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where $f(w)$ is defined only if w starts with 1.

$\cdots$	B	1	1	0	1	0	1	1	1	1	B	$\cdots$

1: Check if the first bit is 1.
2: Move to the end of the input.
3: Repeatedly replace the rightmost 1 with 0.
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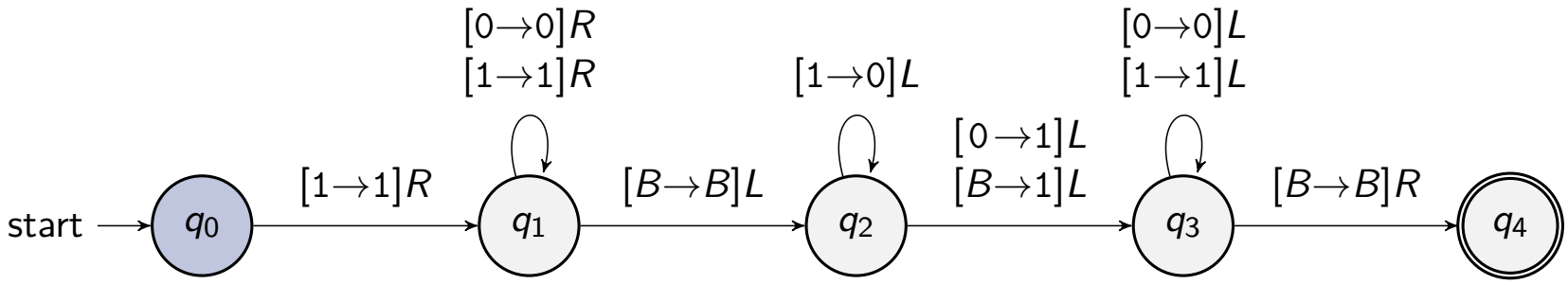

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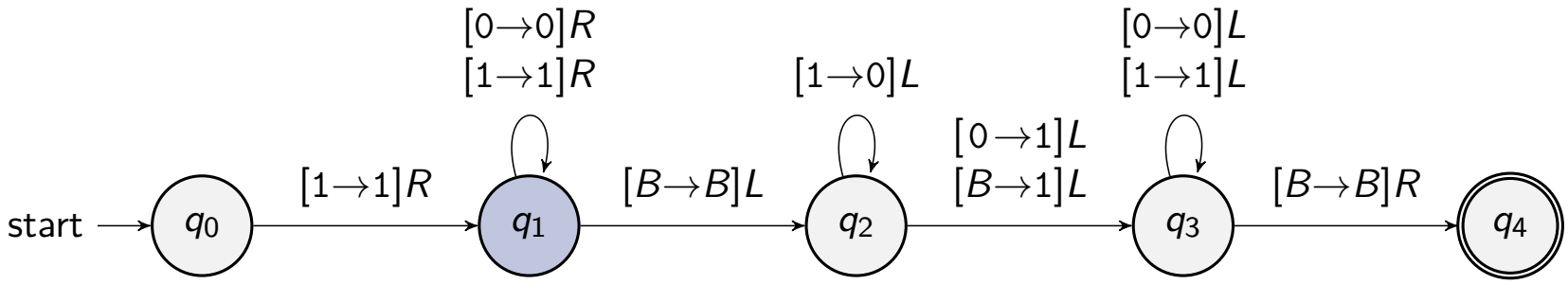

