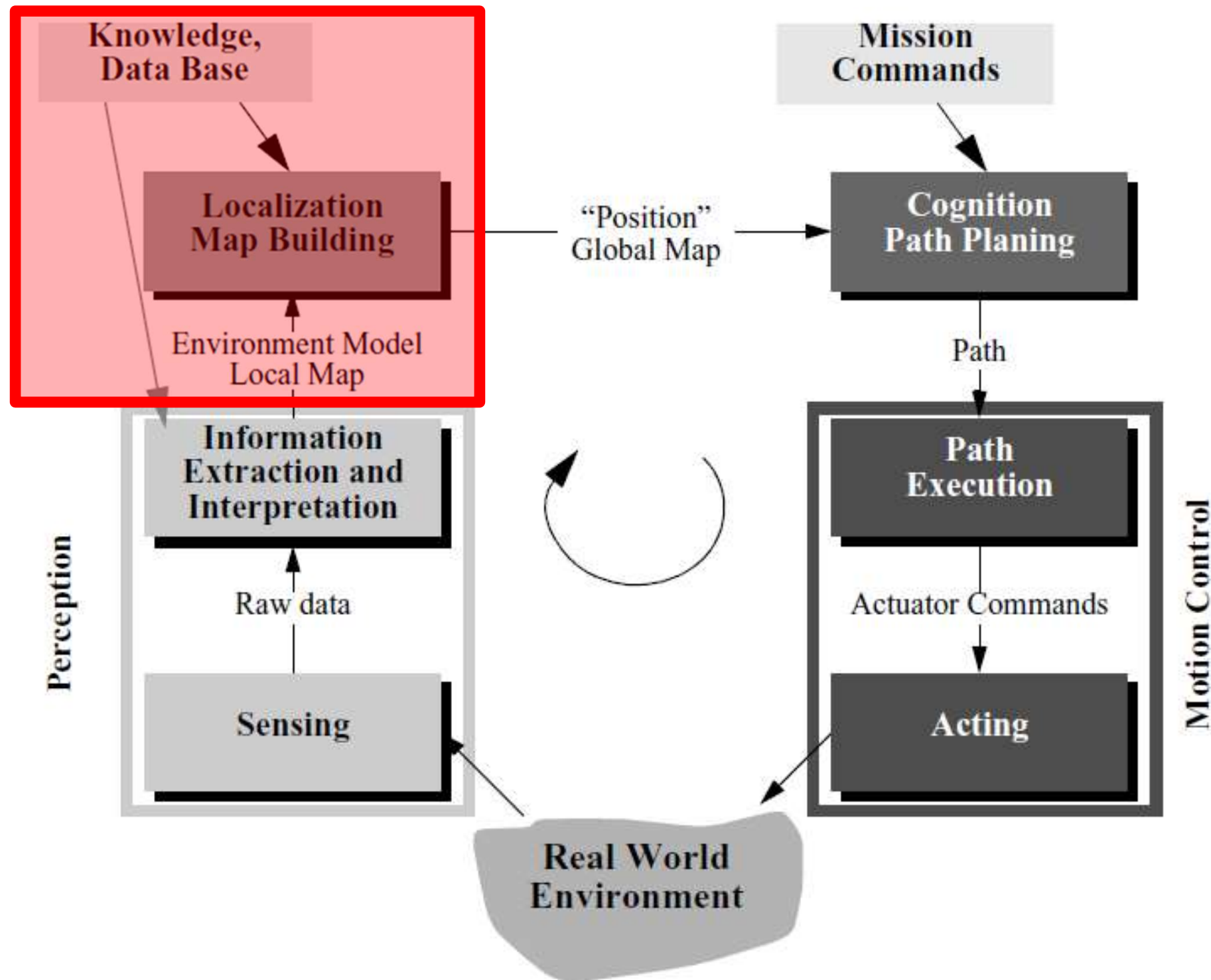


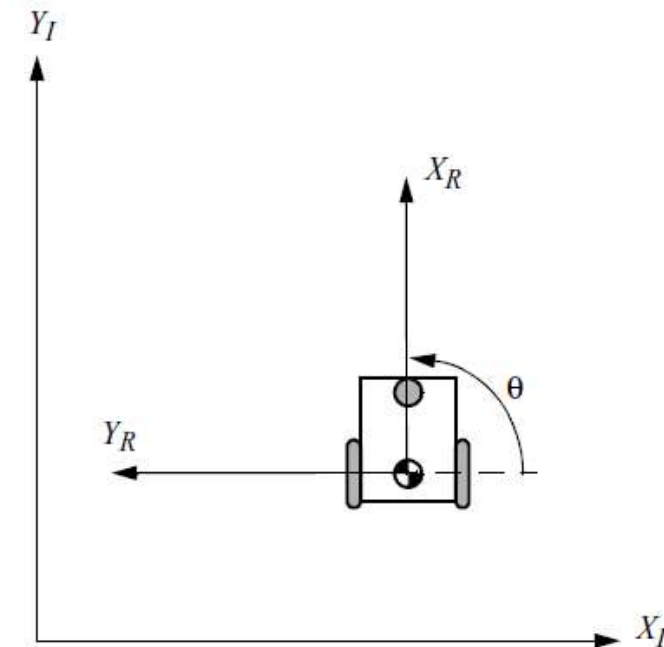
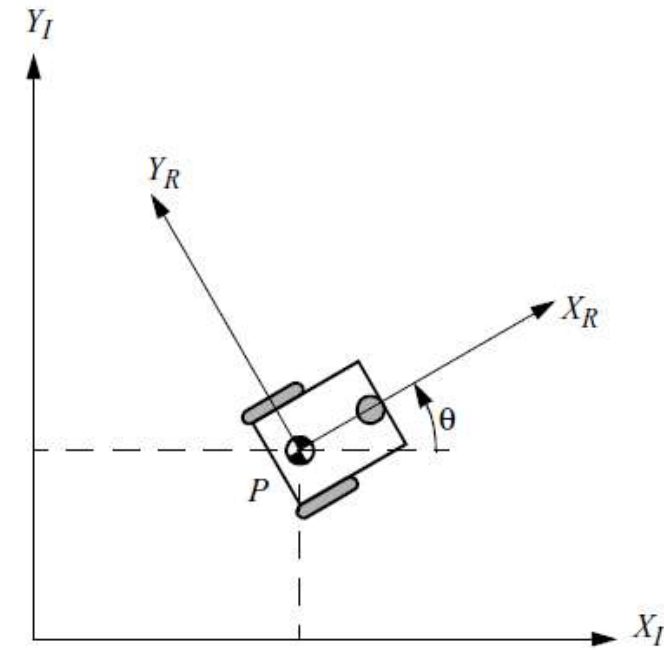
ENPM 809T

UMCP, Mitchell

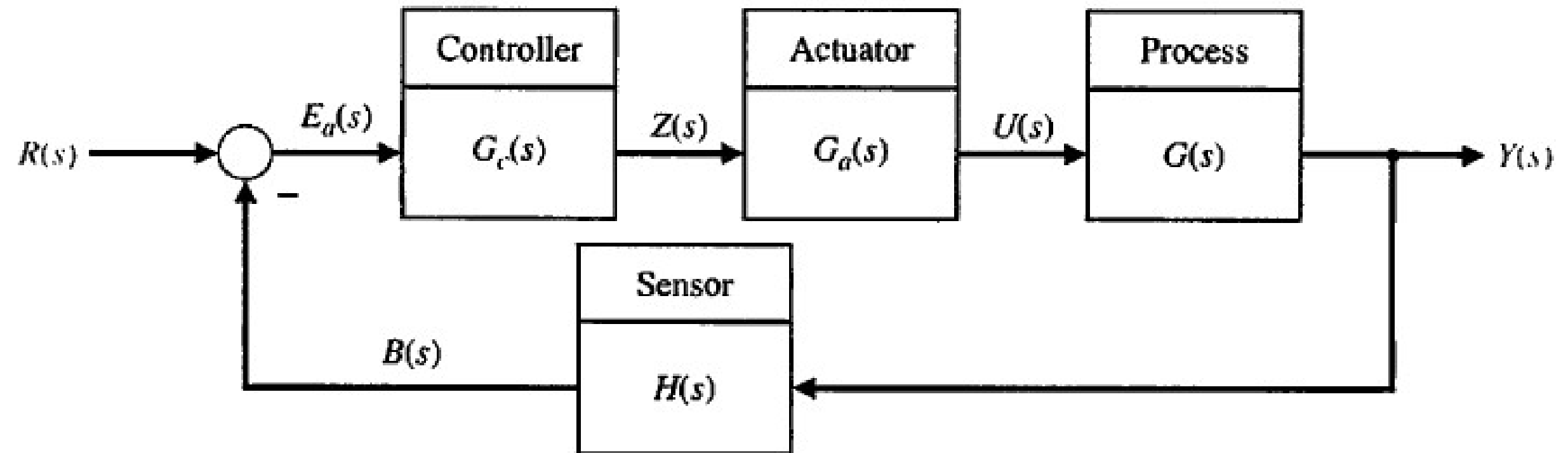


Kinematics

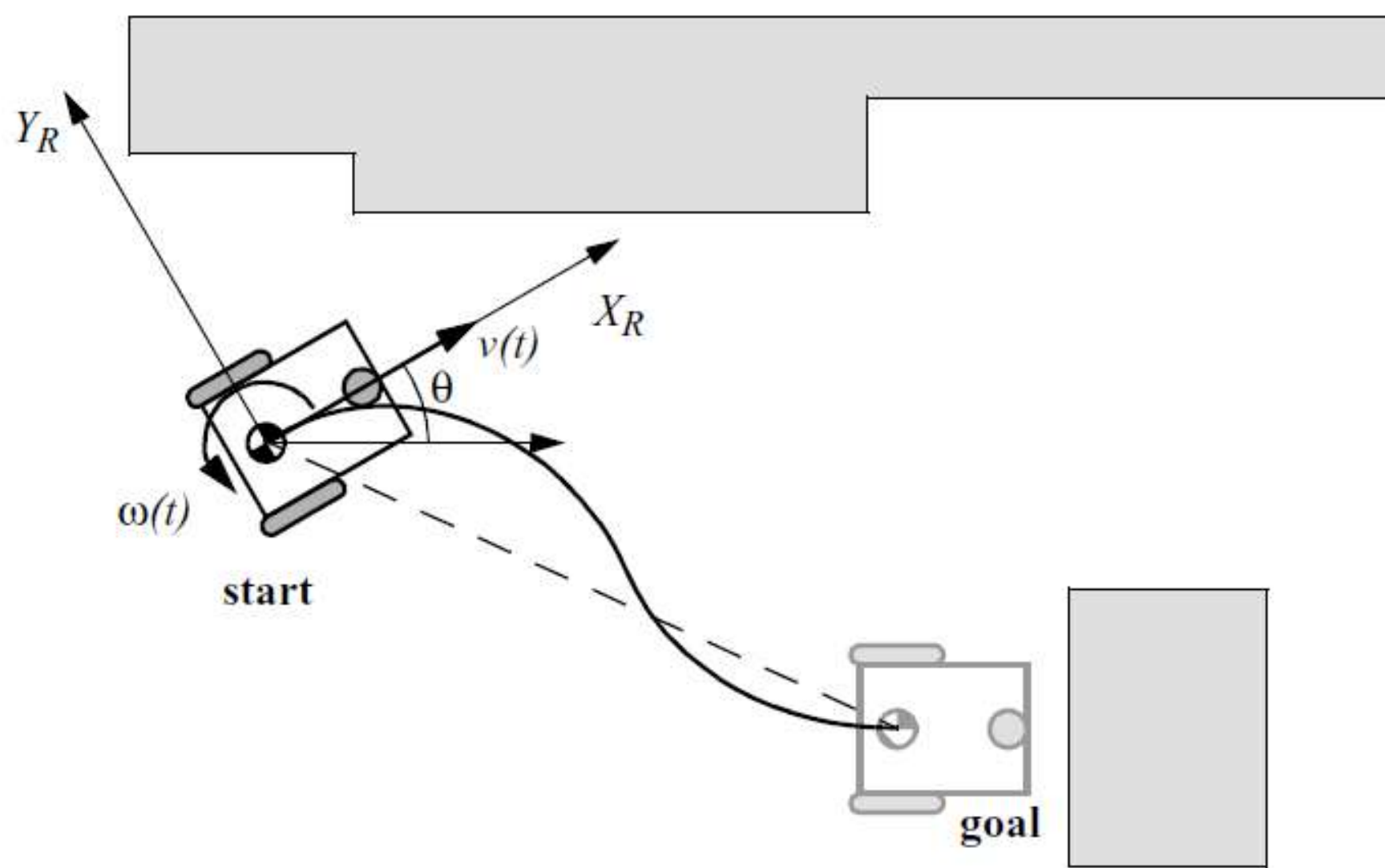
- Study of how mechanical systems behave
- Mobile robotics
 - Design for specific tasks
 - Create control software to drive hardware
- Global reference frame & robot local reference frame



Control Theory

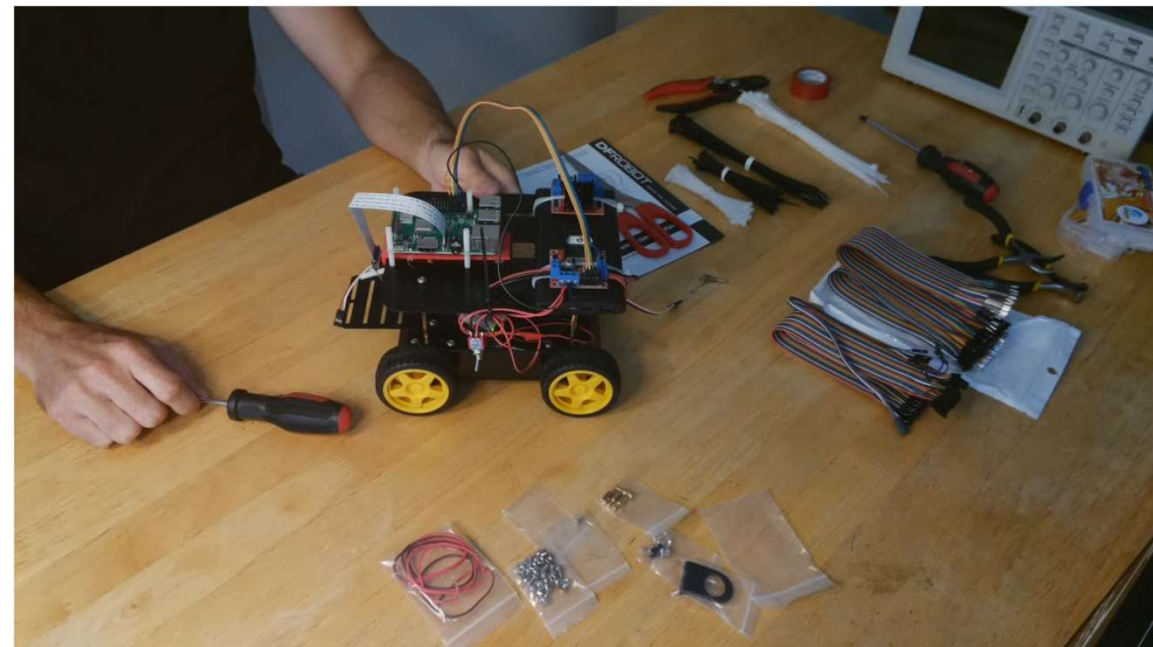
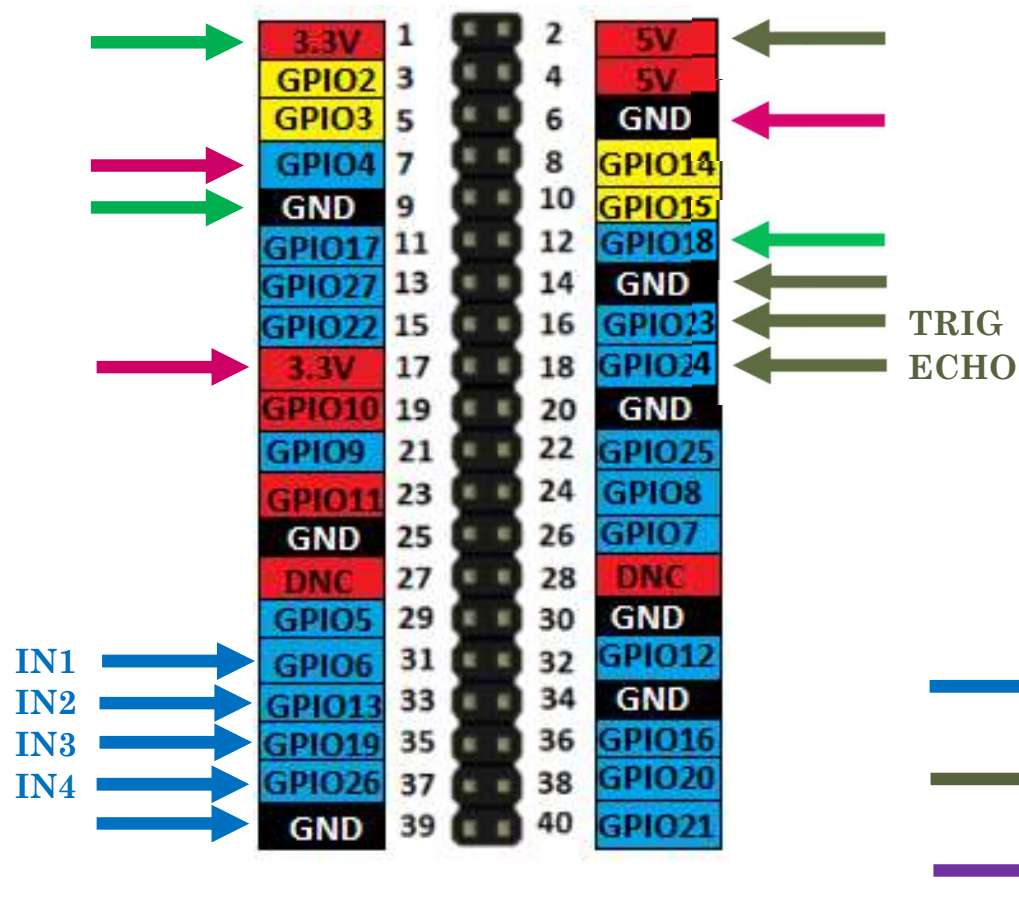


