MAT 167: STATISTICS

FINAL EXAM

Instructor: Anthony Tanbakuchi

Fall 2008

Name:	
	Computer / Seat Number:

No books, notes, or friends. **Show your work.** You may use the attached equation sheet, R, and a calculator. No other materials. If you choose to use R, write what you typed on the test. Using any other program or having any other documents open on the computer will constitute cheating.

You have until the end of class to finish the exam, manage your time wisely.

If something is unclear quietly come up and ask me.

If the question is legitimate I will inform the whole class.

Express all final answers to 3 significant digits. Probabilities should be given as a decimal number unless a percent is requested. Circle final answers, ambiguous or multiple answers will not be accepted. Show steps where appropriate.

The exam consists of 21 questions for a total of 71 points on 9 pages.

This Exam is being given under the guidelines of our institution's **Code of Academic Ethics**. You are expected to respect those guidelines.

Points Earned:	_ out of 71	total	points
Exam Score:			

- 1. The following is a partial list of statistical methods that we have discussed:
 - 1. mean
 - 2. median
 - 3. mode
 - 4. standard deviation
 - 5. z-score
 - 6. percentile
 - 7. coefficient of variation
 - 8. scatter plot
 - 9. histogram
 - 10. pareto chart
 - 11. box plot
 - 12. normal-quantile plot
 - 13. confidence interval for a mean

- 14. confidence interval for difference in means
- 15. confidence interval for a proportion
- 16. confidence interval for difference in proportions
- 17. one sample mean test
- 18. two independent sample mean test
- 19. one sample proportion test
- 20. two sample proportion test
- 21. test of homogeneity
- 22. test of independence
- 23. linear correlation coefficient & test
- 24. regression
- 25. 1-way ANOVA

For each situation below, which method is most applicable?

- If it's a hypothesis test, also state what the null and alternative hypothesis are.
- If it's a graphical method, also describe what you would be looking for.
- If it's a statistic, how susceptible to outliers is it?
- (a) (2 points) A student needs to conduct at t-test on a small set of data. Before conducting the test, the student needs determine if the data appears to have a normal distribution.
- (b) (2 points) A department of labor researcher wants to determine if there is a dependence between an individual's ethnicity and the type of industry they work in.
- (c) (2 points) A drug research would like to test the claim that the mean absorption of 1 gram of vitamin E is the same for four methods of delivery: topical, intravenous, oral, and nasal spray.

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- (d) (2 points) A researcher would like to estimate the proportion of people who are dyslexic.
- (e) (2 points) A fertility researcher wants to determine if a new drug can decrease the proportion of infertile mice. Twenty mice are randomly divided into two groups, a treatment group and a control group.

- 2. (1 point) The test of homogeneity can be thought of as a generalization of what two sample test?
- 3. (1 point) If the mean, median, and mode for a data set are all the same, what can you conclude about the data's distribution?
- 4. (2 points) Under what conditions can we approximate a binomial distribution as a normal distribution?
- 5. (1 point) What percent of data lies within three standard deviations of the mean as stated by the Empirical Rule?
- 6. (1 point) Why is it important to use random sampling?
- 7. For the following statements, determine if the calculation requires the use of a **population** distribution or a sampling distribution.
 - (a) (1 point) Computing a confidence interval for a mean.
 - (b) (1 point) Computing an interval that contain 95% of individual's weights.

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8. (1 point) If the normal approximation to the binomial is valid, write what the following binomial probability statement is approximately equal to in terms of the normal distribution.

$$P_{\rm binom}(x=8) \approx$$

- 9. (1 point) For the test of homogeneity, what is the distribution of the test statistic? (Give the specific name.)
- 10. (2 points) A hypothesis test was conducted for $H_0: p = 0.5$ and $H_a: p > 0.5$. The test statistic is z = 1.3. Find the p-value.

