Lecture 2 – Random Testing

AAA705: Software Testing and Quality Assurance

Jihyeok Park



2024 Spring

Recall



- Equivalence Partitioning (EP)
- Boundary Value Analysis (BVA)
- Category Partition Method (CPM)
- Combinatorial Testing (CT)
 - Covering Array (CA)
 - Fault Detection Effectiveness
 - Greedy Algorithm IPOG Strategy
 - Greedy vs. Meta-heuristic

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2. Adaptive Random Testing (ART)

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Distance Comparison Target
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Quasi-Random Strategy for ART

3. Fuzz Testing

Pre-process
Input Generation – Mutation-Based Fuzzing
Input Generation – Generation-Based Fuzzing
Test Oracles (Sanitizers)
De-duplication





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- What happens if we just sample the input randomly?
 - Since developers has their own mental model of the software, they
 often have a biased view of the input space.
 - Random testing can help to ignore this bias.



• **SUT**: Software Under Test



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• S: Set of all possible test inputs for SUT



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Failure Rate
$$t = \frac{|F|}{|S|}$$

(The probability that a randomly sampled test input is fail when we sample uniformly at random from S)

Random Testing – Example



- Failure Rate $t \approx 0.5$
- Oracle
 - assertEqual(abs(-5), 5)
 - assertEqual(abs(5), 5)



Pseudo-random number generators (PRNGs)

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- True-random number generators (TRNGs) expensive
 - Atmospheric noise https://random.org
 - Quantum random number generator (QRNG) https://qrng.anu.edu.au
 - Lava lamps Cloudflare

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The new Galaxy Quantum 4 is equipped with the world's smallest (width 2.5mm x length 2.5mm) **Quantum Random Number Generator** (QRNG) chipset, enabling trusted authentication and encryption of information.

Probabilistic Analysis



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Probabilistic Analysis



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 Given a failure rate p, how many test inputs do we need to sample to find the first failure?

 Given n random test inputs, what is the probability of finding at least one failure?



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- The most popular example is the coin flipping.
- The probability mass function (PMF) of the geometric distribution:

$$Pr(X = k) = (1 - p)^{k-1}p$$

It is the probability that the first success occurs on the *n*-th trial.





$$E(X) = \sum_{k=1}^{\infty} k \cdot Pr(X = k)$$



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- Given a failure rate *p*, **how many** test inputs do we need to sample to find the **first failure**?
- Mean (If p = 0.01, the average test inputs = 100)

 $\frac{1}{p}$

• **Median** (If p = 0.01, the median test inputs \approx 69)

$$\left\lceil \frac{-1}{\log_2(1-p)} \right\rceil$$

• Variance (If p = 0.01, the variance = 9900)

$$\frac{1-p}{p^2}$$



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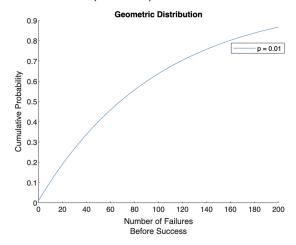
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Probabilistic Analysis – Geometric Distribution



- If we test n = 100 random test inputs, the probability of finding at least one failure is $1 (1 0.01)^{101} = 63.76\%$.
- If we test n = 200 random test inputs, the probability of finding at least one failure is $1 (1 0.01)^{201} = 86.74\%$.



Probabilistic Analysis – Geometric Distribution



- Unfortunately, failure rate *p* is **unknown** in practice.
- But, we can **estimate** *p* in various ways:
 - Previous versions of the software
 - Similar software
 - Literature

