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Word $w =$ a b b a a a a

Stack $\alpha =$

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$b\ [N \to NN]$

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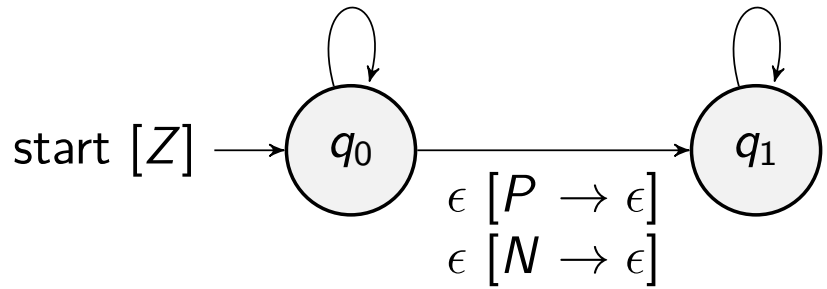

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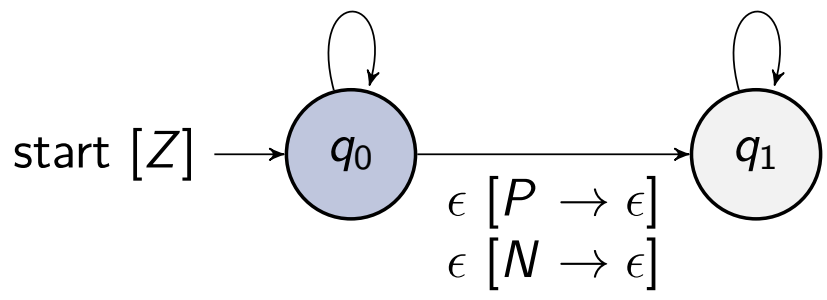

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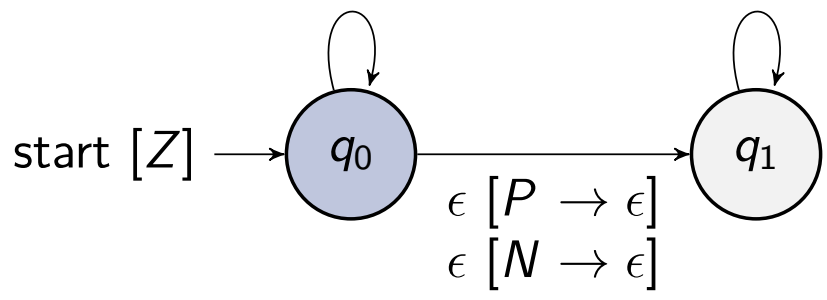

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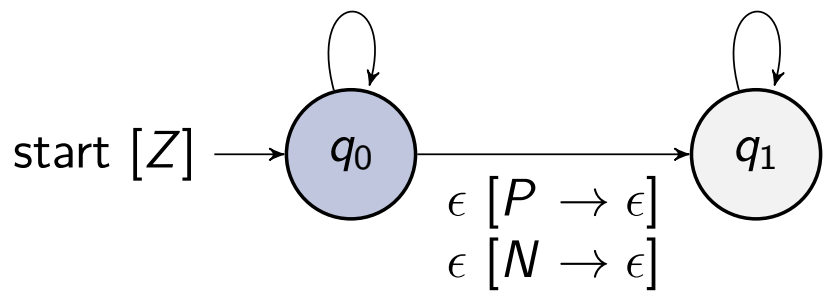

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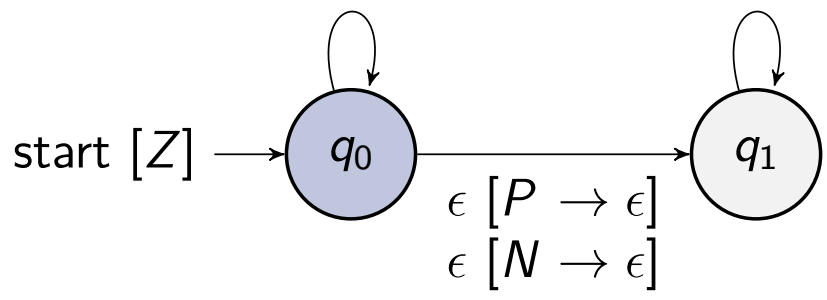

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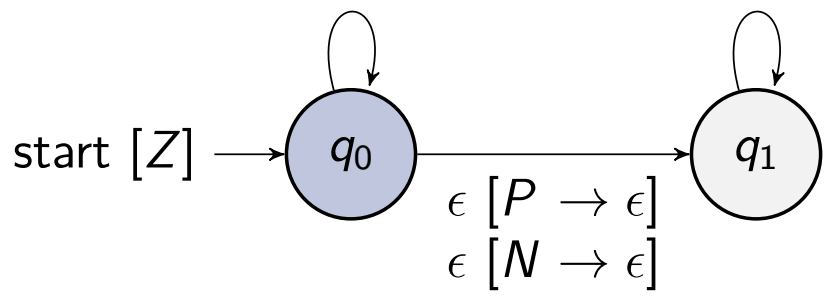

