

# REDUCING COMMUNICATION OVERHEAD IN DISTRIBUTED LEARNING BY AN ORDER OF MAGNITUDE (ALMOST)

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大规模分布式学习在现代计算中扮演着越来越重要的角色。但是，无论是使用具有数千个节点的计算机集群，还是使用单个多GPU机器，最重要的瓶颈是通信。在这项工作中，我们探讨了量化和编码对分布式模型参数的影响。我们证明了，对于神经网络，这可以在不减缓收敛速度，或损害模型的泛化的情况下完成。事实上，在我们的实验中，我们能够减少几乎一个数量级的通信开销，同时实际上提高泛化精度。

## ABSTRACT

Large-scale distributed learning plays an ever-more increasing role in modern computing. However, whether using a compute cluster with thousands of nodes, or a single multi-GPU machine, the most significant bottleneck is that of *communication*. In this work, we explore the effects of applying quantization and encoding to the parameters of distributed models. We show that, for a neural network, this *can* be done – without slowing down the convergence, or hurting the generalization of the model. In fact, in our experiments we were able to reduce the communication overhead by nearly an order of magnitude – while actually improving the generalization accuracy.

**Keywords:** Neural Networks, Distributed Training, Compression

## 1. INTRODUCTION

With the sizes of today's datasets growing to giga- and petabytes, we see an increasing need for distributed solutions to learning problems. In particular, in the deep learning literature, we have seen the number of parameters in a single model reach the billions [1, 2]. This renders training on a single node infeasible - both with respect to memory requirements and execution time. It becomes necessary, and indeed imperative, to distribute the computation across many machines.

However, distributed computing requires communication: data and model parameters must be exchanged between the worker machines that collaborate on the computation. Even using the fastest interconnects, such as InfiniBand (IB) or PCI Express 3.0 (PCIe), this communication overhead can become a serious bottleneck and greatly slow down the learning.

In this paper we address the problem of reducing communication overhead in distributed learning of large neural networks.

Communication overhead arises both from the need to transfer data to the workers, and the need to share model parameters among them. In our work we focus on the latter, minimizing the communication overhead due to **exchange of model parameters**. Specifically, we focus on gradient-based methods in a *data-parallel* setting [3]; *i.e. where the dataset is distributed across workers, and each worker has a complete copy of the model*. During training, each worker locally updates its own model, and the updated model parameters must periodically be synchronized among all of the workers.

The general approach to minimizing communication overhead has been just to reduce the *number* of parameters that are exchanged, *e.g.* by having fewer parameters in the first place by sparsifying them, exchanging only some of the parameters, or by sending them less frequently [4, 2].

We take a different approach – rather than impoverishing the number of parameters exchanged, we reduce the communication overhead by reducing the *number of bits* used to transmit each parameter. We achieve this by quantizing the transmitted values. The

entropy [5] of the parameters of the network vary with training epoch, and the layer of the network that they represent. To take advantage of this, we vary the number of bits used to quantize any value dynamically, based on the observed entropy of the parameter values in any layer, at any epoch. Additional compression is obtained through Huffman coding [6] of the parameters prior to transmission. The additional overhead of conveying the information about the quantization levels and Huffman code dictionaries, so that the machines receiving these communicated values can decode them, is insignificant compared to the actual number of bits needed to represent the parameters. We are thus able to achieve a compression of nearly an order of magnitude in the communication overhead, for no loss of generalization error in the trained network, as evaluated on a standard classification task.

In the process, we also achieve a second, surprising result. The introduction of quantization noise appears to have a beneficial effect on the training. When the parameters are quantized to a slightly higher bit rate than that required to maintain generalization error, the resulting network actually achieves *lower* generalization error than that obtained with unquantized transmission of parameters. Moreover, the training often appears to converge faster. In effect, we simultaneously achieve reduced communication overhead, improved generalization error, and faster convergence by quantizing the parameters for communication.

The proposed method can also be coupled with techniques that only transmit a subset of the parameters. Here too the parameters could be further compressed as we propose, resulting in large reductions in the communication overhead.

The rest of the paper is structured as follows. In Section 2 we briefly outline the training setup. In Section 3 we discuss the rationale behind our compression scheme. In Section 4 we outline our compression algorithm. In Section 5 we provide experimental analysis of our solution, and in Section 6 we conclude with discussion.

