

Please write ***Your name:*** _____

Show all work. You should either write at a sentence explaining your reasoning, or annotate your math work with brief explanations. There is no need to simplify, and no calculators are needed.

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Let X be a discrete random variables uniformly distributed on the numbers $\{1, 2, 3\}$.

(1) Find the moment generating function for X .

(2) Find $m''(0)$.

(3) Find $\mathbb{E}X^2$ and $\text{Var}X$.

On this page X_1, X_2, \dots, X_{25} are independent identically distributed random variables and $S_{25} = \sum_{k=1}^{25} X_k$.

- (1) If X_1, X_2, \dots, X_{25} are discrete random variables uniformly distributed on the numbers $\{1, 2, 3\}$, use the Central Limit Theorem to approximate $\mathbb{P}(S_{25} > 55)$. Your final answer should contain Φ , square roots, and fractions, but should not contain symbols μ, σ .
- (2) If X_1, X_2, \dots, X_{25} are continuous random variables uniformly distributed on the interval $[1, 3]$, use the Central Limit Theorem to approximate $\mathbb{P}(S_{25} > 55)$. Your final answer should contain Φ , square roots, and fractions, but should not contain symbols μ, σ .