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1. Decode the following ASCII code:

[2 marks]

1010011 1110100 1100101 1110110 1100101 0100000 1001010 1101111
1100010 1110011

Answer

1010011- 83- S

1110100- 116- t

1100101- 101- e

1110110- 118- v

1100101- 101- e

0100000- 32 -space

1001010- 74- J

1101111- 111- o

1100010- 98- b

1110011- 115- s

Steve Jobs

2. The state of a 12-bit register is 100010010111. What is its content if it represents

(a) Three decimal digits in BCD?

[1 mark]

(b) Three decimal digits in the excess-3 code?

[1 mark]

(c) Three decimal digits in the 84-2-1 code?

[1 mark]

(d) A binary number?

[1 mark]

Answer

a) Divide the binary into 4-bits beginning from the right = 897

$$0111 - 2^0 + 2^1 + 2^2 = 7$$

$$1001 - 2^0 + 2^3 = 9$$

$$1000 - 2^3 = 8$$

b) Decimal digits in the excess-3 code

$$8+3 = 11$$

$$9+3 = 12$$

$$7+3 = 10$$

c)

Decimal digits	8	4	-2	-1
8	1	0	0	0
9	1	1	1	1
7	1	0	0	1

d) Binary number = 100010010111

3. Add and multiply the following numbers without converting them to decimal.

(a) Binary numbers 1011 and 101.

[2 marks]

(b) Hexadecimal numbers 2E and 34

[2 marks]

Answer

a) $1011 + 101 = 10000$

a. $1011 * 101 = 1011 + 00000 + 1011100 = 110111$

b) $2E * 34 = 1B8 + 8A0 = 958$

b. $2E + 34 = 62$

4. Convert the hexadecimal number 64CD to binary, and then convert it from binary to octal.

[2 marks]

Answer

$64CD = 110010011001101$

$6 - 2^2 + 2^1 = 0110$

$4 - 2^2 = 0100$

$C - 12 - 2^3 + 2^2 = 1100$

$D - 13 - 2^3 + 2^2 + 2^0 = 1101$

Binary to Octal

$110 - 6$

$010 - 2$

$011 - 3$

$001 - 1$

$101 - 5$

$110010011001101 = 62315 \text{ base } 8$

5. What is the exact number of bytes in a system that contains

(a) 32K bytes

[1 mark]

(b) 64M bytes

[1 mark]

(c) 6.4G bytes

[1 mark]

Answer

a. For 32k bytes:

1 kilobyte (KB) = 1024 bytes

So, 32 kilobytes = $32 * 1024$ bytes = 32,768 bytes

b. For 64m bytes:

1 megabyte (MB) = 1024 kilobytes (KB)

So, 64 megabytes = $64 * 1024 * 1024$ bytes = 67,108,864 bytes

c. For 6.4g bytes:

1 gigabyte (GB) = 1024 megabytes (MB)

So, 6.4 gigabytes = $6.4 * 1024 * 1024 * 1024$ bytes = 6,871,948,800 bytes

6. Determine the base of the numbers in each case for the following operations to be correct:

(a) $14/2 = 5$

[0.5 mark]

(b) $54/4 = 13$

[0.5 mark]

(c) $24 + 17 = 40$

[0.5 mark]

Answer

a) $14/2=5$

Solution: $14_{\{x\}}/2_{\{x\}}=5_{\{x\}} [(1 \times x^1) + (4 \times x^0)]/(2x) = (5 \times x^0) \times (x+4)/2 = 5x+4 = 5 \times 2x = 10 - 4x = 6$

$14/2=5$, is correct in base 6.

(b) $54/4=13$

Solution: $54_{\{x\}}/4_{\{x\}}=13_{\{x\}} [(5 \times x^1) + (4 \times x^0)]/(4x) = (1x^1) + (3x^0) (5x+4)/4 = (x+3) (5x+4) = 4x+12 - 5x-4x = 12-4x = 8$

(c) $24+17=40$

Solution: $24x/17x=40x [(2 \times x) + (4 \times x^0)] + [(1 \times x) + (7 \times x^0)] = [(4 \times x) + (0 \times x^d)] (2x+4) + (x+7) = 4x \times 3x + 11 = 4x \times 11 = 4x - 3x = 11$

7. Convert the following numbers to base 10:

(a) $1100_2 = ?_{10}$

[1 mark]

(b) $1111\ 1111\ 1111_2 = ?_{10}$

[1 mark]

(c) $77_8 = ?_{10}$

[1 mark]

(d) $221_8 = ?_{10}$

[1 mark]

(e) $5BC_{16} = ?_{10}$

[1 mark]

