Lecture 4 – Nondeterministic Finite Automata (NFA) COSE215: Theory of Computation

Jihyeok Park



2024 Spring





- 1 Deterministic Finite Automata (DFA)
 - Definition
 - Transition Diagram and Transition Table
 - Extended Transition Function
 - Acceptance of a Word
 - Language of DFA (Regular Language)
 - Examples

Contents



1. Nondeterministic Finite Automata (NFA)

Definition

Transition Diagram and Transition Table

Extended Transition Function

Language of NFA

Examples

2. Equivalence of DFA and NFA

 $\mathsf{DFA} \to \mathsf{NFA}$

DFA ← NFA (Subset Construction)

Contents



1. Nondeterministic Finite Automata (NFA)

Definition

Transition Diagram and Transition Table

Extended Transition Function

Language of NFA

Examples

Equivalence of DFA and NFA

 $\mathsf{DFA} \to \mathsf{NFA}$

DFA ← NFA (Subset Construction)

Definition of NFA



Definition (Nondeterministic Finite Automaton (NFA))

A **nondeterministic finite automaton** is a 5-tuple:

$$N = (Q, \Sigma, \delta, q_0, F)$$

- Q is a finite set of **states**
- Σ is a finite set of **symbols**
- $\delta: Q \times \Sigma \to \mathcal{P}(Q)$ is the transition function
- $q_0 \in Q$ is the initial state
- $F \subseteq Q$ is the set of **final states**

$$N = (\{q_0, q_1, q_2\}, \{a, b\}, \delta, q_0, \{q_2\})$$

$$\delta(q_0, \mathtt{a}) = \{q_0, q_1\}$$
 $\delta(q_1, \mathtt{a}) = \{q_2\}$ $\delta(q_2, \mathtt{a}) = \varnothing$ $\delta(q_0, \mathtt{b}) = \{q_0\}$ $\delta(q_1, \mathtt{b}) = \varnothing$ $\delta(q_2, \mathtt{b}) = \varnothing$

Definition of NFA



```
// The definition of NFA
case class NFA(
  states: Set[State],
  symbols: Set[Symbol],
  trans: Map[(State, Symbol), Set[State]],
  initState: State,
  finalStates: Set[State],
)
```

Definition of NFA



```
// The definition of NFA
case class NFA(
  states: Set[State],
  symbols: Set[Symbol],
  trans: Map[(State, Symbol), Set[State]],
  initState: State,
  finalStates: Set[State],
)
```

You can **skip empty transitions** using withDefaultValue method.

Transition Diagram and Transition Table

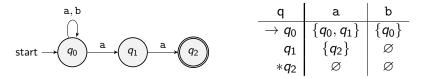


$$N_1 = (\{q_0, q_1, q_2\}, \{a, b\}, \delta, q_0, \{q_2\})$$

$$egin{aligned} \delta(q_0,\mathtt{a}) &= \{q_0,q_1\} & \delta(q_1,\mathtt{a}) &= \{q_2\} & \delta(q_2,\mathtt{a}) &= \varnothing \ \delta(q_0,\mathtt{b}) &= \{q_0\} & \delta(q_1,\mathtt{b}) &= \varnothing & \delta(q_2,\mathtt{b}) &= \varnothing \end{aligned}$$

Transition Diagram

Transition Table

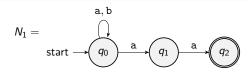




Definition (Extended Transition Function)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **extended transition function** $\delta^* : \mathcal{P}(Q) \times \Sigma^* \to \mathcal{P}(Q)$ is defined as follows:

- (Basis Case) $\delta^*(S, \epsilon) = S$
- (Induction Case) $\delta^*(S, xw) = \delta^*(\bigcup_{q \in S} \delta(q, x), w)$



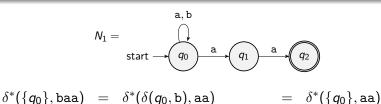
$$\delta^*(\{q_0\}, baa)$$



Definition (Extended Transition Function)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **extended transition function** $\delta^* : \mathcal{P}(Q) \times \Sigma^* \to \mathcal{P}(Q)$ is defined as follows:

