MAT 167: STATISTICS

# FINAL EXAM

Instructor: Anthony Tanbakuchi

Fall 2007

Name:		
	Computer / Seat Number:	

Multiple choice part: fill in answer on the scan form. Do not attach work for this section (no partial credit is awarded).

Written part: Write all final answers on the exam. Actual work should be attached so partial credit can be given.

No books, notes, or friends. You may use the attached equation sheet, R, and a calculator. No other materials. If you choose to use R, copy and paste your work into a word document labeling the question number it corresponds to. When you are done with the test print out the document. Be sure to save often on a memory stick just in case. Using any other program or having any other documents open on the computer will constitute cheating.

You have until the end of class to finish the exam, manage your time wisely.

If something is unclear quietly come up and ask me.

If the question is legitimate I will inform the whole class.

Express all final answers to 3 significant digits. Probabilities should be given as a decimal number unless a percent is requested. Circle final answers, ambiguous or multiple answers will not be accepted. Show steps where appropriate.

The exam consists of 9 questions for a total of 36 points on 13 pages.

This Exam is being given under the guidelines of our institution's **Code of Academic Ethics**. You are expected to respect those guidelines.

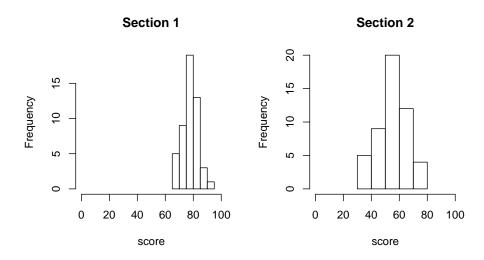
Points Earned:	_ out of 36	total	points
Exam Score:			

a statistics class.

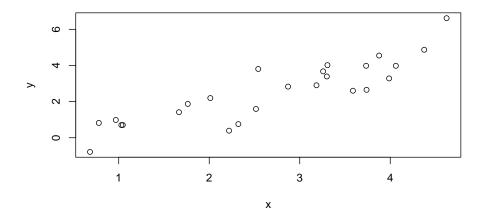
1. Given the following data from a random sample: 21 11 21 14 20 26 17 220 (a) (1 point) Find the mean of the data. (b) (1 point) Find the median of the data. (c) (1 point) Since the mean and the median are not equal, what does this indicate about the data? (d) (1 point) Which measure of center (mean or median) do you think is better for describing this data and why? (e) (1 point) Find the standard deviation of the data. 2. In regards to  $\bar{x}$  and the Central Limit Theorem: (a) (1 point) What are the two conditions under which the CLT applies? (b) (1 point) If the conditions are met, what does the CLT state about  $\bar{x}$ ?

Points earned: \_\_\_\_\_ / 7 points Instructor: Anthony Tanbakuchi

3. The following are histograms of student scores on the same exam for two different sections of



- (a) (1 point) Which section had a higher mean score?
- (b) (1 point) Which section had a larger standard deviation?
- 4. The following questions regard hypothesis testing in general.
  - (a) (1 point) When we conduct a hypothesis test, we assume something is true and calculate the probability of observing the sample data under this assumption. What do we assume is true?
  - (b) (1 point) If you are using a hypothesis test to make a decision where the effect of a Type I error may negatively effect human lives, should you increase or decrease the significance level  $\alpha$  used in making the decision?
  - (c) (1 point) The 1-Way ANOVA is a many sample generalization of what two sample test?
- 5. Use the following plot of paired x-y data and the computer analysis output for the following questions, assume that the linear correlation coefficient is statistically significant.



```
> mean(x)
[1] 2.697902
> mean(y)
[1] 2.552376
> results = lm(y ~ x)
> results
Call:
lm(formula = y ~ x)

Coefficients:
(Intercept) x
-0.82 1.25
```

- (a) (1 point) Which linear correlation coefficient below best matches the plot?  $10,\,1,\,0.9,\,0.09,\,0,\,-0.09,\,-0.9,\,-1,\,-10$
- (b) (1 point) Based on your above answer, what percent of variation in y is explained by x?
- (c) (1 point) What is the linear equation that models the data?
- (d) (1 point) Using your previous answers, what is your best point estimate for y if x = 4?