## 2. DISTRIBUTED TRAINING SETUP

Our experiments were performed on a multi-GPU architecture: five NVIDIA GTX 780s connected by a single PCIe 3.0 bus. We used a custom neural network (NN) implementation written in a combination of Cuda and MATLAB; GPU-GPU copying was enabled by a single MEX file that wraps a call to *cudaMemCpyPeer*. A worker in this scenario, is thus a dedicated CPU thread controlling one GPU.

The NN was trained using standard Backprop with SGD and mini-batches, exponential learning rate decay, and light  $\ell_1$  regularization. As mentioned, we have focused solely on the *data-parallel* setting, where each worker has a complete copy of the model, but works on an exclusive segment of the dataset. For sake of consistency and repeatability of our experiments, we chose a *synchronous*

然而，分布式计算需要通信。数据和模型参数必须在协作进行计算的工作机器之间交换。即使使用最快的互连，如InfiniBand (IB)或PCI Express 3.0 (PCIe)，这种通信开销也会成为严重的瓶颈，大大降低学习速度。

通信开销既来自于向工作人员传输数据的需要，也来自于在他们之间共享模型参数的需要。数据集分布在各个工作节点之间，每个工作节点都有模型的完整副本。

减少通信开销的一般方法就是减少交换的参数数量，首先通过减少参数，只交换一些参数，或者减少发送它们的频率。

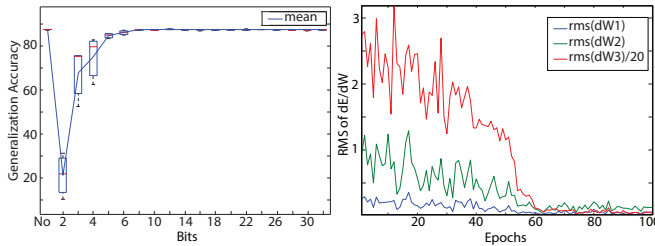
我们采用了一种不同的方法——通过减少用于传输每个参数的比特数来减少通信开销，而不是减少交换的参数数量。我们通过量化传输值来实现这一点。

为了利用这一点，我们改变了用于动态量化任何值的比特数，基于观测到的任何层、任何时期参数值的熵。通过对传输前的参数[6]进行Huffman编码，得到了额外的压缩。

量化噪声的引入似乎对训练产生了有益的影响。当参数量化到比维持泛化误差所需的稍高的比特率时，得到的网络实际上比不量化传输参数得到的泛化误差更低。此外，训练似乎集中得更快。实际上，我们通过量化通信参数，同时降低了通信开销，提高了泛化误差，提高了收敛速度。

该方法还可以与只传输参数子集的技术相结合。在这里，参数也可以进一步压缩，从而大大减少通信开销。

如前所述，我们只关注数据并行设置，其中每个工作人员都有一个完整的模型副本，但是工作在数据集的一个专用段上。



**Fig. 1.** Generalization accuracy vs. quantization level of weights. **Fig. 2.** RMS MSE derivative w.r.t. weights vs. training epoch.

weight exchange scheme. That is, after each epoch the workers exchange weights, such that they all end up having the exact same averaged weights. This exchange can be done in various ways, depending on the context, and it can be done *asynchronously* too [1]. Our proposed method is however agnostic to all of this, as each transmission of parameters, from worker to worker (or e.g. slave to master node), is completely self-contained. **When a worker transmits something, it must send along some quantization and encoding meta-data; the receiver then uses that meta-data to decode and de-quantize the signal.** Whenever a worker changes anything, e.g. averages the weights it received with its own, and sends along the results - it must first adapt the quantization and encoding meta-data; i.e. the *codebook* etc. is not static.

### 3. PARAMETER COMPRESSION 压缩参数

**Our solution to reducing communication overhead is to compress parameters before transmission.** In choosing a compression scheme, we must consider many factors including **cost** (complexity and execution time), **memory usage**, **effectiveness** (compression ratio), and **impact on learning** (the generalization error of the model). Obviously, the cost of encoding, sending, and decoding the data must be less than simply sending the data as is. Similarly, cutting down the cost of communication is meaningless if it affects the learning negatively, such that either the generalization error increases, or it takes considerably more iterations to converge (so that nothing is gained with respect to the total execution time).