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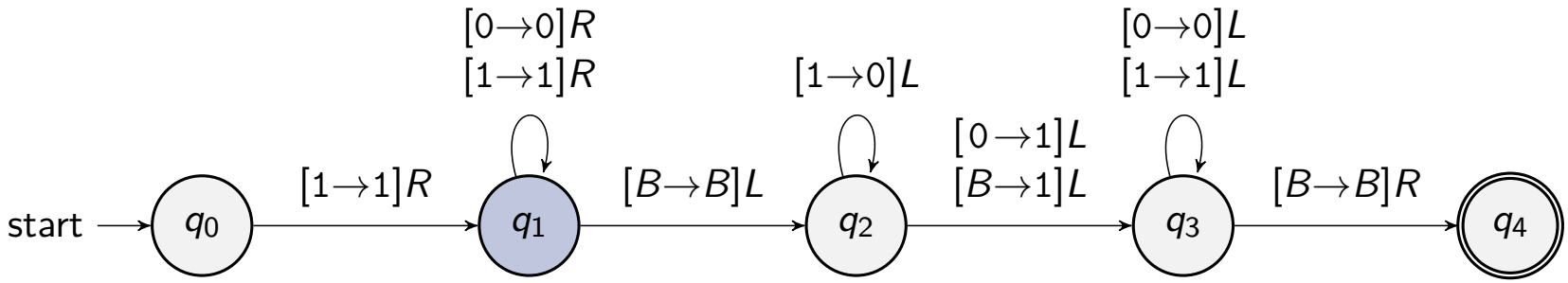

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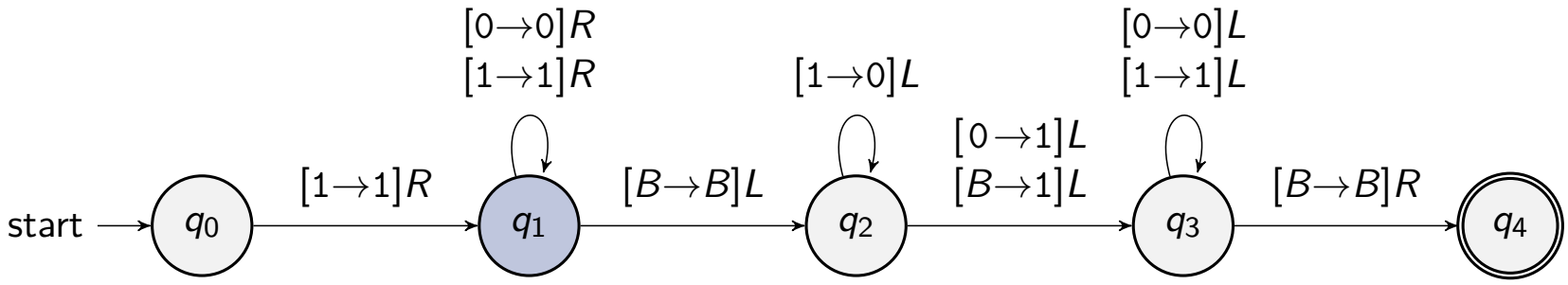

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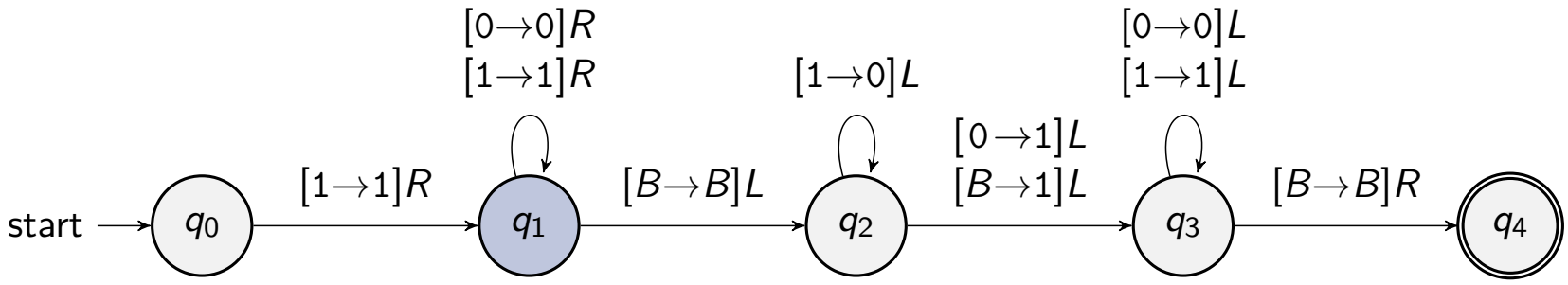