Weaknesses of Random Testing



 Random testing provides no guidance; it is the needle in a haystack problem – the probability of finding a failure is low.

```
/* C */
void foo(int x) {
  if (x == 0) {
    /* faulty code here */
  }
}
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# Python
def foo(x):
    # e.g., x = 2840
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- We need biased random testing with predefined probability:
 - Special values (-0, null, π , ...)
 - Extracted values from code (e.g., constants, literals)
 - Previously successful values



• **Apple** (1983) - "Monkey" for random events (e.g., mouse clicks, key presses, etc.) to test the robustness of the MacWrite and MacPaint applications.



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- Netflix (2011) "Chaos Monkey" that randomly terminates AWS instances to test the fault tolerance of the Netflix infrastructure.





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We call such clustered reasons faulty regions.



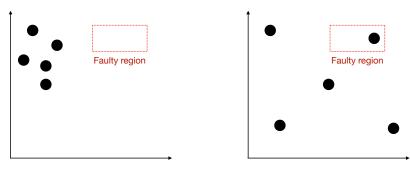
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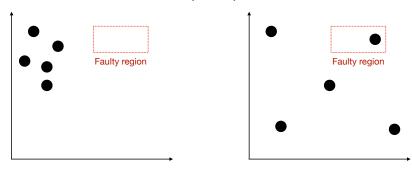
 Without knowing the faulty regions, what is the best way to sample the test inputs?





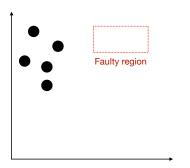
• A more **diverse** set of test inputs is more likely to find a failure.

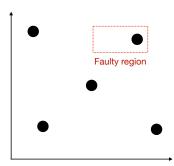




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- Diversity is depending on the **distance** between test inputs.



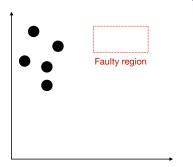


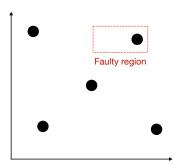


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- If input data is numeric, we can use the Euclidean distance.

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• Then, how to measure the distance between complex data types?



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• and the distance between "uninformed" and "uniform" is 3:

"uninformed"
$$\xrightarrow[n]{\text{delete}}$$
 "uniformed" $\xrightarrow[e]{\text{delete}}$ "uniformd" $\xrightarrow[d]{\text{delete}}$ "uniform"





$$lev(a,b) = \begin{cases} |a| & \text{if } |b| = 0 \\ |b| & \text{if } |a| = 0 \\ lev(tail(a), tail(b)) & \text{if } head(a) = head(b) \\ 1 + \min \begin{cases} lev(tail(a), b) & \text{(insert)} \\ lev(a, tail(b)) & \text{(delete)} \end{cases} & \text{otherwise} \end{cases}$$





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- It is usually extended into a parameterized version with a set of allowed edit operations (e.g., transposition) with different costs.
- Wagner-Fischer algorithm (1967) O(mn) time complexity
- Indyk and Bačkurs (2015) proved that the problem of finding the edit distance cannot be solved in less than quadratic time. (We cannot do better than the Wagner-Fischer algorithm.)



$$diversity(T) = \sum_{(t_1, t_2) \in T \times T} d(t_1, t_2)$$



 The diversity of a test suite is defined as the sum of distances between all pairs of test inputs.

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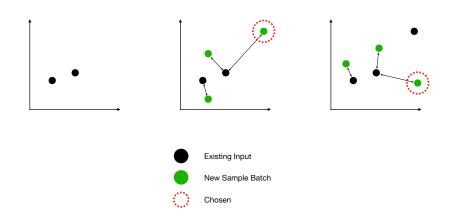
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- Choose the test input that has the maximum distance from the existing test inputs.
- Add the **chosen new test input** to the set of existing test inputs.
- Iterate the process until the stopping criterion is met.





 It samples Z = 3 new test inputs and chooses the one with the maximum distance from the existing test inputs.

Distance Comparison Target



 For each new test case t, we need to choose the target for comparison in the existing test suite T.³

³[CSUR'19] R. Huang et al. "A survey on adaptive random testing."

