

# Lecture 3 – Coverage Criteria

## AAA705: Software Testing and Quality Assurance

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2024 Spring

- Random Testing (RT)
  - Probabilistic Analysis
  - Weaknesses of Random Testing
  - Examples
- Adaptive Random Testing (ART)
  - Levenshtein (Edit) Distance
  - Distance Comparison Target
  - Complexity of ART
  - Quasi-Random Strategy for ART
- Fuzz Testing
  - Pre-process
  - Input Generation – Mutation-Based Fuzzing
  - Input Generation – Generation-Based Fuzzing
  - Test Oracles (Sanitizers)
  - De-duplication

## 1. Graph Coverage

- Structural Coverage

- Data-Flow Coverage

- Subsumption Relationships

## 2. Logic Coverage

- Simple Logic Expression Coverage

- Active Clause Coverage

- Inactive Clause Coverage

- Subsumption Relationships

## 3. Neuron Coverage

## 4. Feature-Sensitive Coverage

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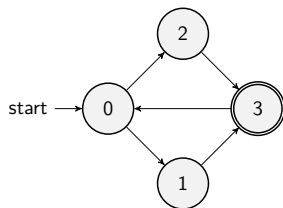
## 4. Feature-Sensitive Coverage

- **Graphs** are the most **commonly** used structure in software.
  - Control Flow Graphs (CFGs)
  - Call Graphs
  - Design Structure
  - Finite State Machines (FSMs)
  - etc.
- We want to ensure that our **tests** properly **cover** the graph.

## Definition (Graph)

A **graph**  $G = (N, E, N_s, N_f)$  is a quadruple consisting of

- ① a set of **nodes**  $N$ ,
- ② a set of **edges**  $E \subseteq N \times N$ ,
- ③ a set of **start nodes**  $N_s \subseteq N$ , and
- ④ a set of **final nodes**  $N_f \subseteq N$ .



$$G = \begin{cases} N = \{0, 1, 2, 3\} \\ E = \{(0, 1), (0, 2), (1, 3), (2, 3), (3, 0)\} \\ N_s = \{0\} \\ N_f = \{3\} \end{cases}$$

- A **path**  $p = (n_0, n_1, \dots, n_k) \in N^*$  in a graph  $G = (N, E, N_s, N_F)$  is a sequence of nodes such that  $(n_i, n_{i+1}) \in E$  for  $0 \leq i < k$ .

$$P_G = \{p \in N^* \mid p \text{ is a path in } G\}$$

- The **length** of a path is the **number of edges** in the path.

$$|p| = k$$

- A **subpath**  $q$  of a path  $p$  is a **subsequence** of  $p$  (i.e.,  $q \preceq p$ ).

$$q \preceq p \iff \exists 0 \leq i \leq j \leq k. q = (n_i, n_{i+1}, \dots, n_j)$$

- A path  $p$  is a **test path** if it starts from the **start node** and ends at a **final node**, and it represents an **execution** of a **test case**.

$$n_0 \in S \wedge n_k \in F$$

- A test path  $p$  **visits** a node  $n$  if it is in the path.

$$\exists 0 \leq i \leq k. n_i = n$$

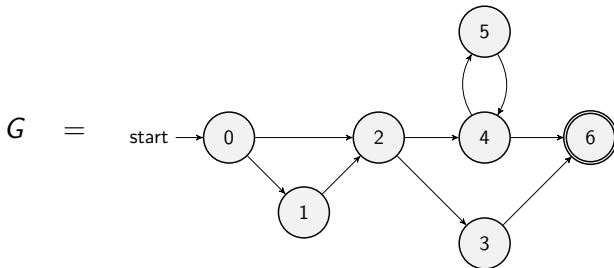
- A test path  $p$  **visits** an edge  $(n, m)$  if it is in the path.

$$\exists 0 \leq i \leq k. n_i = n \wedge n_{i+1} = m$$

- The **path**( $t$ ) is the test path executed by a test case  $t$ .
- The **path**( $T$ ) is the set of test paths executed by a test suite  $T$ .



Consider a path  $p = [0, 2, 4, 6]$  in the graph  $G$ .



- $|p| = 3$
- $[0, 2, 6]$  is a **subpath** of  $p$  (i.e.,  $[0, 2, 6] \preceq p$ )
- $p$  is a **test path**
- $p$  **visits** nodes 0, 2, 4, and 6
- $p$  **visits** edges  $(0, 2)$ ,  $(2, 4)$ , and  $(4, 6)$

## Definition (Graph Coverage Criterion)

A **graph coverage criterion**  $C_G = (R_G, \sim_G)$  for a given graph  $G$  is defined with:

- a set of **test requirements (TRs)**  $R_G$ , and
- a **cover relation**  $\sim \subseteq P_G \times R_G$  between paths and test requirements.
- A **test case**  $t$  **covers** a TR  $r$  if its test path satisfies the TR.

$$t \sim r \iff \text{path}(t) \sim r$$

- A **test suite**  $T$  **satisfies** the coverage criterion  $C_G$  if it covers all TRs.

$$T \vdash C_G \iff \forall r \in R_G. \exists t \in T. t \sim r$$

- A **structural coverage criterion** is defined on a graph in terms of **nodes**, **edges**, and **paths**.
- A **data-flow coverage criterion** is defined on a graph annotated with references to **variables**.