The model parameters to be transmitted are **single- or double-precision floating point numbers**. We find simple lossless compression of these parameters through algorithms such as LZW [7] to generally be ineffective. They achieve little, if any, reduction in the size of the data, at a significant computational cost.

Instead, we will utilize the robustness of model parameters to minor perturbation, particularly during training, to compose an inexpensive *lossy* compression scheme through quantization. Secondly, we will utilize the relatively narrow range within which most parameter values lie to further compress the parameters through a lossless compression scheme.

In the following subsections all illustrations are based on experiments on the MNist database [8] with a deep neural network comprising 784 units in the input layer and three subsequent layers of size 392, 50 and 10 neurons respectively. The network is fully connected between any two consecutive layers. There are thus three sets of weights of size  $784 \times 392$ ,  $392 \times 50$  and  $50 \times 10$  respectively. The activation functions of all neurons were tanh non-linearities.

#### 3.1. Quantizing the parameters 量化参数

As a first try, we attempted to simply quantize all parameters to a fixed number of bits. **To quantize the values to  $N$  bits, we find the largest and minimum values of all weights in each epoch,** and evenly

split the range up into  $2^N$  bins. **Each weight is quantized to the center of the bin that it falls into.** In terms of communication, it will require only  $N$  bits to transmit any weight.

Figure 1 shows results obtained with quantization to various levels. The plot shows the classification accuracy obtained with the fully trained network, as a function of the number of bits used to quantize the weights. The boxes show the mean, median (red line) and standard deviation of the results obtained from 1500 runs of training with different initializations. The accuracy obtained with 8-bit quantization is comparable to that obtained without quantization. This compares very favorably with the 32 bits typically required to represent floating point numbers in IEEE format.

#### 3.2. Dynamic Selection of Quantization Levels 动态选择量化级别

As network training progresses, the derivative of the mean squared error (MSE) being minimized with respect to the weights converges towards a small value approaching zero, albeit in a somewhat noisy manner. Figure 2 shows the root-mean squared (RMS) value of the derivatives of the error with respect to network weights for each of the three layers in our network as a function of epoch. The derivatives for the third layer are scaled by 20 to fit in the plot. We note that the derivatives converge towards zero for all layers. Also, the derivatives are generally larger at higher layers of the network.

The derivatives are directly indicative of the degree of quantization that can be tolerated by the weights. When the derivatives are large, relatively small perturbations of weights can result in relatively large changes in the error. On the other hand, when the derivatives are small, the network is tolerant to larger perturbations of the weights. We also know that quantization to a larger number of bits results in smaller expected quantization error, while quantization to a fewer number of bits results in larger quantization error.

These observations together suggest that when the RMS value of the derivative is large, a larger number of bits are required to quantize the weights. On the other hand, at small RMS values of the derivative, a smaller number of quantization levels will suffice.

This leads us to propose **a dynamic selection** of the number of bits to quantize the weights. **In each epoch, for each layer, we will choose the number of bits to quantize the weights in that layer according to the RMS value of the derivative of the MSE with respect to the weights.** Specifically, assuming the tolerance to changes in the MSE to be some constant  $T$ , and the RMS value of the derivatives to be  $G$ , the bin size  $\Delta W$  that may be expected to perturb the objective to within  $T$  is given by  $\Delta W \propto T/(G + c_0)$ , where  $c_0$  is a floor that enforces an upper bound on  $\Delta W$ . Consequently, the number of bins that the weights are quantized to,  $N_{bin} \propto \Delta W^{-1} \Rightarrow N_{bin} \propto (G + c_0)$ . The number of bits required to quantize the weights comes out to  $N = \log N_{bin} = \log(G + c_0) + c_1$ .  $c_1$  may be viewed as a floor on the number of bits used to quantize the weights. To ensure that  $N$  does not go below this value,  $c_0$  must be set to 1.0.

#### 3.3. Lossless Compression 无损压缩

The distribution of the weights is not uniform in any layer. Figure 3 shows the estimated entropy of the network weights in the various layer of the network, as a function of epoch. In each case, for  $N$ -bit quantization we have computed the entropy from the normalized histogram of the weights over the  $2^N$  quantization bins. The four panels shows the entropy obtained with different levels of quantization of the weights. Expectedly, increasing the number of bits used to quantize the weights increases their entropy; however the overall trend of the entropy remains the same in all cases.