- 6. You are a crime scene investigator trying to match the lead content of bullet fragments found at a crime scene to the lead content of a box of bullets found with a suspect. To simplify this question, assume that the instrument you use gives you one measurement per fragment in grams/cm<sup>3</sup>. Assume that you have 5 measurements from fragments found at the crime scene and 7 measurements from bullets found with the suspect.
  - (a) (1 point) What type of hypothesis test will you use?
  - (b) (1 point) What are  $H_0$  and  $H_a$ ? Write them both mathematically and in words.

- (c) (1 point) You run the analysis and the *p*-value is 0.0001 and  $\alpha = 0.001$ , and  $\beta = 0.9$ . If you **reject**  $H_0$ , what is the probability that you made the wrong decision in this case?
- (d) (1 point) You run the analysis and the *p*-value is 0.9,  $\alpha = 0.001$  and  $\beta = 0.01$ . If you **fail** to reject  $H_0$ , What is the probability that you made the wrong decision in this case?
- (e) (1 point) Under what conditions could an expert witness give the following statement based solely on lead bullet statistical evidence:

"The bullet fragments must have come from the same box or from another box that would have been made by the same company on the same day."

7. The clothing manufacturer's association (CMA) publishes data that manufacture's use to determine what sizes of clothing they should make. As mentioned before, the CMA states that men's waists are normally distributed with  $\mu=35$  in and  $\sigma=2.3$  in. You believe that the mean waist size of men is actually larger than 35.

Instructor: Anthony Tanbakuchi Points earned: \_\_\_\_\_ / 5 points

(a) (1 point) You would like to conduct a study to estimate (at the 90% confidence level) the mean waist size of men with a margin of error of 1 in. Assuming that the standard deviation of waist sizes is  $\sigma = 2.3$  in, what sample size should you use for this study?

(b) (1 point) A study was conducted (and they ignored your recommendation of sample size!) of 5 randomly selected men and the following waist sizes were measured:

 $37.3\ 43.5\ 36.3\ 34\ 35.4$ 

Construct a 90% confidence interval for the true population mean waist size using the above data. (Assume  $\sigma$  is unknown.)

- (c) (1 point) Can you reject the claim that the mean waist size of men is 35 in based on the confidence interval that you constructed above?
- 8. A group supporting Hillary Clinton who sees Mitt Romney as her strongest republican competitor makes the statement that "Hillary has more support in the democratic party than Mitt Romney has in the republican party". After a little investigating you find out the political group did a random survey of 500 democratic voters and found 170 supported Hillary. They conducted a second survey of 420 republican voters and found 135 supported Romney. Does this data support the claim that the proportion of democrats who support Hillary is greater than the proportion of republicans who support Romney?

Instructor: Anthony Tanbakuchi Points earned: \_\_\_\_\_ / 3 points

<sup>&</sup>lt;sup>1</sup>The sample data in this problem is fictitious and is not an endearment of any candidate.

- (a) (1 point) What type of hypothesis test will you use?
- (b) (1 point) What are the test's requirements?
- (c) (1 point) Are the requirements satisfied? State how they are satisfied.
- (d) (1 point) What are the hypothesis  $H_0$  and  $H_a$ ?
- (e) (1 point) What  $\alpha$  will you use?
- (f) (1 point) Conduct the hypothesis test. What is the p-value?
- (g) (1 point) What is your formal decision?
- (h) (1 point) State your final conclusion in words.