## Definition (Node Coverage (NC))

The **node coverage** criterion  $C_G = (R_G, \sim)$  is defined with:

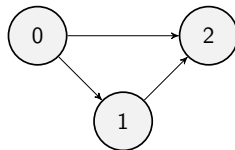
- the set of **TRs** is a set of nodes  $R_G = N$
- a path  $p$  **covers** a node  $n$  if  $p$  visits  $n$

## Definition (Edge Coverage (EC))

The **edge coverage** criterion  $C_G = (R_G, \sim)$  is defined with:

- the set of **TRs** is a set of edges  $R_G = E$
- a path  $p$  **covers** an edge  $(n, m)$  if  $p$  visits  $(n, m)$

NC and EC are only different when there is an edge and another subpath between a pair of nodes (e.g., an **if-else** statement).



Definition ( $k$ -Limiting Path Coverage ( $k$ -PC))

The  $k$ -**limiting path coverage** criterion  $C_G = (R_G, \sim)$  is

- the set of **TRs** is a set of paths whose lengths are bounded by  $k$ :

$$R_G = \{p \in P_G \mid |p| \leq k\}$$

- a path  $p$  **covers** a path  $q$  if  $q$  is a subpath of  $p$ :

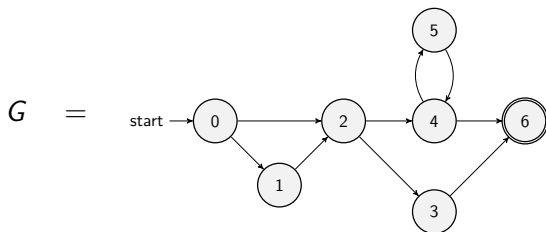
$$p \sim q \iff q \preceq p$$

## Definition (Edge-Pair Coverage (EPC))

The **edge-pair coverage** criterion is 2-limiting path coverage.

## Definition (Complete Path Coverage (CPC))

The **complete path coverage** criterion is  $\infty$ -limiting path coverage.



- Node Coverage (NC)

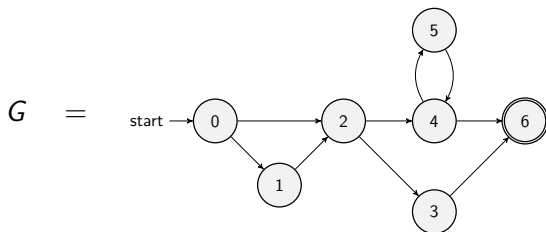
TRs  $R_G = \{0, 1, 2, 3, 4, 5, 6\}$

Test Paths =  $\{[0, 1, 2, 3, 6], [0, 1, 2, 4, 5, 4, 6]\}$

- Edge Coverage (EC)

TRs  $R_G = \{\dots, (0, 1), (0, 2), (1, 2), (2, 3), (2, 4), (3, 6), (4, 5), (4, 6)\}$

Test Paths =  $\{[0, 1, 2, 3, 6], [0, 1, 2, 4, 5, 4, 6]\}$



- Edge-Pair Coverage (EPC)

TRs  $R_G = \{$   
     $\dots, [0, 1, 2], [0, 2, 3], [0, 2, 4], [1, 2, 3], [1, 2, 4], [2, 3, 6],$   
     $[2, 4, 5], [2, 4, 6], [4, 5, 4], [5, 4, 5], [5, 4, 6]$   
     $\}$

Test Paths =  $\{$   
     $[0, 1, 2, 3, 6], [0, 1, 2, 4, 6], [0, 2, 3, 6], [0, 2, 4, 5, 4, 5, 4, 6]$   
     $\}$

- If a graph contains a loop, it has an **infinite** number of paths
- In this case, the **complete path coverage** (CPC) is not feasible.
- One possible solution is to use a **specified path coverage (SPC)** criterion with a set of paths manually specified by the tester.
- However, it is highly **dependent** on the tester's **expertise**.
- Attempts to deal with loops:
  - 1970s: Execute cycles once ([4, 5, 4] in the previous example)
  - 1980s: Execute each loop, exactly once
  - 1990s: Execute loops 0 times, once, more than once
  - 2000s: **Prime paths**

## Definition (Simple Path)

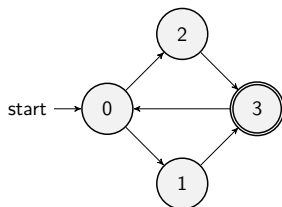
A **simple path** is a path that does not contain a repeated node, except for the start and final nodes. In other words,

- No internal loops
- A loop is a simple path

## Definition (Prime Path)

A **prime path** is a simple path that is not a subpath of other simple paths.



