mathsf{undefined} :: s \mid \mid H \mid \mid M \rangle
                        \langle (\sigma \vdash n) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
                                                                                                                        \rightarrow \langle \kappa \mid \mid n :: s \mid \mid H \mid \mid M \rangle
ENum
EBool
                        \langle (\sigma \vdash b) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
                                                                                                                        \rightarrow \langle \kappa \mid \mid b :: s \mid \mid H \mid \mid M \rangle
EAdd
                        \langle (\sigma \vdash e_1 + e_2) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
                                                                                                                        \rightarrow \langle (\sigma \vdash e_1) :: (\sigma \vdash e_2) :: (+) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
EMul
                        \langle (\sigma \vdash e_1 * e_2) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
                                                                                                                        \rightarrow \langle (\sigma \vdash e_1) :: (\sigma \vdash e_2) :: (\star) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
EDiv
                        \langle (\sigma \vdash e_1 / e_2) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
                                                                                                                        \rightarrow \langle (\sigma \vdash e_1) :: (\sigma \vdash e_2) :: (/) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
EMod
                        \langle (\sigma \vdash e_1 \% e_2) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
                                                                                                                       \rightarrow \langle (\sigma \vdash e_1) :: (\sigma \vdash e_2) :: (\%) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
                        \langle (\sigma \vdash e_1 == e_2) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
EEa
                                                                                                                       \rightarrow \langle (\sigma \vdash e_1) :: (\sigma \vdash e_2) :: (==) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
ELt
                        \langle (\sigma \vdash e_1 \lessdot e_2) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
                                                                                                                       \rightarrow \langle (\sigma \vdash e_1) :: (\sigma \vdash e_2) :: (<) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
EVar
                        \langle (\sigma \vdash \mathsf{var} \ x = e_1; \ e_2) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \rightarrow \langle (\sigma \vdash e_1) :: \mathsf{def}[x][\sigma \vdash e_2] :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
EId
                        \langle (\sigma \vdash x) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
                                                                                                                      \rightarrow \langle \kappa \mid \mid M(\sigma(x)) :: s \mid \mid H \mid \mid M \rangle
EAssign \langle (\sigma \vdash x=e) :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle
                                                                                                                        \rightarrow \langle (\sigma \vdash e) :: write(\sigma(x)) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle
                        \langle (\sigma \vdash e_1; e_2) :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle
                                                                                                                    \rightarrow \langle (\sigma \vdash e_1) :: \mathsf{pop} :: (\sigma \vdash e_2) :: \kappa \mid | s \mid | H \mid | M \rangle
ESeq
```

4.1.1 Conditionals and While Loops.

EIf
$$\langle (\sigma \vdash if (e_1) e_2 \text{ else } e_3) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle$$
 $\langle (\sigma \vdash e_1) :: jmp-if[\langle (\sigma \vdash e_2) :: \kappa \mid\mid s \mid\mid H \rangle] :: (\sigma \vdash e_3) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle$ EWhile $\langle (\sigma \vdash while (e_1) e_2) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle$ $\langle (\sigma \vdash e_1) :: jmp-if[\psi_{body}] :: \kappa \mid\mid undefined :: s \mid\mid H \mid\mid M \rangle$
$$\begin{cases} \psi_{body} &= \langle (\sigma \vdash e_2) :: jmp[continue] :: \Box \mid\mid s \mid\mid H_{body} \rangle \\ H_{body} &= H[continue \mapsto \psi_{continue}, break \mapsto \psi_{break}] \\ \psi_{continue} &= \langle pop :: (\sigma \vdash while (e_1) e_2) :: \kappa \mid\mid s \mid\mid H \rangle \end{cases} \\ \text{EBreak} & \langle (\sigma \vdash break) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \\ \rightarrow & \langle jmp[break] :: \Box \mid\mid undefined :: s \mid\mid H \mid\mid M \rangle \end{cases}$$

$$EContinue & \langle (\sigma \vdash continue) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \\ \downarrow_{jmp}[continue] :: \Box \mid\mid undefined :: s \mid\mid H \mid\mid M \rangle \end{cases}$$