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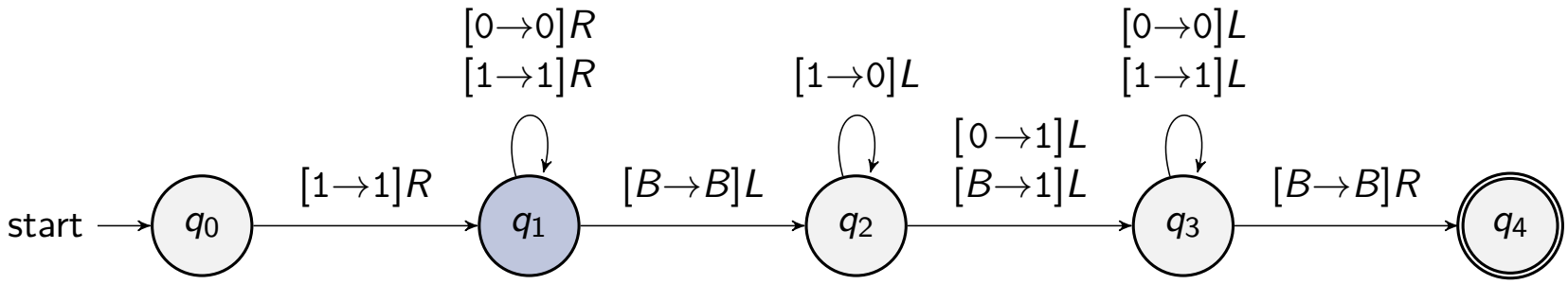

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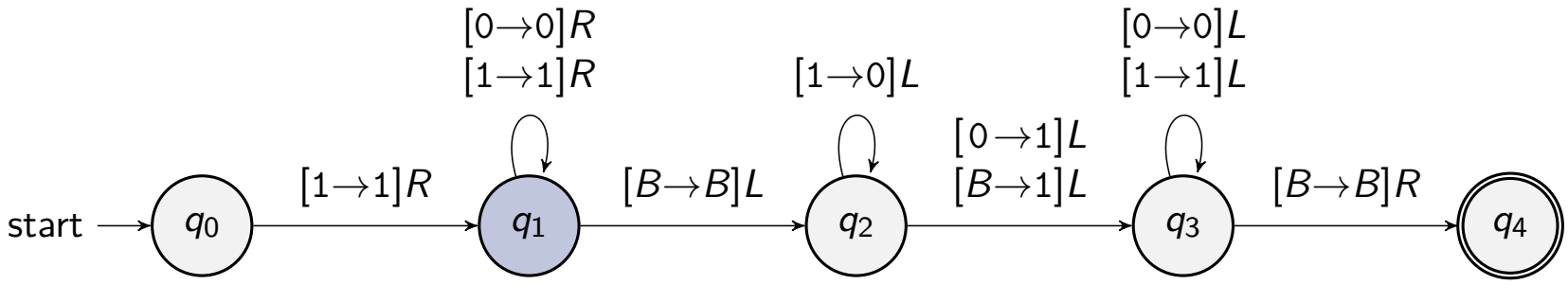

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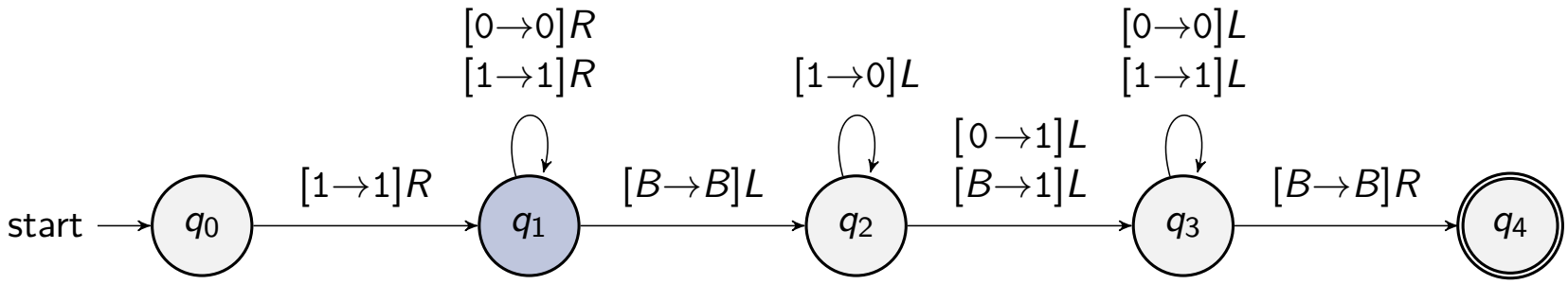