- 11. Provide **short succinct** written answers to the following conceptual questions.
 - (a) (1 point) Would temperature measured in Kelvin be classified as a nominal, ordinal, interval, or ratio level of measurement?
 - (b) (1 point) Which of the following measures of variation is most susceptible to outliers: standard deviation, inter-quartile range, range
 - (c) (1 point) What percent of data is greater than Q_2 ?
 - (d) (1 point) What does the standard deviation represent conceptually **in words**? (Be concise but don't simply state the equation in words verbatim.)
 - (e) (2 points) A histogram is a useful tool that can quickly communicate many traits about a set of data. List 4 useful pieces of information that an observer can easily assess using a histogram.
 - (f) (1 point) Why would a SAT percentile be preferred over a raw SAT score for college admissions committees?

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12. (2 points) When doing blood testing for HIV infections, the procedure can be made more efficient and less expensive by combining samples of blood specimens. If samples from five people are combined and the mixture tests negative, we know that all five individual samples are negative. Find the probability of a positive result for five samples combined into one mixture, assuming the probability of an individual blood sample testing positive is 10%. (Based on data from the NY State Health Department)

13. (2 points) You would like to conduct a study to estimate (at the 95% confidence level) the proportion of households that own one or more encyclopedias. What sample size do you need to estimate the proportion with a margin of error of 2%.

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- 14. (2 points) If a class consists of 20 males and 8 females, what is the probability of drawing 4 females without replacement?
- 15. The following questions regard hypothesis testing in general.
 - (a) (1 point) When we conduct a hypothesis test, we assume something is true and calculate the probability of observing the sample data under this assumption. What do we assume is true?
 - (b) (1 point) If you reject H_0 but H_0 is true, what type of error has occurred? (Type I or Type II)
 - (c) (1 point) What variable represents the actual Type I error?
 - (d) (1 point) What does the power of a hypothesis test represent?

16. Eighteen students were randomly selected to take the SAT after having either no breakfast or a complete breakfast A researcher would like to test the claim that students who eat breakfast score higher than students who do not.

Group without breakfast: SAT Score 480 510 530 540 550 560 600 620 660 Group with breakfast: SAT Score 460 500 520 580 580 690 530 560 640

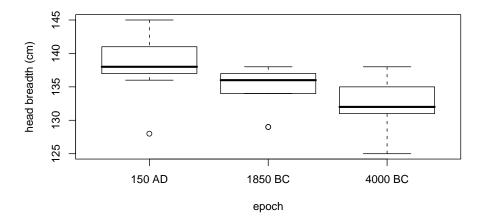
- (a) (1 point) What type of hypothesis test will you use?
- (b) (2 points) What are the test's requirements?
- (c) (2 points) What are the hypothesis H_0 and H_a ?
- (d) (1 point) What α will you use?

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Points earned: _____ / 12 points

- (e) (2 points) Conduct the hypothesis test. What is the p-value?
- (f) (1 point) What is your formal decision?
- (g) (2 points) State your final conclusion in words.
- 17. Samples of head breadths were obtained by measuring skulls of Egyptian males from three different epochs, and the measurements are listed below (based on data from Ancient Races of the Tebaid, by Thomas and Randall-Maciver). Changes in head shape over time suggest that interbreeding occurred with immigrant populations. Test the claim that the different epochs do not all have the same mean head breadth.

A box plot of the data is shown below.



- (a) (1 point) What type of hypothesis test (of those discussed in class) should you use?
- (b) (1 point) What is the alternative hypothesis for this test?
- (c) (1 point) What alpha will you use?
- (d) (1 point) What is the response variable for this study?

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- (e) (1 point) What is the factor variable for this study?
- (f) (1 point) The analysis of the data was run and the output is shown below: What is your

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
epoch	2	138.74	69.37	4.05	0.0305
Residuals	24	411.11	17.13		

final conclusion (not the formal decision)?