- (i) (1 point) Assume that you failed to reject  $H_0$ . Hillary's political party truly believes that they do have more support. If they were to re-run the study, what should they change to increase their chances of being able to statistically support their claim?
- 9. Chest deceleration data are given below. A researcher wants to test the claim that vehicle size has an effect on the mean chest deceleration at the 0.05 significance level.

vehicle size chest deceleration (g)

Subcompact: 55, 47, 59, 49, 42

Compact: 57, 57, 46, 54, 51

Midsize: 45, 53, 49, 51, 46

Full-size: 44, 45, 39, 58, 44

- (a) (1 point) What type of hypothesis test (of those discussed in class) should you use?
- (b) (1 point) What is the null hypothesis for this test?
- (c) (1 point) If you analyze the data and your p-value is 0.2, what would your conclusion be?

Instructor: Anthony Tanbakuchi Points earned: \_\_\_\_\_ / 4 points

2) \_\_\_

3) \_\_\_\_

Fill in answers on the scan form for this part of the test.

MULTIPLE CHOICE	Choose the one alternative that best com	pletes the statement or answers the o	mestion

Determine whether the given value is a statistic or a parameter.	
1) A health and fitness club surveys 40 randomly selected members and found that the average	1)
weight of those questioned is 157 lb.	

A) Parameter B) Statistic

# Identify which of these types of sampling is used: random, stratified, systematic, cluster, convenience.

- The name of each contestant is written on a separate card, the cards are placed in a bag, and three names are picked from the bag.
  - A) Systematic
  - B) Convenience
  - C) Random
  - D) Cluster
  - E) Stratified

# Construct the cumulative frequency distribution that corresponds to the given frequency distribution.

3)

Height (inches) Frequency
69.0 - 71.9 17
72.0 - 74.9 21
75.0 - 77.9 21
78.0 - 80.9 18

81.0 - 83.9

A)

Height	Cumulative
(inches)	Frequency
69.0 - 71.9	38
72.0 - 74.9	59
75.0 - 77.9	77
78.0 - 80.9	80
81.0 - 83.9	83

3

C)

Height	Cumulative
(inches)	Frequency
69.0 - 71.9	17
72.0 - 74.9	38
75.0 - 77.9	59
78.0 - 80.9	75
81.0 - 83.9	80

B)

Height	Cumulative
(inches)	Frequency
69.0 - 71.9	0.212
72.0 - 74.9	0.263
75.0 - 77.9	0.263
78.0 - 80.9	0.225
81.0 - 83.9	0.037

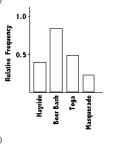
D)

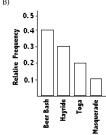
Height	Cumulative
(inches)	Frequency
69.0 - 71.9	17
72.0 - 74.9	38
75.0 - 77.9	59
78.0 - 80.9	77
81.0 - 83.9	80

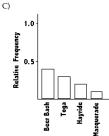
## Solve the problem.

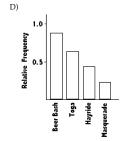
4) The Kappa Iota Sigma Fraternity polled its members on the weekend party theme. The vote was 4) as follows: six for toga, four for hayride, eight for beer bash, and two for masquerade. Display

the vote count in a Pareto chart. A) B)









Find the z-score corresponding to the given value and use the z-score to determine whether the value is unusual. Consider a score to be unusual if its z-score is less than -2.00 or greater than 2.00. Round the z-score to the nearest tenth if necessary.

- 5) A time for the 100 meter sprint of 13.7 seconds at a school where the mean time for the 100 meter sprint is 17.5 seconds and the standard deviation is 2.1 seconds.

  - A) -3.8; unusual

B) -1.8; not unusual

C) -1.8; unusual

D) 1.8: not unusual

Find the mode(s) for the given sample data.

- 6) 20, 27, 46, 27, 49, 27, 49 A) 46
- B) 27

- C) 35
- D) 49

5)

Provide a written description of the complement of the given event.