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Centroid-Distance

$$fitness(t, T) = d(t, 1/|T| \sum t')$$

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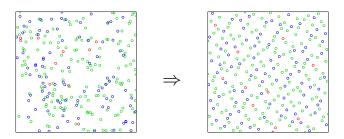


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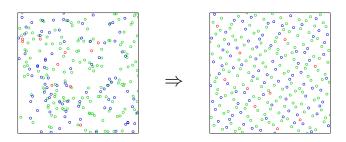
- $O(k^2Z)$ time complexity this could be expensive.
- It may be difficult to choose the meaningful distance metric for complex data types.





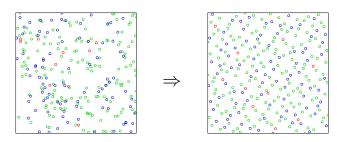
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- Quasi-random sequences could be a good choice.
- Let's learn Halton sequence, one of the representative quasi-random sequences.

Quasi-Random Strategy for ART - Halton Sequence PLRG

 The halton sequence is constructed in a deterministic way using co-prime numbers.

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$\frac{1}{2}$			
$\frac{1}{4}$	$\frac{3}{4}$		
<u>1</u> 8	<u>5</u> 8	<u>3</u>	7 8
$\frac{1}{16}$			

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- For example, generate the sequence of numbers in the range [0,1] by recursively splitting the range into $\mathbf 2$ or $\mathbf 3$ subintervals.

• Generate a sequence of pairs of numbers (x, y) by combining above sequences.

$$(\frac{1}{2}, \frac{1}{3}), (\frac{1}{4}, \frac{2}{3}), (\frac{3}{4}, \frac{1}{9}), (\frac{1}{8}, \frac{4}{9}), (\frac{5}{8}, \frac{7}{9}), (\frac{3}{8}, \frac{2}{9}), (\frac{7}{8}, \frac{5}{9}), (\frac{1}{16}, \frac{8}{9}), \cdots$$



We can utilize other quasi-random sequences for ART:⁴

Halton Sequence

$$\phi_b(i) = \sum_{j=0}^{\omega} i_j b^{-j-1}$$

Sobol Sequence

$$Sobol(i) = XOR_{j=1,2,\cdots,\omega}(i_j\delta_j)$$

where

$$\delta_j = XOR_{k=1,2,\cdots,r} \left(\frac{\beta_k \delta_{j-k}}{2^j} \right) \oplus \frac{\delta_{j-k}}{2^{j+r}}$$

Niederreiter Sequence

⁴[CSUR'19] R. Huang et al. "A survey on adaptive random testing."

Adaptive Random Testing (ART) – Summary



Application Domains

- Numeric Programs
- Object-Oriented Programs
- Configurable Systems
- Web Services and Applications
- Embedded Systems
- Simulations and Models

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- Application Domains
 - Numeric Programs
 - Object-Oriented Programs
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 - Simulations and Models
- Faulty regions may not apply to all types of faults.
- ART is still mostly an academic idea, with debates going on:
 - [ISSTA'11] A. Arcuri et al. "Adaptive random testing: an illusion of effectiveness?"
 - [CSUR'19] R. Huang et al. "A survey on adaptive random testing."

Contents



1. Random Testing (RT)

Probabilistic Analysis Weaknesses of Random Testing Examples

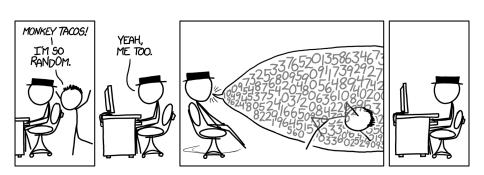
2. Adaptive Random Testing (ART)

Distance Comparison Target
Complexity of ART
Quasi-Random Strategy for ART

3. Fuzz Testing

Pre-process
Input Generation – Mutation-Based Fuzzing
Input Generation – Generation-Based Fuzzing
Test Oracles (Sanitizers)
De-duplication





https://xkcd.com/1210/



• [CACM'90] B. P. Miller et al. "An empirical study of the reliability of UNIX utilities." 5

"On a dark and stormy night one of the authors was logged on to his workstation on a dial-up line from home and the rain had affected the phone lines; there were frequent spurious characters on the line. The author had to race to see if he could type a sensible sequence of characters before the noise scrambled the command. This line noise was not surprising; but we were surprised that these spurious characters were causing programs to crash."

⁵https://alastairreid.github.io/RelatedWork/papers/miller:cacm:1990/