- (g) (1 point) Assuming the researcher rejected the null hypothesis, what is the probability of a Type I error for this study?
- 18. The following table lists midterm and final exam grades for eight statistics students.

midterm	75.00	49.00	95.00	82.00	83.00	43.00	95.00	98.00
final	44.00	35.00	82.00	89.00	73.00	43.00	85.00	71.00

- (a) (2 points) Upon looking at the scatter plot of the data, the relationship of midterm score and final exam score appears linear. Is the linear relationship statistically significant? (Justify your answer by conducting an analysis, state the p-value and the conclusion.)
- (b) (1 point) What percent of a student's final exam score can be explained by their midterm score?
- (c) (2 points) You want to model a student's final exam score as linearly related to their midterm grade. Write the equation for fitted model (with the actual values of the coefficients). (Assume the linear correlation is significant.)

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- (d) (1 point) What range of midterm scores is the model valid for making predictions about final exam scores?
- (e) (1 point) What is the best predicted final exam score for a student who gets a 75 on the midterm? (Assume the linear correlation is significant.)
- (f) (1 point) If the liner relationship had not been statistically significant, what is the best predicted final exam score for a student who gets a 75 on the midterm?
- 19. (2 points) A researcher is trying to determine the ideal temperature to brew coffee. A random sample of 8 of the top 100 coffee shops in New York city had their brewer temperatures (in Celsius) measured. The data is shown below.

Construct a 90% confidence interval for the true population mean temperature using the above data. (Assume σ is unknown.)

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20. (2 points) A ski resort is designing a new super tram to carry 40 people. If the mean weight of humans is approximately 165 lbs with a standard deviation of 25 lbs, what should the tram's maximum weight limit be so that it can carry the desired capacity 95% of the time?

21. (2 points) Given $y = \{a, -2a, 4a\}$, completely simplify the following expression. Assume a is an unknown constant. $\left(\sum (y_i - 2a)\right)^2$

End of exam. Reference sheets follow.