- (Basis Case) $\delta^*(S, \epsilon) = S$
- (Induction Case) $\delta^*(S, xw) = \delta^*(\bigcup_{q \in S} \delta(q, x), w)$

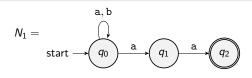




Definition (Extended Transition Function)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **extended transition function** $\delta^* : \mathcal{P}(Q) \times \Sigma^* \to \mathcal{P}(Q)$ is defined as follows:

- (Basis Case) $\delta^*(S, \epsilon) = S$
- (Induction Case) $\delta^*(S, xw) = \delta^*(\bigcup_{q \in S} \delta(q, x), w)$



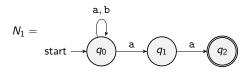
$$\delta^*(\lbrace q_0 \rbrace, \mathtt{baa}) = \delta^*(\delta(q_0, \mathtt{b}), \mathtt{aa}) = \delta^*(\lbrace q_0 \rbrace, \mathtt{aa}) = \delta^*(\lbrace q_0 \rbrace, \mathtt{aa}) = \delta^*(\lbrace q_0, q_1 \rbrace, \mathtt{a})$$



Definition (Extended Transition Function)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **extended transition function** $\delta^* : \mathcal{P}(Q) \times \Sigma^* \to \mathcal{P}(Q)$ is defined as follows:

- (Basis Case) $\delta^*(S, \epsilon) = S$
- (Induction Case) $\delta^*(S, xw) = \delta^*(\bigcup_{q \in S} \delta(q, x), w)$



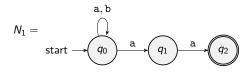
$$\begin{array}{lll} \delta^*(\{q_0\}, \mathtt{baa}) & = & \delta^*(\delta(q_0, \mathtt{b}), \mathtt{aa}) & = & \delta^*(\{q_0\}, \mathtt{aa}) \\ & = & \delta^*(\delta(q_0, \mathtt{a}), \mathtt{a}) & = & \delta^*(\{q_0, q_1\}, \mathtt{a}) \\ & = & \delta^*(\delta(q_0, \mathtt{a}) \cup \delta(q_1, \mathtt{a}), \epsilon) & = & \delta^*(\{q_0, q_1, q_2\}, \epsilon) \end{array}$$



Definition (Extended Transition Function)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **extended transition function** $\delta^* : \mathcal{P}(Q) \times \Sigma^* \to \mathcal{P}(Q)$ is defined as follows:

- (Basis Case) $\delta^*(S, \epsilon) = S$
- (Induction Case) $\delta^*(S, xw) = \delta^*(\bigcup_{q \in S} \delta(q, x), w)$



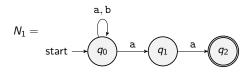
$$\delta^*(\{q_0\}, \mathsf{baa}) = \delta^*(\delta(q_0, \mathsf{b}), \mathsf{aa}) = \delta^*(\{q_0\}, \mathsf{aa}) = \delta^*(\delta(q_0, \mathsf{a}), \mathsf{a}) = \delta^*(\{q_0, q_1\}, \mathsf{a}) = \delta^*(\delta(q_0, \mathsf{a}) \cup \delta(q_1, \mathsf{a}), \epsilon) = \delta^*(\{q_0, q_1, q_2\}, \epsilon) = \{q_0, q_1, q_2\}$$



Definition (Extended Transition Function)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **extended transition function** $\delta^* : \mathcal{P}(Q) \times \Sigma^* \to \mathcal{P}(Q)$ is defined as follows:

- (Basis Case) $\delta^*(S, \epsilon) = S$
- (Induction Case) $\delta^*(S, xw) = \delta^*(\bigcup_{q \in S} \delta(q, x), w)$