Kinematics & Localization



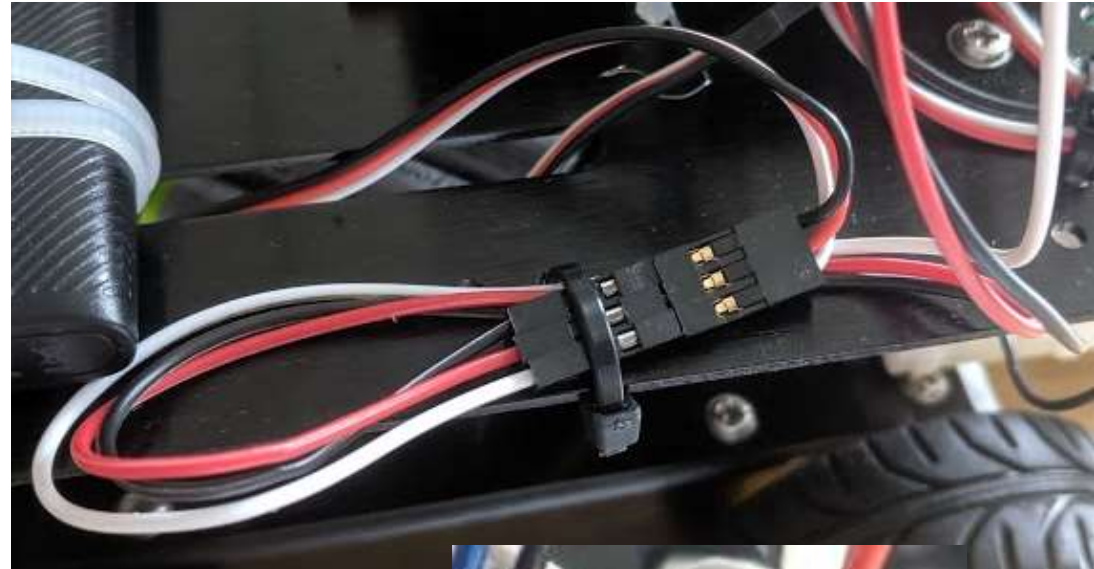
Assembly

- Confirm proper wiring of motor encoders to Raspberry Pi



Encoder Circuit

- Plug **red** male-female wire into pin 1 or 17
 - Encoder 3.3V **power**
- Plug **black** male-female wire into pin 9 or 6
 - Encoder **GND**
- Plug white male-female wire into pin 12 or 7
 - Encoder signal



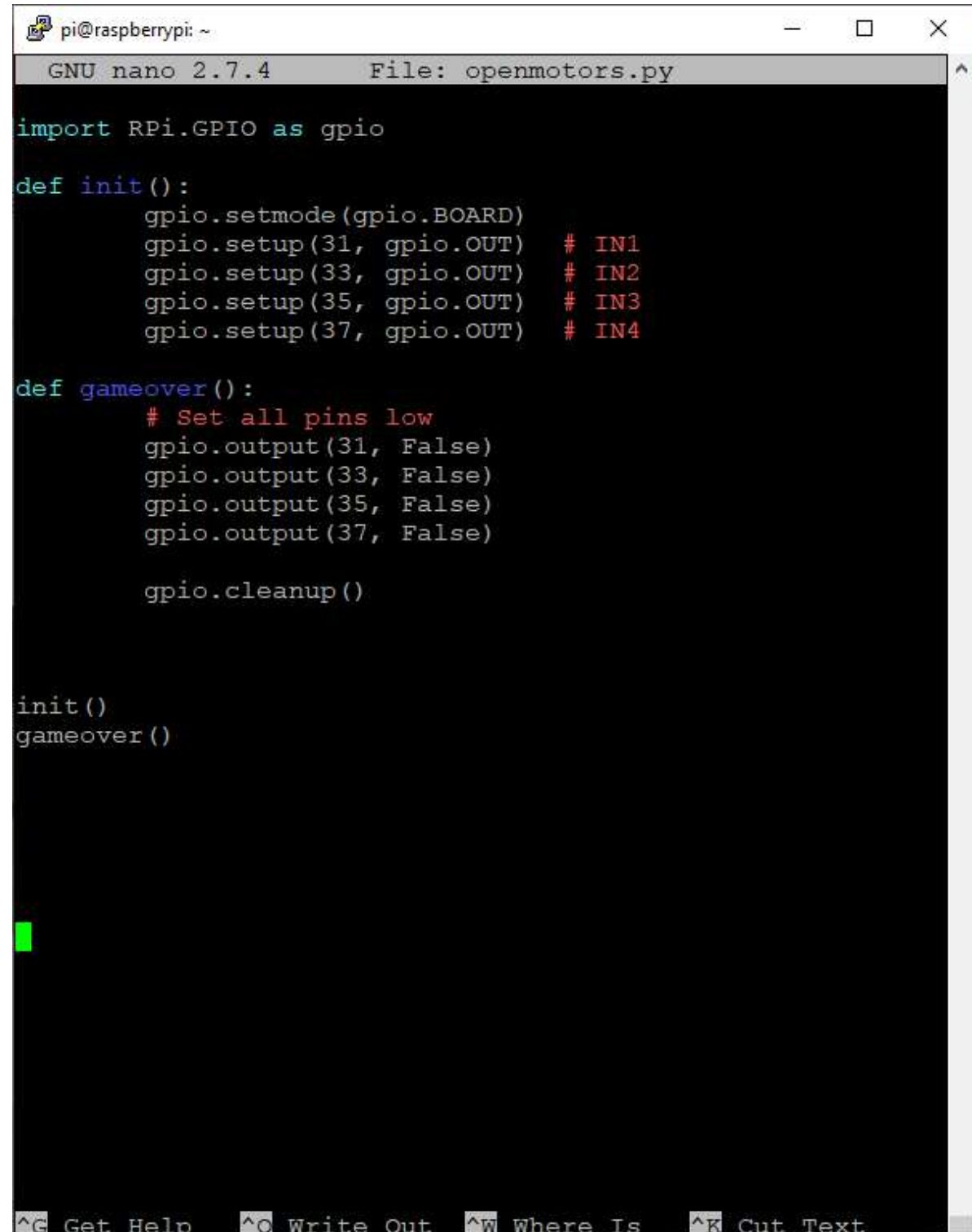
* DISCLAIMER *

- It is **vitaly important** to be careful NOT to plug in any 5V pins!
- ...sending 5V to the 3.3V GPIO pins will ***permanently damage*** your RPi!!
- In general, recommend transferring/backing up all .py files to your laptop before each lecture



Assembly

- **Double check all electrical connections!**
- Power Raspberry Pi via USB battery pack
- Connect to Raspberry Pi using Putty/Terminal and VNC
- Run ***openmotors.py*** prior to applying power to the H-bridge

A screenshot of a terminal window on a Raspberry Pi. The window title is "pi@raspberrypi: ~". The terminal shows the GNU nano 2.7.4 editor editing a file named "openmotors.py". The code in the file is as follows:

```
import RPi.GPIO as gpio

def init():
    gpio.setmode(gpio.BOARD)
    gpio.setup(31, gpio.OUT) # IN1
    gpio.setup(33, gpio.OUT) # IN2
    gpio.setup(35, gpio.OUT) # IN3
    gpio.setup(37, gpio.OUT) # IN4

def gameover():
    # Set all pins low
    gpio.output(31, False)
    gpio.output(33, False)
    gpio.output(35, False)
    gpio.output(37, False)

    gpio.cleanup()

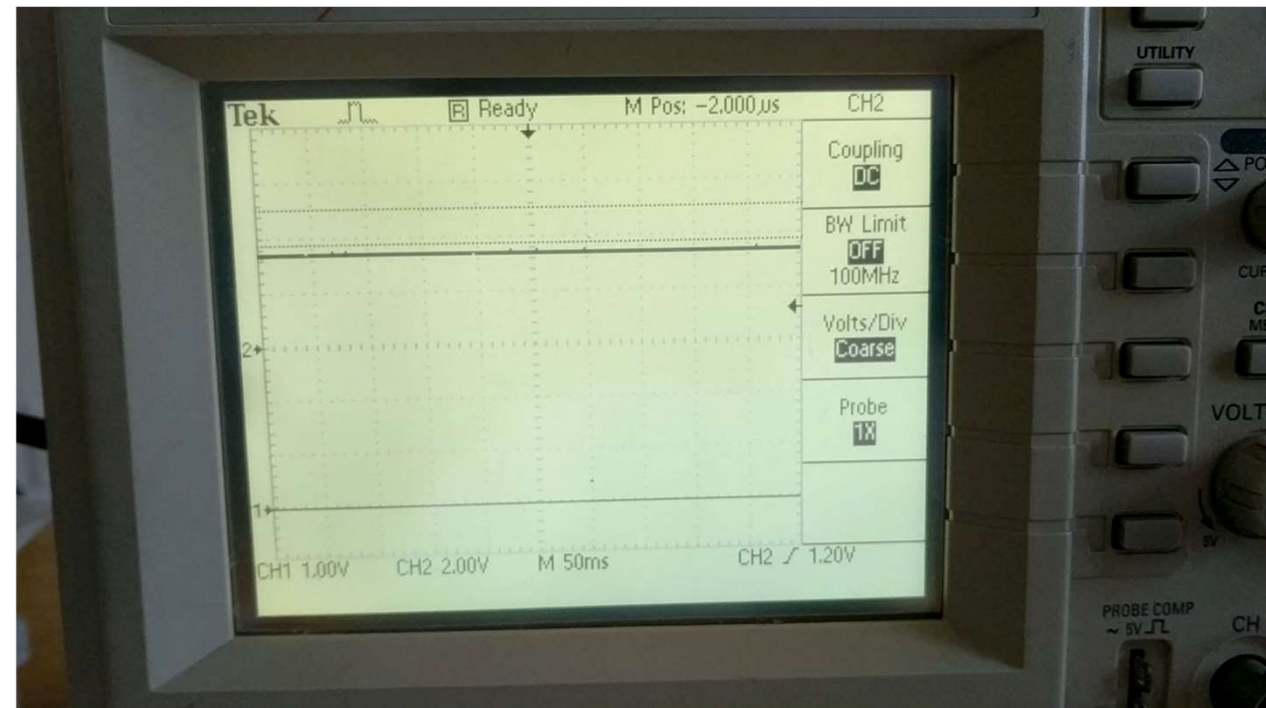
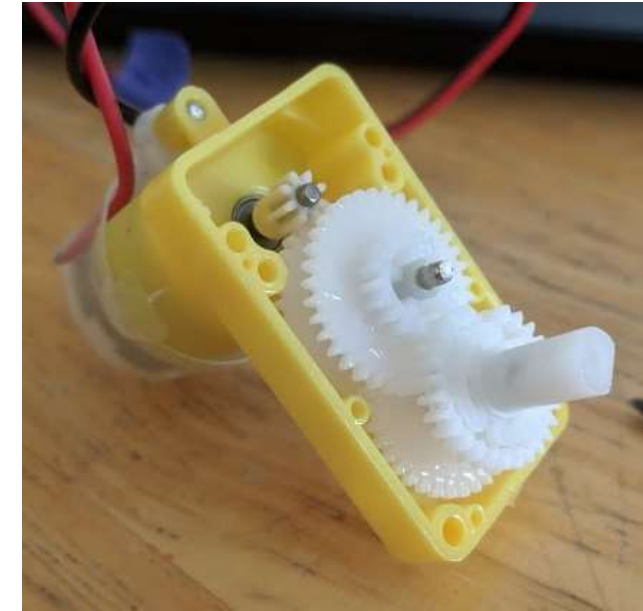
init()
gameover()
```

The terminal shows the script has been executed, with a green cursor on the line following the last line of code. The bottom of the terminal window shows standard nano editor shortcuts: ^G Get Help, ^O Write Out, ^W Where Is, ^K Cut Text.

Encoders

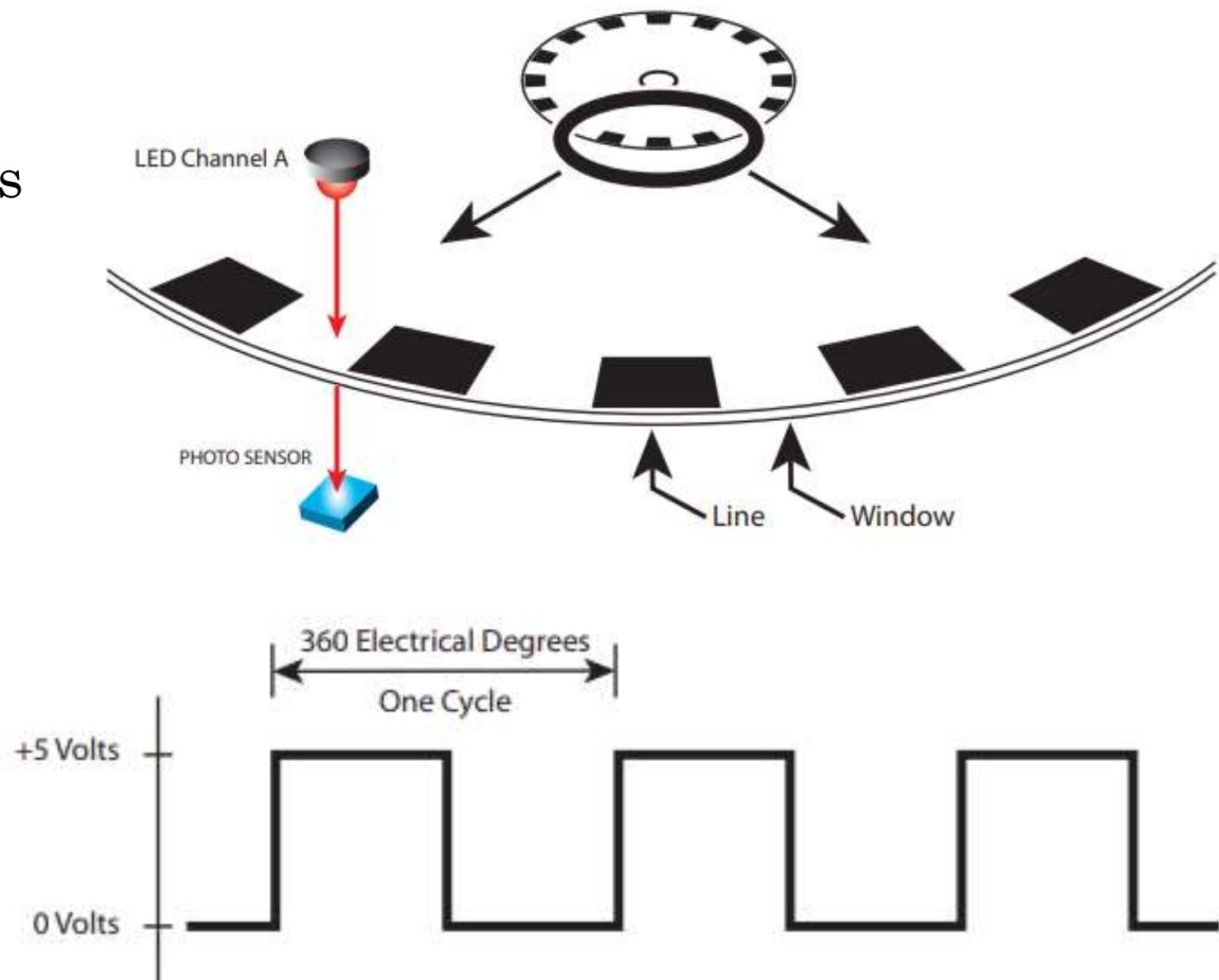
- Electro-mechanical device
- Converts motion into sequence of digital pulses
- Pulse train converted to position measurements
 - Robot **localization**
- Typically magnetic or optical