Statistics Quick Reference	e	2.3 VISUAL All plots have optional arguments:		5 Continuous random variables CDF F(x) gives area to the left of x, F ⁻¹ (y) expe	oto	6 Sampling distributions	
Card & R Commands by Anthony Tanbakuchi, Version 1.8.2		main="" sets title		is area to the left.	cts p	$\mu_{\bar{x}} = \mu$ $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{\sigma}}$ (57)	,
http://www.tanbakuchi.com		• xlab="", ylab="" sets x/y-axis label		f(x): probability density	(34)	V ⁿ	
ANTHONY@TANBAKUCHI-COM		 type="p" for point plot type="1" for line plot 				$\mu_{\hat{p}} = p$ $\sigma_{\hat{p}} = \sqrt{\frac{pq}{\pi}}$ (58)	
Get R at: http://www.r-project.org R commands: bold typewriter text		type="b" for both points and lines		$E = \mu = \int_{-\infty}^{\infty} x \cdot f(x) dx$	(35)	y n	
==		Ex:plot(x, y, type="b", main="My Plot")		$\sigma = \sqrt{\int_{-\infty}^{\infty} (x - \mu)^2 \cdot f(x) dx}$		7 Estimation	
1 Misc R		Plot Types: hist(x) histogram		$G = \sqrt{\int_{-\infty}^{\infty} (x - \mu)^2 \cdot f(x) dx}$	(36)	7.1 CONFIDENCE INTERVALS	
To make a vector / store data: x=c(x1, x2, Help: general RSiteSearch ("Search Phrase		stem(x) stem & leaf		F(x): cumulative prob. density (CDF)	(37)	proportion: $\hat{p} \pm E$, $E = z_{\alpha/2} \cdot \sigma_{\hat{n}}$ (59)	
Help: function ?functionName	- /	boxplot(x) box plot		$F^{-1}(x)$: inv. cumulative prob. density	(38)	mean (σ known): $\bar{x}\pm E$, $E = z_{\alpha/2} \cdot \sigma_{\bar{x}}$ (60)	
Get column of data from table:		<pre>plot(T) bar plot, T=table(x) plot(x,y) scatter plot, x, y are ordered vectors</pre>		$F(x) = \int_{-x}^{x} f(x') dx'$	(39)		
tableName\$columnName List all variables: 1s()		plot (t,y) time series plot, t, y are ordered vectors	tors	J-m		mean (σ unknown, use s): $\bar{x} \pm E$, $E = t_{\alpha/2} \cdot \sigma_{\bar{x}}$, (61)	
Delete all variables: rm(list=ls())		curve(expr, xmin,xmax) plot expr involving	g x	p = P(x < x') = F(x')	(40)	df = n - 1	
		2.4 Assessment Nonversion		$x' = F^{-1}(p)$	(41)	variance: $\frac{(n-1)s^2}{s^2} < \sigma^2 < \frac{(n-1)s^2}{s^2}$, (62)	,
$\sqrt{x} = \mathbf{sqrt}(\mathbf{x})$	(1)	2.4 ASSESSING NORMALITY Q-Q plot: qqnorm(x); qqline(x)		p = P(x > a) = 1 - F(a)	(42)	AR AL.	
$x^n = \mathbf{x}^{\wedge} \mathbf{n}$	(2)	Q-Q piot: qqnorm(x); qqiine(x)		p = P(a < x < b) = F(b) - F(a)	(43)	df = n - 1	
n = length(x)	(3)	3 Probability		E.I. Harmony promprayment		2 proportions: $\Delta \hat{p} \pm z_{\alpha/2} \cdot \sqrt{\frac{\hat{p}_1 \hat{q}_1}{n_1} + \frac{\hat{p}_2 \hat{q}_2}{n_2}}$ (63)	,
$T = \mathtt{table}(\mathbf{x})$	(4)	Number of successes x with n possible outcomes.		5.1 Uniform distribution		1 11 12	
2 Descriptive Statistics		(Don't double count!)		p = P(u < u') = F(u')		2 means (indep): $\Delta \bar{x} \pm t_{\alpha/2} \cdot \sqrt{\frac{s_1^2}{m} + \frac{s_2^2}{m}}$, (64)	,
2.1 NUMERICAL		$P(A) = \frac{x_A}{}$	(17)	= punif(u', min=0, max=1)	(44)	V #1 #2	
Let x=c (x1, x2, x3,)		n n	` ' '	$u' = F^{-1}(p) = qunif(p, min=0, max=1)$	(45)	$df \approx \min(n_1 - 1, n_2 - 1)$	