- 7) When 100 engines are shipped, none of them are defective.
  - A) All of the engines are defective.
  - B) At least one of the engines is defective.
  - C) None of the engines are defective.

Find the indicated probability.
8) A study conducted at
d · 1 c · 1 · · d

8) A study conducted a	t a certain college shows	s that 65% of the school's	graduates find a job in
their chosen field wit	hin a year after graduat	ion. Find the probability	that among 5 randomly
selected graduates, a	t least one finds a job in	his or her chosen field wi	ithin a year of graduating.
A) 0.650	B) 0.995	C) 0.200	D) 0.884

lomly luating.

9) The table below shows the soft drinks preferences of people in three age groups.

9)		
	9)	

10)

11)

12)

13)

14) \_\_\_\_

8) \_\_\_\_

	cola	root beer	lemon-lime
under 21 years of age	40	25	20
under 21 years of age between 21 and 40	35	20	30
over 40 years of age	20	30	35

If one of the 255 subjects is randomly selected, find the probability that the person is over 40 years of age given that they drink root beer.

A) 
$$\frac{6}{17}$$

B) 
$$\frac{2}{5}$$

C) 
$$\frac{5}{17}$$

D) None of the above is correct.

10) A sample of 4 different calculators is randomly selected from a group containing 48 that are defective and 23 that have no defects. What is the probability that all four of the calculators selected are defective?

A) 0.2089

C) 0.0527

D) 0.2003

Find the standard deviation,  $\sigma$ , for the binomial distribution which has the stated values of n and p. Round your answer to the nearest hundredth.

B) 
$$\sigma = 20.84$$

C) 
$$\sigma = 23.25$$

D)  $\sigma = 27.37$ 

Find the indicated probability.

12) The incomes of trainees at a local mill are normally distributed with a mean of \$1100 and a standard deviation \$150. What percentage of trainees earn less than \$900 a month?

A) 9.18%

C) 90.82%

D) 40.82%

Solve the problem.

13) A bank's loan officer rates applicants for credit. The ratings are normally distributed with a mean of 200 and a standard deviation of 50. If 40 different applicants are randomly selected, find the probability that their mean is above 215.

A) 0.1179

B) 0.3821

C) 0.0287

D) 0.4713

Find the indicated probability.

14) Based on meteorological records, the probability that it will snow in a certain town on January 1st is 0.269. Find the probability that in a given year it will not snow on January 1st in that town.

A) 1.269

B) 0.731

C) 0.368

D) 3.717

,	elow describes	ccasional I		Heavy			15)
l <sub>1</sub>	Nonsmoker		smoker s	_	Total		
Men	356	42	70	44	512		
Women	315	50	66	45	476		
Total	671	92	136	89	988		
If one of th	ie 988 people is	randomly s	elected, fir	nd the pi	obability t	hat the person is a man or a	
heavy smo				-		•	
A) 0.56	4	B) 0.519		C)	0.494	D) 0.608	
Determine whether	the given proce	dure result	s in a bino	mial di	stribution.	If not, state the reason why.	
16) Rolling a s	ingle "loaded" o	lie 40 times,	keeping t	rack of t	he number	s that are rolled.	16)
A) Not	binomial: the tr	ials are not	independe	ent.			
B) Not	binomial: there	are more th	an two ou	tcomes	or each tri	al.	
C) Proc	edure results in	a binomial	distribution	on.			
D) Not	binomial: there	are too mar	ny trials.				
ormulate the indica	ited conclusion	in nontech	nical term	s. Be su	re to addre	ss the original claim.	
17) A psycholo	ogist claims that	t more than	47 percen	t of the p	opulation	suffers from professional	17)
problems of	due to extreme s	shyness. Ass	suming tha	at a hypo	othesis test	of the claim has been	
conducted	and that the co	nclusion is f	ailure to r	eject the	null hypot	thesis, state the conclusion in	
nontechnic	cal terms.						
	re is not sufficie ercent.	nt evidence	to suppor	t the clai	m that the	true proportion is less than	
B) There		vidence to s	upport the	claim t	nat the true	e proportion is less than 47	
	re is not sufficie 47 percent.	nt evidence	to suppor	t the clai	m that the	true proportion is greater	
D) The	re is sufficient e	vidence to s	upport the	claim t	nat the true	proportion is greater than 47	
perc	ent.						
ssume that a hypot	thesis test of the	e given clai	m will be	conduct	ed. Identif	y the type I or type II error for	the test.
18) A research	er claims that th	ne amounts	of acetami	nophen	in a certair	n brand of cold tablets have a	18)
standard d	leviation differe	nt from the	$\sigma = 3.3 \text{ mg}$	g claime	d by the m	anufacturer. Identify the type	
II error for	the test.						
	error of failing ally different fro		claim that	the stan	dard devi	ation is 3.3 mg when it is	
B) The		g the claim	that the st	andard o	leviation is	s more than 3.3 mg when it	
			that the st	andard o	leviation is	3.3 mg when it really is 3.3	

