TooManyCells identifies and visualizes relationships of single-cell clades

Gregory W. Schwartz et al. (2020/04)

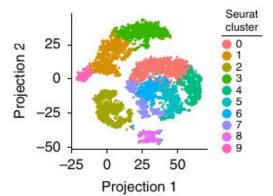
Outlines

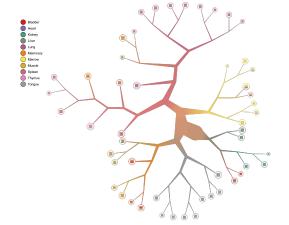
- 1. Describe the method in human language
- 2. The Development of key concepts
- 3. How it works
- 4. How it helps my project

1 TooManyCells: Clustering Algorithm

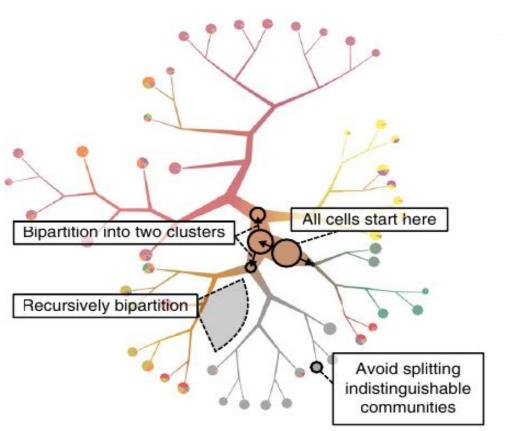
Seurat Nearest neighbor clustering determine a unique position of each cell based on their coordination in latent space (e.g. PCA).

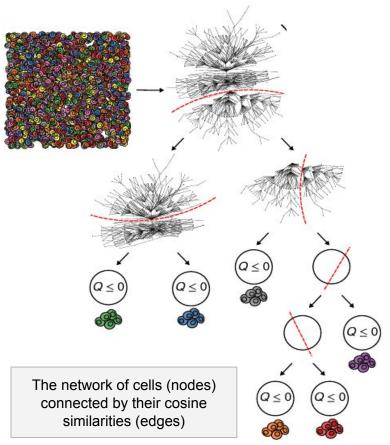
too-many-cells algorithm recursively divides cells into two clusters each time and relates clusters while branching the tree.





1 TooManyCells: Clustering Algorithm





2 Development of Key Concepts: Computer Vision

Normalized Cuts and Image Segmentation (Jianbo Shi et al. 2000)

- Similarity between pixels are calculated by color change in euclidean space **A**.
- Define Normalized Cuts, Graph Laplacian Matrix L
- Bring up a brilliant idea that it is possible to optimally biparition a picture by the second smallest eigenvector of matrix L





2 Development of Key Concepts: Text Mining

Normalized Cuts and Image Segmentation (Jianbo Shi et al. 2000)

- Similarity between pixels are calculated by color change in euclidean space A.
- Define Normalized Cuts, Graph Laplacian Matrix L
- Bring up a brilliant idea that it is possible to optimally biparition a picture by the second smallest eigenvector of matrix **L**

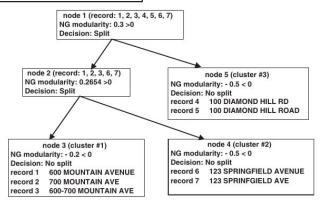
Efficient Spectral Neighborhood Blocking for Entity Resolution (Liangcai et al 2011)

- Use q-gram, TF-IDF and cosine similarity to describe the similarities A among records
- Build "Graph" Laplacian Matrix L based on A
- Fast way to calculate the second eigenvector in **sparse** matrix
- Introduce Newman-Girvan modularity from social network research to decide when to stop splitting.





| Record# | Address | |
|---------|------------------------|--|
| 1 | 600 MOUNTAIN AVENUE | |
| 2 | 700 MOUNTAIN AVE | |
| 3 | 600-700 MOUNTAIN AVE | |
| 4 | 100 DIAMOND HILL RD | |
| 5 | 100 DIAMOND HILL ROAD | |
| 6 | 123 SPRINGFIELD AVENUE | |
| 7 | 123 SPRINFGIELD AVE | |



2 Development of key concepts: Single Cells

Normalized Cuts and Image Segmentation (Jianbo Shi et al. 2000)

- Similarity between pixels are calculated by color change in euclidean space **A**.
- Define Normalized Cuts, Graph Laplacian Matrix L
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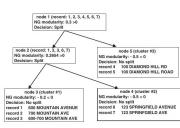
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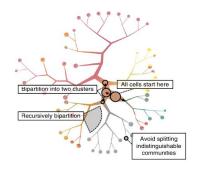
- TF-IDF and cosine similarity to describe the similarities A among cells.
- Implement Liangcai's clustering algorithm
- Add more downstream analysis tools: preprocessing options, normalization methods, visualization, Differentially Expression, Diversity Analysis and Cluster Purity...