 Fuzz testing is a random testing technique to find exceptional outcomes (e.g., crashes, exceptions, freezes, etc.) of a software system.

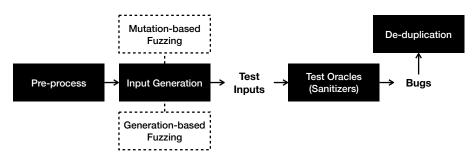




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- 1990 study found crashes in: adb, as, bc, cb, col, diction, emacs, eqn, ftp, indent, lex, look, m4, make, nroff, plot, prolog, ptx, refer!, spell, style, tsort, uniq, vgrind, vi

Fuzz Testing - Overview





- Pre-process prepare the SUT for fuzz testing
- Input Generation generate test inputs
 - Mutation-Based Fuzzing modify existing test inputs
 - Generation-Based Fuzzing generate new test inputs
- Test Oracles (Sanitizers) detect exceptional outcomes
- **De-duplication** remove duplicate test inputs



 Instrumentation – source-level or binary-level modification of the SUT to collect information about the execution in compile time (static) or runtime (dynamic).



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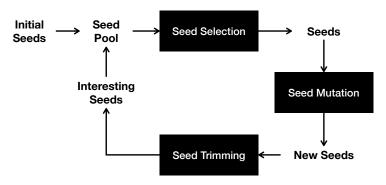
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 - Libraries a driver program that calls functions in the library
 - Kernels may fuzz user-land applications to test kernels
 - IoT devices a driver communicate with the corresponding smartphone application.

Input Generation – Mutation-Based Fuzzing

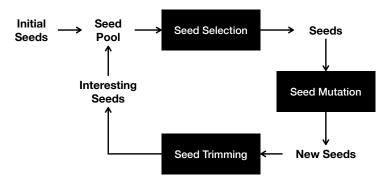




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Input Generation – Mutation-Based Fuzzing





- In the mutation-based fuzzing, a seed is a test input that is used to generate new test inputs.
- Mutation-Based Fuzzing first initializes seed pool with the initial seeds, and then mutates them to generate new test inputs and updates the seed pool when a new test input is interesting.

Input Generation - Mutation-Based Fuzzing



 Initial Seeds – from the existing test suite, manually crafted, inferred from the SUT or specification.

⁶[ICSE'21] J. Park et al. "JEST: N+1-version Differential Testing of Both JavaScript Engines and Specification."

Input Generation - Mutation-Based Fuzzing



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- Seed Trimming filter out the uninteresting test inputs (e.g., no coverage increase).

⁶[ICSE'21] J. Park et al. "JEST: N+1-version Differential Testing of Both JavaScript Engines and Specification."





Generation-Based Fuzzing generates new test inputs from a **model** that represents the **input space** of the SUT.

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- Encoder Model generates test inputs for decoder programs (e.g., image decoders, audio decoders, etc.) using the corresponding encoder programs.



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- They are usually instrumented into the SUT to collect information about the execution in compile time (static) or runtime (dynamic) with runtime overhead.



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- Coverage-based De-duplication compare the coverage of the test inputs (e.g., node, branch, grammar, semantics, etc.)
- Semantic-aware De-duplication compare the semantics of the test inputs (e.g., backward data-flow analysis for blaming)



If you are interested in further more details about fuzz testing, please refer to the following resources:

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ClusterFuzz developed by Google

https://google.github.io/clusterfuzz

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Levenshtein (Edit) Distance Distance Comparison Target Complexity of ART Quasi-Random Strategy for ART

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De-duplication

Next Lecture



• Coverage Criteria

Jihyeok Park
 jihyeok_park@korea.ac.kr
https://plrg.korea.ac.kr