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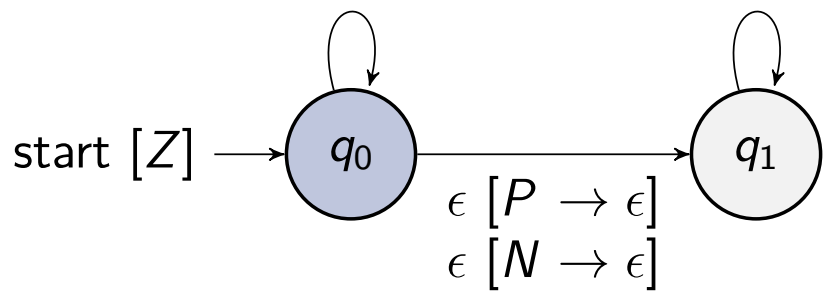

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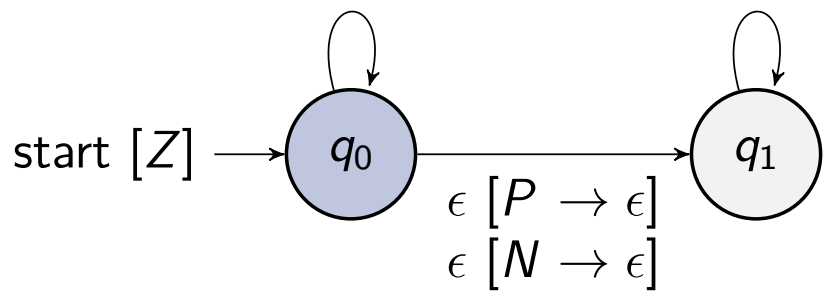

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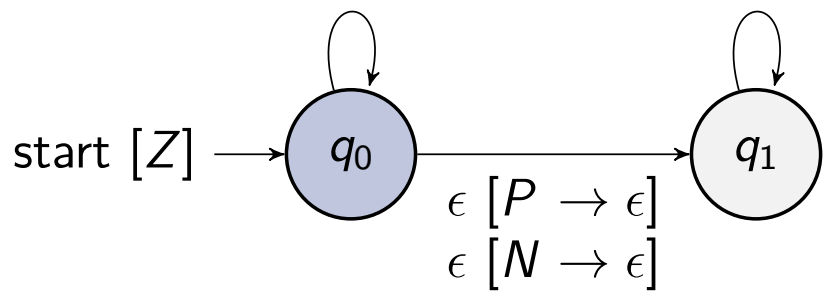

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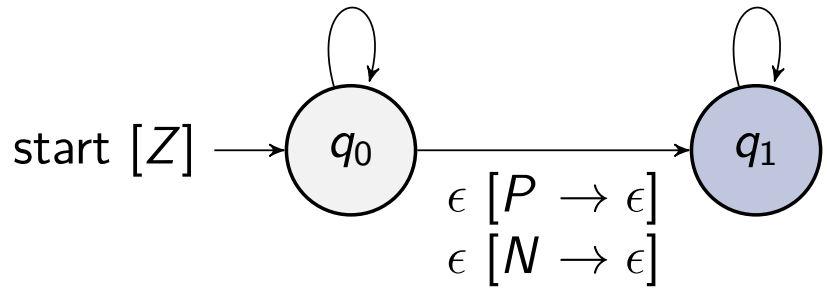

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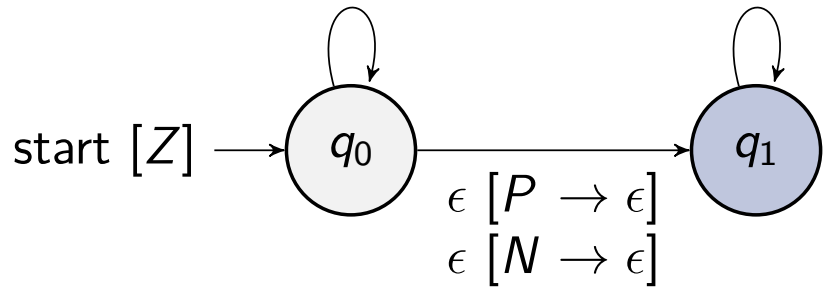

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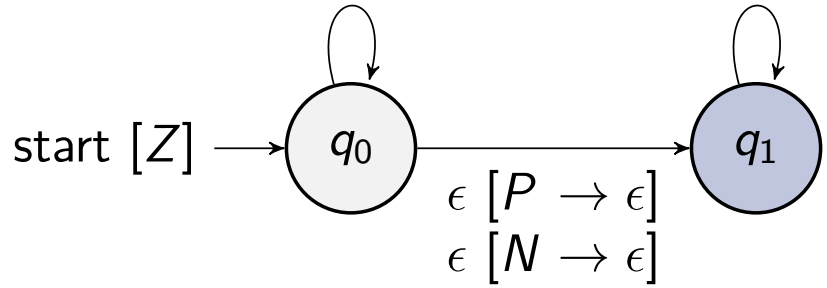

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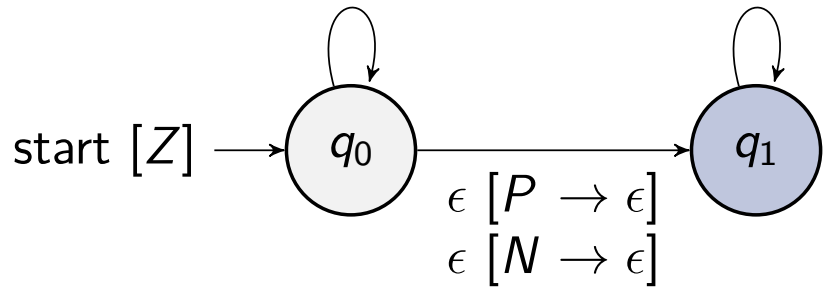

abbaaaa $\in L_E(P)$!