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| | | |





Suppose you have a similarity matrix \mathbf{A} where A(i, j) represents the similarity between item i and j. Then we can calculate the degree matrix $\mathbf{D} = \text{diag}(\mathbf{A1})$, there d(i) is $\text{sum}_{j} A(i, j)$. Define graph laplace matrix:

$$\mathcal{L}(\mathbf{A}) = \mathbf{I} - \mathbf{D}^{-1/2} \mathbf{A} \mathbf{D}^{-1/2}$$

It is shown that the second smallest eigenvector can be used to optimally bipartition the dataset.

Suppose **B1** (m x n) is a SC-seq UMI read matrix. Use **TF-IDF** to normalize the counts.

$$\mathbf{B}_2 = \log(\mathbf{m}/\mathbf{d}_i)\mathbf{B}_1(i,j)$$
 (If the degree is high, then we add a penalty to the frequency.)

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Suppose **B1** (m x n)is a SC-seq UMI read matrix. Use **TF-IDF** to normalize the counts **B2**. Use Cosine Similarity to represent the distance between two cells.

$$\mathbf{A}(i,j) = \frac{\sum_{k=1}^{n} \mathbf{B}_{2}(i,k) \mathbf{B}_{2}(j,k)}{\sqrt{\sum_{k=1}^{n} \mathbf{B}_{2}^{2}(i,k)} \sqrt{\sum_{k=1}^{n} \mathbf{B}_{2}^{2}(j,k)}}$$

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Suppose you have a similarity matrix **A** where A(i, j) represents the similarity between item i and j. Then we can calculate the degree matrix **D** = diag(**A1**), there d(i) is sum $\{i\}$ A(i, j).

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$$\mathcal{L}(\mathbf{A}) = \mathbf{I} - \mathbf{D}^{-1/2} \mathbf{A} \mathbf{D}^{-1/2}$$

It is shown that the second smallest eigenvector can be used to optimally bipartition the dataset.

Use Newman-Girvan Modularity as stopping criteria.

$$Q(C_1, C_2) = \sum_{k=1}^{2} \left(\frac{O_{kk}}{L} - \left(\frac{L_k}{L} \right)^2 \right)$$

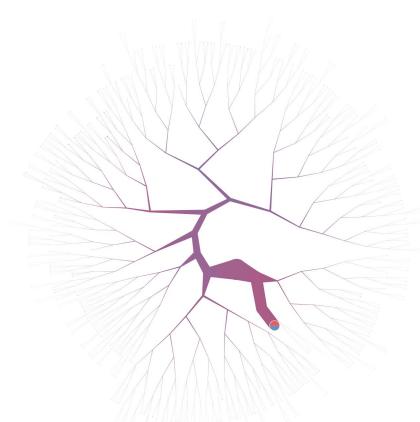
Q > 0 denotes non-random communities

Q < 0 demonstrates communities randomly found

4 TooManyCells on Traf6 dataset

After integration, apply tooManyCells algorithm on 20-dim latent subspace.

But there are too many subsets in binary tree and we should consider pruning the branches.



4 TooManyCells on Traf6 dataset

| MAD * 5 | | | | |
|---------|------|-------|--|--|
| Cluster | Size | WT% | | |
| 10 | 255 | 67.06 | | |
| 11 | 159 | 72.32 | | |
| 7 | 203 | 65.51 | | |
| 8 | 218 | 65.51 | | |
| 13 | 208 | 52.40 | | |
| 14 | 218 | 52.40 | | |
| 15 | 231 | 58.44 | | |
| 16 | 251 | 62.15 | | |
| 22 | 231 | 55.41 | | |
| 21 | 2674 | 49.92 | | |
| 18 | 240 | 58.75 | | |
| 19 | 236 | 59.32 | | |