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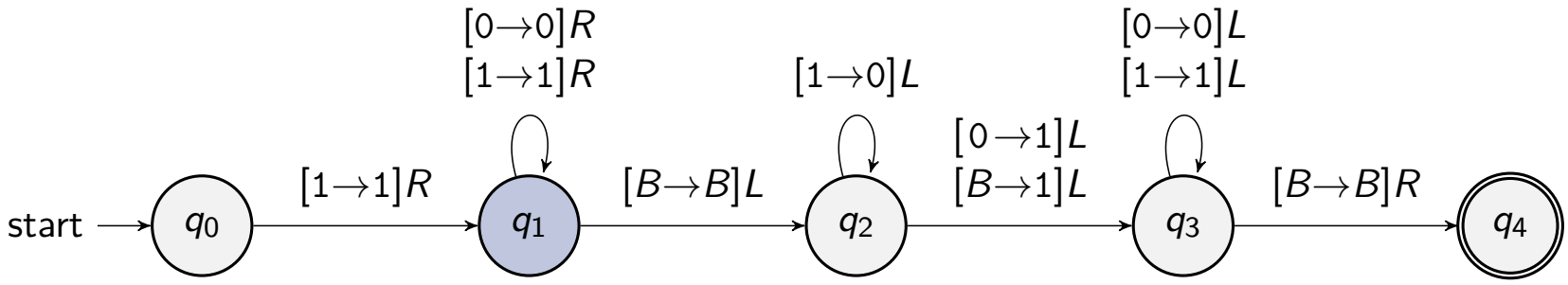

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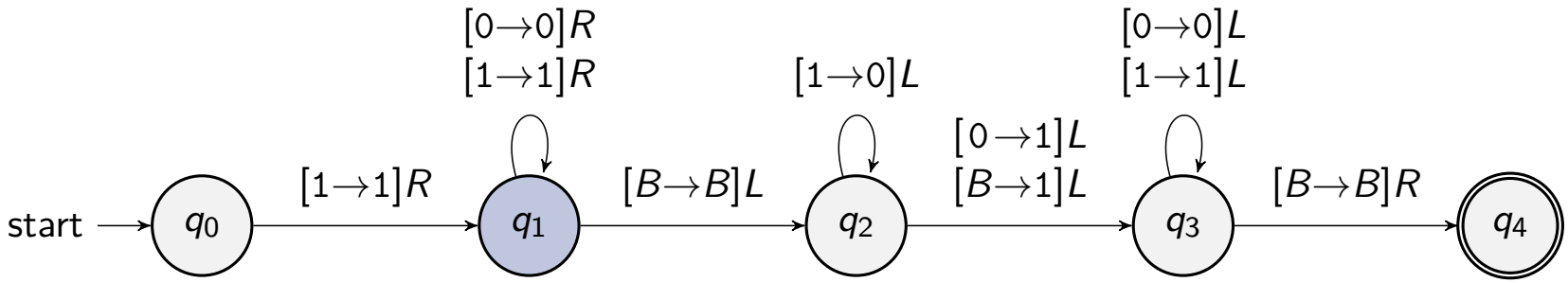