Proprioceptive Sensor

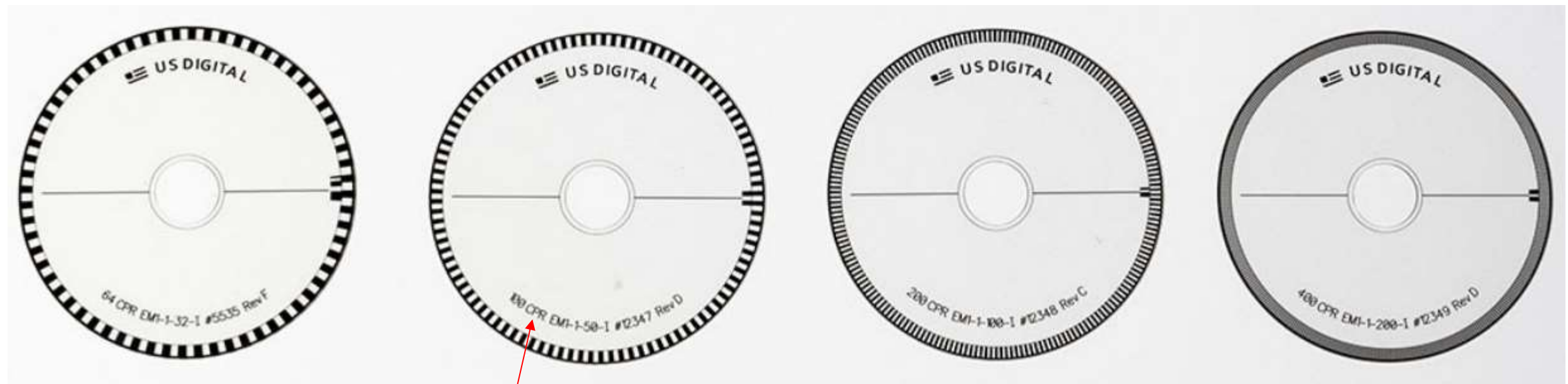


Encoders

- Resolution: number of times the output signal goes high per revolution
- Lines & windows represent *relative* positions on disk



Encoders

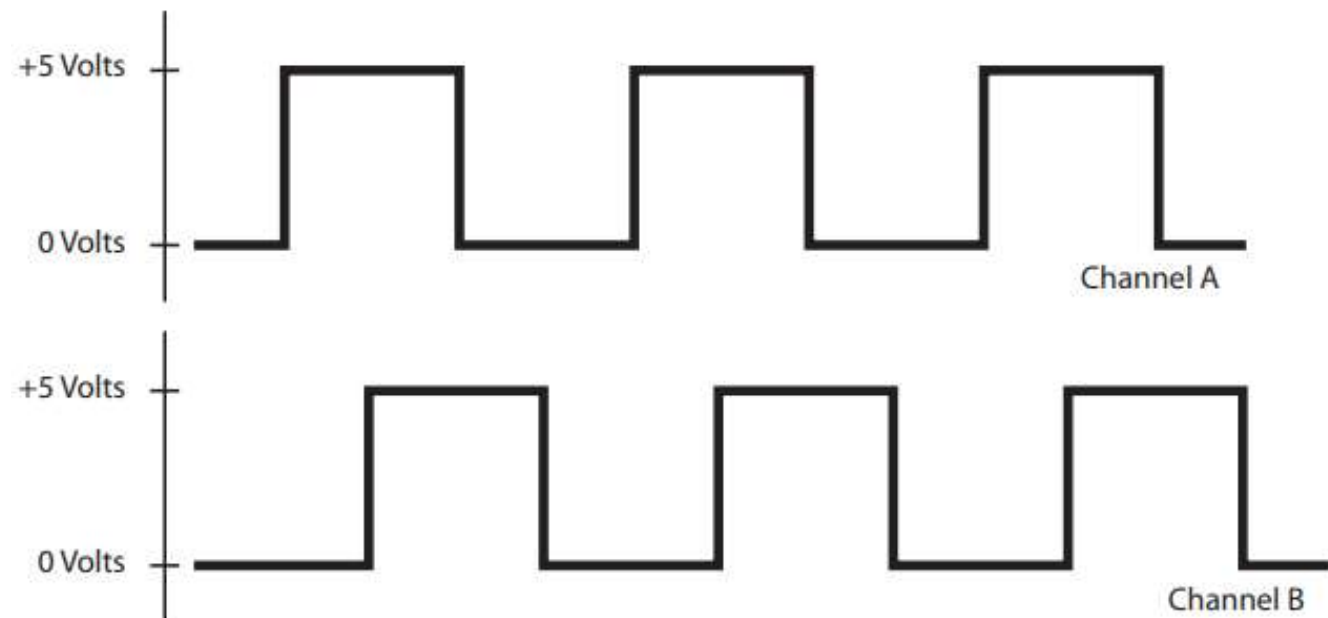
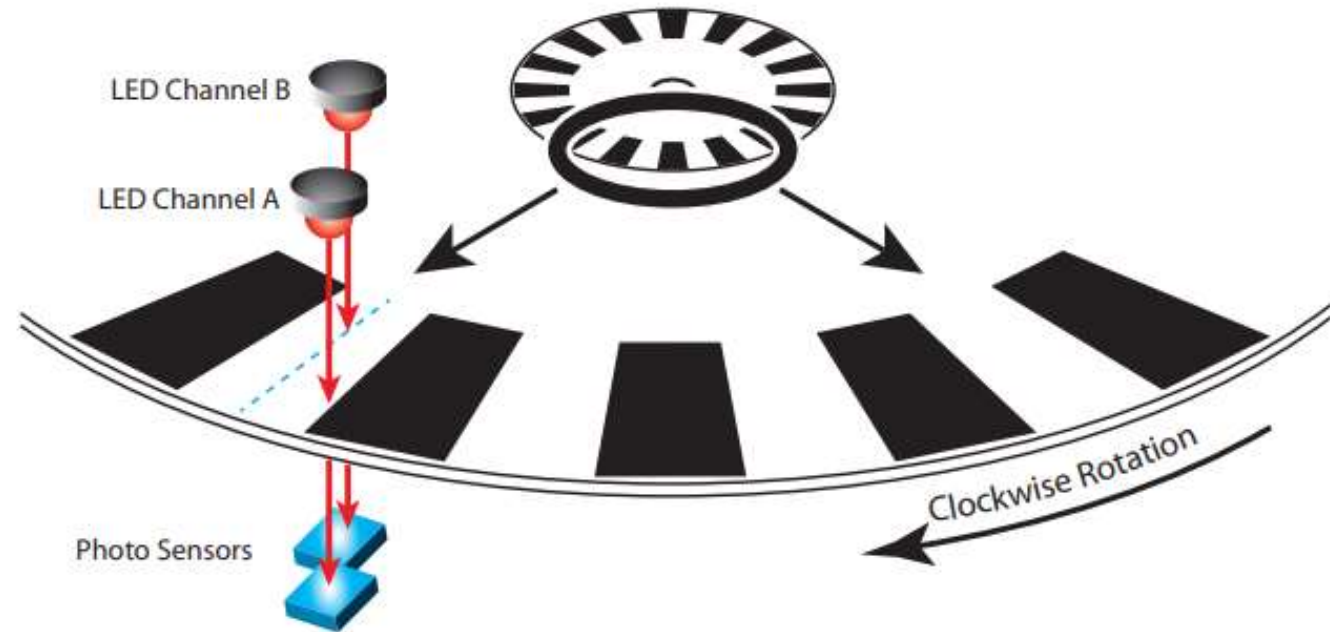


Cycles per Revolution (CPR): number of line/window pairs

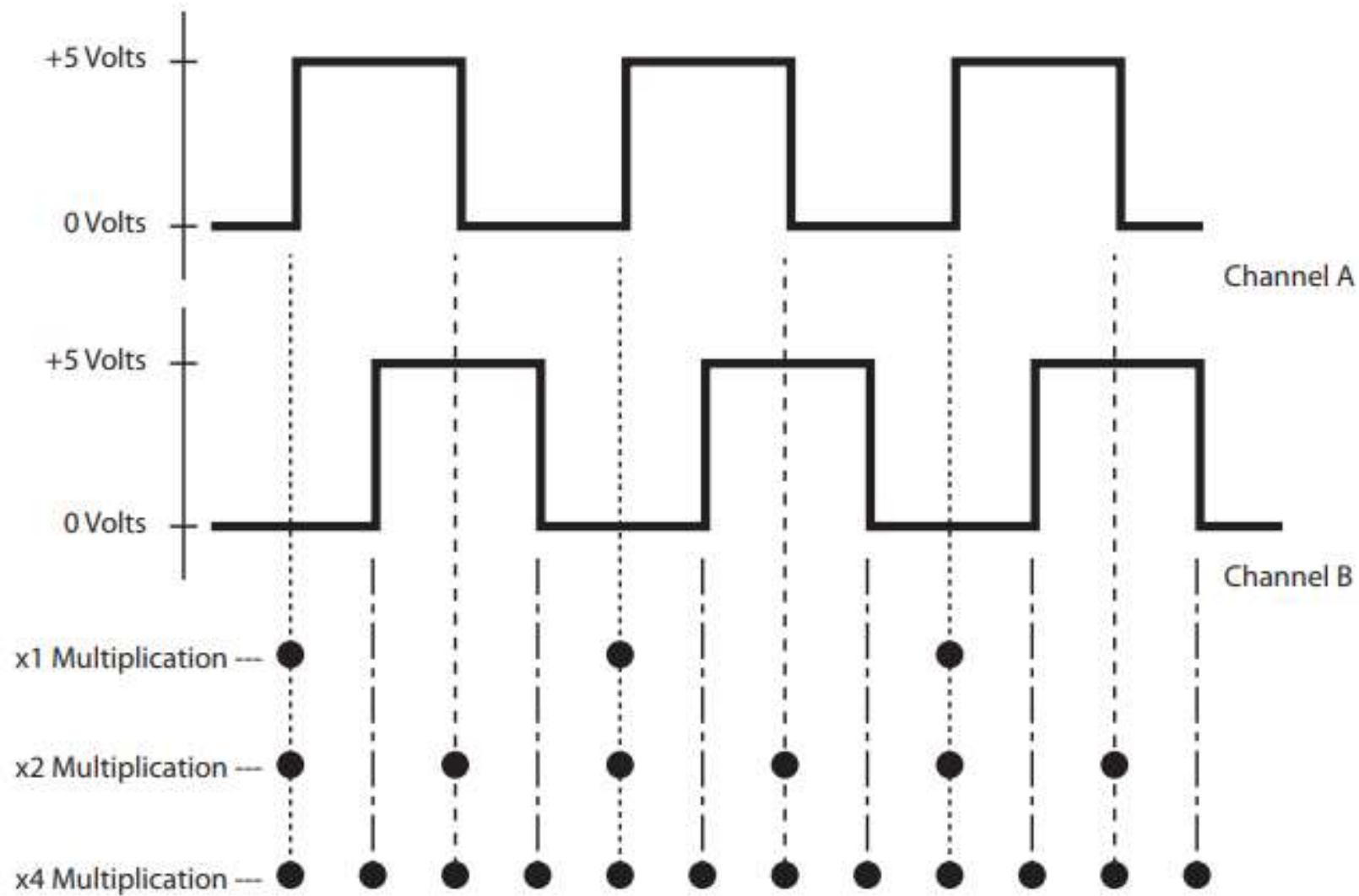
Encoders

- Quadrature: additional LED & photosensor displaced by 90-deg electrically

1. Direction
2. Resolution increased

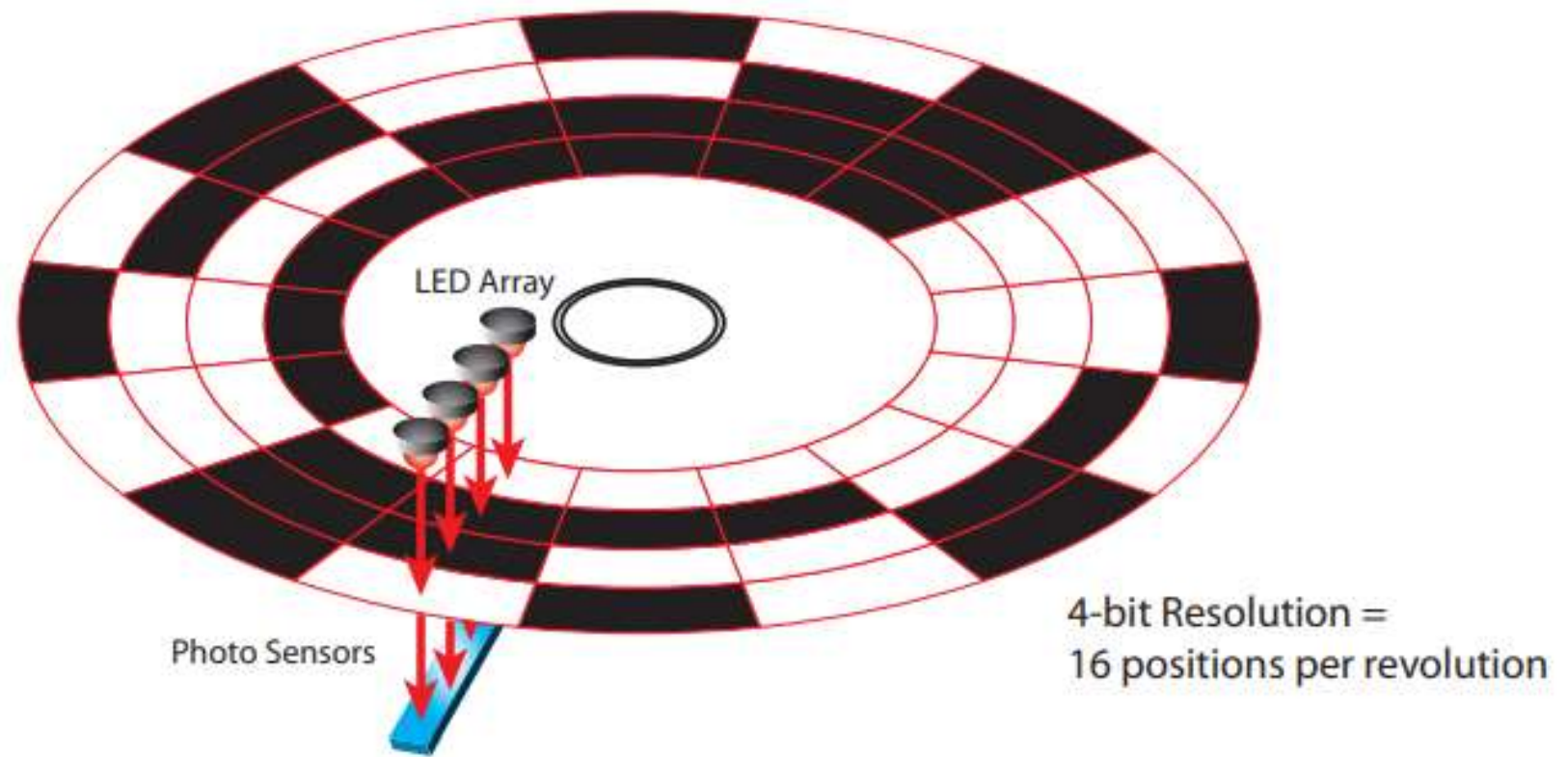


Encoders



Encoders

- Absolute: output unique code for each position on disk
- Resolution defined here in terms of bits



Resolution in Bits	Positions per Revolution	Degrees of Rotation
8-bit resolution	256 positions	1.41° of rotation per position
10-bit resolution	1,024 positions	0.35° of rotation per position
12-bit resolution	4,096 positions	0.09° of rotation per position

Encoders

- Neodymium 8-pole magnet
 - 4 north poles
 - 4 south poles
- Hall effect sensor

Specifications:

