# LEARNING NATURAL STATISTICS OF BINOCULAR CONTRAST FOR NO REFERENCE QUALITY ASSESSMENT OF STEREOSCOPIC IMAGES

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#### ABSTRACT

Algorithms for no-reference (NR) stereoscopic image quality assessment (SIQA) aim to evaluate the perceptual quality of a stereoscopic/3D image without the assistance of its reference. Current NR SIQA models often require training on 3D distorted images and their associated human opinion scores, which ultimately restrict their further application. In this paper, we present a simple yet effective NR SIQA model that does not require training on existing 3D image databases. Instead, we train our model on a large dataset of natural stereoscopic images based on learning the local statistics of the Cyclopean contrast maps, and then use the existing 2D NR IQA model to help guide the NR SIQA task. Experimental results demonstrate the efficacy of our proposed method.

*Index Terms*— Stereoscopic image quality assessment, binocular contrast, log-derivative statistics, no-reference quality assessment

#### 1. INTRODUCTION

Research in image quality assessment (IQA) has grown tremendously over the last two decades leading to numerous powerful algorithms for evaluating 2D image quality with or without the reference information (see [1] for reviews). IQA of stereoscopic/3D images, however, is relatively new and less mature, due in large part to the difficulties and complexities in mimicking binocular visual processing in the human visual system (HVS). As with 2D IQA, the stereoscopic image quality assessment (SIQA) problem can be broadly classified into three main categories based on the availability of a reference image: full-reference (FR), reduced-reference (RR), and no-reference (NR). The vast majority of SIQA algorithms have addressed the FR and RR scenarios (e.g., [2, 3, 4], etc.).

In this paper, we address NR SIQA (or *blind* SIQA), in which only the distorted stereoscopic image is available to the IQA algorithm. Blind assessment of a 3D image quality is extremely challenging because of the complex binocular fusion and rivalry behaviors that will occur when the human eyes are presented with asymmetrically distorted views. This

difficulty has been elaborated in [5] that binocular combinations under different distortion types should be considered: the high quality view that contains sufficient information will help suppress the low quality view with information-loss distortion (e.g., blurring) [6], while for the information-additive distortion (e.g., blockiness), the low quality view cannot be compensated [7].

To model the complex behaviors of the HVS on the NR SIQA task, various models have been proposed by using different quality-related features (e.g., [5, 8, 9, 10], etc.). However, most of these approaches share a common requirement: they need training on 3D images with anticipated distortion information as well as their associated human opinion scores; consequently, the limited number of existing 3D image databases potentially restrict their wider applicability. To the best of our knowledge, only a few NR SIQA algorithms (e.g., [10, 11]) require no training on distorted stereoscopic images, but their performances are less competitive. To release the dependence of NR SIQA algorithms on prior knowledge of distorted stereopairs, while still maintaining competitive predictive performance, here, we present a simple, yet effective NR SIQA algorithm which operates by learning the local natural statistics (NS) of the Cyclopean contrast maps.

The proposed SIQA algorithm, called 3DLN (QA of 3D images via Learning Natural statistics), is inspired by three previous works: the log-derivative-statistics-based DE-SIQUE [12] model, the cyclopean-feature-image-based 3D-MAD model [3], and the multivariate Gaussian (MVG)-based NIQE model [13]. To blindly assess stereoscopic image quality without depending on training on existing 3D image databases, 3DLN employs log-derivative-based statistical features computed from Cyclopean contrast maps of the natural and distorted stereoscopic images, and also utilizes the 2D-stereopair distortion information to help guide the NR SIQA task. The qualities obtained from both the stereopairs and the Cyclopean-contrast-maps are combined to yield an overall quality estimate of the stereoscopic image.

This paper is organized as follows: Section 2 provides details of the proposed 3DLN algorithm. In Section 3, we

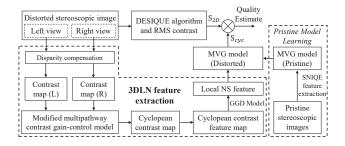


Fig. 1. A block diagram of the 3DLN algorithm.

analyze the performance of 3DLN on two 3D image quality databases. General conclusions are presented in Section 4.