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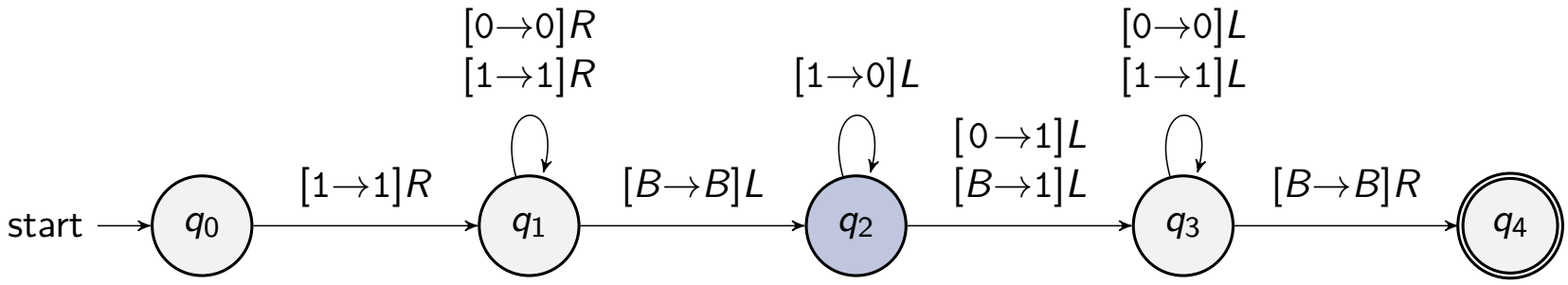

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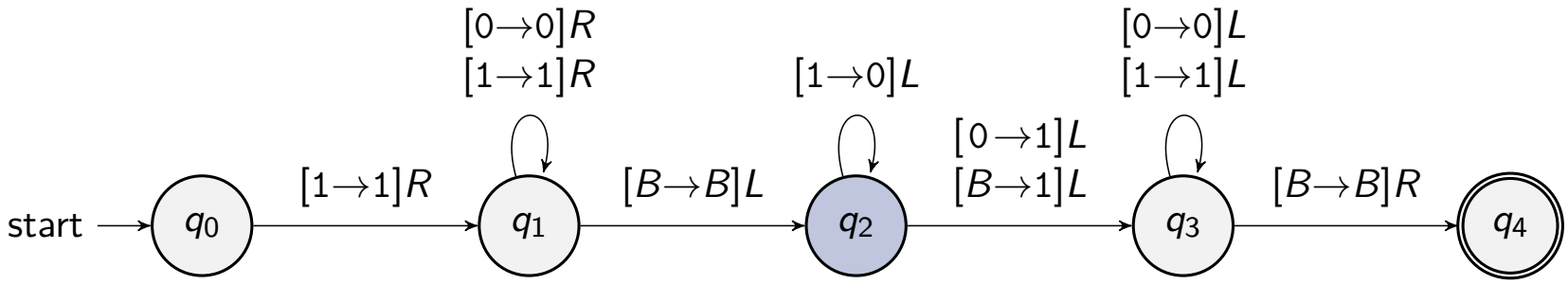

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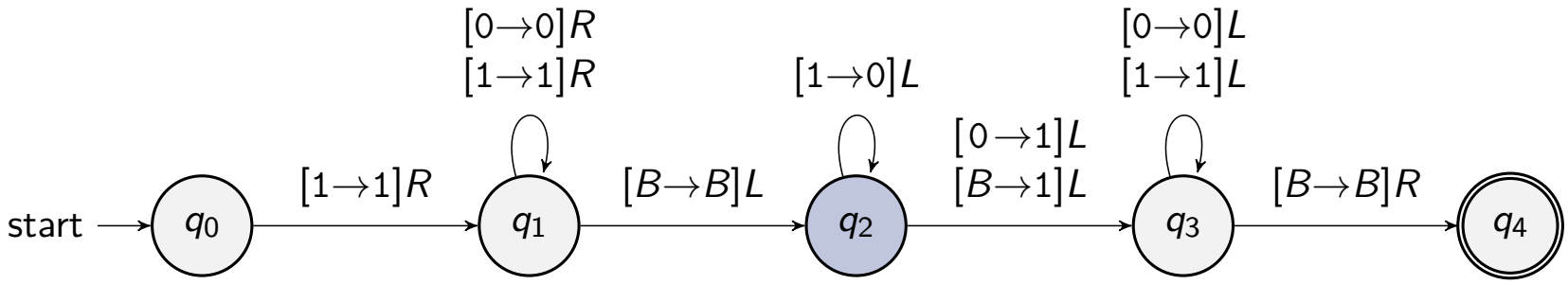