The entropy is generally less than  $N$ , the number of bits used to quantize the weights, and decreases with the epochs. This indicates

每个重量都被量化到它掉进去的箱子的中心。

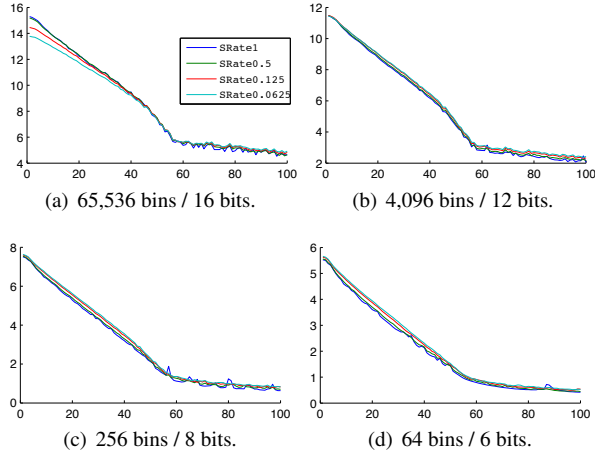
图中显示了经过充分训练的网络获得的分类准确度，它是用于量化权重的比特数的函数。8位量化得到的精度与未量化得到的精度相当。

图2显示了误差对网络权重的导数的均方根(root-mean squared, RMS)值，作为epoch的函数，在每一层的误差对网络权重的导数。此外，在网络的高层，导数通常更大。当导数较大时，权重的相对较小的扰动会导致误差的相对较大的变化。另一方面，当导数很小时，网络能够承受较大的权值扰动。我们还知道，量化到更大的比特数会导致更小的预期量化误差，而量化到更少的比特数会导致更大的量化误差。这些观察结果表明，当导数的均方根值较大时，需要大量的位来量化权值。另一方面，当导数的均方根值很小时，更少的量化级别就足够了。

在每一个epoch中，对于每一层，我们将根据MSE相对于权重的导数的均方根值，选择要量化该层权重的比特数。假设对变化的容忍度MSE是一个常数T，导数的RMS值是G，bin的尺寸w可能期望被打扰。

这里没有看值？？？？权重被量化的bins的数量。量化值所需的比特数是  $N = \log N_{bin} = \log(G + c_0) + c_1$ 。c1可以被看作是用于量化权重的比特数的下限。

各层权重分布不均匀。



**Fig. 3.** Computing the entropy using different sample ratios and number of histogram bins (bits). The sample ratio (denoted SRate in the legend), representing the fraction of the total set of weights that was used to estimate the entropy, has very little affect. Lowering the number of bins merely results in a shift of the entire curve.

that **lossless Huffman coding of the quantized weights can result in significant compression of the weights.**

### 3.4. Bits Required to Quantize the Weights

Comparing Figure 3 and Figure 2 we note that the **entropy** is well correlated with the RMS value of the gradient. Empirically, we find the normalized correlation between  $\log(G + c_0)$  for  $c_0 = 1$  and the entropy of the weights to be greater than 0.75 at all times, and frequently higher than 0.95, particularly in the higher layers.

This correlation is sufficient for us to use the entropy of the weights as a proxy for the RMS value in determining the desired quantization. Thus we arrive at the following estimate for the number of bits required to quantize the weights in the  $k^{\text{th}}$  level of the network in the  $e^{\text{th}}$  training epoch:  $N_{k,e} = H_{k,e} + c$ , where  $H_{k,e}$  is the entropy of the weights in the  $k^{\text{th}}$  layer, in epoch  $e$ , and  $c$  is a floor on the number of bits to be used.

The above formula appears self-referential at first glance: the entropy estimate  $H_{k,e}$  itself depends on the number of bits used to quantize the weights as noted earlier. **To resolve this, we compute  $H_{k,e}$  from a preliminary quantization of the weights to  $M$  bits.** Typically, it is sufficient to estimate  $H_{k,e}$  **from only a small sample of the complete set of weights.** Empirically, we have found that using as few as 3% of the total set of weights can provide us with reliable estimates of the entropy of the weights in any layer.  $M$  is a parameter we can choose.  **$c$  must be empirically determined,** and now also accounts for the fact that  $H_{k,e}$  depends on  $M$ , since increasing  $M$  by a factor of  $2^K$  will increase  $H_{k,e}$  by approximately  $K$  bits. On the other hand, decreasing  $M$  results in smoother, and potentially more robust estimates of the entropy as seen from Figure 3.