Supply voltage: 3V-24V

Supply current: 4mA per sensor

Output voltage: 26V maximum

Output current: 25mA continuous

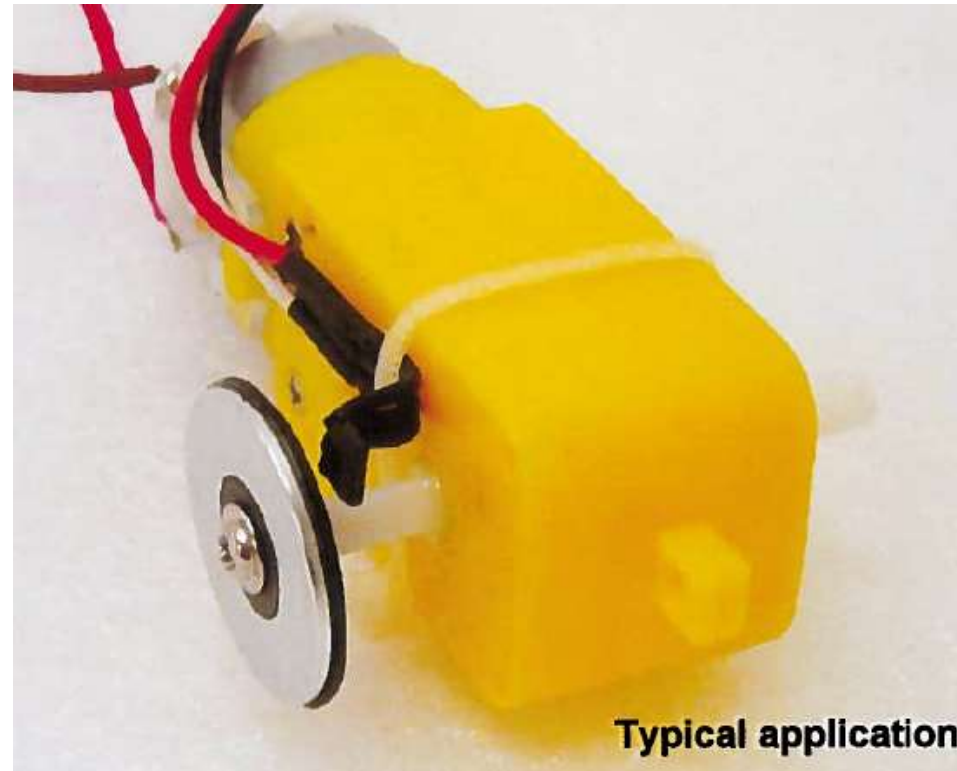
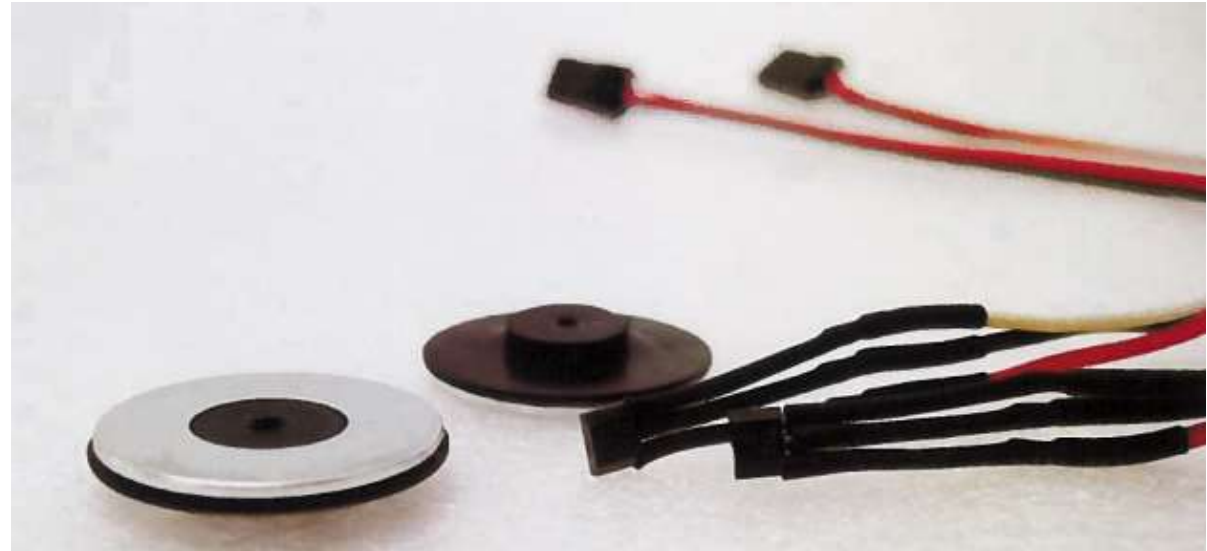
Output type: Open drain

Wiring:

White wire: Output

Red wire: +3V to 24V

Black wire: Ground (0V)

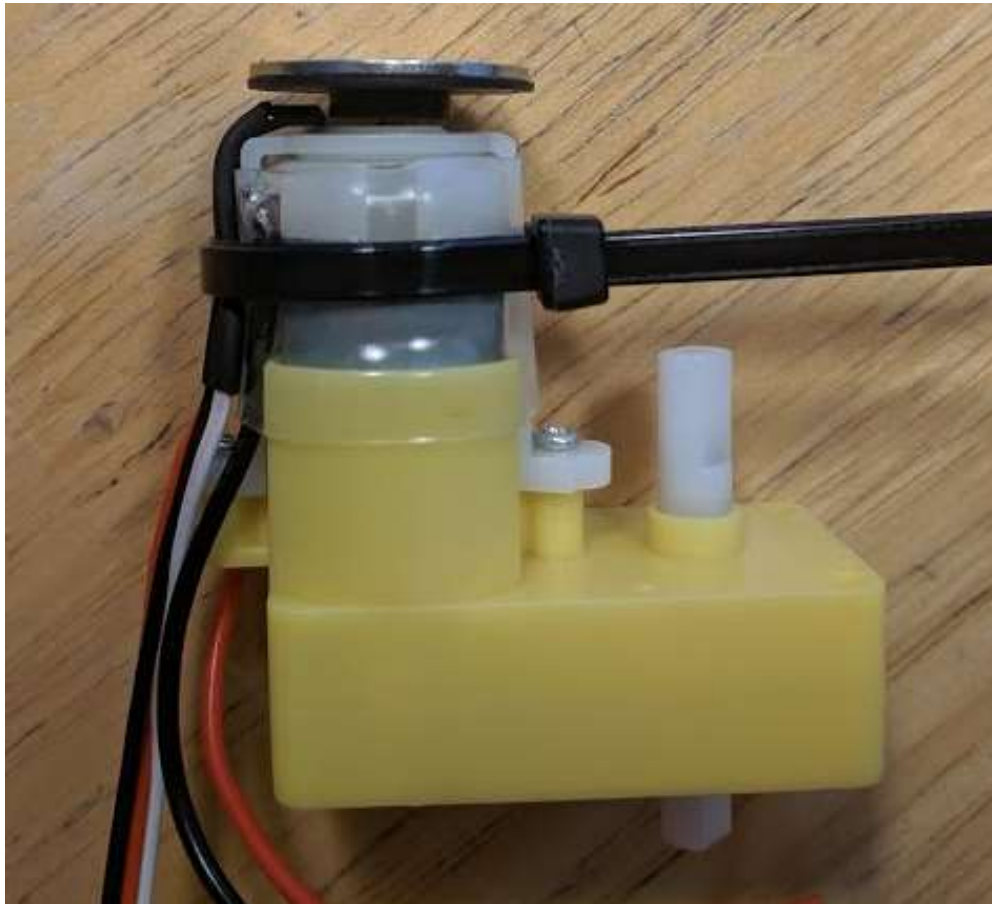


Typical application

ENPM 809T: Autonomous Robotics

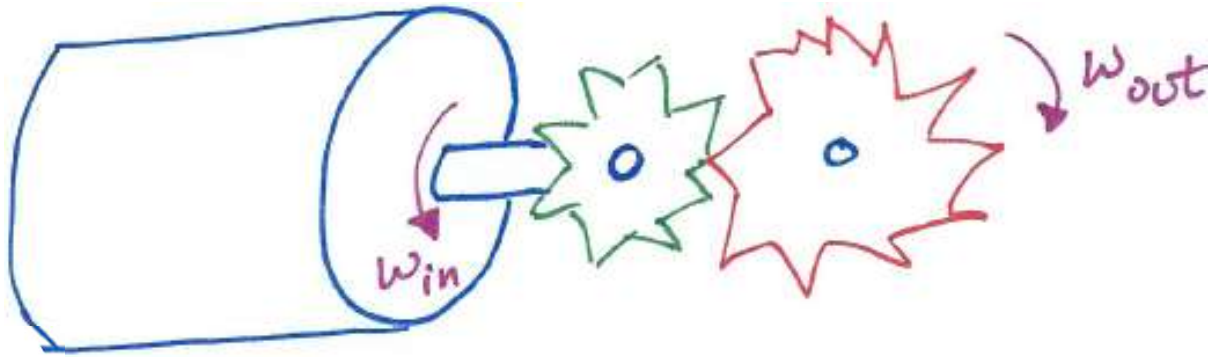


Encoders



<https://www.youtube.com/watch?v=oLBYHbLO8W0>

DC motor gearing

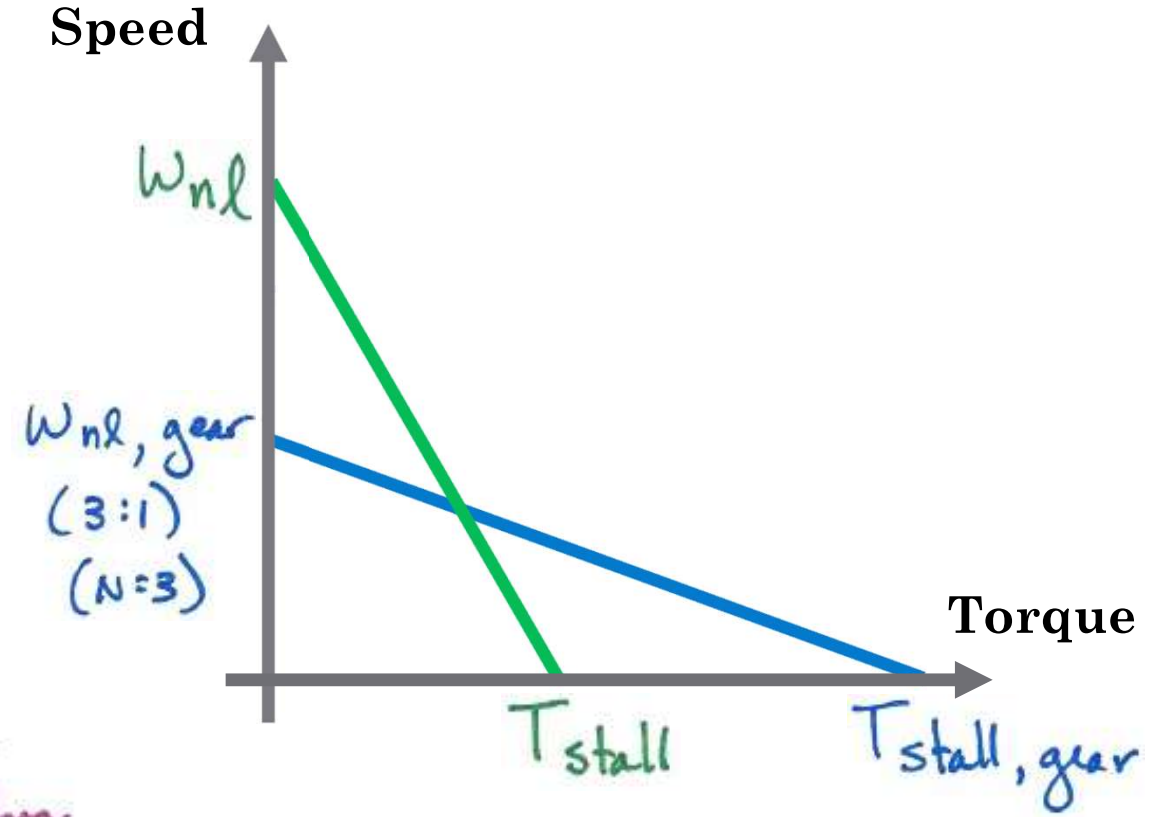


gear Ratio

$$N = \frac{\omega_{in}}{\omega_{out}} = \frac{\text{input speed from motor}}{\text{output speed from gearbox}}$$

$$\omega_{nl} = 1000 \text{ rpm}$$

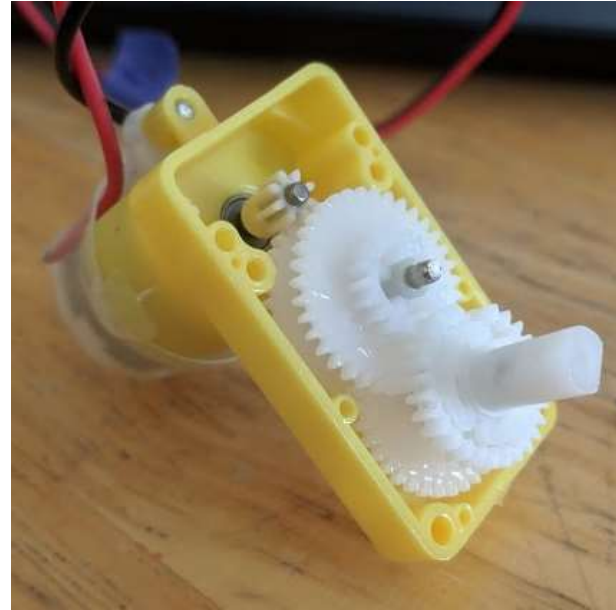
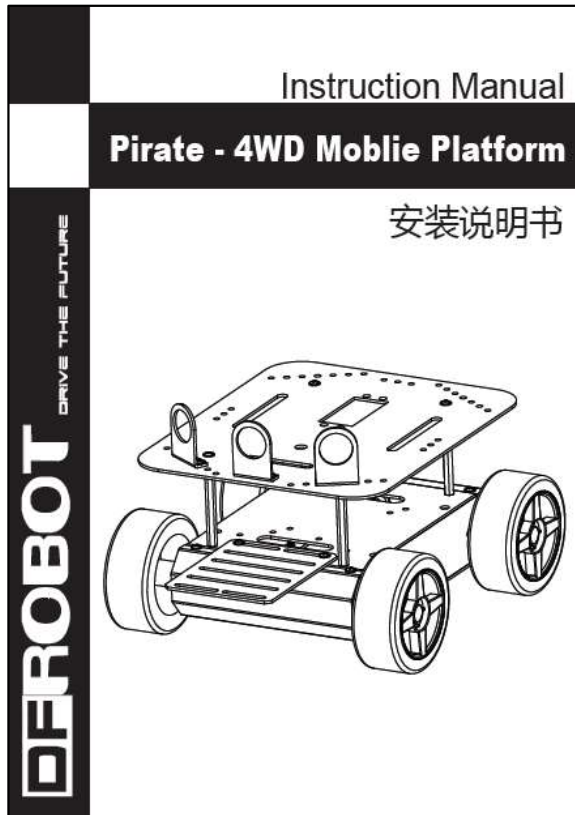
$$10:1 \text{ gear ratio } (N=10)$$



$$\eta_{gearbox} = \frac{T_{out} \omega_{out}}{T_{in} \omega_{in}}$$

$$\frac{T_{out}}{T_{in}} = N \cdot \eta_{gearbox}$$

DC motor gearing

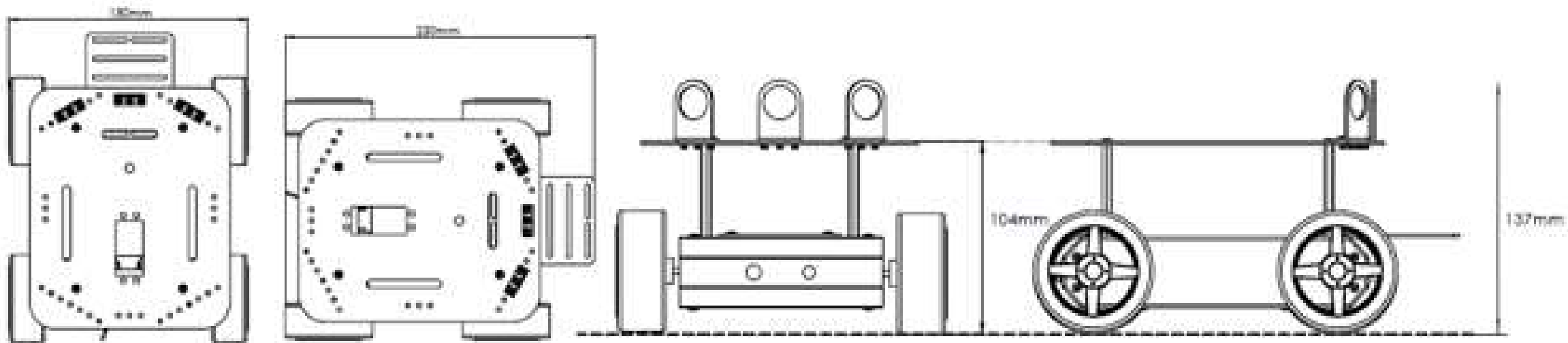


Motor Feature :

- Gear Ratio : 1:120
- No-load speed (3V): 100RPM
- No-load speed (6V): 200RPM
- No-load current (3V): 60mA
- No-load current (6V): 71mA
- Stall current (3V): 260mA
- Stall current (6V): 470mA
- Torque (3V): 1.2Kgcm
- Torque (6V): 1.92Kgcm
- Weight : 45g

Localization

- Motor diameter & gear ratio



Complete Machine Weight: 710g
Wheel Diameter : 65mm
Highest Speed: 61cm/s

Motor Feature :

- Gear Ratio : 1:120

Localization

- Motor revolutions required to drive **1 meter in a straight line**:

$$\left(\frac{120 \text{ motor rev}}{1 \text{ wheel rev}} \right)$$

$$\left(\frac{120 \text{ motor rev}}{1 \text{ wheel rev}} \right) \left(\frac{1 \text{ wheel rev}}{2\pi r \text{ meter}} \right)$$

$$\left(\frac{120 \text{ motor rev}}{1 \text{ wheel rev}} \right) \left(\frac{1 \text{ wheel rev}}{2\pi(0.0325) \text{ meter}} \right) (1 \text{ meter}) = \mathbf{587.6 \text{ motor rev}}$$

