

## Simple Implementation of fully connected deep-learning architecture

```
In [1]: # import libraries
import uuid
import numpy as np
```

### Define activation functions and its derivatives

```
In [2]: #####
### Logistic ###
#####
def logistic(x):
    return 1./(1+np.exp(x))
# end def
def diff_logistic(x):
    return x*(1-x)
# end def

#####
##### ReLU #####
#####
def ReLU(x):
    return max(0, x)
# end def
def diff_ReLU(x):
    if x <= 0:
        return 0
    else:
        return 1
    # end if
# end def
```

### Define network class

```
In [3]: class Net:
        def __init__(self):
            self.layers = []
            self.learning_rate = 0.05
        # end def

        def add_layer(self, layer):
            self.layers.append(layer)
            # register the neuron
            for neuron in self.layers[-1].get_all_neurons():
                neuron.net = self
            # end for
            self.reset_layers_index()
        # end def

        def reset_layers_index(self):
            for i in range(len(self.layers)):
                self.layers[-1].index = i
            # end for
        # end def

        # forward pass
        def forward(self):
            for layer in self.layers[1:]:
                for neuron in layer.neurons:
                    neuron.forward()
                # end for
            # end for

            neurons = self.layers[-1].get_all_neurons()
            output = [_.value for _ in neurons]

            return np.array(output)
        # end def

        # backward pass
        def backprop(self):
            for layer in reversed(self.layers):
                for neuron in layer.neurons:
                    neuron.backprop()
                # end for
            # end for
        # end def

        def get_all_neurons(self):
            for layer in self.layers:
                for neuron in layer.get_all_neurons():
                    yield neuron
                # end for
            # end for
        # end def

        def delta_update(self):
            pass
        # end def

# end class
```

**Define Layer class**

```
In [4]: class Layer:
        def __init__(self, net):
            self.index = None

            self.net = net
            self.neurons = []
        # end def

        def add_neuron(self, neuron):
            self.neurons.append(neuron)
            self.neurons[-1].layer = self
            self.neurons[-1].net = self.net
        # end def

        def size(self):
            return len(self.neurons)
        # end def

        def get_all_neurons(self):
            for neuron in self.neurons:
                yield neuron
            # end for
        # end def

        def fully_connect(self, next_layer):
            neuron_qs = list(next_layer.get_all_neurons())
            for neuron_p in self.get_all_neurons():
                neuron_p.add_children(neuron_qs)
            # end for
        # end def
    # end class
```

**Define Neuron class**

```

In [5]: class Neuron:
    def __init__(self, name, func, diff_func):
        self.uuid = str(uuid.uuid4())
        self.name = name
        self.net = None
        self.layer = None

        self.value = None
        self.delta = None
        self.parents = {}
        self.children = {}
        self.weights = {}
        self.biases = {}

        self.func = func
        self.diff_func = diff_func
        self.learning_rate = None
    # end def

    def set_activation_func(self, func, diff_func):
        self.func = func
        self.diff_func = diff_func
    # end def

    def add_parents(self, parents):
        for parent in parents:
            if parent.uuid not in self.parents:
                self.parents.update({parent.uuid: parent})
                parent.add_children([self])
            # end if
        # end for
    # end def

    def add_children(self, children):
        for child in children:
            if child.uuid not in self.children:
                self.children.update({child.uuid: child})
                child.add_parents([self])
            # end if
        # end for
    # end def

    def init_weights(self):
        '''Glorot initialization'''
        j = self.layer.index
        l = min(j+1, len(self.net.layers) - 1)
        nj = self.net.layers[j].size()
        nl = self.net.layers[l].size()

        lb = -np.sqrt(6) / np.sqrt(nj+nl)
        ub = np.sqrt(6) / np.sqrt(nj+nl)

        for parent in self.parents:
            self.weights[parent] = np.random.uniform(lb, ub)
            self.biases[parent] = 0
        # end for
    # end def

    def forward(self):
        s = 0.0
        for parent_id, parent in self.parents.items():
            value = parent.value
            s += self.weights[parent_id]*value + self.biases[parent_id]
        # end for
        self.value = self.func(s)
    # end def

```

**Initialize a network**

```
In [6]: net = Net()
```

**Initialize layers**

```
In [7]: l1 = Layer(net)
l2 = Layer(net)
l3 = Layer(net)
l4 = Layer(net)
```

```
In [8]: _layers = [l1, l2, l3, l4]
```

**Initialize neurons and add to layers**

```
In [9]: architecture = [3, 10, 5, 3]
```

```
In [10]: # Input layer
for l in range(len(architecture)):
    # get corresponding layer
    layer = _layers[l]

    # initialize all neurons
    num_neurons = architecture[l]
    for i in range(num_neurons):
        name = str((l, i))
        _neuron = Neuron(
            name = name,
            func = logistic,
            diff_func = diff_logistic
        ) # end neuron
        # add to layer
        layer.add_neuron(_neuron)
    # end for
# end for
```

**Adding layers to net**

```
In [11]: for _layer in _layers:
net.add_layer(_layer)
# end for
```

**Fully connect the layers**

```
In [12]: for i in range(len(net.layers)-1):
layer_p = net.layers[i]
layer_q = net.layers[i+1]
layer_p.fully_connect(layer_q)
# end for

...
# or more explicitly:
l1.fully_connect(l2)
l2.fully_connect(l3)
l3.fully_connect(l4)
...;
```

**Initialize weights for all neurons**

```
In [13]: for neuron in net.get_all_neurons():
         neuron.init_weights()
         # end for
```

**Set input values at input layer**

```
In [14]: # assumed input values
         x = (0.5, 0.3, 0.8)

         layer_in = net.layers[0]
         neurons_in = list(layer_in.get_all_neurons())
         for i in range(len(x)):
             neurons_in[i].value = x[i]
         # end for
```

**Forward pass (compute value)**

```
In [15]: out = net.forward()
         out
```

```
Out[15]: array([0.38125397, 0.22368634, 0.66421561])
```

**Compute error and values at output layer**

```
In [16]: # assumed target values
         target = np.array([0.5, 0.5, 0.5])
```

```
In [17]: layer_out = net.layers[-1]
         neurons_out = list(layer_out.get_all_neurons())
         for i in range(len(neurons_out)):
             neuron = neurons_out[i]

             # error
             err = neuron.value - target[i]
             # regularizer value
             l2_reg = 2*sum(neuron.weights.values())

             # compute delta
             delta = neuron.cal_grad() * (err+l2_reg)
             neuron.delta = delta
         # end for
```

**Backward pass (Backpropagation)**

```
In [18]: for layer in reversed(net.layers[:-1]):
         for neuron in layer.get_all_neurons():
             neuron.backprop()
         # end for
         # end for
```

**Demonstrating vanishing gradient**

```
In [19]: print('Demonstrating vanishing gradient')
         for i in range(len(net.layers)):
             deltas = [neuron.delta for neuron in net.layers[i].get_all_neurons()]
             abs_mean_delta = np.mean(np.abs(deltas))
             print ('layer-%d: delta=%4.4f' % (i+1, abs_mean_delta))
```

Demonstrating vanishing gradient

layer-1: delta=0.0039

layer-2: delta=0.0196

layer-3: delta=0.0616

layer-4: delta=0.4051

#### Update weights

```
In [20]: for neuron in net.get_all_neurons():
         neuron.update_weights()
         # end for
```

```
In [21]: net.forward()
```

```
Out[21]: array([0.38945027, 0.23961475, 0.65030059])
```

```
In [ ]:
```