#### 2. ALGORITHM

The proposed 3DLN algorithm consists of two main stages: (1) the 2D-DESIQUE-based quality estimate on stereopairs, and (2) the local NS-based quality estimate on Cyclopean contrast maps. A block diagram of the algorithm is shown in Figure 1.

# 2.1. 2D-DESIQUE on Stereopairs

In the 2D-DESIQUE-based QA stage, the conventional DE-SIQUE algorithm [12] is applied to the stereopairs (i.e., the left and right view images) to estimate the perceived distortion corresponding to each monocular view. Then, the overall 2D-DESIQUE quality is computed as the weighted sum of both stereopair distortion measures, where the weights are computed based on a block-based RMS contrast measure.

Specifically, given an image, we first divide it into blocks of  $16 \times 16$  pixels (with 75% overlap), and then compute the RMS contrast of each block via

$$C(b) = \tilde{\sigma}(b)/\mu(b) \tag{1}$$

where  $\mu(b)$  represents the average luminance value of block b, and  $\tilde{\sigma}(b)$  represents the minimum standard deviation among the four  $8\times 8$  subblocks within b (see Appendix A in [14]). Using Eq.(1), we compute block-based contrast maps for the left and right views of the distorted stereoscopic image (denoted by  $C_L$  and  $C_R$ , respectively), and then the 2D-DESIQUE score is given by

$$\mathbf{S}_{2D} = (\bar{C}_L \cdot Q_L + \bar{C}_R \cdot Q_R) / (\bar{C}_L + \bar{C}_R) \tag{2}$$

where  $\bar{C}$  is the mean value of C;  $Q_L$  and  $Q_R$  denote the DE-SIQUE quality estimates of the left and right views.

# 2.2. Local NS-based Cyclopean IQA

The local NS-based Cyclopean IQA explores the idea in [13] that image quality can be measured locally, but extends

this idea from 2D to 3D by using an efficient binocular fusion/rivalry model, and different quality-related features. In addition, important distortion information obtained in the first stage of 3DLN is used to guide the Cyclopean QA process.

# 2.2.1. Cyclopean Contrast Maps

Motivated by [3], we propose two types of contrast as the algorithm's raw inputs for the Cyclopean IQA stage:

$$f_{1}(x,y) = \frac{2\sqrt{L(x,y) \cdot \bar{L}_{B}(x,y)}}{L(x,y) + \bar{L}_{B}(x,y) + K},$$
 (3)

$$f_2(x,y) = L(x,y)/[\bar{L}_B(x,y) + K],$$
 (4)

where L denotes the luminance value;  $\bar{L}_B(x,y)$  denotes the average luminance value of a 9×9 block centered around pixel (x,y); K=0.001 is a small constant that prevents division by zero.

Given the two contrast maps for each view of the stereoscopic image, we next build disparity-compensated Cyclopean contrast maps based on a modified multipathway contrast-gain control model (MCM) [3]. In our previous FR SIQA work [3], we argued that the quality of a monocular scene with higher contrast will play a more dominant role in determining the HVS's judgment of the 3D image quality. In this paper, we further argue that if the two monocular scenes have similar contrast, then the scene with greater quality degradation should weigh more toward determining the overall 3D image quality. This statement is also in accord with findings in [7] that the low quality view caused by information-additive distortion (e.g., blockiness) cannot be compensated by the high quality view. Thus, to better model the binocular interactions between the two monocular views, we modify MCM in [3] as follows: if the two views have significantly different quality ratings but similar averaged RMS contrast values, then the view with lower quality will be compensated by a larger weight in the Cyclopean-view-build process.