## 4. AN ALGORITHM FOR DYNAMIC COMPRESSION OF NETWORK WEIGHTS

Algorithm 1 describes our final algorithm for compressing the network weights. **The output of the algorithm is a set of packaged weights,** where the package contains all the necessary information required to decode the quantized weights to their actual values. Algorithm 2 describes the algorithm used to decode the packaged

### Algorithm 1 Weight Compression Algorithm

```

1: Input: Weights  $\mathcal{W}_l$ ,  $l = 1..L$  for each of the  $L$  layers in the net,
    $F, M, c$ . 每一层的权重
2: for layer  $l = 1..L$  do
3:   Find  $w_{max}^l = \max_{w \in \mathcal{W}_l} w$  and  $w_{min}^l = \min_{w \in \mathcal{W}_l} w$ . 找出最小的和最大的
4:   Entropy  $H = \text{Estimate Entropy}(\mathcal{W}_l, F, w_{min}^l, w_{max}^l, M)$ 
5:   Compute the number of bits:  $N = H + c$ . 计算bit数
6:   Quantize  $\mathcal{W}_l$ :  $\mathcal{Q}_l = \text{Quantize}(\mathcal{W}_l, w_{min}^l, w_{max}^l, N)$ . 量化
7:   Estimate Probability  $\mathbf{P}_l = \text{Estimate Distribution}(\mathcal{Q}_l, N)$  估计可能性
8:   Huffman Codebook  $\mathcal{C}_l = \text{HuffmanCodebook}(\mathbf{P}_l)$ . 霍夫曼码
9:   Encode  $\mathcal{Q}_l$ :  $\mathcal{E}_l = \text{Encode}(\mathcal{Q}_l, \mathcal{C}_l)$ . 编码
10:  Package  $\mathcal{P}_l = [\mathcal{E}_l, w_{min}^l, w_{max}^l, \mathbf{P}_l, N]$ .
11: end for
12: Output:  $\mathcal{P}_l$ ,  $l = 1..L$ .

1: function QUANTIZE( $\mathcal{W}, w_{min}, w_{max}, K$ )
2:   Return  $\mathcal{Q} = \left\{ \left\lfloor \frac{2^K (w_{max} - w)}{w_{max} - w_{min}} \right\rfloor \mid w \in \mathcal{W} \right\}$  为什么是用这个公式?
3: end function

1: function ESTIMATE DISTRIBUTION( $\mathcal{Q}, K$ )
2:   Compute a  $2^K$ -bin histogram  $h(i)$ ,  $i = 1..2^K$  from  $\mathcal{Q}$ .
3:   Normalize the histogram:  $p(i) = \frac{h(i)}{\sum_i h(i)}$ .
4:   Return  $\mathbf{P} = \{p(i), i = 1..2^K\}$ 
5: end function

1: function ESTIMATE ENTROPY( $\mathcal{W}, F, w_{min}, w_{max}, M$ ) 估计熵
2:   Select a random subset  $\mathcal{W}_{sel}$  of  $\mathcal{W}$  of size  $F|\mathcal{W}|$ .
3:   Quantize  $\mathcal{W}_{sel}$ :  $\mathcal{Q}_{sel} = \text{Quantize}(\mathcal{W}_{sel}, w_{min}, w_{max}, M)$ 
4:   Estimate  $\mathbf{P} = \text{Estimate Distribution}(\mathcal{Q}_{sel}, M)$ 
5:   Return  $H = - \sum_{i=1}^{2^K} p(i) \log p(i)$ .
6: end function

```

### Algorithm 2 Weight De-Compression Algorithm

```

1: Input:  $\mathcal{E}_l, w_{min}^l, w_{max}^l, \mathbf{P}_l, N$ 
2: Huffman Codebook  $\mathcal{C}_l = \text{HuffmanCodebook}(\mathbf{P}_l)$ .
3: Decode  $\mathcal{Q}_l = \text{Decode}(\mathcal{E}_l, \mathcal{C}_l)$ .
4:  $\mathcal{W}_l = \{w_{min} + \frac{(w_{max} - w_{min})(i + 0.5)}{2^N} \mid i \in \mathcal{Q}_l\}$ .
5: Output:  $\mathcal{W}_l$ 

```

用于将打包后的权值解码为可由接收节点使用的实数的算法。

weights to real numbers that can be used by the receiving node. **HuffmanCodebook, Encode and Decode** are standard algorithms for computing the Huffman codebook, encoding a sequence of bits with a given Huffman code, and decoding a stream of Huffman codes.