Localization

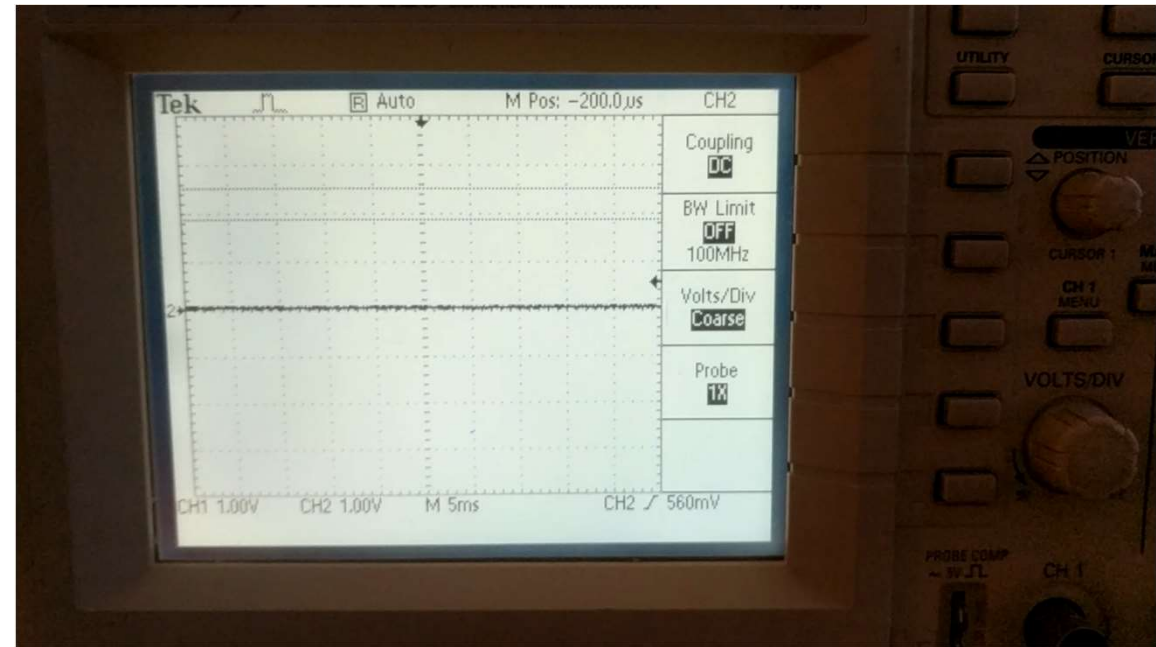
- Encoder ticks required to drive **2 meters in a straight line**:

$$\left(\frac{1 \text{ wheel rev}}{120 \text{ motor rev}} \right)$$

$$\left(\frac{1 \text{ wheel rev}}{120 \text{ motor rev}} \right) \left(\frac{1 \text{ motor rev}}{8 \text{ encoder ticks}} \right) = \left(\frac{1 \text{ wheel rev}}{960 \text{ encoder ticks}} \right) = \left(\frac{960 \text{ encoder ticks}}{1 \text{ wheel rev}} \right)$$

$$\left(\frac{1 \text{ wheel rev}}{2\pi(0.0325) \text{ meter}} \right) \left(\frac{960 \text{ encoder ticks}}{1 \text{ wheel rev}} \right) = \left(\frac{4701.2 \text{ encoder ticks}}{\text{meter}} \right)$$

$$\left(\frac{4701.2 \text{ encoder ticks}}{\text{meter}} \right) (2 \text{ meters}) = \mathbf{9402.4 \text{ encoder ticks}}$$



Localization

- Encoder ticks required to drive **2 meters in a straight line:**

$$\left(\frac{1 \text{ wheel rev}}{120 \text{ motor rev}} \right)$$

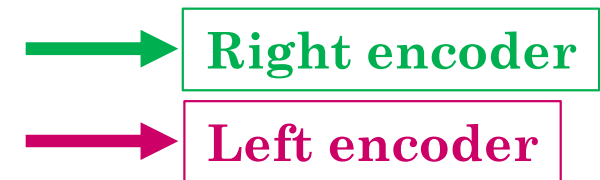
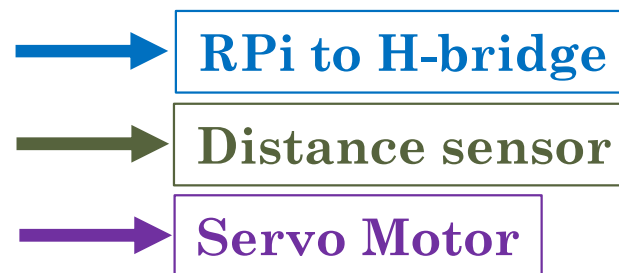
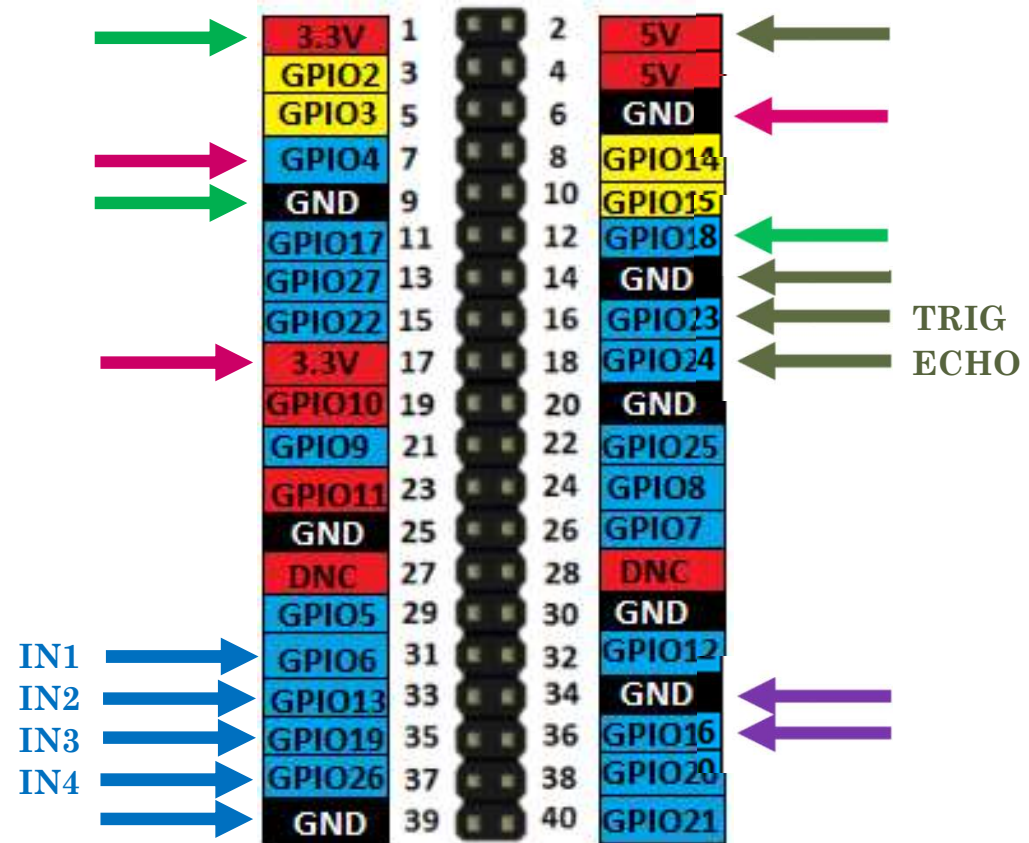
$$\left(\frac{1 \text{ wheel rev}}{20 \text{ encoder ticks}} \right) = \left(\frac{20 \text{ encoder ticks}}{1 \text{ wheel rev}} \right)$$

$$\left(\frac{1 \text{ wheel rev}}{2\pi(0.0325) \text{ meter}} \right) \left(\frac{20 \text{ encoder ticks}}{1 \text{ wheel rev}} \right) = \left(\frac{98 \text{ encoder ticks}}{\text{meter}} \right)$$

$$\left(\frac{98 \text{ encoder ticks}}{\text{meter}} \right) (2 \text{ meters}) = \mathbf{196 \text{ encoder ticks}}$$

Teleoperation

- Import RPi.GPIO library
- Utilize PWM functionality of GPIO library to control motor speed



Tracking Encoder Counts

- Setup GPIO pins as inputs

```
GPIO.setup(channel, GPIO.IN, pull_up_down=GPIO.PUD_UP)
```

1. Attach interrupts

```
GPIO.add_event_detect(channel, GPIO.RISING)
```

2. Polling

- Processor intensive

```
if GPIO.input(channel):  
    print('Input was HIGH')  
else:  
    print('Input was LOW')
```

Teleoperation

- Create new Python script: *encodercontrol01.py*
- Monitor back right encoder
- Run *encodercontrol01.py*
- Spin wheel slowly **by hand** through 1 revolution



```
pi@raspberrypi: ~
GNU nano 2.7.4 File: encodercontrol01.py Modified

import RPi.GPIO as gpio
import numpy as np

#### Initialize GPIO pins ####

def init():
    gpio.setmode(gpio.BOARD)
    gpio.setup(12, gpio.IN, pull_up_down = gpio.PUD_UP)

def gameover():
    gpio.cleanup()

#### Main code ####
init()

counter = np.uint64(0)
button = int(0)

while True:

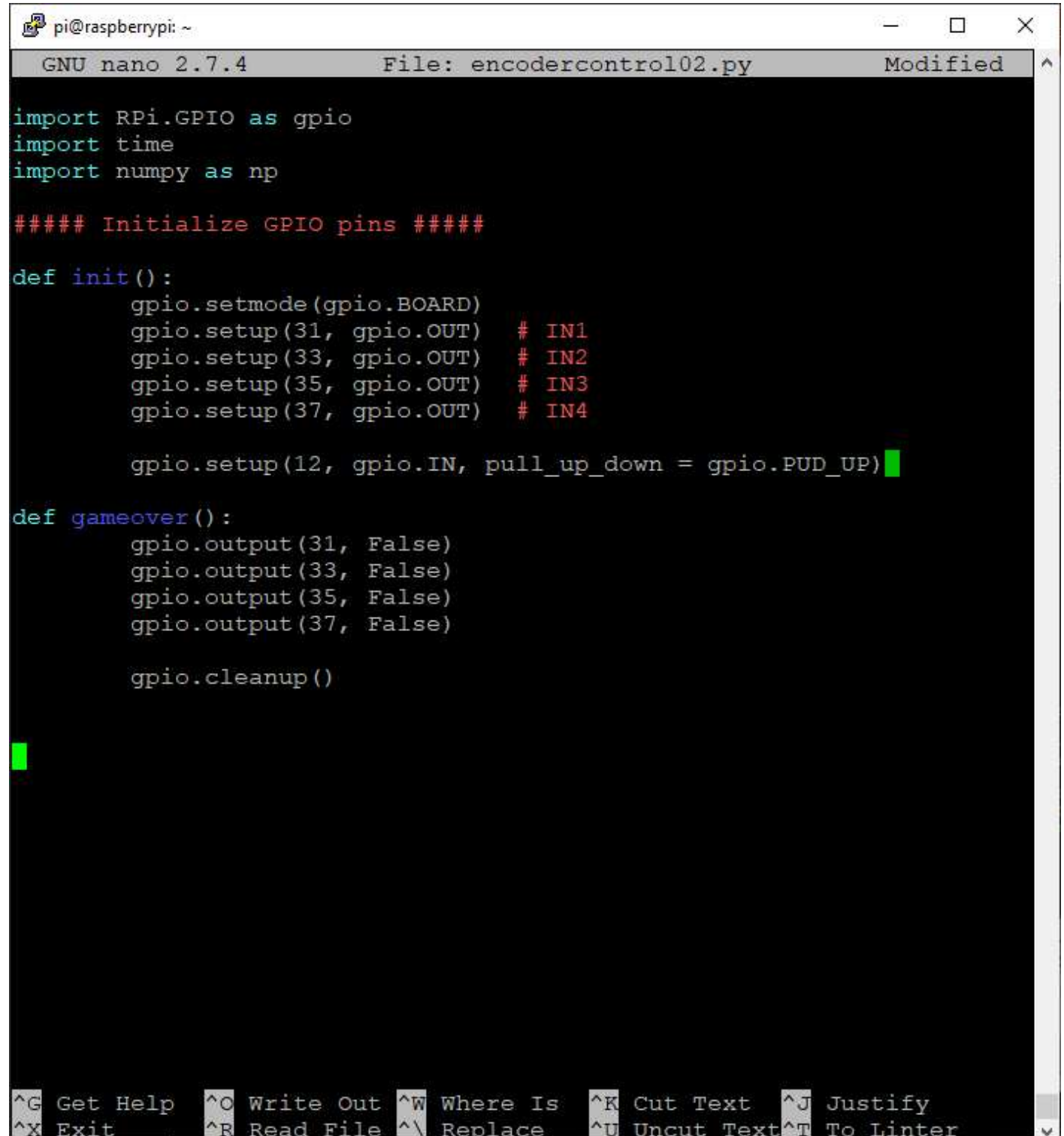
    if int(gpio.input(12)) != int(button):
        button = int(gpio.input(12))
        counter += 1
        print(counter)

    if counter >= 960:
        gameover()
        print("Thanks for playing!")
        break

[ Cancelled ]
^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify
^X Exit ^R Read File ^\ Replace ^U Uncut Text ^T To Linter
```

Teleoperation

- Create new Python script: *encodercontrol02.py*
- Drive both right-side motors using PWM
- Monitor back right encoder



```
pi@raspberrypi: ~
GNU nano 2.7.4      File: encodercontrol02.py      Modified

import RPi.GPIO as gpio
import time
import numpy as np

##### Initialize GPIO pins #####

def init():
    gpio.setmode(gpio.BOARD)
    gpio.setup(31, gpio.OUT)      # IN1
    gpio.setup(33, gpio.OUT)      # IN2
    gpio.setup(35, gpio.OUT)      # IN3
    gpio.setup(37, gpio.OUT)      # IN4

    gpio.setup(12, gpio.IN, pull_up_down = gpio.PUD_UP)

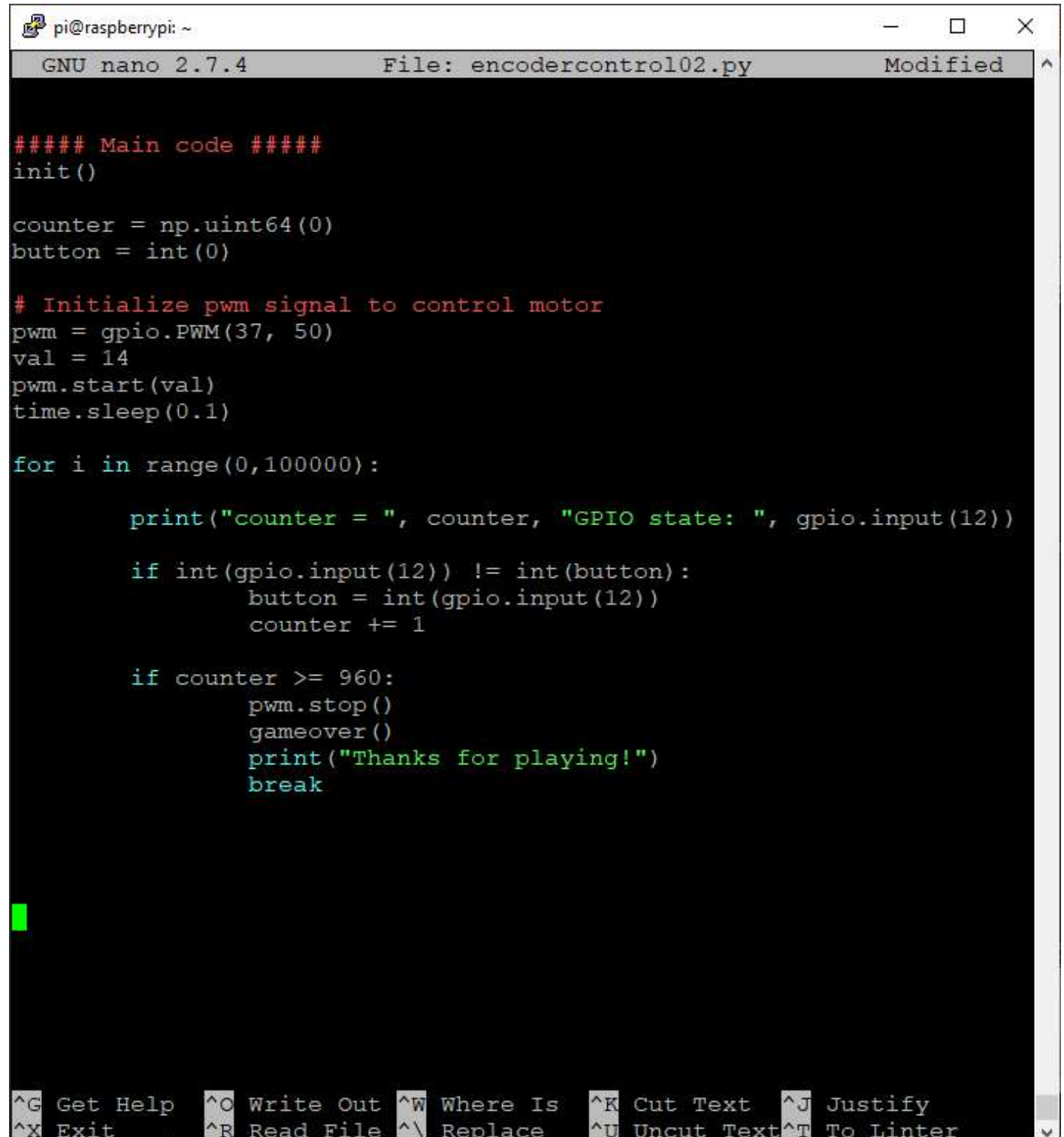
def gameover():
    gpio.output(31, False)
    gpio.output(33, False)
    gpio.output(35, False)
    gpio.output(37, False)

    gpio.cleanup()

^G Get Help  ^O Write Out ^W Where Is  ^K Cut Text  ^J Justify
^X Exit      ^R Read File ^\ Replace   ^U Uncut Text ^T To Linter
```