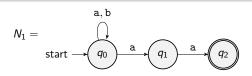
$$\delta^*(\{q_0\}, \mathtt{aba})$$



Definition (Extended Transition Function)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **extended transition function** $\delta^* : \mathcal{P}(Q) \times \Sigma^* \to \mathcal{P}(Q)$ is defined as follows:

- (Basis Case) $\delta^*(S, \epsilon) = S$
- (Induction Case) $\delta^*(S, xw) = \delta^*(\bigcup_{q \in S} \delta(q, x), w)$



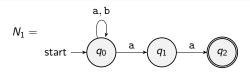
$$\delta^*(\lbrace q_0 \rbrace, \mathtt{aba}) = \delta^*(\delta(q_0, \mathtt{a}), \mathtt{ba}) = \delta^*(\lbrace q_0, q_1 \rbrace, \mathtt{ba})$$



Definition (Extended Transition Function)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **extended transition function** $\delta^* : \mathcal{P}(Q) \times \Sigma^* \to \mathcal{P}(Q)$ is defined as follows:

- (Basis Case) $\delta^*(S, \epsilon) = S$
- (Induction Case) $\delta^*(S, xw) = \delta^*(\bigcup_{q \in S} \delta(q, x), w)$



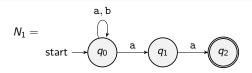
$$\begin{array}{lcl} \delta^*(\{q_0\},\mathtt{aba}) &=& \delta^*(\delta(q_0,\mathtt{a}),\mathtt{ba}) &=& \delta^*(\{q_0,q_1\},\mathtt{ba}) \\ &=& \delta^*(\delta(q_0,\mathtt{b})\cup\delta(q_1,\mathtt{b}),\mathtt{a}) &=& \delta^*(\{q_0\},\mathtt{a}) \end{array}$$



Definition (Extended Transition Function)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **extended transition function** $\delta^* : \mathcal{P}(Q) \times \Sigma^* \to \mathcal{P}(Q)$ is defined as follows:

- (Basis Case) $\delta^*(S, \epsilon) = S$
- (Induction Case) $\delta^*(S, xw) = \delta^*(\bigcup_{q \in S} \delta(q, x), w)$



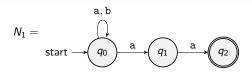
$$\begin{array}{lll} \delta^*(\{q_0\},\mathsf{aba}) &=& \delta^*(\delta(q_0,\mathsf{a}),\mathsf{ba}) &=& \delta^*(\{q_0,q_1\},\mathsf{ba}) \\ &=& \delta^*(\delta(q_0,\mathsf{b})\cup\delta(q_1,\mathsf{b}),\mathsf{a}) &=& \delta^*(\{q_0\},\mathsf{a}) \\ &=& \delta^*(\delta(q_0,\mathsf{a}),\epsilon) &=& \delta^*(\{q_0,q_1\},\epsilon) \end{array}$$



Definition (Extended Transition Function)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **extended transition function** $\delta^* : \mathcal{P}(Q) \times \Sigma^* \to \mathcal{P}(Q)$ is defined as follows:

- (Basis Case) $\delta^*(S, \epsilon) = S$
- (Induction Case) $\delta^*(S, xw) = \delta^*(\bigcup_{q \in S} \delta(q, x), w)$



$$egin{array}{lll} \delta^*(\{q_0\}, { t aba}) &=& \delta^*(\delta(q_0, { t a}), { t ba}) &=& \delta^*(\{q_0, q_1\}, { t ba}) \ &=& \delta^*(\delta(q_0, { t b}) \cup \delta(q_1, { t b}), { t a}) &=& \delta^*(\{q_0\}, { t a}) \ &=& \delta^*(\{q_0, q_1\}, \epsilon) \ &=& \{q_0, q_1\} \end{array}$$