Answer

a) $1100\ 2^3 + 2^2 = 8 + 4 = 12$

b) $1111\ 1111\ 1111 = FFF$
 $= (15 \cdot 16^2) + (15 \cdot 16^1) + (15 \cdot 16^0)$
 $= 3840 + 240 + 15$
 $= 4095 \text{ base } 10$

c) $77 \text{ base } 8 = (7 \cdot 8^1) + (7 \cdot 8^0)$
 $= 56 + 7$
 $= 63 \text{ base } 10$

d) $221 \text{ base } 8 = (2 \cdot 8^2) + (2 \cdot 8^1) + (1 \cdot 8^0)$
 $= 128 + 16 + 1$
 $= 145 \text{ base } 10$

e) $5BC \text{ base } 16 = (5 \cdot 16^2) + (11 \cdot 16^1) + (12 \cdot 16^0)$
 $= 1280 + 176 + 12$
 $= 1468 \text{ base } 10$

8. Convert the following base 10 numbers to the base indicated:

(a) $56_{10} = ?_2$

(b) $56_{10} = ?_8$

[1 mark]

(c) $56_{10} = ?_{16}$

[1 mark]

(d) $221_{10} = ?_2$

[1 mark]

(e) $221_{10} = ?_8$

[1 mark]

(f) $221_{10} = ?_{16}$

[1 mark]

Answer

a) $56/2 = 28$ remainder 0

$28/2 = 14$ remainder 0

$14/2 = 7$ remainder 0

$7/2 = 3$ remainder 1

$3/2 = 1$ remainder 1

$1/2 = 0$ remainder 1

56 base 10 = 111000 base 2

b) $56/8 = 7$ remainder 0

$7/8 = 0$ remainder 7

56 base = 70 base 8

c) $56/16 = 3$ remainder 8

$3/16 = 0$ remainder 3

56 base 10 = 38 base 16

d) $221/2 = 110$ remainder 1

$110/2 = 55$ remainder 0

$55/2 = 27$ remainder 1

$27/2 = 13$ remainder 1

$13/2 = 6$ remainder 1

$6/2 = 3$ remainder 0

$3/2 = 1$ remainder 1

$\frac{1}{2} = 0$ remainder 1

221 base 10 = 11011101 base 2

- e) $221/8 = 27$ remainder 5
 $27/8 = 3$ remainder 3
 $3/8 = 0$ remainder 3
221 base 10 = 335 base 8
- f) $221/16 = 13$ – D remainder 13
 $13/16 = 0$ remainder 13 – D
221 base 10 = DD base 16

9. Convert the following numbers from base 10 to base 16

(a) $(2020)_{10}$

[1 mark]

(b) $(2020.65625)_{10}$

[1 mark]

(c) $(172)_{10}$

[1 mark]

(d) $(172.983)_{10}$

[1 mark]

Answer

a) $2020 \div 16 = 126$ remainder 4 (4 in hex)

$126 \div 16 = 7$ remainder 14 (E in hex)

$7 \div 16 = 0$ remainder 7 (7 in hex)

$(2020)_{10} = (7E4)_{16}$.

Integer part

b) $2020 \div 16 = 126$ remainder 4 (4 in hex)

$$126 \div 16 = 7 \text{ remainder } 14 \text{ (E in hex)}$$

$$7 \div 16 = 0 \text{ remainder } 7 \text{ (7 in hex)}$$

Fractional part:

$$0.65625 \times 16 = 10.5 \text{ (A in hex)}$$

$$0.5 \times 16 = 8.0 \text{ (8 in hex)}$$

$$(2020.65625)_{10} = (7E4.A8)_{16}.$$

c) Fractional part: $0.983 \times 16 = 15.728 \text{ (F in hex)}$

$$0.728 \times 16 = 11.648 \text{ (B in hex)}$$

$$0.648 \times 16 = 10.368 \text{ (A in hex)}$$

$$(172.983)_{10} = (AC.BFA)_{16}.$$

11. Convert 43.2 base 8 to binary, base 3, decimal and hexadecimal. Any fractions that do not terminate should be truncated to 4 digits in the fractional part. [1.5 marks]

Answer

convert 43.2 base 8 to decimal

$$43.2_8 = 4 \times 8^1 + 3 \times 8^0 + 2 \times 8^{-1} = 32 + 3 + 0.25 = 35.25_{10}$$

Binary:

$$35_{10} = 100011 \text{ base 2}$$

$$0.25_{10} = 0.01 \text{ base 2}$$

13. Each of the following base 10 numbers in signed magnitude, one's complement and two's complement. Each of the numbers should be represented in 8 bits. [7.5 marks]

Base 10	Signed Magnitude Binary Representation	One's Complement Binary Representation	Two's Complement Binary Representation
43	001010111	001010111	001010111
-43	10101011	11010100	11010101
-128	Invalid	Invalid	Invalid
127	01111111	10000000	10000001
-1	100000001	11111110	11111111