			(18)			matched pairs: $\tilde{d} \pm t_{\alpha/2} \cdot \frac{s_d}{\sqrt{n}}$, $d_i = x_i - y_i$, (65)	
$total = \sum_{i=1} x_i = sum(x)$	(5)		(19)	5.2 NORMAL DISTRIBUTION		df = n - 1	
min = min(x)	(6)	(, , (, , , , , , , , , , , , , , , ,	(20)	$f(x) = \frac{1}{\sqrt{2-a^2}} \cdot e^{-\frac{1}{2} \cdot \frac{(x-\mu)^2}{a^2}}$	(46)	uj = n - 1	
max = max(x)	(7)	$P(A \text{ and } B) = P(A) \cdot P(B A)$ $P(A \text{ and } B) = P(A) \cdot P(B)$ if $A \cdot B$ independent		V 200°		7.2 CI CRITICAL VALUES (TWO SIDED)	
six number summary : summary (x)	(8)	$r(A \text{ and } B) = r(A) \cdot r(B)$ if A, B independent $n! = n(n-1) \cdots 1 = \text{factorial (n)}$	` '	p = P(z < z') = F(z') = pnorm(z')	(47)	$z_{\alpha/2} = F_r^{-1}(1 - \alpha/2) = \text{qnorm}(1-\text{alpha/2})$ (66)	
$\mu = \frac{\sum x_i}{\sum x_i} = \text{mean}(\mathbf{x})$	(9)			$z' = F^{-1}(p) = qnorm(p)$	(48)	$t_{\alpha/2} = F_i^{-1}(1 - \alpha/2) = \text{qt}(1-\text{alpha/2}, df)$ (67)	
. N	(9)	$_{n}P_{k} = \frac{n!}{(n-k)!}$ Perm. no elem. alike	(24)	p = P(x < x') = F(x')			
$\bar{x} = \frac{\sum x_i}{\sum x_i} = \text{mean}(\mathbf{x})$	(10)	n!		$=$ pnorm(x' , mean= μ , sd= σ)	(49)	$\chi_L^2 = F_{\chi^2}^{-1}(\alpha/2) = \text{qchisq(alpha/2, df)}$ (68)	
$\bar{x} = P_{00} = \text{median}(\mathbf{x})$	(11)	$= \frac{n!}{n_1! n_2! \cdots n_k!} \text{ Perm. } n_1 \text{ alike, } \dots $	(25)	$x' = F^{-1}(p)$		$\chi_R^2 = F_{y^2}^{-1}(1 - \alpha/2) = \text{qchisq(1-alpha/2, df)}$)
	(11)	${}_{n}C_{k} = \frac{n!}{(n-k)!k!} = \text{choose}(n,k)$	(26)	= qnorm(p, mean=μ, sd=σ)	(50)	(69)	
$\sigma = \sqrt{\frac{\sum (x_i - \mu)^2}{N}}$	(12)	4 Discrete Random Variables		5.3 t-distribution		7.3 REQUIRED SAMPLE SIZE	
$s = \sqrt{\frac{\sum (x_i - \vec{x})^2}{n-1}} = \operatorname{sd}(\mathbf{x})$		4 Discrete Random variables		p = P(t < t') = F(t') = pt(t', df)	(51)	proportion: $n = \hat{p}\hat{q}\left(\frac{z_{\alpha/2}}{r}\right)^2$, (70)	
$s = \sqrt{\frac{1}{n-1}} = sd(x)$	(13)	$P(x_i)$: probability distribution	(27)	$t' = F^{-1}(p) = qt(p, df)$	(52)	(E /	
$CV = \frac{\sigma}{u} = \frac{s}{\overline{v}}$	(14)	$E = \mu = \sum x_i \cdot P(x_i)$	(28)	**		$(\hat{p} = \hat{q} = 0.5 \text{ if unknown})$	
$\mu = \bar{x}$	` '	$\sigma = \sqrt{\sum (x_i - \mu)^2 \cdot P(x_i)}$	(29)	5.4 χ ² -distribution		mean: $n = \left(\frac{z_{\alpha/2} \cdot \hat{\sigma}}{E}\right)^2$ (71)	,
2.2 RELATIVE STANDING		12,		$p = P(\gamma^2 < \gamma^{2'}) = F(\gamma^{2'})$		(E)	
$z = \frac{x - \mu}{\sigma} = \frac{x - \bar{x}}{z}$	(15)	4.1 BINOMIAL DISTRIBUTION		= pchisq(X ² ', df)	(53)		
Percentiles:		$u = n \cdot n$	(30)				
$P_k = x_i$, (sorted x)			(31)	$\chi^{2'} = F^{-1}(p) = \operatorname{qchisq}(p, df)$	(54)		
$k = \frac{i - 0.5}{\cdot 100\%}$	(16)			5.5 F-DISTRIBUTION			
n	(10)	$P(x) = {}_{n}C_{x}p^{x}q^{(n-x)} = dbinom(x, n, p)$	(32)				
To find x_i given P_k , i is: 1. $L = (k/100\%)n$		4.2 POISSON DISTRIBUTION		p = P(F < F') = F(F')			
 if L is an integer: i = L+0.5; 		,x ,-p		= pf(F', df1, df2)	(55)		
otherwise i=L and round up.		$I'(x) = \frac{1}{x!} = \text{dpois}(\mathbf{x}, \mu)$	(33)	$F' = F^{-1}(p) = qf(p, df1, df2)$	(56)		

