

$$T(n) = \begin{cases} a & \text{if } n \leq 1 \\ 3T(\frac{n}{4}) + n & \end{cases}$$

LIV

INPUT

CONTRIBUTO RAMI

$$T(n) = 3T(\frac{n}{4}) + n \quad 0$$

$$T(\frac{n}{4}) = 3T(\frac{n}{4^2}) + \frac{n}{4} \quad 1$$

$$T(\frac{n}{4^2}) = 3T(\frac{n}{4^3}) + \frac{n}{4^2} \quad 2$$

$$T(\frac{n}{4^i}) = 3T(\frac{n}{4^{i+1}}) + \frac{n}{4^i} \quad i$$

$n$

$\frac{n}{4}$

$\frac{n}{4^2}$

$\frac{n}{4^i}$



$n$

$\frac{n}{4}$

$\frac{n}{4^2}$

$\frac{n}{4^i}$

TOTALE

$$T(\frac{n}{4^k})$$

$$0 \quad n \cdot 1 = n$$

$$1 \quad \frac{n}{4} \cdot 3 = n \frac{3}{4}$$

$$2 \quad \frac{n}{4^2} \cdot 3^2 = n \left(\frac{3}{4}\right)^2$$

$$i \quad \frac{n}{4^i} \cdot 3^i = n \left(\frac{3}{4}\right)^i$$

$$\frac{n}{4^k} = 1 \quad k = \log_4 n$$

~~RAMI~~

$$\sum_{i=0}^{k-1} n \frac{3^i}{4^i} = n \sum_{i=0}^{k-1} \left(\frac{3}{4}\right)^i = \frac{1}{1 - \frac{3}{4}} = 4n = \Theta(n)$$

$+ 3^k a$

FOGLIE

non so QUANTO VALE

$$4n + 3^{\log_4 n} = 4n + n \log_4 3 < 1 = \Theta(n)$$