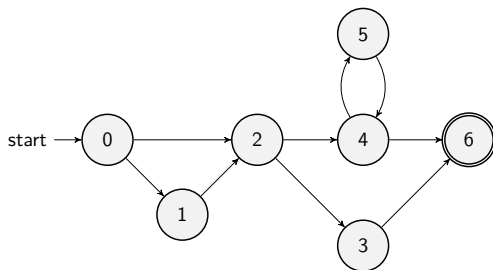


- **23 Simple Paths:**

[0], [1], [2], [3], [0, 1], [0, 2], [1, 3], [2, 3], [3, 0],  
[0, 1, 3], [0, 2, 3], [1, 3, 0], [2, 3, 0], [3, 0, 1], [3, 0, 2],  
[0, 1, 3, 0], [0, 2, 3, 0], [1, 3, 0, 1], [1, 3, 0, 2],  
[2, 3, 0, 1], [2, 3, 0, 2], [3, 0, 1, 3], [3, 0, 2, 3]

- **8 Prime Paths:**

[0, 1, 3, 0], [0, 2, 3, 0], [1, 3, 0, 1], [1, 3, 0, 2],  
[2, 3, 0, 1], [2, 3, 0, 2], [3, 0, 1, 3], [3, 0, 2, 3]



- **38 Simple Paths**

- **9 Prime Paths:**

[0, 1, 2, 3, 6]

[5, 4, 6]

[0, 2, 4, 6] executes the loop **0** times

[0, 1, 2, 4, 5]

[4, 5, 4]

[4, 5, 4] executes the loop **once**

[0, 1, 2, 4, 6]

[5, 4, 5]

[5, 4, 5] executes the loop **more than once**

[0, 2, 3, 6]

[0, 2, 4, 5]

[0, 2, 4, 6]

## Definition (Prime Path Coverage (PPC))

The **prime path coverage** criterion  $C_G = (R_G, \sim)$  is

- the set of **TRs** is a set of prime paths:

$$R_G = \{p \in P_G \mid p \text{ is a prime path}\}$$

- a path  $p$  **covers** a prime path  $q$  if  $q$  is a subpath of  $p$ :

$$p \sim q \iff q \preceq p$$

## Definition (Round-Trip Path)

A **round-trip path** is a prime path that starts and ends at the same node.

## Definition (Complete Round-Trip Path Coverage (CRPC))

The **complete round-trip path coverage** criterion  $C_G = (R_G, \sim)$  is

- the set of **TRs** is a set of all round-trip paths:

$$R_G = \{p \in P_G \mid p \text{ is a round-trip path}\}$$

- a path  $p$  **covers** a round-trip path  $q$  if  $q$  is a subpath of  $p$ :

$$p \sim q \iff q \preceq p$$

## Definition (Simple Round-Trip Path Coverage (SRPC))

The **simple round-trip path coverage** criterion  $C_G = (R_G, \sim)$  is

- the set of **TRs** is a set of nodes visited by at least one round-trip path:

$$R_G = \{n \in N \mid \exists p \in P_G. p \text{ is a round-trip path} \wedge n \in p\}$$

- a path  $p$  **covers** a node  $n$  if at least one round-trip path for  $n$  is a subpath of  $p$ :

$$p \sim n \iff \exists q \in P_G. q \text{ is a round-trip path} \wedge n \in q \wedge q \preceq p$$

- CRPC and SRPC omit nodes and edges not in round-trip paths
- In other words, they only focus on loops

Prime paths do not have **internal loops**!

## Definition (Tour)

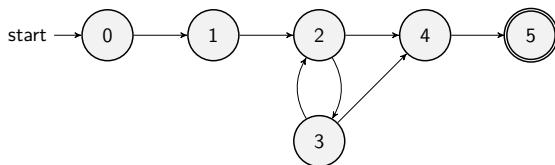
A test pest  $p$  **tours** a path  $q$  if  $q$  is a subpath of  $p$

## Definition (Tour with Sidetrips)

A test pest  $p$  **tours** a path  $q$  with **sidetrips** if and only if every **edge** in  $q$  is also in  $p$  in **the same order**.

## Definition (Tour with Detours)

A test pest  $p$  **tours** a path  $q$  with **detours** if and only if every **node** in  $q$  is also in  $p$  in **the same order**.



$[0, 1, 2, 4, 5]$  **tours**  $[1, 2, 4]$

$[0, 1, 2, 3, 2, 4, 5]$  does **not tour**  $[1, 2, 4]$  but **tours** it with **sidetrips** ( $[2, 3, 2]$  is a sidetrip)

$[0, 1, 2, 3, 4, 5]$  does **not tour**  $[1, 2, 4]$  with sidetrips but **tours** it with **detours** ( $[2, 3, 4]$  is a detour)

- An **infeasible** test requirement **cannot be satisfied**
  - Unreachable statements (dead code)
  - A subpath that can only be executed with a contradiction
- Most **coverage criteria** have some infeasible test requirements
- It is usually **undecidable** whether all test requirements are feasible
- When **sidetrips** or **detours** are not allowed, many structural coverage criteria have **more infeasible test requirements**
- **Practical solutions:** (1) try to satisfy as many test requirements as possible **without** sidetrips or detours, (2) **allow** sidetrips or detours to try to satisfy not yet satisfied test requirements



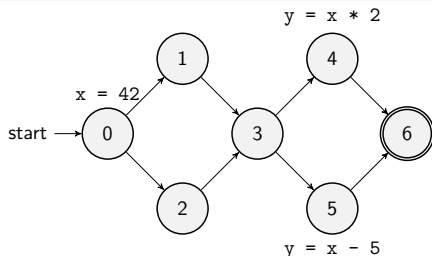
Our goal is to try to **ensure** that values are computed and **used** correctly.