Teleoperation

- Create new Python script: *encodercontrol02.py*
- Drive both right-side motors using PWM
- Monitor back right encoder



```
pi@raspberrypi: ~
GNU nano 2.7.4      File: encodercontrol02.py      Modified

##### Main code #####
init()

counter = np.uint64(0)
button = int(0)

# Initialize pwm signal to control motor
pwm = gpio.PWM(37, 50)
val = 14
pwm.start(val)
time.sleep(0.1)

for i in range(0,100000):

    print("counter = ", counter, "GPIO state: ", gpio.input(12))

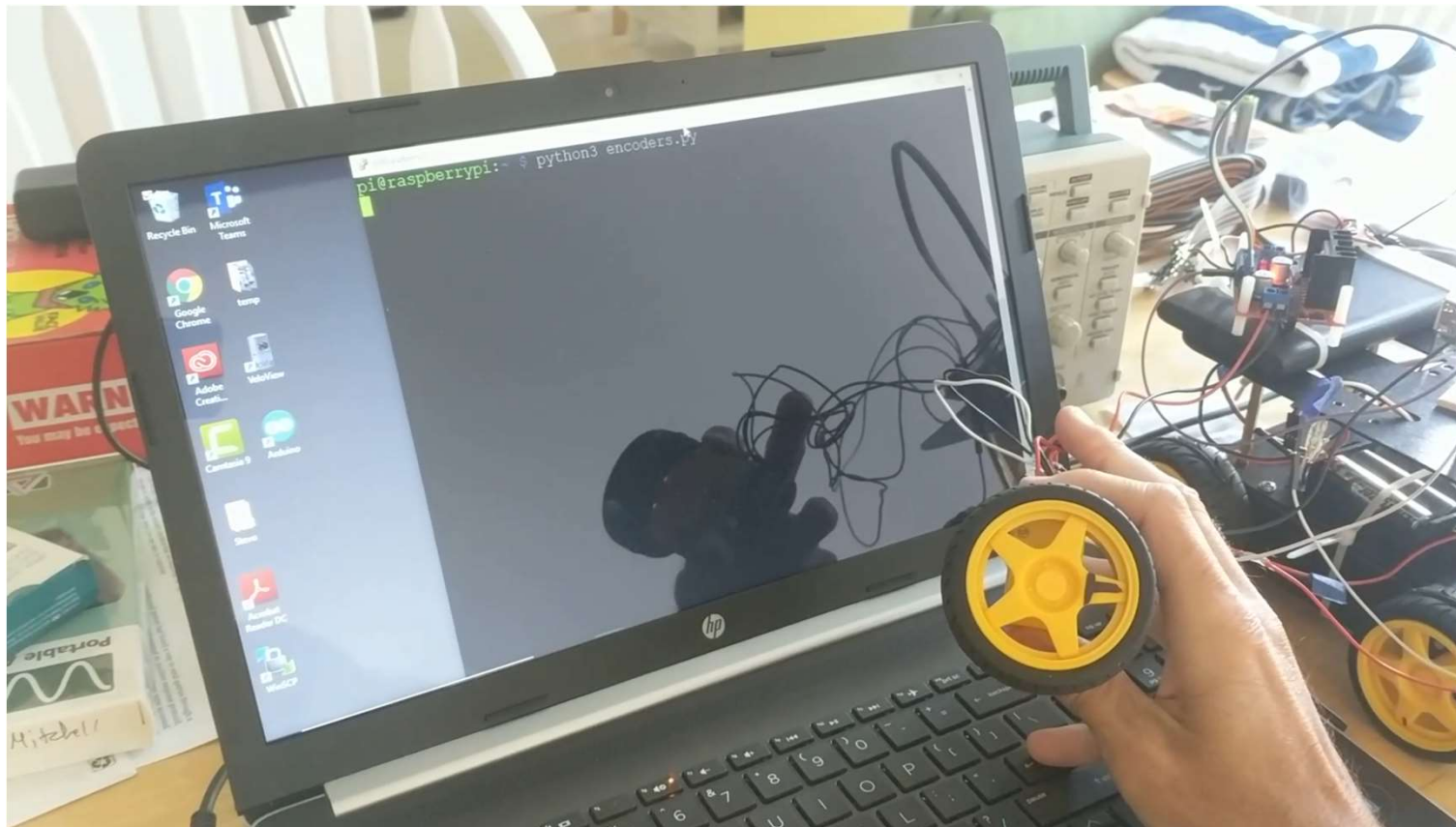
    if int(gpio.input(12)) != int(button):
        button = int(gpio.input(12))
        counter += 1

    if counter >= 960:
        pwm.stop()
        gameover()
        print("Thanks for playing!")
        break

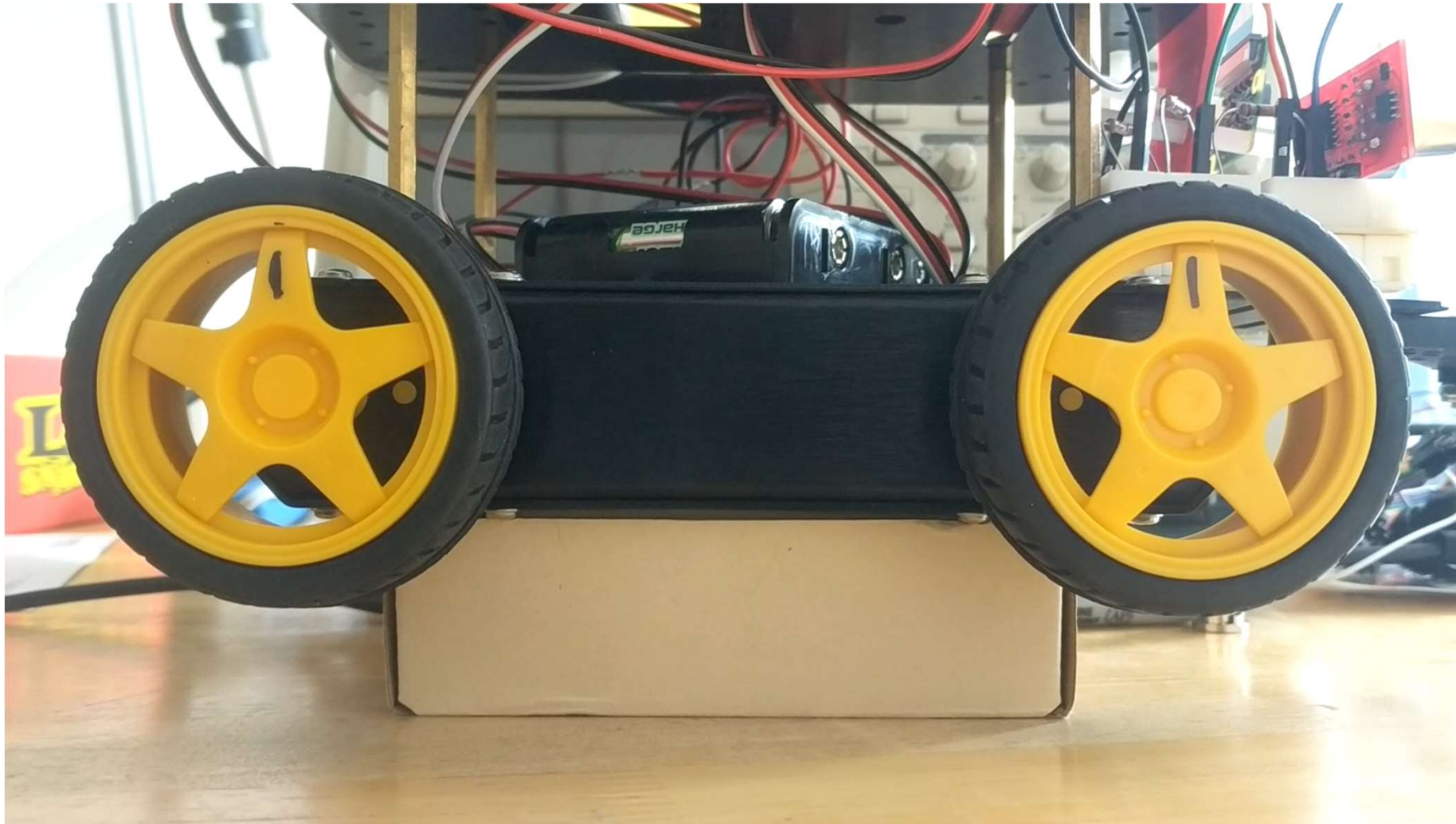
^G Get Help  ^O Write Out ^W Where Is  ^K Cut Text  ^J Justify
^X Exit      ^R Read File ^\ Replace   ^U Uncut Text ^T To Linter
```


Teleoperation

- Run *encodercontrol02.py*
- Confirm wheels rotate through 1 rev & 960 encoder ticks

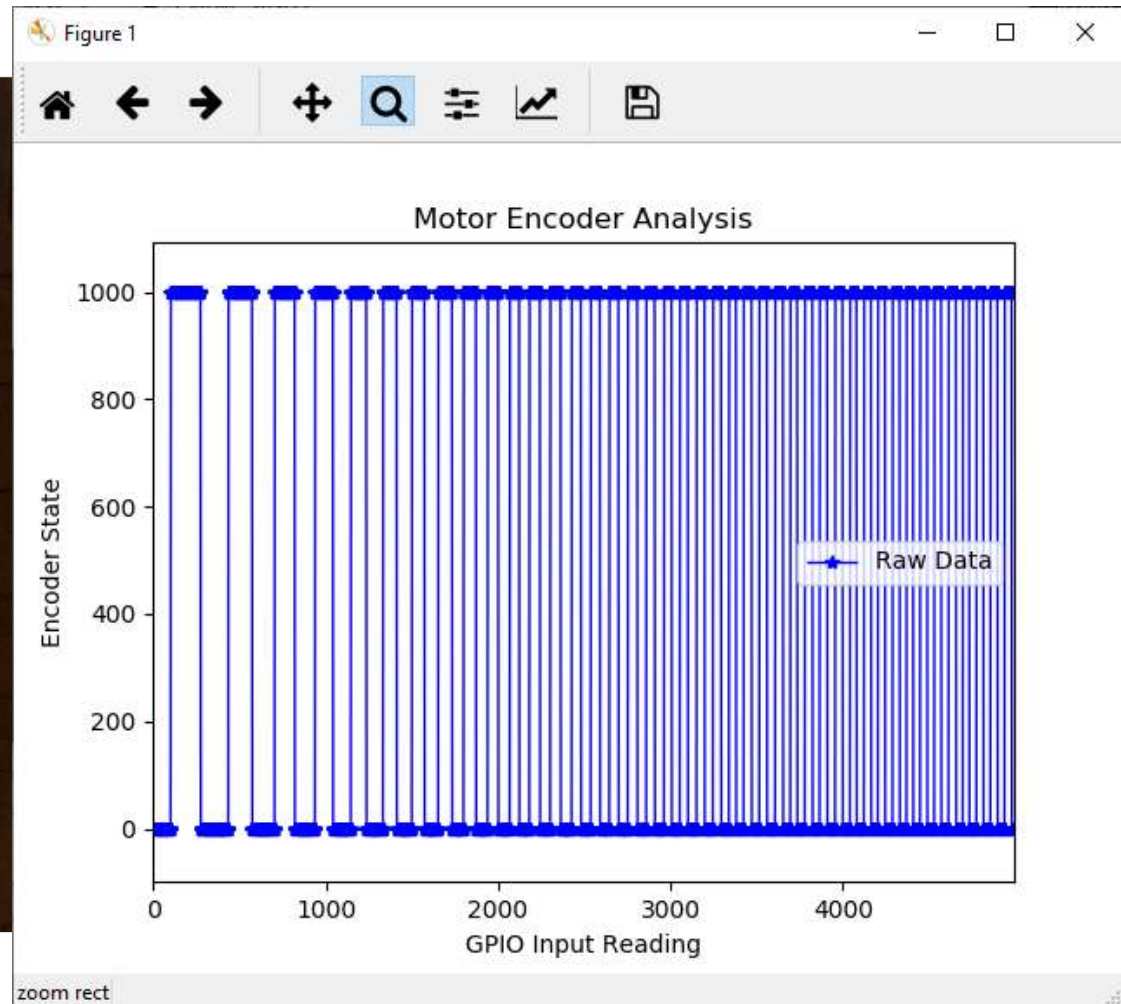
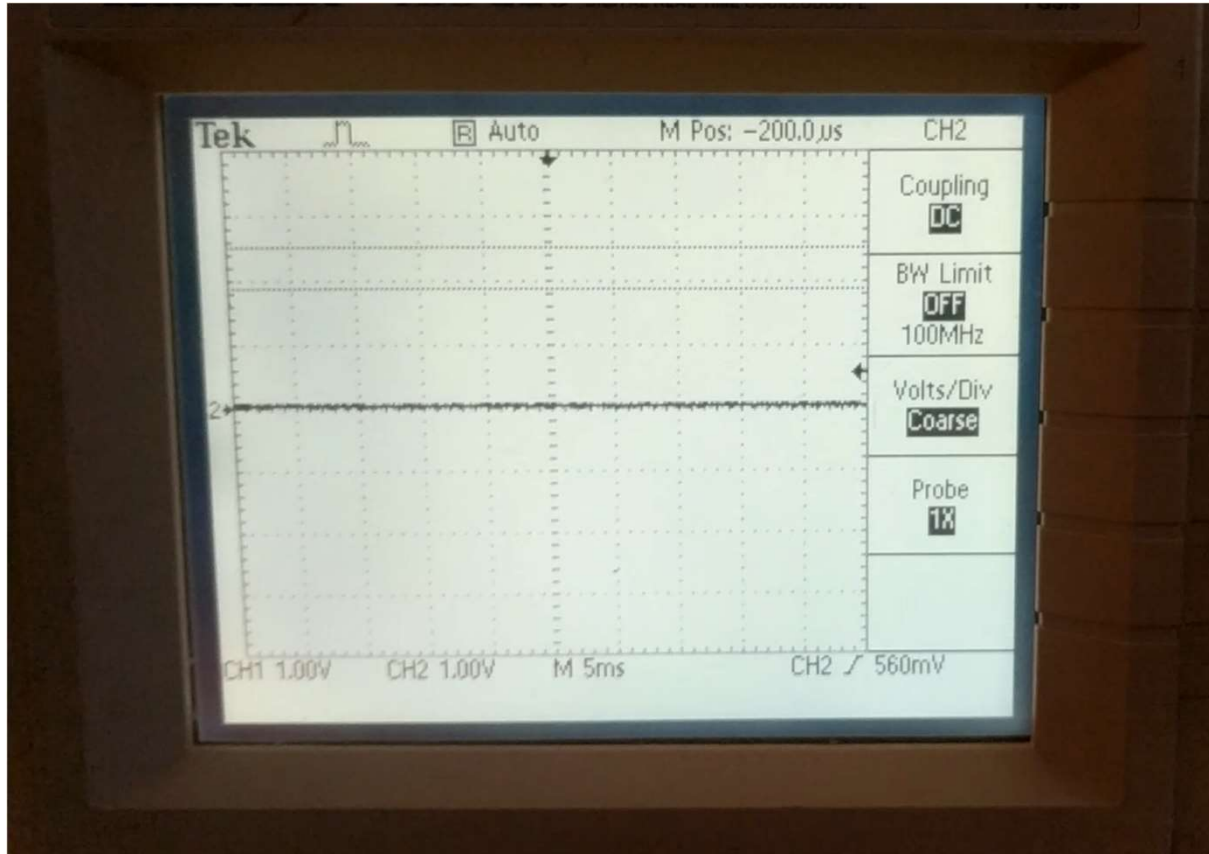


Localization Errors



In-Class Exercise

- Update *encodercontrol02.py* to save encoder states to .txt file
- Open & plot data in Matplotlib