4.1.2 Functions and Return.

$$\begin{split} & \mathsf{EFun} \qquad \langle (\sigma \vdash \lambda(x,\ldots,x).e) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \\ & \to \qquad \langle \kappa \mid\mid \langle \lambda(x,\ldots,x).e,\sigma \rangle :: s \mid\mid H \mid\mid M \rangle \\ & \mathsf{EApp} \qquad \langle (\sigma \vdash e(e_1,\ldots,e_n)) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \\ & \to \qquad \langle (\sigma \vdash e) :: (\sigma \vdash e_1) :: \ldots :: (\sigma \vdash e_n) :: \mathsf{call}[n] :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \\ & \to \qquad \langle (\sigma \vdash e) :: \mathsf{return} \: e) :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \\ & \to \qquad \langle (\sigma \vdash e) :: \mathsf{return} :: \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \end{aligned}$$

4.1.3 Exceptions.

$$\begin{split} \mathsf{ETry} & \quad \langle (\sigma \vdash \mathsf{try} \ e_1 \ \mathsf{catch} \ (x) \ e_2) \ :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle \\ \to & \quad \langle (\sigma \vdash e_1) \ :: \ \mathsf{jmp[finally]} \ :: \ \square \mid \mid s \mid \mid H_{\mathsf{body}} \mid \mid M \rangle \\ & \quad \mathsf{where} \left\{ \begin{array}{l} H_{\mathsf{body}} \ = \ H[\mathsf{throw} \mapsto \psi_{\mathsf{throw}}, \mathsf{finally} \mapsto \psi_{\mathsf{finally}}] \\ \psi_{\mathsf{throw}} \ = \ \langle \mathsf{def[}x\mathsf{]} [\sigma \vdash e_2] \ :: \kappa \mid \mid s \mid \mid H \rangle \\ \psi_{\mathsf{finally}} \ = \ \langle \kappa \mid \mid s \mid \mid H \rangle \\ \end{array} \right. \\ & \quad \mathsf{EThrow} \quad \langle (\sigma \vdash \mathsf{throw} \ e) \ :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle \\ \to & \quad \langle (\sigma \vdash e) \ :: \ \mathsf{jmp[throw]} \ :: \ \square \mid s \mid \mid H \mid \mid M \rangle \\ \end{split}$$

4.1.4 Generators.

EGen
$$\langle (\sigma \vdash \lambda*(x_1,\ldots,x_n).e) :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$$
 $\rightarrow \qquad \langle \kappa \mid \mid \langle \lambda*(x_1,\ldots,x_n).e,\sigma \rangle :: s \mid \mid H \mid \mid M \rangle$

EIterNext₁ $\langle (\sigma \vdash e_1.\operatorname{next}()) :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$
 $\rightarrow \qquad \langle (\sigma \vdash e_1) :: (\sigma \vdash \operatorname{undefined}) :: \operatorname{next} :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$

EIterNext₂ $\langle (\sigma \vdash e_1.\operatorname{next}(e_2)) :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$
 $\rightarrow \qquad \langle (\sigma \vdash e_1) :: (\sigma \vdash e_2) :: \operatorname{next} :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$

EYield $\langle (\sigma \vdash e_1) :: (\sigma \vdash e_2) :: \operatorname{next} :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$

$$\rightarrow \qquad \langle (\sigma \vdash e) :: \operatorname{yield} :: \Box \mid \mid \operatorname{false} :: \psi_{\operatorname{next}} :: s \mid \mid H \mid \mid M \rangle$$

where $\psi_{\operatorname{next}} = \langle \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$

EValueField $\langle (\sigma \vdash e.\operatorname{value}) :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$

$$\rightarrow \qquad \langle (\sigma \vdash e) :: \operatorname{value} :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$$

EDoneField $\langle (\sigma \vdash e.\operatorname{done}) :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$

$$\langle (\sigma \vdash e) :: \operatorname{done} :: \kappa \mid \mid s \mid \mid H \mid \mid M \rangle$$

4.2 Reduction Relations for Other Instructions

$$\text{where eq}(v_1,v_2) = \left\{ \begin{array}{lll} \text{true} & \text{if } v_1 = v_2 = \text{iter} \llbracket a \rrbracket & \text{true} & \text{if } v_1 = v_2 = \text{undefined} \\ \text{true} & \text{if } v_1 = v_2 = n & \text{true} & \text{if } v_1 = v_2 = \{\text{value}: v, \text{done}: b\} \\ \text{true} & \text{if } v_1 = v_2 = b & \text{false} & \text{otherwise} \end{array} \right.$$

$$\begin{split} & \text{IDef} & \langle \text{def}[x_1,\ldots,x_n][\sigma \vdash e] :: \kappa \mid\mid v_n :: \ldots :: v_1 :: s \mid\mid H \mid\mid M \rangle \\ & \to & \langle \sigma[x_1 \mapsto a_1,\ldots,x_n \mapsto a_n] \vdash e :: \kappa \mid\mid s \mid\mid H \mid\mid M[a_1 \mapsto v_1,\ldots,a_n \mapsto v_n] \rangle \\ & \text{where } \forall 1 \leq p \leq n. \ a_p \notin \text{Domain}(M) \land (\forall 1 \leq q < p. \ a_q \neq a_p) \end{split}$$

$$& \text{IWrite} & \langle \text{write}[a] :: \kappa \mid\mid v :: s \mid\mid H \mid\mid M \rangle \\ & \to & \langle \kappa \mid\mid v :: s \mid\mid H \mid\mid M \rangle \\ & \to & \langle \kappa \mid\mid v :: s \mid\mid H \mid\mid M \rangle \\ & \to & \langle \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \end{split}$$