### Introductory Statistics Quick Reference & R Commands

by Anthony Tanbakuchi. Version 1.1 ANTHONY @TANKA KUCHLCOM

Get R at: http://www.r-project.org More R help & examples at:

http://tanbakuchi.com/Resources/R\_Statistics/RBasics.html R commands: bold text

# 1 Misc R

To make a vector / store data: x=c (x1, x2, ...) Get help on function: ?functionName

Get column of data from table: tableNameScolumnName List all variables: 1s()

Delete all variables: rm(list=ls())

# 2 Descriptive Statistics

### 2.1 NUMERICAL

Let x=c (x1, x2, x3, ...)

total = 
$$\sum_{i=1}^{n} x_i = sum(\mathbf{x})$$
 (5)  
min = min( $\mathbf{x}$ ) (6)  
max = max( $\mathbf{x}$ ) (7)  
mmary: summary( $\mathbf{x}$ ) (8)

six number summary : summary (x)  $\mu = \frac{\sum x_i}{\sum x_i} = \text{mean}(\mathbf{x})$ 

$$\bar{x} = \frac{\sum x_i}{n} = \text{mean}(\mathbf{x})$$
 (10)  
 $\bar{x} = P_{50} = \text{median}(\mathbf{x})$  (11)

(9)

(12)

$$\sigma = \sqrt{\frac{\sum (x_i - \mu)^2}{N}}$$

$$s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n - 1}} = \operatorname{sd}(\mathbf{x})$$
(12)

$$s = \sqrt{\frac{S(x)}{n-1}} = sd(x)$$
 (13)  
 $CV = \frac{\sigma}{\pi} = \frac{s}{\pi}$  (14)

### 2.2 RELATIVE STANDING $z = \frac{x - \mu}{1 - \mu} = \frac{x - \bar{x}}{1 - \mu}$

Percentiles

 $P_r = r$ : (sorted r)  $k = \frac{i-0.5}{\cdot 100\%}$ (16)

To find  $x_i$  given  $P_k$ , i is:

 $1:L=\frac{k}{10000}\cdot n$ (17)

2 · if I is an integer: i = I+0.5: otherwise i=I and round up 2.3 VISUAL

All plots have optional arguments: main=" " care title

xlab="", ylab="" sets x/y-axis label type="p" for point plot type="1" for line plot type="b" for both points and lines

Ex: plot(x, v, type="b", main="My Plot") Histogram: hist (x) Stem & leaf: stem(x)

Box plot: boxplot (x) Barplot: plot (T) (where Tetable (x)) Scatter plot: plot (x, v) (where x, y are ordered vectors)

Time series plot: plot (t, y) (where t, y are ordered vectors) Graph function: curve (expr. xmin, xmax) plot expr involving x 2.4 ASSESSING NORMALITY

O-O plot: ganorm(x): galine(x)

3 Probability

Number of successes x with n possible outcomes. (Don't double count!)