Teleoperation

- Create new Python script:
encodercontrol03.py
- Drive right-side wheels only
- Track both encoders (left & right)


```
pi@raspberrypi: ~
GNU nano 2.7.4 File: encodercontrol03.py Modified
import RPi.GPIO as gpio
import time
import numpy as np

#### Initialize GPIO pins ####

def init():
    gpio.setmode(gpio.BOARD)
    gpio.setup(31, gpio.OUT) # IN1
    gpio.setup(33, gpio.OUT) # IN2
    gpio.setup(35, gpio.OUT) # IN3
    gpio.setup(37, gpio.OUT) # IN4

    gpio.setup(7, gpio.IN, pull_up_down = gpio.PUD_UP)
    gpio.setup(12, gpio.IN, pull_up_down = gpio.PUD_UP)

def gameover():
    gpio.output(31, False)
    gpio.output(33, False)
    gpio.output(35, False)
    gpio.output(37, False)

    gpio.cleanup()

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos ^Y Prev Page M-^ First Line
^X Exit ^R Read File ^\ Replace ^U Uncut Text ^T To Linter ^_ Go To Line ^V Next Page M-^ Last Line
```

```
pi@raspberrypi: ~
GNU nano 2.7.4 File: encodercontrol03.py Modified
##### Main code #####
init()
counterBR = np.uint64(0)
counterFL = np.uint64(0)

buttonBR = int(0)
buttonFL = int(0)

# initialize pwm signal to control motor
pwm = gpio.PWM(37, 50)
val = 16
pwm.start(val)
time.sleep(0.1)

for i in range(0,200000):

    print("counterBR: ", counterBR, "counterFL: ", counterFL, "BR state: ", gpio.input(12), "FL state: ", gpio.input(7))

    if int(gpio.input(12)) != int(buttonBR):
        buttonBR = int(gpio.input(12))
        counterBR += 1

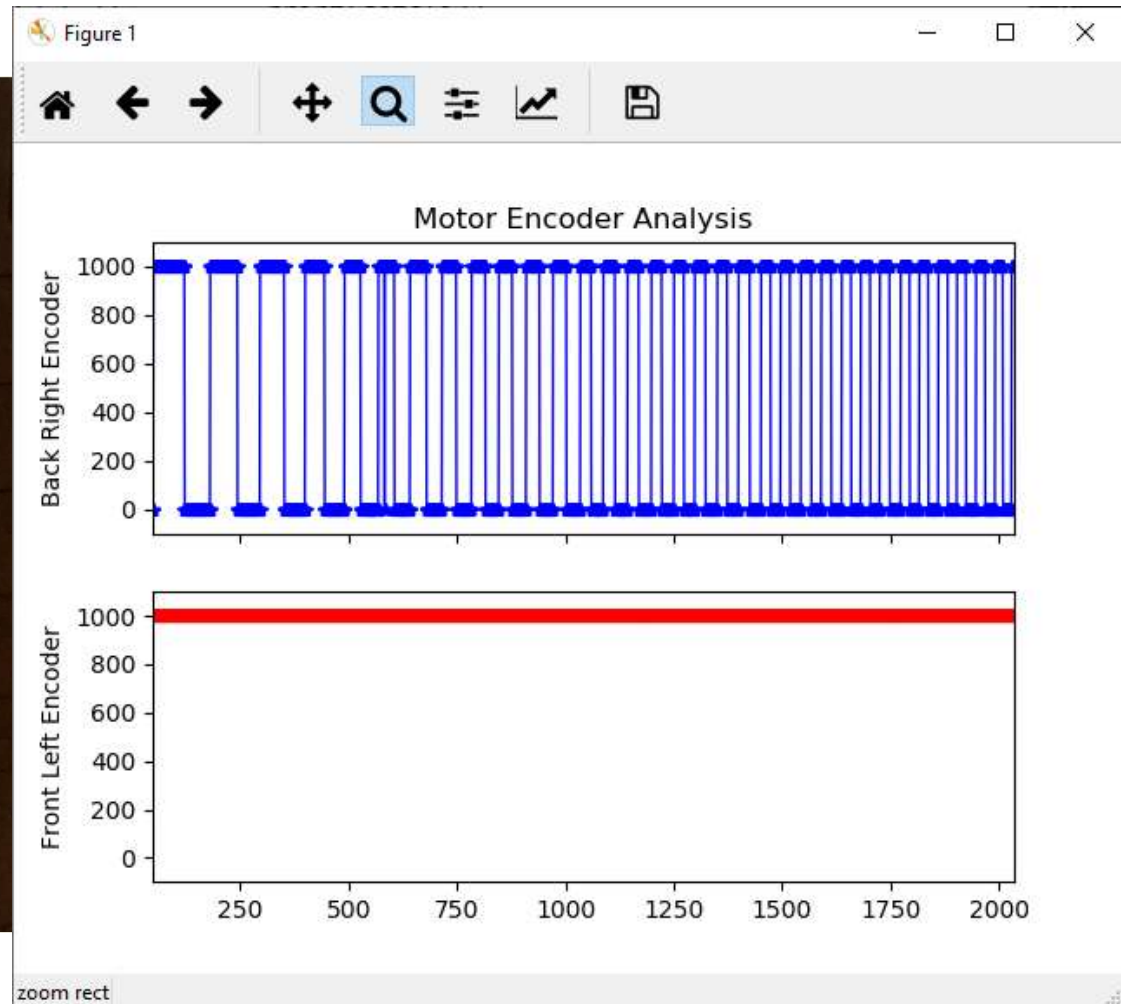
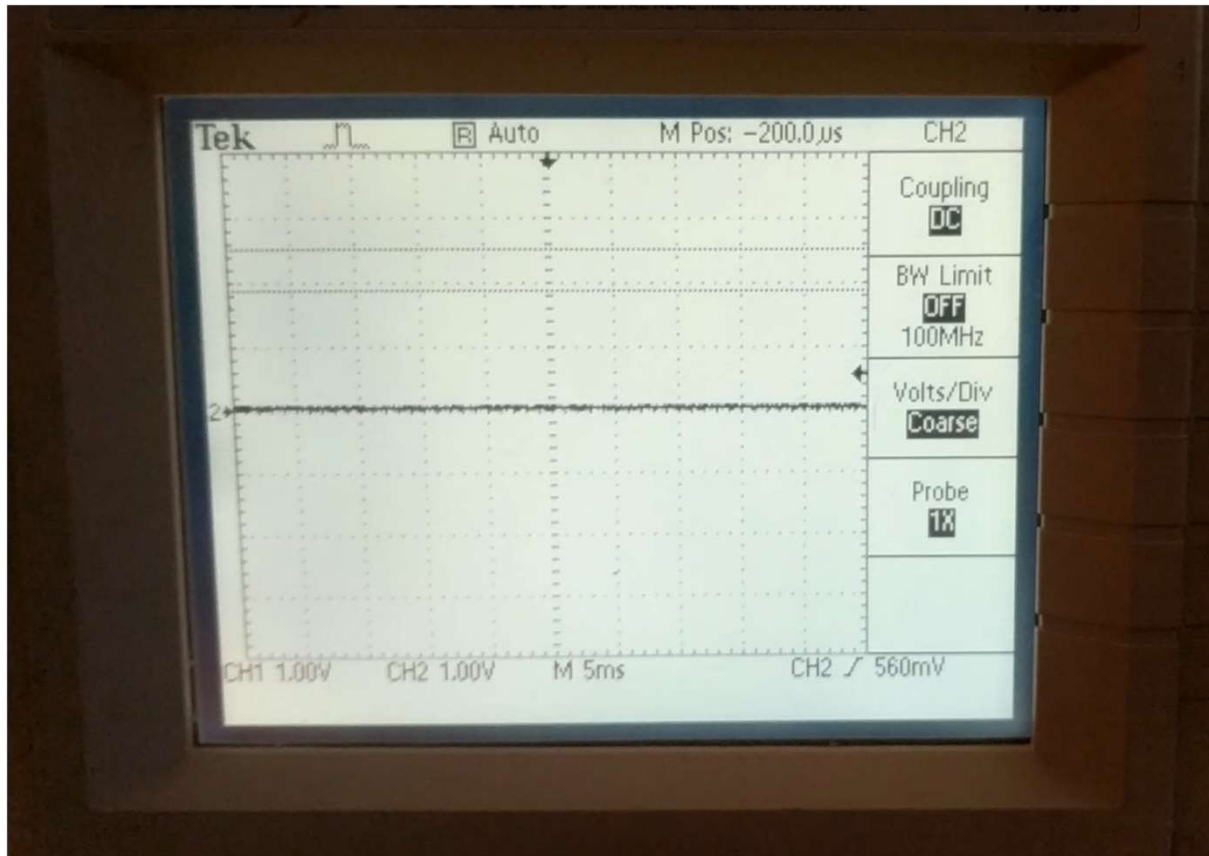
    if int(gpio.input(7)) != int(buttonFL):
        buttonFL = int(gpio.input(7))
        counterFL += 1

    if counterBR >= 960:
        pwm.stop()
        gameover()
        print("Thanks for playing!")
        break
```

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos ^Y Prev Page M-^ First Line
^X Exit ^R Read File ^\ Replace ^U Uncut Text ^T To Linter ^_ Go To Line ^V Next Page M-/_ Last Line

In-Class Exercise

- Update *encodercontrol03.py* to save both encoder states to .txt file
- Open & subplot all data in Matplotlib



Localization Errors

Teleoperation

- Create new Python script:
encodercontrol04.py
- Drive all four motors
- Track both encoders (left & right)

```
pi@raspberrypi: ~
GNU nano 2.7.4 File: encodercontrol04.py Modified
import RPi.GPIO as gpio
import time
import numpy as np

##### Initialize GPIO pins #####

def init():
    gpio.setmode(gpio.BOARD)
    gpio.setup(31, gpio.OUT) # IN1
    gpio.setup(33, gpio.OUT) # IN2
    gpio.setup(35, gpio.OUT) # IN3
    gpio.setup(37, gpio.OUT) # IN4

    gpio.setup(7, gpio.IN, pull_up_down = gpio.PUD_UP)
    gpio.setup(12, gpio.IN, pull_up_down = gpio.PUD_UP)

def gameover():
    gpio.output(31, False)
    gpio.output(33, False)
    gpio.output(35, False)
    gpio.output(37, False)

    gpio.cleanup()

#####
```

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos ^Y Prev Page M-\ First Line
^X Exit ^R Read File ^\ Replace ^U Uncut Text ^T To Linter ^_ Go To Line ^V Next Page M-/ Last Line

```
pi@raspberrypi: ~
GNU nano 2.7.4 File: encodercontrol04.py Modified
##### Main code #####
init()
counterFL = np.uint64(0)
counterBR = np.uint64(0)

buttonFL = int(0)
buttonBR = int(0)

# Independent motor control via pwm
pwm1 = gpio.PWM(31, 50) # BackLeft motor
pwm2 = gpio.PWM(37, 50) # FrontRight motor
val = 22
pwm1.start(val)
pwm2.start(val)
time.sleep(0.1)

for i in range(0,100000):
    print("counterBR: ", counterBR, "counterFL: ", counterFL, "BR state: ", gpio.input(12), "FL state: ", gpio.input(7))
    if int(gpio.input(12)) != int(buttonBR):
        buttonBR = int(gpio.input(12))
        counterBR += 1

    if int(gpio.input(7)) != int(buttonFL):
        buttonFL = int(gpio.input(7))
        counterFL += 1

    if counterFL >= 960:
        pwm1.stop()

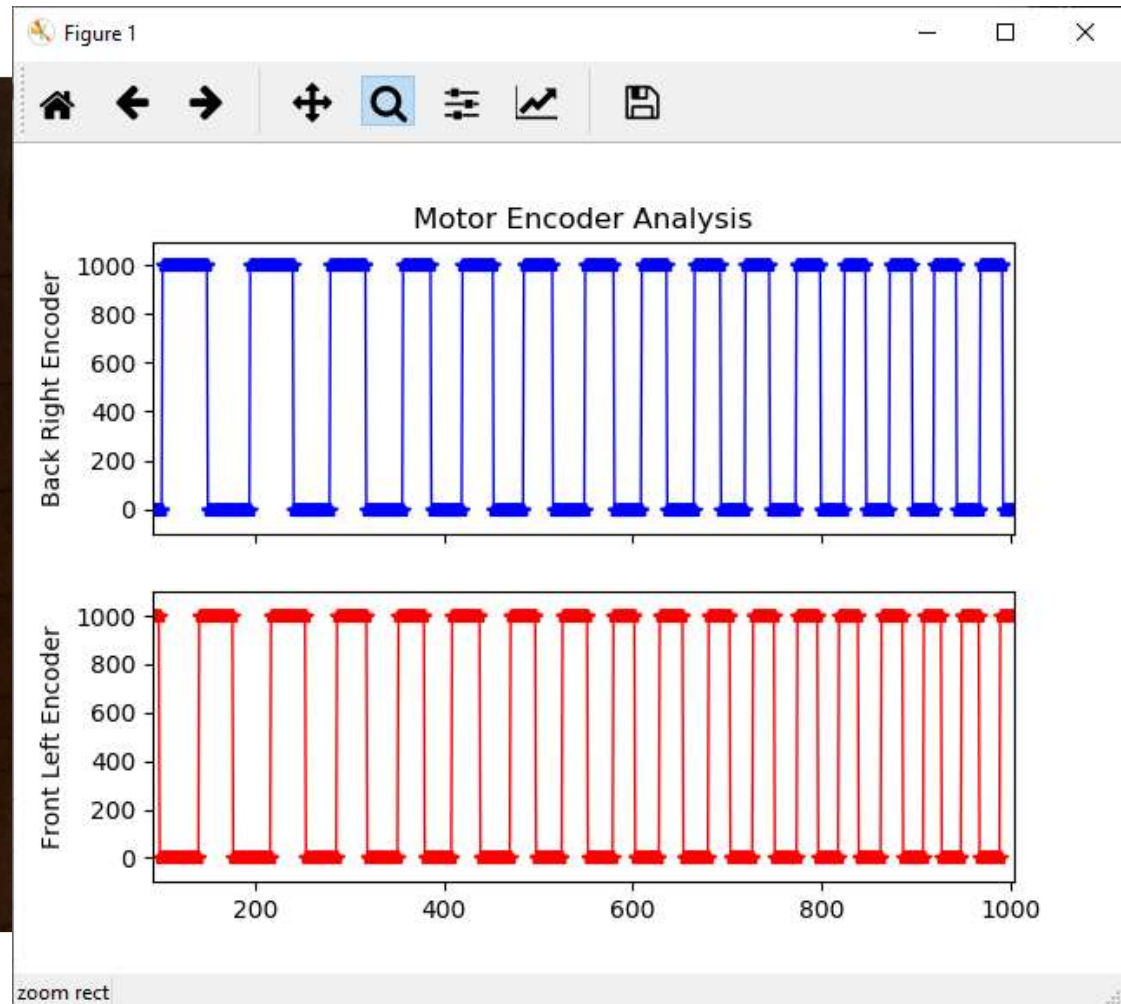
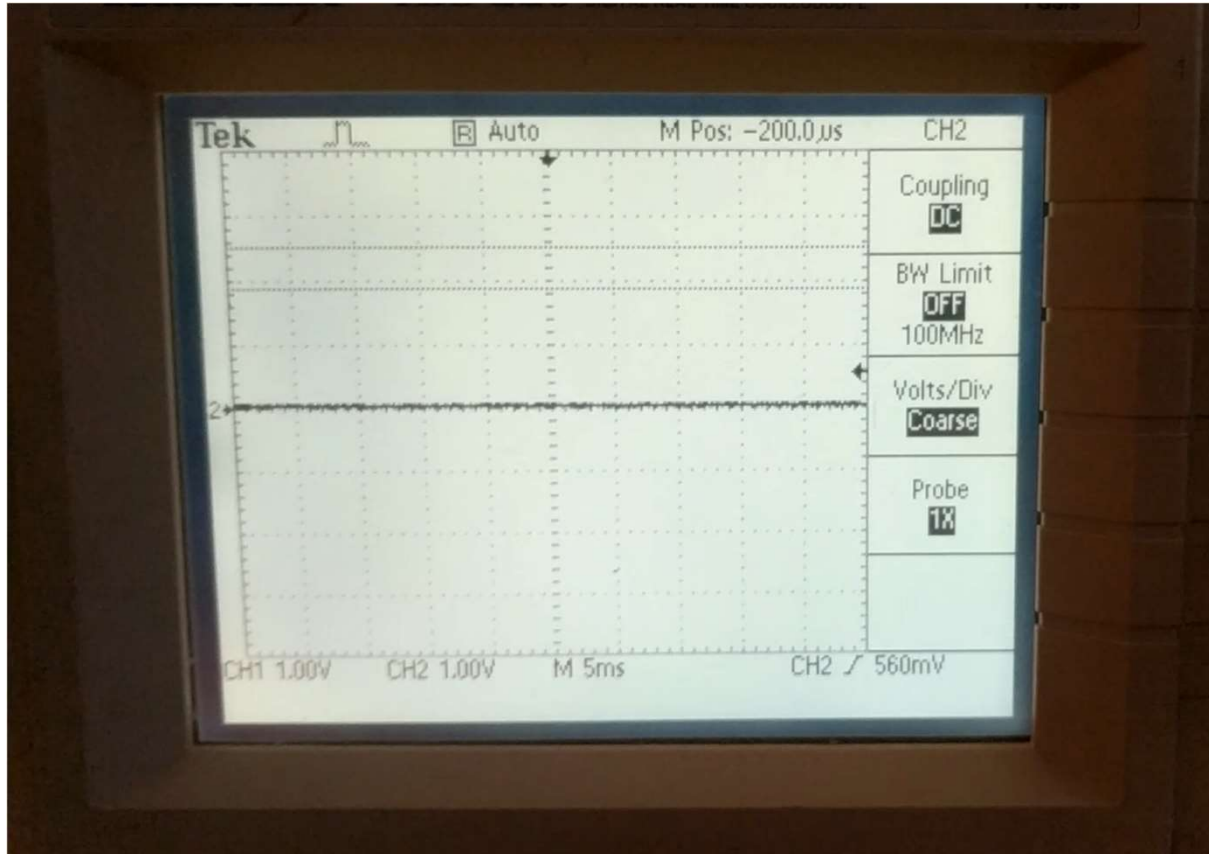
    if counterBR >= 960:
        pwm2.stop()

    if counterBR >= 960 and counterFL >= 960:
        gameover()
        break

^G Get Help ^O Write Out ^W Where Is ^K Cut Text ^J Justify ^C Cur Pos ^Y Prev Page M-\ First Line
^X Exit ^R Read File ^\ Replace ^U Uncut Text ^T To Linter ^_ Go To Line ^V Next Page M-/ Last Line
```