4.2.1 Control Flow Instructions.

$$\begin{split} \operatorname{IJmpIf}_{\operatorname{true}} \ \langle \operatorname{jmp-if[}\langle \kappa \mid \mid s \mid \mid H \rangle] &:: _ \mid \mid \operatorname{true} :: _ \mid \mid _ \mid \mid M \rangle \rightarrow \langle \kappa \mid \mid s \mid \mid H \mid \mid M \rangle \\ \operatorname{IJmpIf}_{\operatorname{false}} \ \langle \operatorname{jmp-if[}_] &:: \kappa \mid \mid \operatorname{false} :: s \mid \mid H \mid \mid M \rangle \qquad \rightarrow \langle \kappa \mid \mid s \mid \mid H \mid \mid M \rangle \\ \operatorname{IJmp} \ \ \langle \operatorname{jmp[}c] &:: \kappa \mid \mid v :: s \mid \mid H \mid \mid M \rangle \qquad \rightarrow \langle \kappa' \mid \mid v :: s' \mid \mid H'' \mid \mid M \rangle \\ \\ \operatorname{Where} \left\{ \begin{array}{ll} H(c) &= \langle \kappa' \mid \mid s' \mid \mid H' \rangle \\ H'' &= \begin{cases} H'[\operatorname{yield} \mapsto H(\operatorname{yield})] & \text{if yield} \in \operatorname{Domain}(H) \\ H' & \text{otherwise} \end{cases} \right. \end{split}$$

4.2.2 Function Call/Return Instructions.

$$\begin{split} & | \text{ICall}_{\lambda} \quad \langle \text{call}[n] :: \kappa \mid \mid v_n :: \ldots :: v_1 :: \langle \lambda(x_1, \ldots, x_m).e, \sigma' \rangle :: s \mid \mid H \mid \mid M \rangle \\ & \rightarrow \quad \langle \text{def}[x_1, \ldots, x_m][\sigma' \vdash \text{return } e] :: \Box \mid \mid s_{\text{body}} \mid \mid H_{\text{body}} \mid \mid M \rangle \\ & \text{where} \left\{ \begin{array}{l} s_{\text{body}} & = \left\{ \begin{array}{l} v_m :: \ldots :: v_1 :: \blacksquare \\ \text{undefined} :: \ldots :: \text{undefined} :: v_n :: \ldots :: v_1 :: \blacksquare \\ H_{\text{body}} & = H[\text{return} \mapsto \psi_{\text{return}}] \setminus \{\text{break, continue, yield} \} \\ \psi_{\text{return}} & = \langle \kappa \mid \mid s \mid \mid H \rangle \end{array} \right. \end{split}$$

(Note that $A \setminus B$ denotes the removal of B's elements from A)

$$\begin{split} \mathsf{ICall}_{\lambda*} & \quad \langle \mathsf{call}[n] :: \kappa \mid\mid v_n :: \ldots :: v_1 :: \langle \lambda*(x_1, \ldots, x_m).e, \sigma' \rangle :: s \mid\mid H \mid\mid M \rangle \\ \rightarrow & \quad \langle \kappa \mid\mid \mathsf{iter}[a] :: s \mid\mid H \mid\mid M[a \mapsto \psi_{\mathsf{body}}] \rangle \\ \end{split}$$

$$\text{where} \begin{cases} a \notin \text{Domain}(M) \\ \psi_{\text{body}} = \langle \kappa_{\text{body}} \mid \mid s_{\text{body}} \mid \mid \varnothing \rangle \\ \kappa_{\text{body}} = \text{pop} :: \text{def}[x_1, \dots, x_m][\sigma' \vdash \text{return (try e catch (x) x)}] :: \square \\ s_{\text{body}} = \begin{cases} v_m :: \dots :: v_1 :: \blacksquare & \text{if $n > = m$} \\ \text{undefined} :: \dots :: \text{undefined} :: v_n :: \dots :: v_1 :: \blacksquare & \text{otherwise} \end{cases}$$