The parameters  $F$ ,  $M$ , and  $c$  must be empirically determined.  $F$  is the fraction of weights that are used to obtain the preliminary estimate of entropy,  $H$ .  $M$  is the size in bits of the initial quantizer used to obtain this preliminary estimate.  $c$  is the quantization floor. Empirically, we have that  $F = 0.03$ ,  $M = 4$ , and  $c = 6$  provide excellent results. We present experiments that support this conclusion in the next section.

## 5. EXPERIMENTS

We ran experiments to investigate the proposed method and demonstrate its validity. The experimental setup was that described in Section 2. Experiments were run on the 784-392-50-10 neural network described in Section 3, on the MNIST database. In total, we ran the Backpropagation algorithm about 1,500 times, while saving all the parameters of the NN after each of the 100 epochs.

HuffmanCodebook, Encode和Decode是用于计算Huffman codebook的标准算法，它们用给定的Huffman代码编码一个位序列，并对Huffman代码流进行解码。  
F是用于获得初始熵估计值的权重的分数，H、M是用于获得初始熵估计值的初始量化器的比特大小，c是量化层



### 5.1. Establishing Optimal Parameter Values

The proposed algorithm has three parameters: (a) the sample ratio  $F$ , which determines the fraction of the weights we use to arrive at  $H$ , the preliminary estimate of entropy, (b) the quantization floor  $c$ , and (c)  $M$ , the bit size used for the preliminary entropy estimate. We investigate the setting of each of these.

**Estimating  $F$ :** Figure 3 shows the entropy estimates obtained with different sample rates in each panel. The entropy estimates do not vary much with sample rate. We therefore set  $F = 0.03$ , i.e. 3%. For larger networks an even lower value of  $F$  may suffice.

**Estimating  $M$  and  $c$ :** The optimal values of  $M$  and  $c$  are closely coupled. First we establish the *ceiling* on the number of bits needed, through fixed-size quantization. Figure 1 shows the generalization accuracies obtained with fixed-size quantization at every quantization level between 2 and 30 bits. We are able to recover baseline results at 8 bits, which gives us a 75% reduction in communication (in single-precision) by quantization alone. We therefore consider a ceiling of 10 bits to provide room for variation.

Ideally, we must explore the entire range of  $(M, c)$  values to establish the optimal setting. Instead, we present a summary that only considers marginal variation of each of the variables, while assuring the reader that the conclusions noted generalize to the larger search.

In general, we can expect the dynamically assigned quantization size not to exceed the bit-rate ceiling. The maximum value of the preliminary entropy estimate obtained from  $M$ -bit quantization is  $M$ . Thus, we expect  $c + M$  to be no greater than the ceiling. We use this to first establish an effective value for  $M$ . Figure 4a shows the generalization performance obtained on the test set when  $c + M = 10$ . Each point on the plot represents the aggregate statistics of 50 trials run with different initializations. We have varied the floor  $c$  from 2 to 10 bits. A ceiling of 10 and a floor of 10 (represented by “10:10” in the figure) represents fixed quantization to 10 bits. We observe that we obtain the best results with  $M = 4$ , representing a quantization floor of  $c = 6$  bits. Figure 4b shows the performance obtained at different values of the floor  $c$ , at  $M = 4$ . At  $M = 4$ ,  $c = 5$  we obtain performance just marginally below baseline, giving us a “sweet spot” in terms of compression. It is interesting to note that the performance with 9:5, representing  $M = 4$  is actually superior to that obtained with 10:5 representing  $M = 5$ .