## Definition (Def)

A **definition** of a variable is a **location** in the program where a value is assigned to the variable.

## Definition (Use)

A **use** of a variable is a **location** in the program where the value of the variable is accessed.



$$def(0) = \{x\}$$

$$def(4) = \{y\}$$

$$def(5) = \{y\}$$

$$use(4) = \{x\}$$

$$use(5) = \{x\}$$

## Definition (DU-Pair)

A **du-pair** is a pair of a locations  $(l, l')$  such that a variable  $x$  is defined at  $l$  and used at  $l'$ .

## Definition (Def-Clear Path)

A path from  $l$  to  $l'$  is **def-clear** with respect to a variable  $x$  if  $x$  is not given another value on any of the nodes or edges in the path.

## Definition (DU-Path)

A **du-path** is a simple subpath that is def-clear with respect to  $x$  from a def of  $x$  to a use of  $x$ .

- $du(n, n', x)$  is the set of du-paths from  $n$  to  $n'$  with respect to  $x$
- $du(n, x)$  is the set of du-paths from  $n$  to any use of  $x$

## Definition (DU-Tour)

A test path  $p$  **du-tours** a du-path  $q$  with respect to  $x$  if  $p$  tours  $d$  and the subpath taken is def-clear with respect to  $x$

**Sidetrips** or **detours** can be used, just as with previous touring.

## Definition (All-Defs Coverage (ADC))

The **all-defs coverage** criterion  $C_G = (R_G, \sim)$  is

- the set of **TRs** is a set of pairs of nodes and variables such that

$$R_G = \{(n, x) \mid n \in N \wedge |du(n, x)| > 0\}$$

- a path  $p$  **covers** a pair  $(n, x)$  if  $p$  du-tours a du-path in  $du(n, x)$

$$p \sim (n, x) \iff \exists q \in du(n, x). p \text{ du-tours } q$$

## Definition (All-Ues Coverage (AUC))

The **all-uses coverage** criterion  $C_G = (R_G, \sim)$  is

- the set of **TRs** is a set of triples of two nodes and variables such that

$$R_G = \{(n, n', x) \mid n, n' \in N \wedge |du(n, n', x)| > 0\}$$

- a path  $p$  **covers**  $(n, n', x)$  if  $p$  du-tours a du-path in  $du(n, n', x)$

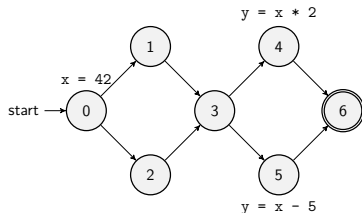
$$p \sim (n, n', x) \iff \exists q \in du(n, n', x). p \text{ du-tours } q$$

## Definition (All-DU-Paths Coverage (ADUPC))

The **all-du-paths coverage** criterion  $C_G = (R_G, \sim)$  is

- the set of **TRs** is a set of du-paths:  $R_G = \{q \in P_G \mid q \text{ is a du-path}\}$
- a path  $p$  **covers** a du-path  $q$  if  $p$  du-tours  $q$ :

$$p \sim q \iff p \text{ du-tours } q$$



- **All-Defs Coverage (ADC)**

TRs  $R_G = \{(0, x)\}$

Test Paths =  $\{[0, 1, 3, 4, 6]\}$

- **All-Uses Coverage (AUC)**

TRs  $R_G = \{(0, 4, x), (0, 5, x)\}$

Test Paths =  $\{[0, 1, 3, 4, 6], [0, 1, 3, 5, 6]\}$

- **All-DU-Paths Coverage (ADUPC)**

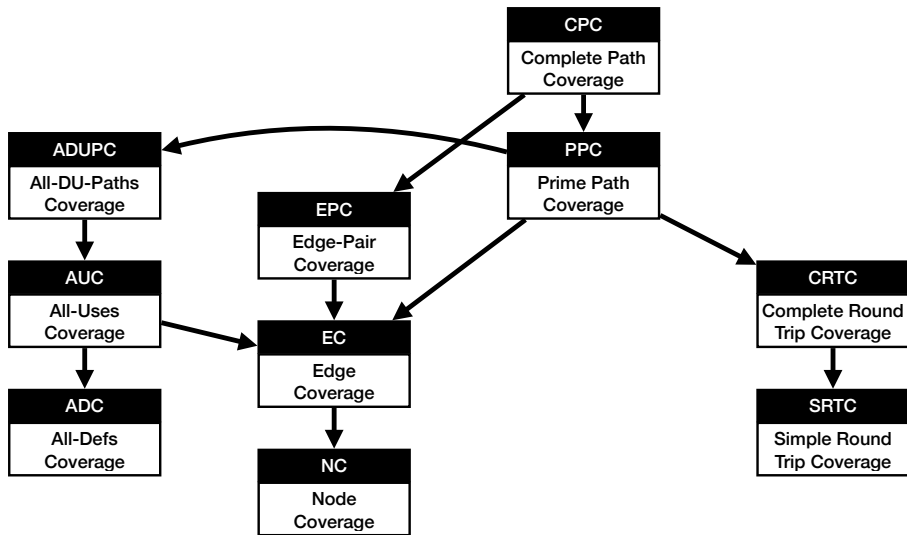
TRs  $R_G = \{[0, 1, 3, 4], [0, 1, 3, 5], [0, 2, 3, 4], [0, 2, 3, 5]\}$