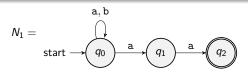
```
// The type definition of words
type Word = String
case class NFA(...):
  // The extended transition function of NFA
 def extTrans(qs: Set[State], w: Word): Set[State] = w match
    case "" => qs
    case x <| w => extTrans(qs.flatMap(q => trans(q, x)), w)
// An example transition for a word "baa"
nfa1.extTrans(Set(0), "baa") // Set(0, 1, 2)
// An example transition for a word "aba"
nfa1.extTrans(Set(0), "aba") // Set(0, 1)
```





Definition (Acceptance of a Word)

For a given NFA $N=(Q,\Sigma,\delta,q_0,F)$, we say that N accepts a word $w\in\Sigma^*$ if and only if $\delta^*(\{q_0\},w)\cap F\neq\varnothing$

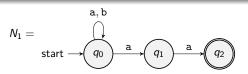






Definition (Acceptance of a Word)

For a given NFA $N=(Q,\Sigma,\delta,q_0,F)$, we say that N accepts a word $w\in\Sigma^*$ if and only if $\delta^*(\{q_0\},w)\cap F\neq\varnothing$



$$\delta^*(\{q_0\},\mathtt{baa})\cap F=\{q_0,q_1,q_2\}\cap \{q_2\}=\{q_2\}
eq arnothing$$

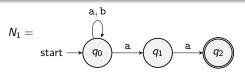
It means that N_1 accepts baa.





Definition (Acceptance of a Word)

For a given NFA $N=(Q,\Sigma,\delta,q_0,F)$, we say that N accepts a word $w\in\Sigma^*$ if and only if $\delta^*(\{q_0\},w)\cap F\neq\varnothing$



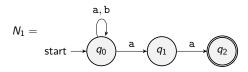
$$\delta^*(\{q_0\},\mathtt{baa})\cap F=\{q_0,q_1,q_2\}\cap \{q_2\}=\{q_2\}
eq arnothing$$

It means that N_1 accepts baa.

$$\delta^*(\{q_0\},\mathtt{aba})\cap F=\{q_0,q_1\}\cap \{q_2\}=arnothing$$

It means that N_1 does **not accept** aba.





```
case class NFA(...):
    ...
    // The acceptance of a word by NFA
    def accept(w: Word): Boolean =
        extTrans(Set(initState), w).intersect(finalStates).nonEmpty

// An example acceptance of a word "baa"
nfa1.accept("baa") // true

// An example non-acceptance of a word "aba"
nfa1.accept("aba") // false
```

Language of NFA



Definition (Language of NFA)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **language** of N is defined as:

$$L(N) = \{ w \in \Sigma^* \mid N \text{ accepts } w \}$$

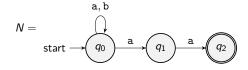
Language of NFA



Definition (Language of NFA)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **language** of N is defined as:

$$L(N) = \{ w \in \Sigma^* \mid N \text{ accepts } w \}$$



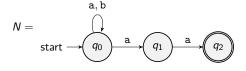
Language of NFA



Definition (Language of NFA)

For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, the **language** of N is defined as:

$$L(N) = \{ w \in \Sigma^* \mid N \text{ accepts } w \}$$



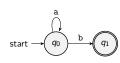
$$L(N) = \{ waa \mid w \in \{a,b\}^* \}$$



$$L = \{a^nb \mid n \ge 0\}$$

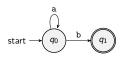


$$L = \{a^nb \mid n \ge 0\}$$





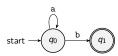
$$L = \{a^nb \mid n \ge 0\}$$



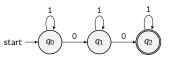
$$L = \{ w \in \{0,1\}^* \mid w \text{ contains }$$
exactly two 0's $\}$



$$L = \{a^nb \mid n \ge 0\}$$

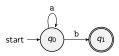


$$L = \{ w \in \{0,1\}^* \mid w \text{ contains }$$
exactly two 0's $\}$

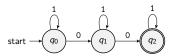




$$L = \{a^nb \mid n \ge 0\}$$



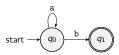
$$L = \{ w \in \{0,1\}^* \mid w \text{ contains }$$
exactly two 0's $\}$