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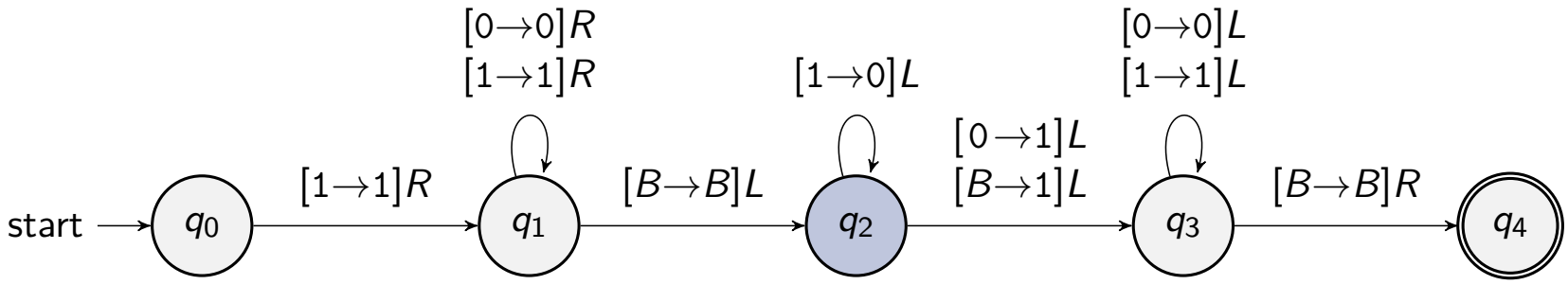

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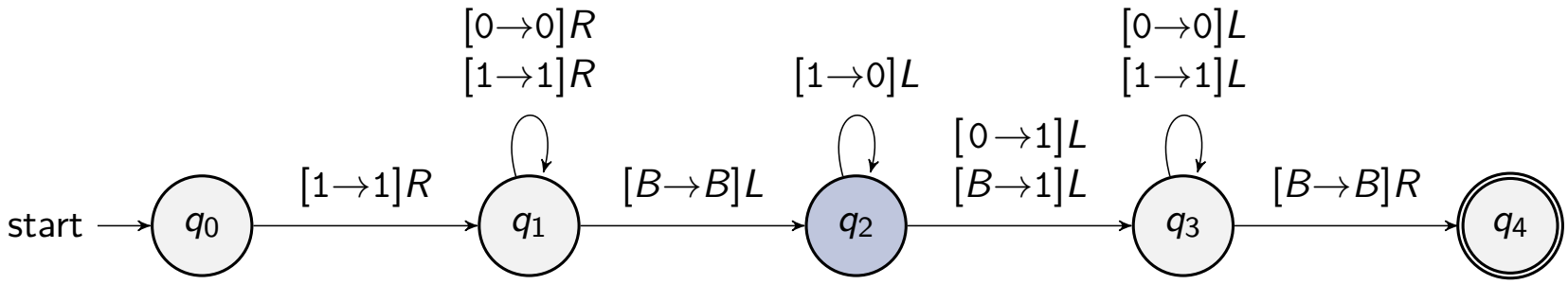

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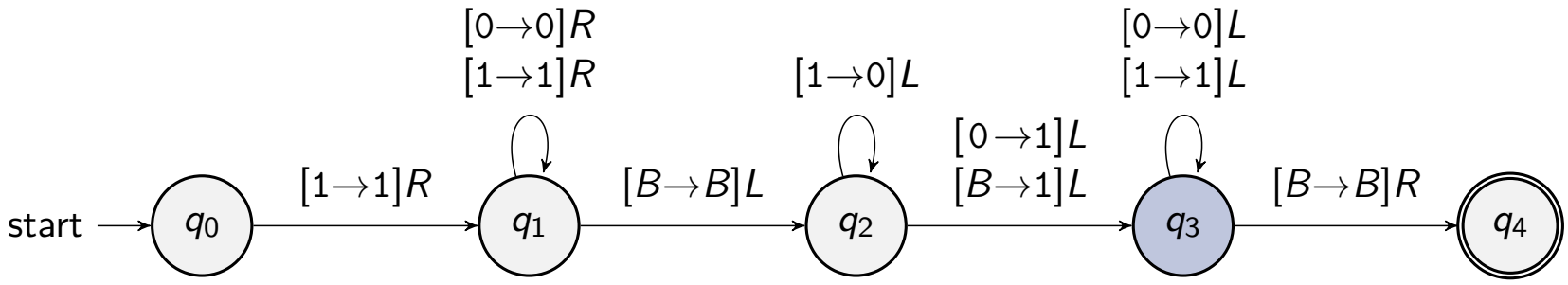