Test Paths =  $\{[0, 1, 3, 4, 6], [0, 1, 3, 5, 6], [0, 2, 3, 4, 6], [0, 2, 3, 5, 6]\}$

## Definition (Subsumption)

A coverage criterion  $C_G = (R_G, \sim)$  **subsumes** another coverage criterion  $C'_G = (R'_G, \sim')$  if and only if any test suite  $T$  satisfying  $C_G$  satisfies  $C'_G$ .

- **Edge Coverage (EC)** subsumes **Node Coverage (NC)**
- **Edge-Pair Coverage (EPC)** subsumes **Edge Coverage (EC)**
- **Prime Path Coverage (PPC)** subsumes **Edge Coverage (EC)**
- However, **Prime Path Coverage (PPC)** does **not** subsume **Edge-Pair Coverage (EPC)**
  - If a node  $n$  has an self-cycle, EPC will require non-prime path  $[n, n, m]$
- **Complete Round-Trip Path Coverage (CRPC)** and **Simple Round-Trip Path Coverage (SRPC)** do not subsume **Node Coverage (NC)**



## 1. Graph Coverage

Structural Coverage

Data-Flow Coverage

Subsumption Relationships

## 2. Logic Coverage

Simple Logic Expression Coverage

Active Clause Coverage

Inactive Clause Coverage

Subsumption Relationships

## 3. Neuron Coverage

## 4. Feature-Sensitive Coverage



- Logic expressions show up in many situations
- Covering logic expressions is required by US Federal Aviation Administration for safety critical software
- Logical expressions can come from many sources
- Tests are intended to choose some subset of the total number of truth assignments to the expressions

- A **predicate** is an expression that evaluates to a **boolean** value
- Predicates can contain
  - **Boolean variables**
  - non-boolean variables with a **comparison** operator
  - Boolean **function** calls
- Internal structure is created by logical operators
  - $\neg$  – the **negation** operator
  - $\wedge$  – the **conjunction** operator
  - $\vee$  – the **disjunction** operator
  - $\oplus$  – the **exclusive or** operator
  - $\Rightarrow$  – the **implication** operator
  - $\Leftrightarrow$  – the **equivalence** operator
- A **clause** is a predicate without logical operators

$$(a < b) \vee f(z) \wedge D \wedge (m \geq n \times o)$$

- Four clauses:
  - $(a < b)$  – relational expression
  - $f(z)$  – boolean-value function
  - $D$  – boolean variable
  - $(m \geq n \times o)$  – relational expression
- Most predicates have few clauses

Abbreviations:

- $P$  is the set of **predicates**
- $p$  is a single **predicate** in  $P$
- $C$  is the set of **clauses**
- $C_p$  is the set of **clauses** in predicate  $p$
- $c$  is a single **clause** in  $C$

## Definition (Predicate Coverage (PC))

For each predicate  $p \in P$ , test requirements are the **truth** or **falsity** of  $p$ .

It is sometimes called **decision coverage**.

## Definition (Clause Coverage (CC))

For each clause  $c \in C$ , test requirements are the **truth** or **falsity** of  $c$ .

It is sometimes called **condition coverage**.

$$p = ((a < b) \vee D) \wedge (m \geq n \times o)$$

- Predicate Coverage (PC)**

$a$	$b$	$D$	$m$	$n$	$o$	$p$
5	10	$T$	1	1	1	$T$
10	5	$F$	1	1	1	$F$

- Clause Coverage (CC)**

$a$	$b$	$D$	$m$	$n$	$o$	$(a < b)$	$D$	$(m \geq n \times o)$
5	10	$F$	1	1	1	$T$	$F$	$T$
10	5	$T$	1	2	2	$F$	$T$	$F$

- PC does not fully exercise all the clauses in the predicate, especially in the presence of **short circuit** evaluation
- CC does not subsume PC. For example, the following test suite satisfies CC but not PC:

$A \vee B$	$A$	$B$	$A \vee B$
	$T$	$F$	$T$
	$F$	$T$	$T$

- The simplest solution is to test **all combinations**

- PC does not fully exercise all the clauses in the predicate, especially in the presence of **short circuit** evaluation
- CC does not subsume PC. For example, the following test suite satisfies CC but not PC:

$A \vee B$	$A$	$B$	$A \vee B$
	$T$	$F$	$T$
	$F$	$T$	$T$

- The simplest solution is to test **all combinations**

## Definition (Combinatorial Coverage (CoC))

For each predicate  $p \in P$ , test requirements in **combinatorial coverage (CoC)** are the all **combinations** of the truth or falsity of the clauses in  $C_p$ .