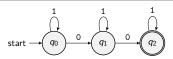
$$L = \{w \in \{a, b\}^* \mid w \text{ contains three consecutive a's } \}$$



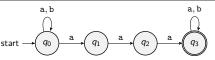
$$L = \{a^nb \mid n \ge 0\}$$



 $L = \{ w \in \{0,1\}^* \mid w \text{ contains }$ exactly two 0's $\}$

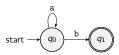


 $L = \{ w \in \{a, b\}^* \mid w \text{ contains three consecutive a's } \}$

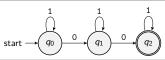




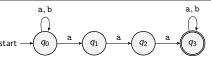
$$L = \{a^nb \mid n \ge 0\}$$



 $L = \{ w \in \{0,1\}^* \mid w \text{ contains }$ exactly two 0's $\}$



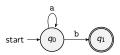
 $L = \{ w \in \{a,b\}^* \mid w \text{ contains three consecutive a's } \}$



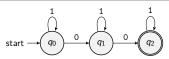
 $L = \{w \in \{0,1\}^* \mid \mathbb{N}(w) \equiv 0 \pmod{3}\}$ where $\mathbb{N}(w)$ is the natural number represented by w in binary



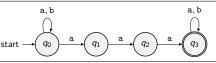
$$L = \{a^nb \mid n \ge 0\}$$



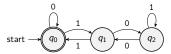
 $L = \{ w \in \{0,1\}^* \mid w \text{ contains }$ exactly two 0's $\}$



 $L = \{ w \in \{a,b\}^* \mid w \text{ contains three consecutive a's } \}$

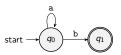


 $L = \{w \in \{0,1\}^* \mid \mathbb{N}(w) \equiv 0 \pmod{3}\}$ where $\mathbb{N}(w)$ is the natural number represented by w in binary

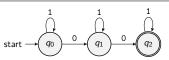




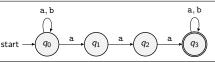
$$L = \{a^nb \mid n \ge 0\}$$



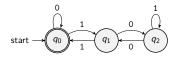
 $L = \{ w \in \{0,1\}^* \mid w \text{ contains }$ exactly two 0's $\}$



 $L = \{ w \in \{a,b\}^* \mid w \text{ contains three consecutive a's } \}$



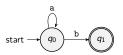
 $L = \{w \in \{0,1\}^* \mid \mathbb{N}(w) \equiv 0 \pmod{3}\}$ where $\mathbb{N}(w)$ is the natural number represented by w in binary



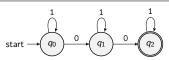
$$L = \{a^n b^n \mid n \ge 0\}$$



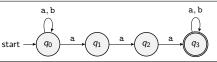
$$L = \{a^nb \mid n \ge 0\}$$



$$L = \{ w \in \{0,1\}^* \mid w \text{ contains }$$
exactly two 0's $\}$



$$L = \{ w \in \{a, b\}^* \mid w \text{ contains three consecutive a's } \}$$



$$L = \{w \in \{0,1\}^* \mid \mathbb{N}(w) \equiv 0 \pmod{3}\}$$
 where $\mathbb{N}(w)$ is the natural number represented by w in binary

start
$$q_0$$
 q_1 q_1 q_2

$$L = \{a^n b^n \mid n \ge 0\}$$

IMPOSSIBLE (\nexists NFA N. L(N) = L)

Contents



1. Nondeterministic Finite Automata (NFA)

Definition

Transition Diagram and Transition Table

Extended Transition Function

Language of NFA

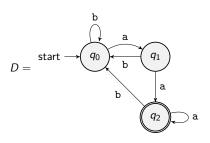
Examples

2. Equivalence of DFA and NFA

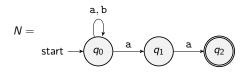
 $\mathsf{DFA} \to \mathsf{NFA}$

 $\mathsf{DFA} \leftarrow \mathsf{NFA} \; (\mathsf{Subset} \; \mathsf{Construction})$