$$\begin{array}{ll} \text{IReturn} & \langle \text{return} :: \kappa \mid \mid v :: s \mid \mid H \mid \mid M \rangle \\ \\ \rightarrow & \begin{cases} \langle \text{yield} :: \square \mid \mid v :: \text{true} :: \psi_{\text{done}} :: s \mid \mid H \mid \mid M \rangle & \text{if yield} \in \text{Domain}(H) \\ \\ \langle \text{jmp[return]} :: \square \mid \mid v :: \blacksquare \mid \mid H \mid \mid M \rangle & \text{otherwise} \end{cases} \\ \\ \text{where} & \psi_{\text{done}} = \langle \text{return} :: \square \mid \mid \blacksquare \mid \mid \varnothing \rangle \\ \end{aligned}$$

4.2.3 Generator Instructions.

INext
$$\langle \text{next} :: \kappa \mid \mid v :: \text{iter}[a] :: s \mid \mid H \mid \mid M \rangle$$

$$\langle \kappa' \mid \mid v :: s' \mid \mid H_{\text{body}} \mid \mid M \rangle$$

$$\text{where } \begin{cases} M(a) = \langle \kappa' \mid \mid s' \mid \mid H' \rangle \\ H_{\text{body}} = H' [\text{yield} \mapsto \psi, \text{return} \mapsto \psi] \\ \psi = \langle \kappa \mid \mid \text{iter}[a] :: s \mid \mid H \rangle \end{cases}$$

$$\text{IYield } \langle \text{yield} :: _ \mid \mid v :: b :: v' :: _ \mid \mid H \mid \mid M \rangle \\ \wedge \langle \kappa' \mid \mid \{ \text{value} :: v, \text{done} :: b \} :: s' \mid \mid H' \mid \mid M [a \mapsto v'] \} \end{cases}$$

$$\text{where } H(\text{yield}) = \langle \kappa' \mid \mid \text{iter}[a] :: s' \mid \mid H' \rangle$$

$$\text{IValueField } \langle \text{value} :: \kappa \mid \mid \{ \text{value} :: v, \text{done} :: _ \} :: s \mid \mid H \mid \mid M \rangle$$

$$\wedge \langle \kappa \mid \mid v :: s \mid \mid H \mid \mid M \rangle$$

$$\text{IDoneField } \langle \text{done} :: \kappa \mid \mid \{ \text{value} :: _, \text{done} :: b \} :: s \mid \mid H \mid \mid M \rangle$$

$$\wedge \langle \kappa \mid \mid b :: s \mid \mid H \mid \mid M \rangle$$

And \rightarrow^* is the reflexive-transitive closure of \rightarrow and denotes the repeated reduction:

$$\langle \kappa \mid \mid s \mid \mid H \mid \mid M \rangle \rightarrow^* \langle \kappa' \mid \mid s' \mid \mid H' \mid \mid M' \rangle$$

$$\frac{\langle \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \rightarrow \langle \kappa' \mid\mid s' \mid\mid H' \mid\mid M' \rangle \qquad \langle \kappa' \mid\mid s' \mid\mid H' \mid\mid M' \rangle \rightarrow^* \langle \kappa'' \mid\mid s'' \mid\mid H'' \mid\mid M'' \rangle}{\langle \kappa \mid\mid s \mid\mid H \mid\mid M \rangle \rightarrow^* \langle \kappa'' \mid\mid s'' \mid\mid H'' \mid\mid M'' \rangle}$$

The evaluation result of an expression e is the value v if

$$\langle (\varnothing \vdash e) :: \Box \mid \mid \blacksquare \mid \mid \varnothing \mid \mid \varnothing \rangle \rightarrow^* \langle \Box \mid \mid v :: \blacksquare \mid \mid _ \mid \mid _ \rangle$$