For example, we need the following combinations for the predicate  $p$

$$p = ((a < b) \vee D) \wedge (m \geq n \times o)$$

$(a < b)$	$D$	$(m \geq n \times o)$	$p$
$T$	$T$	$T$	$T$
$T$	$T$	$F$	$F$
$T$	$F$	$T$	$T$
$T$	$F$	$F$	$F$
$F$	$T$	$T$	$T$
$F$	$T$	$F$	$F$
$F$	$F$	$T$	$F$
$F$	$F$	$F$	$F$



- This is simple, neat, clean, but quite **expensive**!
- $2^N$  tests required for  $N$  clauses
- Let's test each clause **independently** from the other clauses using whether each clause **determines** the entire predicate.

## Definition (Determination)

A clause  $c$  in predicate  $p$ , called the **major clause**, **determines**  $p$  if and only if the values of the remaining **minor clauses**  $c'$  are such that changing the value of  $p$ .

- $A$  (or  $B$ ) **determines**  $A \vee B$  if  $B$  (or  $A$ ) is **false**, and  $A$  (or  $B$ ) **determines**  $A \wedge B$  if  $B$  (or  $A$ ) is **true**.

$A$	$B$	$A \vee B$
$T$	$T$	$T$
$T$	$F$	$T$
$F$	$T$	$T$
$F$	$F$	$F$

$A$	$B$	$A \wedge B$
$T$	$T$	$T$
$T$	$F$	$F$
$F$	$T$	$F$
$F$	$F$	$F$

- $A$  (or  $B$ ) always **determines**  $A \oplus B$ , and  $A$  (or  $B$ ) always **determines**  $A \Leftrightarrow B$ .

$A$	$B$	$A \oplus B$
$T$	$T$	$F$
$T$	$F$	$T$
$F$	$T$	$T$
$F$	$F$	$F$

$A$	$B$	$A \Leftrightarrow B$
$T$	$T$	$T$
$T$	$F$	$F$
$F$	$T$	$F$
$F$	$F$	$T$

## Definition (Active Clause Coverage (ACC))

For each predicate  $p \in P$ , test requirements in **active clause coverage (ACC)** are pairs of (1) **conditions** that make each selected **major clause**  $c \in C_p$  determine  $p$  and (2) the truth or falsity of  $c$ .

- For example,  $p = A \vee B$ , and pick  $A$  (or  $B$ ) as the major clause.
  - ①  $A = \text{true}$  and  $B = \text{false}$  ( $A$  determines  $p$ )
  - ②  $A = \text{false}$  and  $B = \text{false}$  ( $A$  determines  $p$ )
  - ③  $A = \text{false}$  and  $B = \text{true}$  ( $B$  determines  $p$ )
  - ④  $A = \text{false}$  and  $B = \text{false}$  ( $B$  determines  $p$ )
- The last one is **duplicate** and can be omitted.
- Another name of ACC is **modified condition/decision coverage (MC/DC)**, which is required by the **US Federal Aviation Administration** for **safety critical software**.

- **Ambiguity** – Do the **minor clauses** have to have the **same values** when the **major clause** is **true** or **false**?
- For example,  $p = A \vee (B \wedge C)$ , and pick  $A$  as the major clause.
  - ①  $A = \text{true}$ ,  $B = \text{false}$ ,  $C = \text{true}$
  - ②  $A = \text{false}$ ,  $B = \text{false}$ ,  $C = \text{false}$  (is  $C = \text{false}$  allowed?)
- This question caused a **confusion** among testers for years
- Consider this carefully leads to three separate coverage criteria:
  - Minor clauses **do not need** to be the same
  - Minor clauses **must** be the same
  - Minor clauses **force the predicate** to have different values

## Definition (General Active Clause Coverage (GACC))

For each predicate  $p \in P$ , test requirements in **general active clause coverage (GACC)** are pairs of (1) **conditions** that make each selected **major clause**  $c \in C_p$  determine  $p$  and (2) the truth or falsity of  $p$ . The values chosen for the **minor clauses** do **not need** to be the same when the **major clause** is **true** or **false**.

- Unfortunately, GACC does **not subsume predicate coverage (PC)**.
- For example, the following selection satisfies GACC but not PC:

$A$	$B$	$A \Leftrightarrow B$
$T$	$F$	$T$
$T$	$F$	$F$
$F$	$T$	$F$
$F$	$F$	$T$

## Definition (Restricted Active Clause Coverage (RACC))

For each predicate  $p \in P$ , test requirements in **restricted active clause coverage (RACC)** are pairs of (1) **conditions** that make each selected **major clause**  $c \in C_p$  determine  $p$  and (2) the truth or falsity of  $p$ . The values chosen for the **minor clauses** **must** be the same when the **major clause** is **true** or **false**.