8 Hypothesis Tests

Test statistic and R function (when available) are listed for each. Optional arguments for hypothesis tests: alternative="two_sided" can be: "two.sided". "less". "greater"

conf.level=0.95 constructs a 95% confidence interval. Standard CI only when alternative="two.sided". Optional arguments for power calculations & Type II error:

alternative="two.sided" can be: "two sided" or "one sided"

sig.level=0.05 sets the significance level α.

8.1. 1-SAMPLE PROPORTION

prop.test(x, n, p=p0, alternative="two.sided")

$$z = \frac{\hat{p} - p_0}{\sqrt{p_0 q_0/n}}$$

8.2 1-SAMPLE MEAN (σ KNOWN) $H_0: u = u_0$

$$z = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$$
(73)

8.3 1-SAMPLE MEAN (σ UNKNOWN)

 $H_0 : \mu = \mu_0$ t.test(x, mu=u0, alternative="two.sided") Where x is a vector of sample data.

$$t = \frac{\bar{x} - \mu_0}{\sqrt{g}}, df = n - 1$$

$$= n - 1$$

Required Sample size: power.t.test(delta=h, sd =G, sig.level=0, power=1 β, type ="one.sample", alternative="two.sided")

8.4 2-SAMPLE PROPORTION TEST

 $H_0: p_1 = p_2$ or equivalently $H_0: \Delta p = 0$ prop.test(x, n, alternative="two.sided") where: $\mathbf{x} = \mathbf{c}(x_1, x_2)$ and $\mathbf{n} = \mathbf{c}(n_1, n_2)$

 $z = \frac{\Delta \hat{p} - \Delta p_0}{\sqrt{\hat{p}_1^2 + \hat{p}_2^2}}, \quad \Delta \hat{p} = \hat{p}_1 - \hat{p}_2$

$$\sqrt{\frac{\hat{p}\hat{q}}{n_1} + \frac{\hat{p}\hat{q}}{n_2}}$$

$$\bar{p} = \frac{x_1 + x_2}{x_1 + x_2}, \quad \bar{q} = 1 - \bar{p}$$
(7)

$$\bar{p} = \frac{n_1 + n_2}{n_1 + n_2}, \quad \bar{q} = 1 - \bar{p}$$
 (7

Required Sample size power.prop.test(p1= p_1 , p2= p_2 , power= $1-\beta$, sig.level=q, alternative="two.sided")

8.5 2-SAMPLE MEAN TEST

 $H_0: \mu_1 = \mu_2$ or equivalently $H_0: \Delta \mu = 0$

t.test(x1, x2, alternative="two.sided") where: x1 and x2 are vectors of sample 1 and sample 2 data.

$$t = \frac{\Delta \bar{x} - \Delta \mu_0}{\sqrt{\frac{r_1^2}{n_1^2} + \frac{r_2^2}{n_2^2}}} df \approx \min(n_1 - 1, n_2 - 1), \quad \Delta \bar{x} = \bar{x}_1 - \bar{x}_2$$
 (77)

Required Sample size:

power.t.test(delta=h, sd =0, sig.level=0, power=1 β, type ="two.sample", alternative="two.sided")

8.6 2-SAMPLE MATCHED PAIRS TEST $H_0: u_i = 0$

t.test(x, v, paired=TRUE, alternative="two.sided")

where: x and y are ordered vectors of sample 1 and sample 2 data. $t = \frac{\tilde{d} - \mu_{d0}}{\pi_i / . / \tilde{n}}, d_i = x_i - y_i, df = n - 1$

$$i - \frac{1}{s_d/\sqrt{n}}$$
, $u_i - \lambda_i - y_i$, $u_j - n - 1$
Required Sample size:

power.t.test(delta=h, sd =G, siq.level=a, power=1 β, type ="paired", alternative="two.sided")