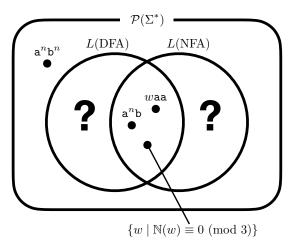


$$\mathit{L}(\mathit{D}) = \{ \mathit{w} \, \mathsf{a} \, | \, \mathit{w} \in \{ \mathsf{a}, \mathsf{b} \}^* \} = \mathit{L}(\mathit{N})$$



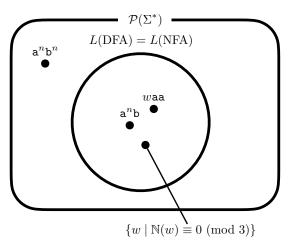


Is there any language that is the language of a DFA but not the language of an NFA, or vice versa?





Is there any language that is the language of a DFA but not the language of an NFA, or vice versa? No! DFA and NFA are **equivalent**.





Theorem (Equivalence of DFA and NFA)

A language L is the language L(D) of a DFA D if and only if L is the language L(N) of an NFA N.



Theorem (Equivalence of DFA and NFA)

A language L is the language L(D) of a DFA D if and only if L is the language L(N) of an NFA N.

Proof) By the following two theorems.

Theorem (DFA to NFA)

For a given DFA $D = (Q, \Sigma, \delta, q, F)$, \exists NFA N. L(D) = L(N).

It means (1) we can always construct an NFA equivalent to a given DFA.

Theorem (NFA to DFA – Subset Construction)

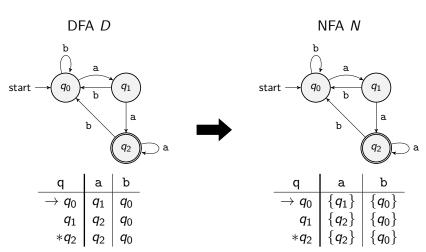
For a given NFA $N = (Q, \Sigma, \delta, q_0, F)$, \exists DFA D. L(D) = L(N).

It means 2 we can always construct a DFA equivalent to a given NFA.

$\mathsf{DFA} \to \mathsf{NFA} - \mathsf{Example}$



① Let's learn how to construct an NFA equivalent to a given DFA.





Theorem (DFA to NFA)

For a given DFA
$$D = (Q, \Sigma, \delta_D, q_0, F)$$
, \exists NFA N . $L(D) = L(N)$.

Proof) Consider the following NFA:

$$N = (Q, \Sigma, \delta_N, q_0, F)$$

where $\forall q \in Q$. $\forall x \in \Sigma$.

$$\delta_N(q,x) = \{\delta_D(q,x)\}\$$

Then,

$$w \in L(D) \iff \delta_D^*(q_0, w) \in F$$
 (: definition of $L(D)$)
 $\iff \{\delta_D^*(q_0, w)\} \cap F \neq \emptyset$ (: set theory)
 $\iff \delta_N^*(\{q_0\}, w) \cap F \neq \emptyset$ (: lemma in the next slide)
 $\iff w \in L(N)$ (: definition of $L(N)$)



Lemma

$$\forall q \in Q. \ \forall w \in \Sigma^*. \ \delta_N^*(\{q\}, w) = \{\delta_D^*(q, w)\}.$$

Proof) By induction on the length of word.