- This has been a **common interpretation** by aviation developers
- RACC often leads to **infeasible test requirements**
- There is **no logical reason** for such a strict restriction
- Our **goal** is just to subsume **predicate coverage (PC)**

## Definition (Correlated Active Clause Coverage (CACC))

For each predicate  $p \in P$ , test requirements in **correlated active clause coverage (CACC)** are pairs of (1) **conditions** that make each selected **major clause**  $c \in C_p$  determine  $p$  and (2) the truth or falsity of  $p$ . The values chosen for the **minor clauses** **force the predicate** to have different values when the **major clause** is **true** or **false**.

- A **more recent** interpretation
- CACC **implicitly** allows minor clauses to have different values
- CACC **explicitly** subsumes **predicate coverage (PC)**

$A$	$B$	$C$	$A \wedge (B \vee C)$
$T$	$T$	$T$	$T$
$F$	$T$	$T$	$F$
$T$	$T$	$F$	$T$
$F$	$T$	$F$	$F$
$T$	$F$	$T$	$T$
$F$	$F$	$T$	$F$

$A$	$B$	$C$	$A \wedge (B \vee C)$
$T$	$T$	$T$	$T$
$T$	$T$	$F$	$T$
$T$	$F$	$T$	$T$
$F$	$T$	$T$	$F$
$F$	$T$	$F$	$F$
$F$	$F$	$T$	$F$

- We pick  $A$  as the major clause
- The left table shows that there are only **three combinations** allowed in **RACC**
- The right table shows that there are **nine combinations** allowed in **CACC** by selecting any three cases for each truth value of  $A$



- **Inactive clause coverage (ICC)** is the **dual** of **active clause coverage (ACC)**
- ACC criteria ensure that **major** clauses **determine** the predicate
- ICC criteria ensure that **major** clauses **do not determine** the predicate

## Definition (Inactive Clause Coverage (ICC))

For each predicate  $p \in P$ , test requirements in **inactive clause coverage (ICC)** are pairs of (1) **conditions** that make each selected **major clause**  $c \in C_p$  **not determine**  $p$  and (2) the truth or falsity of  $c$ .

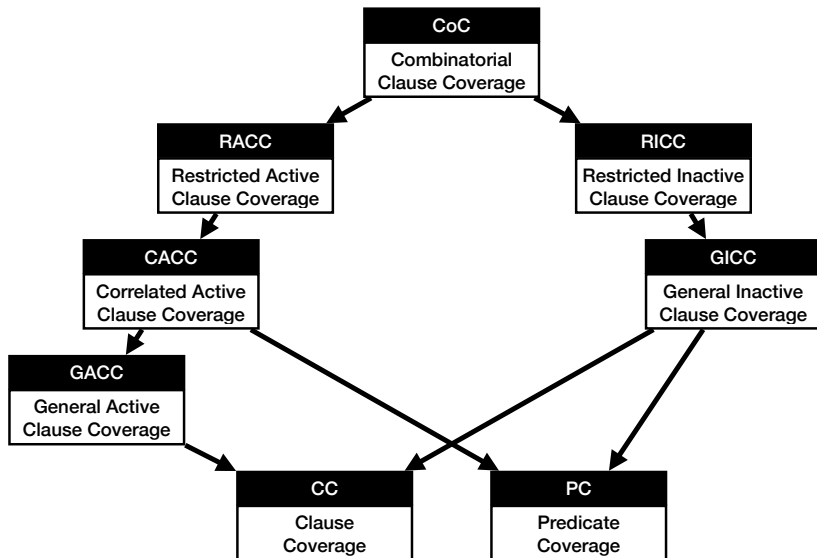
## Definition (General Inactive Clause Coverage (GICC))

For each predicate  $p \in P$ , test requirements in **general inactive clause coverage (GICC)** are pairs of (1) **conditions** that make each selected **major clause**  $c \in C_p$  **not determine**  $p$  and (2) the truth or falsity of  $c$ . The values chosen for the **minor clauses** do **not need** to be the same when the **major clause** is **true** or **false**.

## Definition (Restricted Inactive Clause Coverage (RICC))

For each predicate  $p \in P$ , test requirements in **restricted inactive clause coverage (RICC)** are pairs of (1) **conditions** that make each selected **major clause**  $c \in C_p$  **not determine**  $p$  and (2) the truth or falsity of  $c$ . The values chosen for the **minor clauses** **must** be the same when the **major clause** is **true** or **false**.

- Unlike ACC, the notion of **correlation** is not relevant to ICC (major clause  $c$  does not determine  $p$ , so cannot correlate with it)



## 1. Graph Coverage

Structural Coverage

Data-Flow Coverage

Subsumption Relationships

## 2. Logic Coverage

Simple Logic Expression Coverage

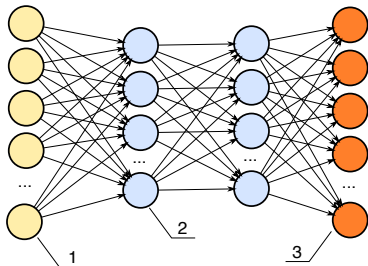
Active Clause Coverage

Inactive Clause Coverage

Subsumption Relationships

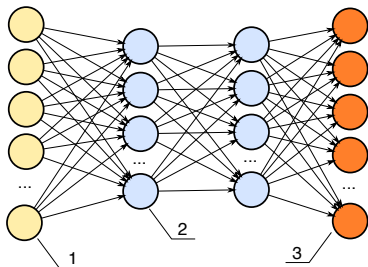
## 3. Neuron Coverage

## 4. Feature-Sensitive Coverage



How to define coverage criteria for **deep neural networks (DNN)**?