 $P(A) = \frac{x_A}{}$ 

 $P(\bar{A}) = 1 - P(A)$ (19) P(A or B) = P(A) + P(B) - P(A and B)(20)

P(A or B) = P(A) + P(B)if A R mutually exclusive (21) $P(A \text{ and } B) = P(A) \cdot P(B|A)$ (22)(23)  $P(A \text{ and } B) = P(A) \cdot P(B)$  if  $A \cdot B$  independent

> $n! = n(n-1)(n-2)\cdots 2 \cdot 1 = factorial(n)$ (24)  $_{n}P_{k} = \frac{n!}{(n-k)!}$  Perm. no elements alike (25) (26)

 $=\frac{n!}{n! - n!}$  Perm.  $n_1$  alike, ...

 $_{n}C_{k} = \frac{n!}{(n-k)!k!} = \text{choose (n, k)}$ 

4 Random Variables

4.1 DISCRETE DISTRIBUTIONS

$$P(x_i)$$
: probability distribution  
 $E = \mu = \sum x_i \cdot P(x_i)$ 

$$\sigma = \sqrt{\sum (x_i - \mu)^2 \cdot P(x_i)}$$
(30)

(28)

(29)

(40)

(41)

(51)

4.2 CONTINUOUS DISTRIBUTIONS

CDF F(x) gives area to the left of x,  $F^{-1}(p)$  expects p is area to the left. f(x): probability density

$$E = \mu = \int_{-\infty}^{\infty} x \cdot f(x) dx$$
 (32)

$$\sigma = \sqrt{\int_{-\infty}^{\infty} (x - \mu)^2 \cdot f(x) dx}$$
(33)

$$F(x)$$
: cumulative prob. density (CDF) (34)  
 $F^{-1}(x)$ : inv. cumulative prob. density (35)

$$F(x') = \int_{-\infty}^{x'} f(x) dx$$
 (36)  
 $p = P(x < x') = F(x')$  (37)

$$x' = F^{-1}(p)$$
 (38)  
 $p = P(x > a) = 1 - F(a)$  (39)

$$p = P(a < x < b) = F(b) - F(a)$$
4.3 Sampling distributions

$$\mu_{\bar{z}} = \mu$$
 $\sigma_{\bar{z}} = \frac{\sigma}{\sqrt{n}}$ 

$$\mu_{\hat{p}} = p$$
  $\sigma_{\hat{p}} = \sqrt{\frac{pq}{n}}$  (42)

4.4 RINOMIAL DISTRIBUTION

(18)

(27)

$$\mu = n \cdot p \qquad (43)$$

$$\sigma = \sqrt{n \cdot p \cdot q} \qquad (44)$$

$$\sigma = \sqrt{n \cdot p \cdot q}$$

$$P(x) = {}_{n}C_{x}p^{x}q^{(n-x)} = \text{dbinom}(\mathbf{x}, \mathbf{n}, \mathbf{p})$$
(45)

$$P(x) = {}_{n}C_{x}p^{\lambda}q^{(n-\lambda)} = \text{dbinom}(\mathbf{x}, \mathbf{n}, \mathbf{p})$$
(45)

4.5 POISSON DISTRIBUTION
$$P(x) = \frac{\mu^{x} \cdot e^{-\mu}}{2\pi} = \operatorname{dpois}(\mathbf{x}, \mu)$$

$$P(x) = \frac{\mu^{-1}e^{-x}}{x!} = \text{dpois}(x, \mu)$$

4.6 NORMAL DISTRIBUTION

 $f(x) = \frac{1}{\sqrt{1 - \alpha^2}} \cdot e^{-\frac{1}{2} \frac{(x-\mu)^2}{\sigma^2}}$ (47)n = P(z < z') = F(z') = pnorm(z')(48)

$$p = F(z < z) = F(z) = \text{pnorm}(z^*)$$
 (48)  
 $z' = F^{-1}(p) = \text{qnorm}(p)$  (49)  
 $p = P(x < x') = F(x') = \text{pnorm}(x', \text{mean}=u, \text{sd}=\sigma)$  (50)

$$x' = F^{-1}(p) = \operatorname{qnorm}(p, \operatorname{mean}=\mu, \operatorname{sd}=\sigma)$$