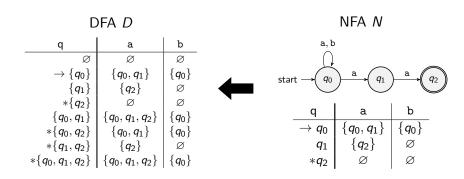
- (Base Case) $\delta_N^*(\{q\}, \epsilon) = \{q\} = \{\delta_D^*(q, \epsilon)\}.$
- (Inductive Case) Assume it holds for w (I.H.).

$$\begin{split} \delta_N^*(\{q\},xw) &= \delta_N^*(\delta_N(q,x),w) &\quad (\because \text{ definition of } \delta_N^*) \\ &= \delta_N^*(\{\delta_D(q,x)\},w) &\quad (\because \text{ definition of } \delta_N) \\ &= \{\delta_D^*(\delta_D(q,x),w)\} &\quad (\because \text{I.H.}) \\ &= \{\delta_D^*(q,xw)\} &\quad (\because \text{ definition of } \delta_D^*) &\quad \Box \end{split}$$

DFA ← NFA (Subset Construction) – Example



② Let's learn how to construct a DFA equivalent to a given NFA. We will use subsets of states in the NFA as states in the DFA. (This is called the subset construction approach.)

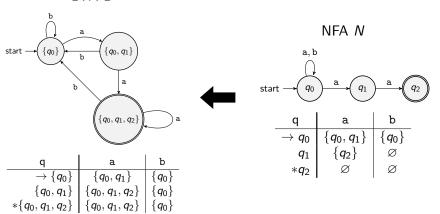


DFA ← NFA (Subset Construction) – Example



② Let's learn how to construct a DFA equivalent to a given NFA. We will use subsets of states in the NFA as states in the DFA. (This is called the subset construction approach.)





DFA ← NFA (Subset Construction)



Theorem (NFA to DFA – Subset Construction)

For a given NFA $N = (Q_N, \Sigma, \delta_N, q_0, F_N)$, \exists DFA D. L(D) = L(N).

Proof) Define a DFA

$$D = (Q_D, \Sigma, \delta_D, \{q_0\}, F_D)$$

where

- $Q_D = \mathcal{P}(Q_N)$
- $\forall S \in Q_D$. $\forall x \in \Sigma$.

$$\delta_D(S,x) = \bigcup_{q \in S} \delta_N(q,x)$$

• $F_D = \{S \in Q_D \mid S \cap F_N \neq \emptyset\}$

Then,

$$w \in L(D) \iff \delta_D^*(\{q_0\}, w) \in F_D$$
 (: definition of $L(D)$)
 $\iff \delta_D^*(\{q_0\}, w) \cap F_N \neq \varnothing$ (: definition of F_D)
 $\iff \delta_N^*(\{q_0\}, w) \cap F_N \neq \varnothing$ (: lemma in the next slide)
 $\iff w \in L(N)$ (: definition of $L(N)$)





Lemma

$$\forall S \in Q_D. \ \forall w \in \Sigma^*. \ \delta_D^*(S, w) = \delta_N^*(S, w)$$

Proof) By induction on the length of word.

- (Base Case) $\delta_D^*(S,\epsilon) = S = \delta_N^*(S,\epsilon)$.
- (Inductive Case) Assume it holds for w (I.H.).

$$\begin{split} \delta_D^*(S,xw) &= \delta_D^*(\delta_D(S,x),w) & (\because \text{ definition of } \delta_D^*) \\ &= \delta_D^*(\bigcup_{q \in S} \delta_N(q,x),w) & (\because \text{ definition of } \delta_D) \\ &= \delta_N^*(\bigcup_{q \in S} \delta_N(q,x),w) & (\because \text{I.H.}) \\ &= \delta_N^*(S,xw) & (\because \text{ definition of } \delta_N^*) & \Box \end{split}$$

Summary



1. Nondeterministic Finite Automata (NFA)

Definition

Transition Diagram and Transition Table

Extended Transition Function

Language of NFA

Examples

2. Equivalence of DFA and NFA

 $\mathsf{DFA} \to \mathsf{NFA}$

DFA ← NFA (Subset Construction)

Next Lecture



• ϵ -Nondeterministic Finite Automata (ϵ -NFA)

Jihyeok Park
 jihyeok_park@korea.ac.kr
https://plrg.korea.ac.kr