Specifically, we use DESIQUE scores as the approximate quality estimates of the two monocular views, and their quality difference is computed by  $r=2Q_LQ_R/(Q_L^2+Q_R^2)$ . We assume that r<0.75 indicates a significant quality difference between the two views, and consequently their corresponding Cyclopean contrast maps (denoted by  $C_{fi}(i=1,2)$ ) are computed via Eq.(5). Note that all symbols in Eq.(5) have the same meanings and values as that defined in [3] except for the two compensation factors  $E_L$  and  $E_R$ , which are given by

$$E_L = e^{1-r} S(\omega) u (Q_L - Q_R), \qquad (6)$$

$$E_R = e^{1-r} S(\omega) u (Q_R - Q_L), \qquad (7)$$

where  $u(\cdot)$  is a step function;  $S\left(\omega\right)$  is a sigmoid transducer function:

$$S(\omega) = \frac{A}{1 + e^{t_1(\omega - t_2)}} + B. \tag{8}$$

$$C_{f_{i}}(x,y) = \frac{\left[ \left( \eta_{L} f_{i,L}(x - d_{x,y}, y) \frac{E_{L}}{1 + \frac{\epsilon_{R}(x - d_{x,y}, y)}{1 + \beta\epsilon_{L}(x - d_{x,y}, y)}} \right)^{\gamma_{2}} + \left( \eta_{R} f_{i,R}(x, y) \frac{E_{R}}{1 + \frac{\alpha\epsilon_{L}(x, y)}{1 + \epsilon_{R}(x, y)}} \right)^{\gamma_{2}} \right]^{\frac{1}{\gamma_{2}}}}{\left[ \left( \frac{\eta_{L} E_{L}}{1 + \frac{\epsilon_{R}(x - d_{x,y}, y)}{1 + \beta\epsilon_{L}(x - d_{x,y}, y)}} \right)^{\gamma_{2}} + \left( \frac{\eta_{R} E_{R}}{1 + \frac{\alpha\epsilon_{L}(x, y)}{1 + \epsilon_{R}(x, y)}} \right)^{\gamma_{2}} \right]^{\frac{1}{\gamma_{2}}}}, (i = 1, 2)$$
(5)

Here,  $\omega=2\bar{C}_L\bar{C}_R/(\bar{C}_L^2+\bar{C}_R^2)$  represents the RMS contrast similarity between the two monocular views. The four free parameters are selected as follows:  $A=9, B=1, t_1=-8$ , and  $t_2=0.6$ . We found that changing these parameter values does not affect the algorithm performance significantly. For those r>0.75 stereopairs, the same MCM-based binocular model [3] is used to compute the Cyclopean contrast maps.

#### 2.2.2. Local NS Feature Extraction

Based on the two Cyclopean contrast maps, the next step is to extract efficient local statistical features that are representative of the quality degradation. Towards this end, for each Cyclopean contrast map, we propose eight derivative-related image operators to build the corresponding eight Cyclopean contrast feature (CCF) maps. Then, the log-derivative statistics are applied to the mean-subtracted contrast-normalized (MSCN) coefficients of each CCF map in a block-based manner to extract the local features.

Specifically, let  $\mathrm{C}_f$  denote one of the two Cyclopean contrast maps, and its elements are denoted by  $C_f(i,j)$ . Then, for each Cyclopean contrast map, its eight CCF maps are computed by

$$\nabla^{1}C_{f}(i,j) = C_{f}(i',j') - C_{f}(i,j)$$
 (9)

$$\nabla^2 C_f(i,j) = \frac{2C_f(i',j')C_f(i,j)}{C_f^2(i',j') + C_f^2(i,j)} \tag{10}$$

where  $\nabla^1$  and  $\nabla^2$  denote the derivative-related image operators;  $C_f(i',j')$  denotes the four neighboring pixels around  $C_f(i,j)$  [i.e.,  $C_f(i',j') = C_f(i,j+1), C_f(i+1,j), C_f(i+1,j+1)$ , or  $C_f(i+1,j-1)$ ].

We found that the MSCN coefficients of these CCF maps fit quite well to the generalized Gaussian distribution (GGD) model when the four-orientation, spatial-domain log-derivative statistics are applied (i.e.,  $D_1$  through  $D_4$  in Section 3.2.1 in [12]). Thus, following from [13], we extract local log-derivative statistical features from the selected CCF map patches, which correspond to the sharper regions of the synthesized Cyclopean view.

In [13], sharp image patches are selected based on their averaged local variances, and this process is applied only to the natural images. In our work, we use  $FISH_{bb}$  algorithm [15] to more accurately measure the local sharpness of a Cyclopean image, and the sharp CCF patches are selected from both the natural and distorted images for feature extraction. We found that even in distorted images with loss of sharpness, those relatively sharper regions still contribute more to-

ward determining the overall image quality. Also, the fewer number of blocks allows less computational complexity.