8.7 Test of homogeneity, test of independence

 $H_0: p_1 = p_2 = \cdots = p_n$ (homogeneity) $H_0: X$ and Y are independent (independence)

chisg.test(D)

Enter table: D=data.frame(c1, c2, ...), where c1, c2, ... are

column data vectors Or generate table: D=table (x1, x2), where x1, x2 are ordered vectors of raw categorical data

$$\chi^2 = \sum \frac{(O_i - E_i)^2}{E_i}$$
, $df = (\text{num rows - 1})(\text{num cols - 1})$ (79)

$$E_i = \frac{\text{(row total)(column total)}}{\text{(erand total)}} = np_i$$
(column total)

(must specify alternative as greater)

9 Linear Regression (74) 9.1 LINEAR CORRELATION

 $H_0: \rho = 0$

cor.test(x, y) where: x and v are ordered vectors.

$$r = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{(n-1)x_x x_y}, \quad t = \frac{r-0}{\sqrt{\frac{1-r^2}{n-2}}}, \quad df = n-2$$
 (81)

9.2 MODELS IN R MODEL TYPE | FOUNTION

linear 1 indep var	$y = b_0 + b_1x_1$	y~x1
0 intercept	$y = 0 + b_1x_1$	y~0+x1
linear 2 indep vars	$y = b_0 + b_1x_1 + b_2x_2$	y~x1+x2
	$y = b_0 + b_1x_1 + b_2x_2 + b_{12}x_1x_2$	y~x1+x2+x1*x2
polynomial	$y = b_0 + b_1x_1 + b_2x_2^2$	y~x1+I(x2 [^] 2)

R MODEL

(83)

(84)

polynomial 9.3 REGRESSION Simple linear regression steps:

- 1. Make sure there is a significant linear correlation
- results=lm(v~x) Linear regression of v on x vectors 3. results View the results
- plot(x, v): abline(results) Plot regression line on data
- 5. plot(x, results\$residuals) Plot residuals

$$y = b_0 + b_1x_1$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2}$$

To predict v when x = 5 and show the 95% prediction interval with regression model in results:

predict (results, newdata=data.frame (x=5), int="pred")

10 ANOVA 10.1 ONE WAY A NOVA

results=aov(depVarColName~indepVarColName,

9.4 PREDICTION INTERVALS

data=tableName) Run ANOVA with data in TableName, factor data in indepVarColName column, and response data in depVarColName column. 2. summary (results) Summarize results

boxplot (depVarColName~indepVarColName, data=tableName) Boxplot of levels for factor

$$F = \frac{MS(\text{treatment})}{MS(\text{error})}, \quad df_1 = k-1, \ df_2 = N-k \tag{85}$$
 To find required sample size and power see power.anova.test(...)

11 Loading and using external data and tables 11.1 LOADING EXCEL DATA

- 1. Export your table as a CSV file (comma seperated file) from Excel.
 - 2. Import your table into MyTable in R using:
 - MvTable=read.csv(file.choose())
- 11.2 LOADING AN RDATA FILE You can either double click on the .RData file or use the menu:
 - Windows: File→Load Worksnace
- Mac: Workspace → Load Workspace File...
- 11.3 HISING TABLES OF DATA
 - 1. To see all the available variables type: 1s () 2. To see what's inside a variable, type its name.
 - 3. If the variable tableName is a table, you can also type
 - names (tableName) to see the column names or type head (tableName) to see the first few rows of data. 4. To access a column of data type tableName\$columnName
- An example demonstrating how to get the women's height data and find the
- mean:

> ls() # See what variables are defined []] "women" "x"

> head(women) #Look at the first few entries

height weight 5.8

- 5.0
- > names(women) # Just get the column names [1] "height" "weight"
- > women\$height # Display the height data
- [1] 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72
- > mean(women\$height) # Find the mean of the heights f11 65