4.7 t-distribution		6 Hypothesis Tests alternative can be:
		"two.sided". "less". "greater"
$p = P(t < t') = F(t') = \operatorname{pt}\left(\operatorname{t}' \;,\; \operatorname{df}\right)$	(52)	Test statistic and R function (when available) are listed for each.
$t' = F^{-1}(p) = \operatorname{qt}(\mathbf{p}, \operatorname{df})$	(53)	6.1 1-SAMPLE PROPORTION
4.8 $\chi^2$ -distribution		$H_0: p = p_0$ prop.test(x, n, p= $p_0$ , alternative="two.sided")
		$z = \frac{\hat{p} - p_0}{\sqrt{p_0 q_0 / p_0}}$
$p = P(\chi^2 < \chi^{2'}) = F(\chi^{2'}) = pchisq(X^2), df$	(54)	$z = \frac{1}{\sqrt{p_0q_0/n}}$
$y^{2'} = F^{-1}(p) = \operatorname{gchisq}(p, df)$	(55)	6.2 1-SAMPLE MEAN (σ KNOWN)
$\chi = r$ $(p) = \text{qenisq}(p, dr)$	(33)	$H_0: \mu = \mu_0$
4.9 F-DISTRIBUTION		$z = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$
p = P(F < F') = F(F') = pf(F', df1, df2)	(56)	6.3 1-SAMPLE MEAN (σ UNKNOWN)
$F' = F^{-1}(p) = \text{af}(p, df1, df2)$	(57)	$H_0: \mu = \mu_0$
· - · (//) - q2 (p), u21, u22)	(31)	t.test(x, mu=µ0, alternative="two.sided")
5 Estimation		Where x is a vector of sample data.
5.1 CONFIDENCE INTERVALS		$t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}},  df = n - 1$
proportion: $\hat{p} \pm E$ , $E = z_{\alpha/2} \cdot \sigma_{\hat{p}}$	(58)	
mean ( $\sigma$ known): $\bar{x} \pm E$ , $E = z_{\alpha/2} \cdot \sigma_{\bar{x}}$		
mean ( $\sigma$ unknown, use $s$ ): $\bar{x} \pm E$ , $E = t_{\alpha/2} \cdot \sigma_{\bar{x}}$ , $df = n - 1$	(60)	
variance: $\frac{(n-1)s^2}{\chi_R^2} < \sigma^2 < \frac{(n-1)s^2}{\chi_L^2}$ , $df = n-1$	(61)	
5.2 CRITICAL VALUES		
$z_{\alpha/2} = P(z > \alpha) = \text{qnorm}(1-\text{alpha/2})$	(62)	
$t_{\alpha/2} = P(t > \alpha) = qt (1-alpha/2, df)$	(63)	
$\gamma_t^2 = P(\gamma^2 < \alpha) = \text{gchisg(alpha/2, df)}$	(64)	
$\chi_p^2 = P(\chi^2 > \alpha) = \text{qchisq}(1-\text{alpha/2}, df)$	(65)	
5.3 REQUIRED SAMPLE SIZE		
proportion: $n = \hat{p}\hat{q}\left(\frac{z_{\alpha/2}}{E}\right)^2$ $(\hat{p} = \hat{q} = 0.5 \text{ if unknown})$	(66)	
mean: $n = \left(\frac{z_{\alpha/2} \cdot \check{\sigma}}{\frac{E}{E}}\right)^2$	(67)	
( E )		

(68)

(69)

(70)