**Neuron Coverage!**



- A **DNN classifier** can be formalized as a function  $f : X \rightarrow Y$ , a mapping from a set of inputs  $X$  into a set of labels  $Y$ .
- The output of the DNN classifier is a **probability distribution**  $P(Y | x)$ , which is the probability that an input vector  $x \in X$  belongs to each class of labels in  $Y$ .
- A DNN classifier  $f$  usually contains an input layer, a number of hidden layers, and an output layer; each layer consists of many **neurons**.

- The **parameters**  $\theta$  of the DNN are the **weights** of each connected edge between neurons of two adjacent layers.
- For an input vector  $x$ , the output of DNN  $f_{\theta}(x)$  can be computed as the **weighted sum** of the outputs of all the neurons.
- Given a training dataset  $D = \{(x_i, y_i)\}_{i=1}^N$ , the goal is to learn to optimize the following **objective**:

$$\min_{\theta} \frac{1}{N} \sum_{i=1}^N \mathcal{L}(f_{\theta}(x_i), y_i)$$

where  $\mathcal{L}$  is a **loss function** to calculate the penalties for incorrect classifications.

- For a neuron  $n$  in a DNN model  $f$ , the **output** of  $n$  for an input  $x$  is denoted as  $f_{\theta}(n, x)$ .

## Definition (Activate Neuron)

A neuron is **activated** if the weighted sum of its inputs exceeds a certain threshold  $t$ .

$$AC(x, t) = \{n \mid f_{\theta}(n, x) > t\}$$

## Definition (Neuron Coverage (NC))

For a DNN model  $f$  and a threshold  $t$ , the test requirements in **neuron coverage (NC)** are the **activation** of each neuron  $n$  in the DNN model  $f$ .

$$NC(T, t) = \frac{|\{n \mid \exists x \in T. f_{\theta}(n, x) > t\}|}{|N|}$$



For a neuron  $n$ , the lower and upper boundary of its output values on **training data** can be denoted as  $low_n$  and  $up_n$ , respectively.

## Definition ( $k$ -Multisection Neuron Coverage (KMNC))

For a DNN model  $f$  and a number of sections  $k$ , the test requirements in  **$k$ -multisection neuron coverage (KMNC)** are  $k$  **equal sections** of  $[low_n, up_n]$  for each neuron  $n$  in the DNN model  $f$ .

$$KMNC = \frac{\sum_{n \in N} |\{S_m^n \mid \exists x \in T. f_\theta(n, x) \in S_m^n\}|}{|N|}$$

where

$$S_m^n = \left[ low_n + \frac{m \times (up_n - low_n)}{k}, low_n + \frac{(m+1) \times (up_n - low_n)}{k} \right]$$

For new test inputs  $T$ , the output values of neurons may fall into  $(-\infty, low_n)$  or  $(up_n, +\infty)$ . instead of the derived boundary  $[low_n, up_n]$ .

## Definition (Upper or Lower Neuron Coverage (UNC or LNC))

For a DNN model  $f$  and a number of sections  $k$ , the test requirements in **upper neuron coverage (UNC)** (or **lower neuron coverage (LNC)**) are the **upper boundary** (or **lower boundary**) of the output values of each neuron  $n$  in the DNN model  $f$ .

$$UNC = \frac{|\{n \mid \exists x \in T. f_{\theta}(n, x) > up_n\}|}{|N|}$$

$$LNC = \frac{|\{n \mid \exists x \in T. f_{\theta}(n, x) < low_n\}|}{|N|}$$

UNC is often called **strong neuron activation coverage (SNAC)**.

**Neuron Boundary Coverage (NBC)** is combination of UNC and LNC.

$$NBC = (|UNC| + |LNC|)/2$$

## Definition (Top- $k$ Neuron Coverage (TKNC))

**TKNC** is a layer-level coverage testing criterion that measures the ratio of neurons that have at least been the **most active  $k$  neurons** of **each layer** on a given test set  $T$  once.

$$TKNC = \frac{|\bigcup_{x \in T} \bigcup_{1 \leq l \leq L} top_k(x, l)|}{|N|}$$

where  $L$  denotes the number of layers in the DNN model  $f$ , and  $top_k(x, l)$  denotes the neurons which have largest  $k$  output values in the  $l$ -th layer of the DNN model  $f$  for the input  $x$ .

We can extend this criterion to the **Top- $k$  Neuron Pattern Coverage (TKNPC)** by considering the **combination** of the most active neurons in each layer.

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- [PLDI'23] J. Park et al. *“Feature-Sensitive Coverage for Conformance Testing of Programming Language Implementations.”*
- It suggests a new way to refine a given graph coverage criterion using **feature-sensitive** information.
- Slides: [link](#)

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## 4. Feature-Sensitive Coverage

- Coverage Criteria (Homework)

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