Finally, the four-orientation, spatial-domain log-derivative statistics are applied to the selected CCF map patch, from which the two GGD parameters ( $\alpha$  and  $\sigma$ ) are estimated. We use  $\log(1+\alpha)$  as the features extracted from  $C_{f_1}$  map, and  $\sigma$  from  $C_{f_2}$  map. Consequently, a total of 64 features (4 log-derivative orientations  $\times$  8 CCF maps  $\times$  2 contrast maps) are extracted from each patch.

### 2.2.3. Cyclopean Quality Estimate

The quality estimation of the two Cyclopean contrast maps [defined in Eqs.(3) and (4)] follows the common framework in [13]. First, the MVG distribution was employed to model the patch-based features extracted from both the pristine and distorted CCF maps, which is given by

$$f_X(x_1, ..., x_k) = \frac{exp\left[-\frac{1}{2}(x - \mu)^T \Sigma^{-1}(x - \mu)\right]}{(2\pi)^{k/2} |\Sigma|^{1/2}}, (11)$$

where  $x_1, ..., x_k$  are the computed feature vector for each patch;  $\mu$  and  $\Sigma$  denote the mean and covariance matrix of the MVG model. Then the quality of each Cyclopean contrast map is given by

$$d_{i} = \sqrt{\left(\mu_{f_{i}}^{d} - \mu_{f_{i}}^{p}\right)^{T} \left(\frac{\sum_{f_{i}}^{d} + \sum_{f_{i}}^{p}}{2}\right)^{-1} \left(\mu_{f_{i}}^{d} - \mu_{f_{i}}^{p}\right)}.$$
(12)

Here,  $\mu_{f_i}^{p/d}$  and  $\Sigma_{f_i}^{p/d}(i=1,2)$  denote the estimated mean and covariance matrix (corresponding to  $C_{f_i}$ ) of the pristine and distorted MVG models, respectively. Finally, the Cyclopean quality is computed by

$$S_{cuc} = \ln(1 + d_1 \times d_2)$$
. (13)

Note that for the noise-corrupted images, quality prediction using Eq.(13) may very likely produce an unexpected deviation from the normal quality range maintained by other distortions. To address this problem, we employ a Gaussian-filter which smooths partial noise in stereopairs before the two contrast maps are computed. In our implementation, we use DESIQUE algorithm [12] to detect noise, and then the Gaussian filter variance is determined by the 2D DESIQUE score of each monocular view through another sigmoid transducer function, which has the same form as Eq.(8). Here, the variable  $\omega$  represents the smaller value of the two DESIQUE scores (i.e.,  $\omega = \min \{Q_L, Q_R\}$ ), and the Gaussian-filter size

is  $5\times5$  pixels. Also, we set the following parameter values: A=0.55, B=0,  $t_1=-0.2$ , and  $t_2=60$ . These parameter values are empirically selected to help achieve the best performance on the LIVE3D image database [16].

# 2.3. 3DLN Quality Index

The final stage of 3DLN is to combine the quality estimates obtained from the two previous stages into an overall quality index, which is given by

$$3DLN = S_{2D} \times S_{cyc}. \tag{14}$$

Smaller values denote predictions of better stereoscopic image quality.

# 3. RESULTS AND ANALYSIS

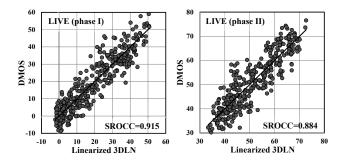
We tested and compared 3DLN with other FR/NR SIQA algorithms on the LIVE3D Phase I and Phase II databases [16] in terms of the Spearman rank-order correlation coefficient (SROCC) values (the Pearson linear correlation coefficient (CC) values follow the similar trend). The three FR SIOA algorithms include the Cyclopean MS-SSIM proposed by Chen et al. [2], the frequency-integrated PSNR (FI-PSNR) proposed by Lin et al. [17], and the BJND-based method proposed by Shao et al. [18]. The four NR SIQA algorithms include two 2D IQA and two SIQA algorithms, all of which do not require training on distorted stereoscopic images. Note that for the two 2D IQA metrics (NIQE [13], and IL NIQE [19]), the predicted quality of a stereoscopic image was taken to be the average quality predicted from the left and right views. The two NR SIQA algorithms are the local-featurebased method proposed by Akhter et al. [11] and the MVGbased method proposed by Zhou et al. [10].