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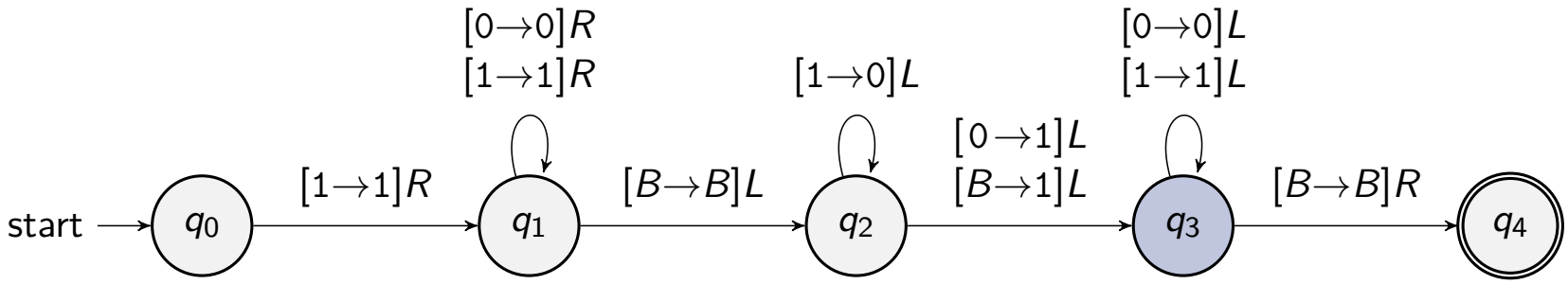

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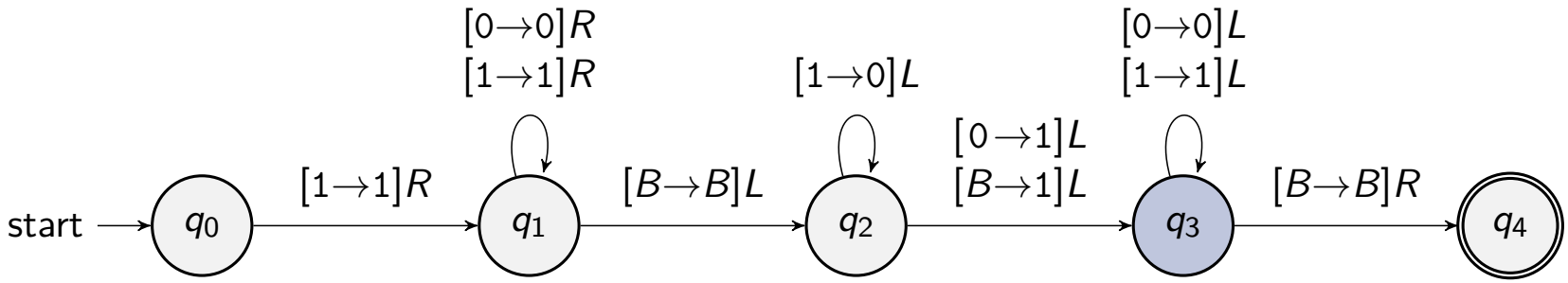