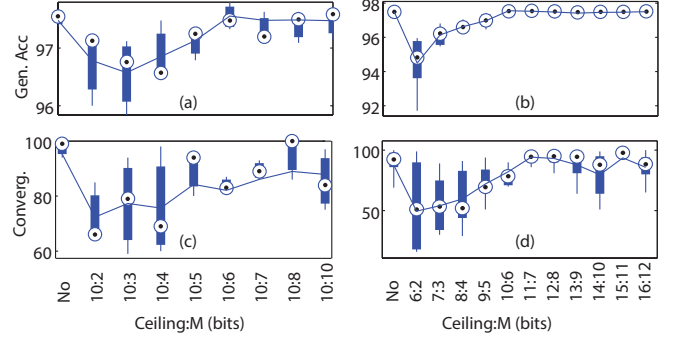
Thus, we establish  $c = 5$ ,  $M = 4$ , since this results in only minor loss of performance. Figure 5 shows the average bit-rate per parameter as a function of epoch. This represents an average bit rate of 6.8 bits/parameter over all training epochs, and an overall compression rate of 4.70.

Finally, we apply the final stage of Huffman coding to the quantized weights. Figure 5 also shows the average bit-rate obtained with Huffman coding. This results in a significant reduction of bit-rate at every stage, and an overall average bit-rate of 3.55 bits/parameter, representing an overall compression rate of 9.01 with respect to the baseline with no compression.

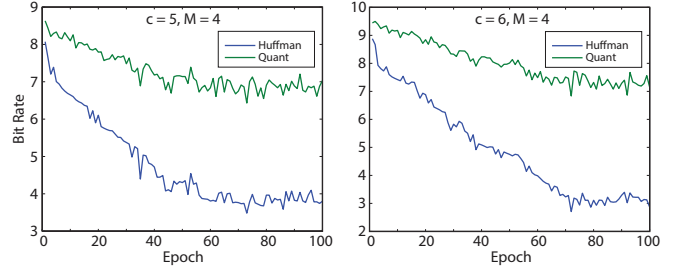
### 5.2. Going beyond the Baseline

Figure 4 reveals an interesting fact. The generalization error obtained with  $c = 6$ ,  $M = 4$  is actually *superior* to the baseline. These results are consistent over a large number of runs of the experiment. The mean bit rate at this setting is 3.78 bits/parameter, representing an overall compression of 8.47.

Figures 4c and 4d show the number of iterations required for the training to achieve convergence, where we define convergence as the peaking of generalization accuracy. In all cases compression of the weights results in faster convergence. At  $c = 6$ ,  $M = 4$ , con-



**Fig. 4. Left:** Generalization accuracies (a), and convergence (c) for fixed quantization ceiling of 10 bits with varying floor. **Right:** Generalization accuracies (b), and convergence (d) for a fixed quantization range of 4 bits with increasing floor. **All:** The left-most value is the baseline, and the dots are medians and the line plots the mean.



**Fig. 5.** Bit-rate as a function of epoch with raw and Huffman coded quantized values. **Left:** at  $c = 5$ ,  $M = 4$ . **Right:** at  $c = 6$ ,  $M = 4$ .

vergence is achieved in 20% fewer iterations than the baseline. Considering both the gains from parameter compression and the faster convergence, we obtain an effective overall reduction of communication of a factor of 10.32, while also improving generalization error.

## 6. CONCLUSION & DISCUSSION

As the size of neural networks and the data used to train them increase, not only will more parameters need to be communicated, they will be done so over increasingly greater numbers of machines. Gains such as those we report will become very important. The computational overhead of compression is miniscule compared to the actual transmission in these scenarios. Although we have presented the compression scheme in the context of neural networks, it will apply to gradient-descent based distributed optimization in general. Moreover, it can also be combined with approaches that only transmit a subset of parameters, for additive gains in compression.

While our results are very promising, the actual numbers reported must still be considered with caution. A part of our current work is validating these results on much larger corpora. We are also investigating extensions to *model-parallel* formalisms [2].

The improved generalization results we observe are, perhaps, not so surprising, since the effect of quantization is to introduce quantization noise. It is well-known that noise may help a learning algorithm escape from local minima [9], and has been used in de-noising Auto-Encoders (DAEs) [10], and other variants such as dropout [11] and DropConnect [12]. However, it remains to confirm our results on larger data sets and networks; this is work in progress. We do not expect any surprises.

## 7. REFERENCES

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