The results are shown in Table 1, in which italicized entries denote FR SIQA algorithms. Also included are the SROCC values of the first and second stage of 3DLN, denoted by 3DLN-2D and 3DLN-cyc, respectively. Observe from Table 1 that 3DLN outperforms the other five NR SIQA algorithms. In regards to the three FR SIQA algorithms, 3DLN achieves a better performance than Lin's method [17] on both databases, and challenges the other two, both of which have taken into account the binocular fusion/rivalry properties for analysis. Compared with 3DLN-2D and 3DLN-cyc, observe that the combined 2D and Cyclopean contrast analysis improves upon each individual stage.

Figure 2 shows the scatter-plots of logistic-transformed 3DLN quality predictions vs. subjective ratings (DMOS) on the two testing databases. In both graphs, the y-axis denotes the subjective ratings of the perceived distortions and the x-axis denotes the predicted quality value after the logistic transform as in [3]. Despite the presence of some outliers, the plots are generally heteroscedastic.

**Table 1**. Performance of 3DLN and other FR/NR SIQA algorithms on the LIVE3D Phase I and Phase II databases.

	JP2K	JPEG	WN	GBLUR	FF	ALL
	LIVE3D phase I					
Chen [2]	0.896	0.558	0.948	0.926	0.688	0.916
Lin [17]	0.839	0.207	0.928	0.935	0.658	0.856
Shao [18]	0.883	0.599	0.930	0.910	0.793	0.927
NIQE [13]	0.632	0.599	0.907	0.861	0.519	0.797
IL_NIQE [19]	0.861	0.544	0.920	0.873	0.536	0.860
Akhter [11]	0.866	0.675	0.914	0.555	0.640	0.383
Zhou [10]	0.837	0.638	0.931	0.833	0.649	0.892
3DLN-2D	0.881	0.592	0.933	0.815	0.713	0.908
3DLN-cyc	0.847	0.579	0.858	0.867	0.759	0.877
3DLN	0.883	0.616	0.933	0.851	0.759	0.915
	LIVE3D phase II					
Chen [2]	0.833	0.840	0.955	0.910	0.889	0.901
Lin [17]	0.719	0.613	0.907	0.711	0.701	0.638
Shao [18]	0.788	0.745	0.807	0.939	0.935	0.819
NIQE [13]	0.599	0.637	0.600	0.851	0.775	0.707
IL_NIQE [19]	0.593	0.491	0.617	0.880	0.758	0.673
Akhter [11]	0.724	0.649	0.714	0.682	0.559	0.543
Zhou [10]	0.553	0.593	0.893	0.869	0.828	0.825
3DLN-2D	0.787	0.826	0.884	0.812	0.910	0.858
3DLN-cyc	0.696	0.657	0.865	0.864	0.817	0.831
3DLN	0.796	0.832	0.954	0.858	0.890	0.884



**Fig. 2**. Scatter-plots of objective scores predicted by 3DLN algorithm after logistic transform versus subjective scores on the LIVE3D Phase I and Phase II databases.

# 4. CONCLUSION

This paper presented an algorithm, called 3DLN, to blindly evaluate the quality of stereoscopic images via learning the local natural statistics of binocular contrast maps, and also by utilizing the 2D distortion information to help guide the SIQA task based on properties of the human binocular vision. The proposed algorithm consists of two main stages. The first stage employs DESIQUE algorithm to assess the quality of each monocular view, and to obtain the basic distortion identification information. The second stage exploys the log-derivative statistics of the Cyclopean contrast map, and estimate the Cyclopean quality based on distorted MVG models and the pre-trained natural MVG models. The overall stereoscopic image quality is a combination of the two quality estimates from the two stages. We demonstrated the efficacy of 3DLN on several image databases.

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