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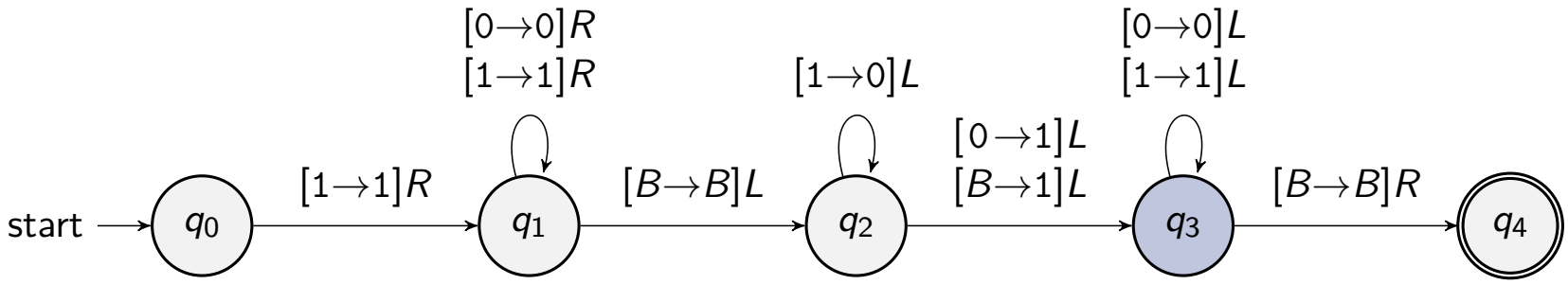

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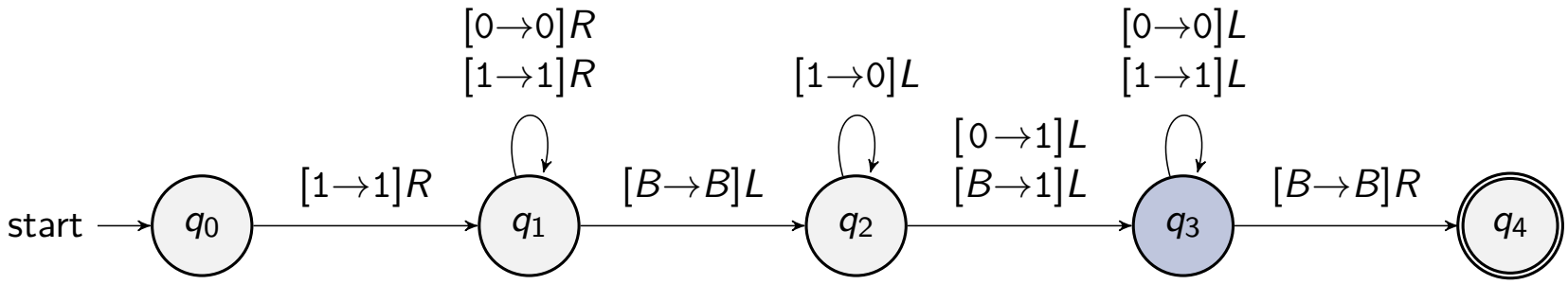

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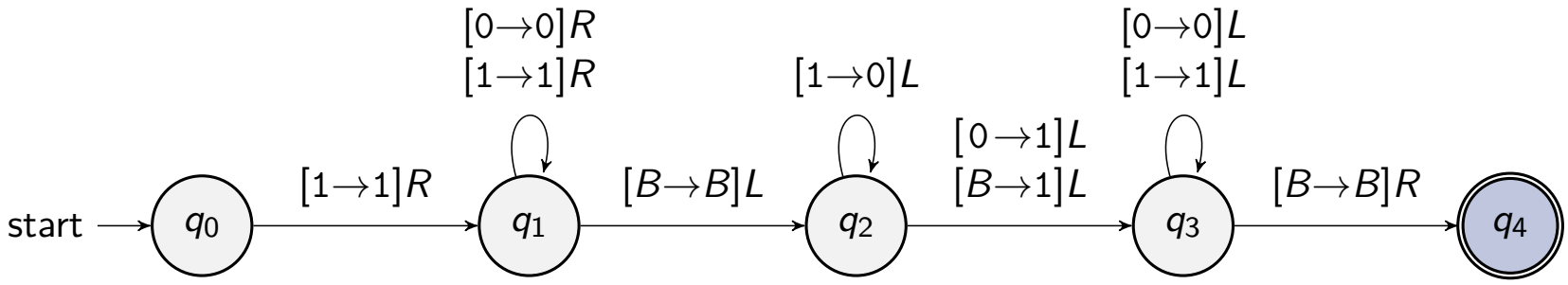

Computed! $f(110101111) = 110110000$