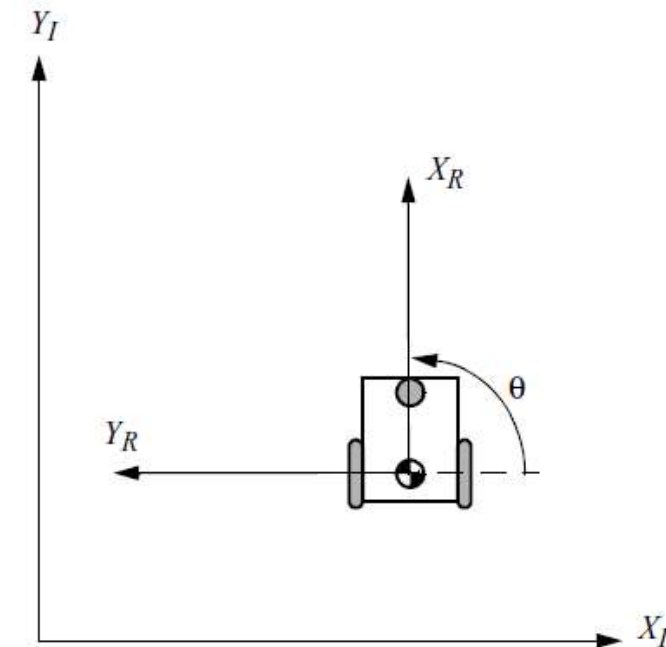
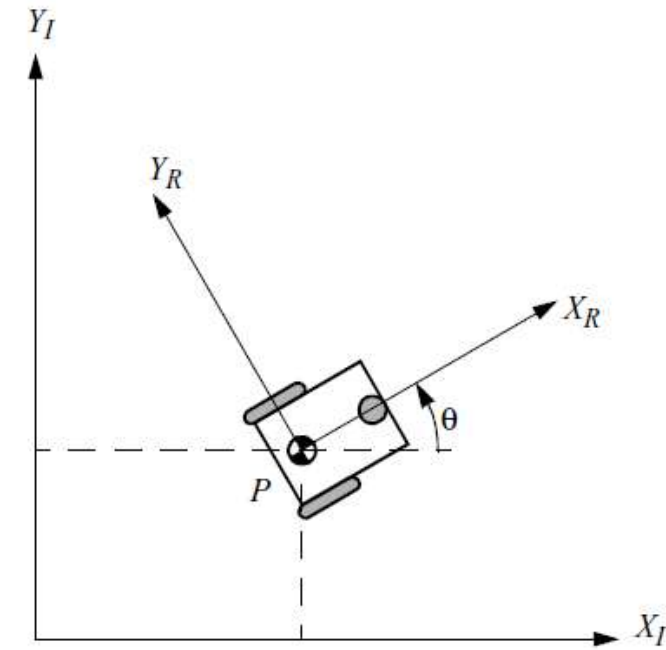
In-Class Exercise

- Update *encodercontrol04.py* to save both encoder states to .txt file
- Open & subplot all data in Matplotlib

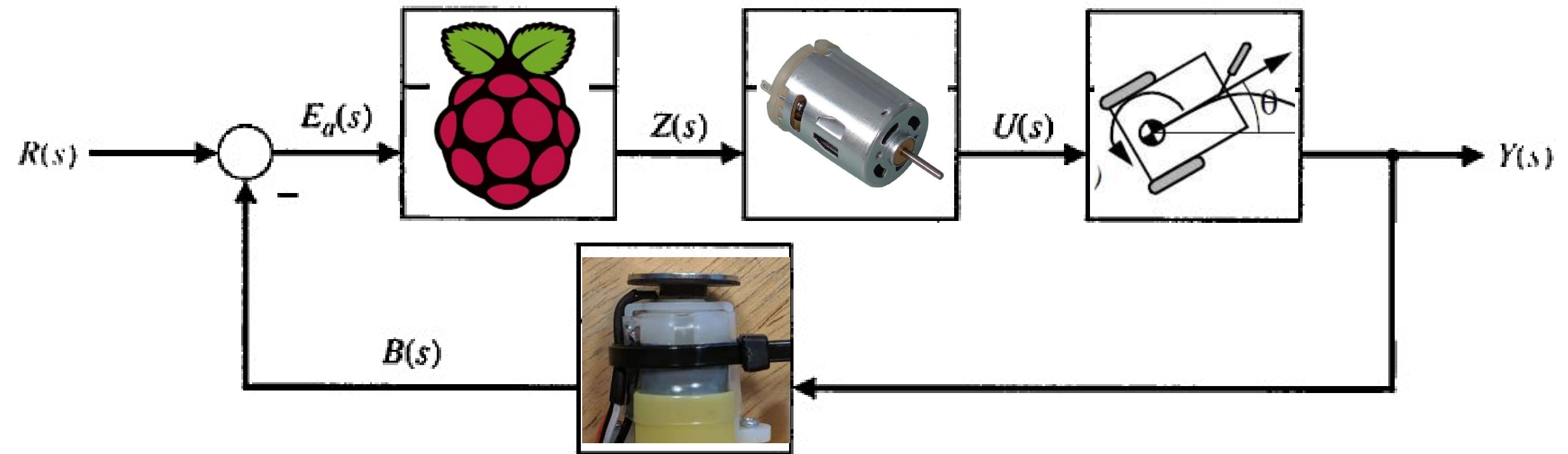


Kinematics

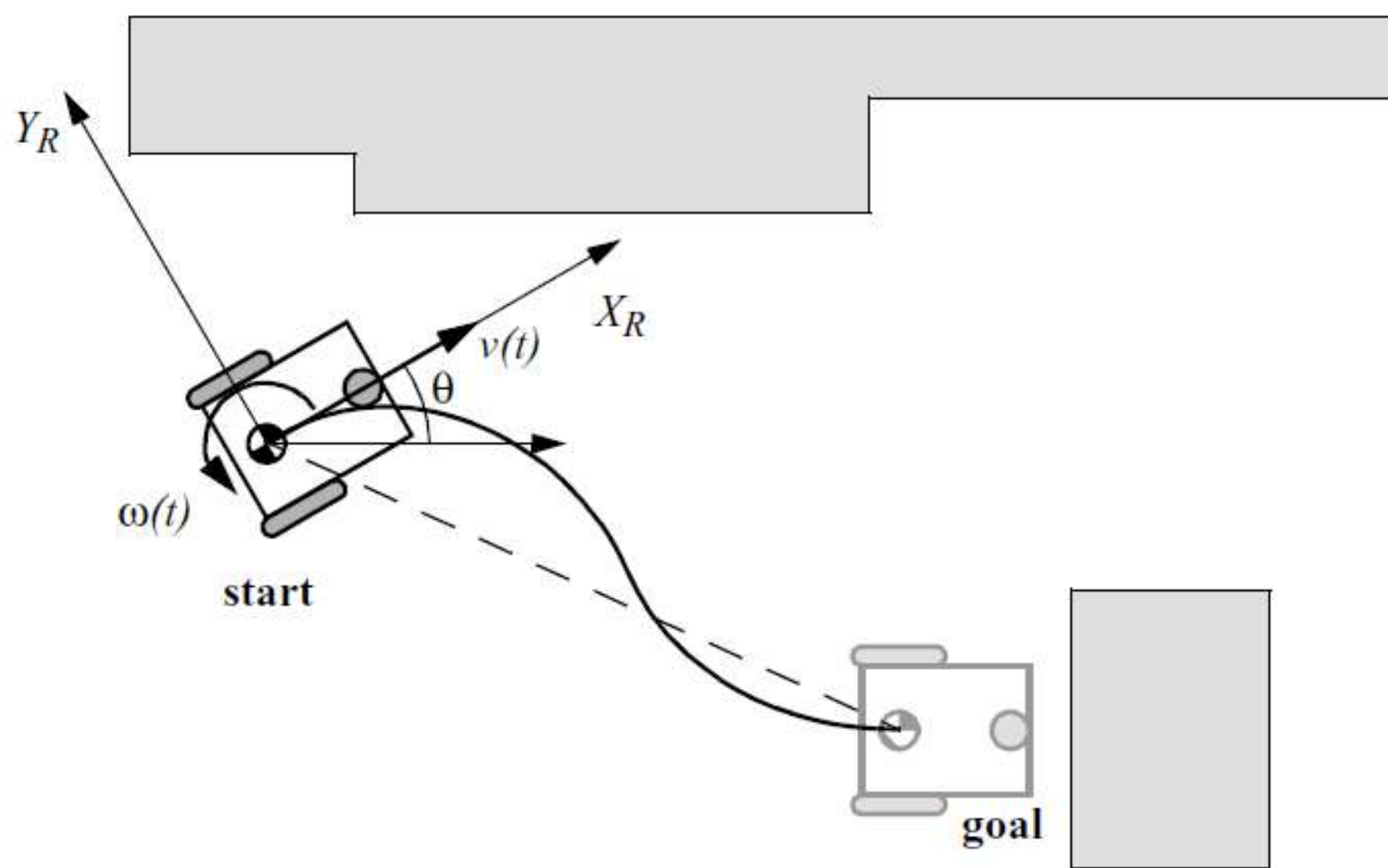
- Study of how mechanical systems behave
- Mobile robotics
 - Design for specific tasks
 - Create control software to drive hardware
- Global reference frame & robot local reference frame



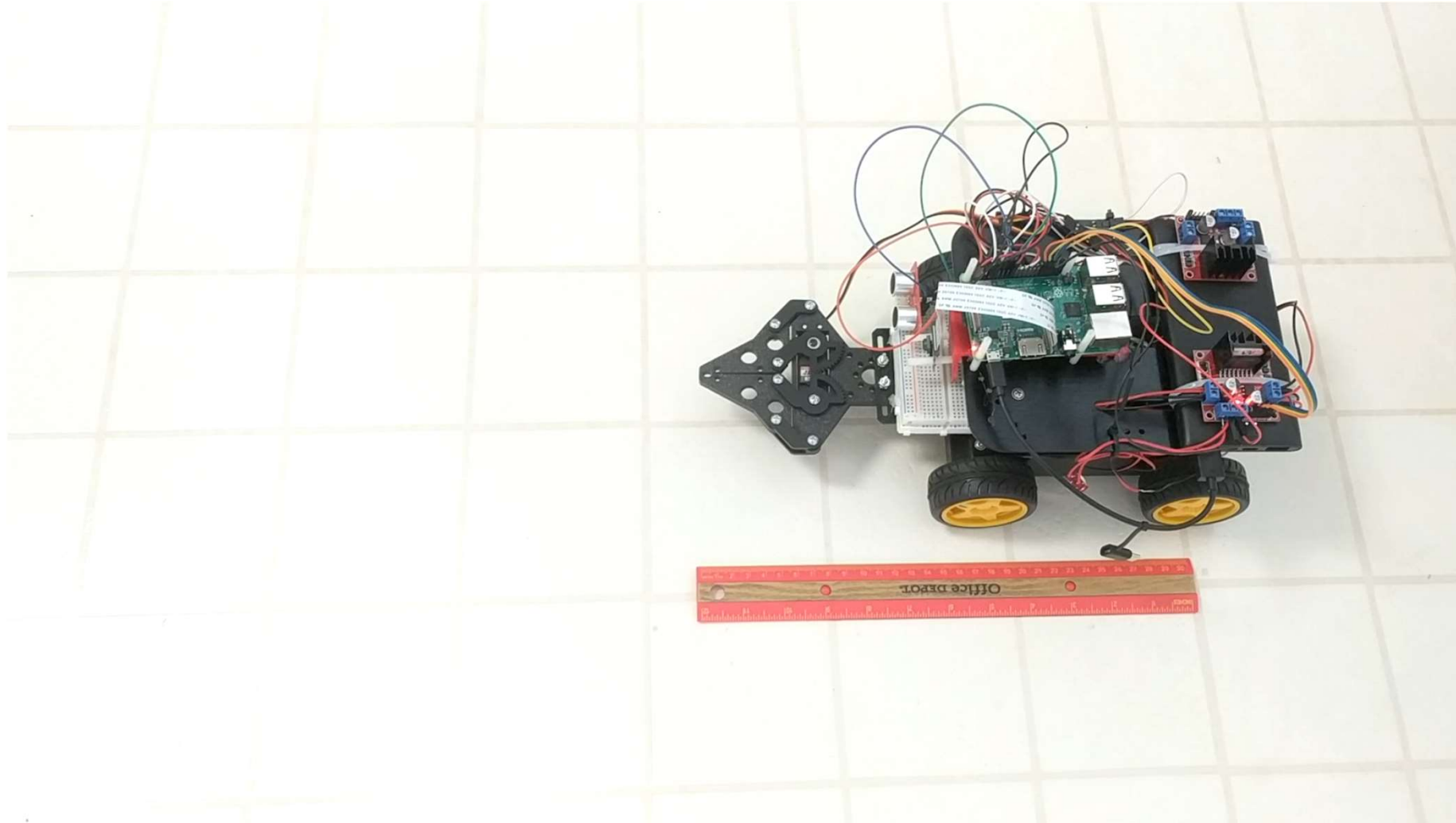
Control Theory



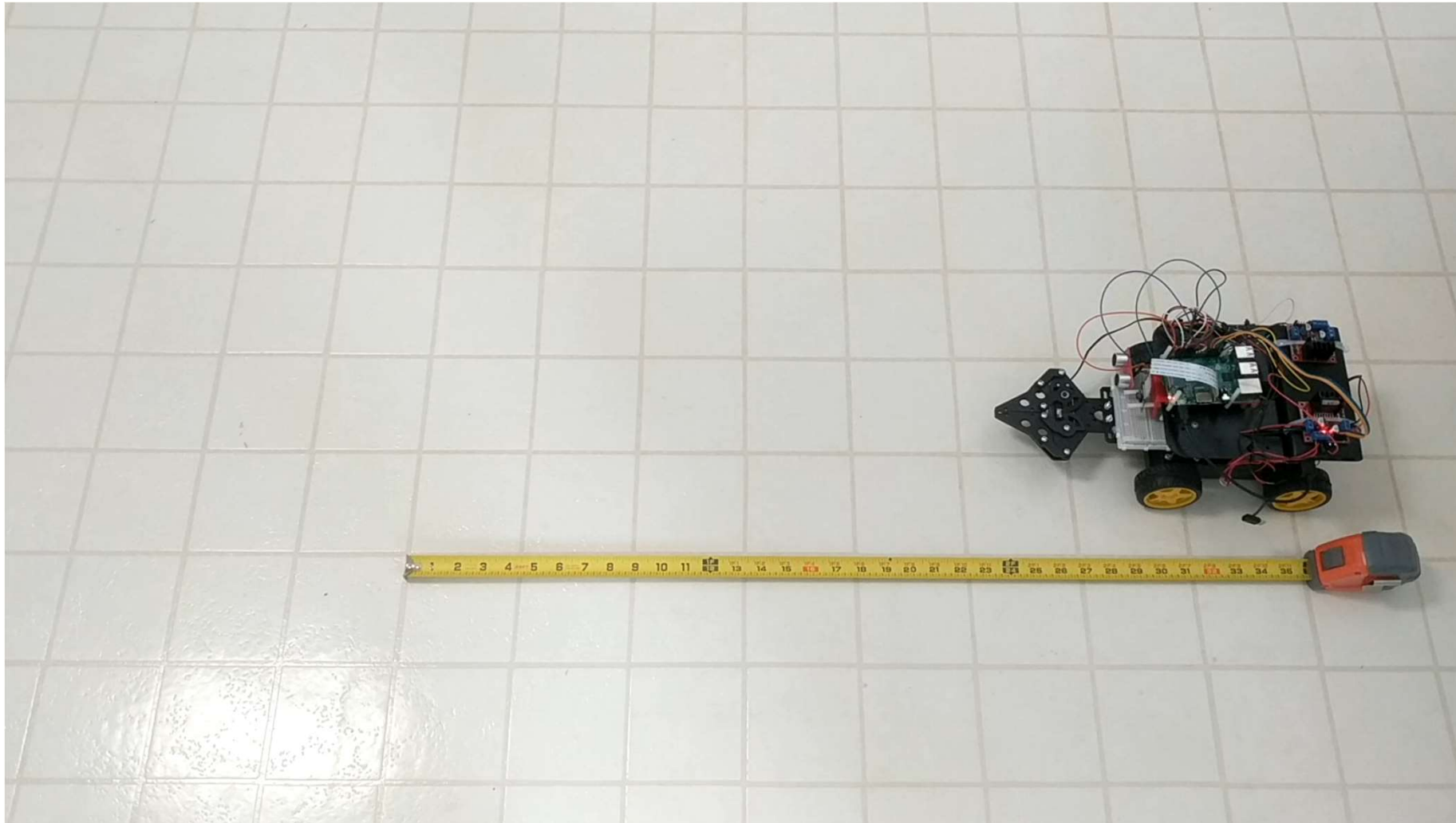
Kinematics & Localization



Kinematics & Localization



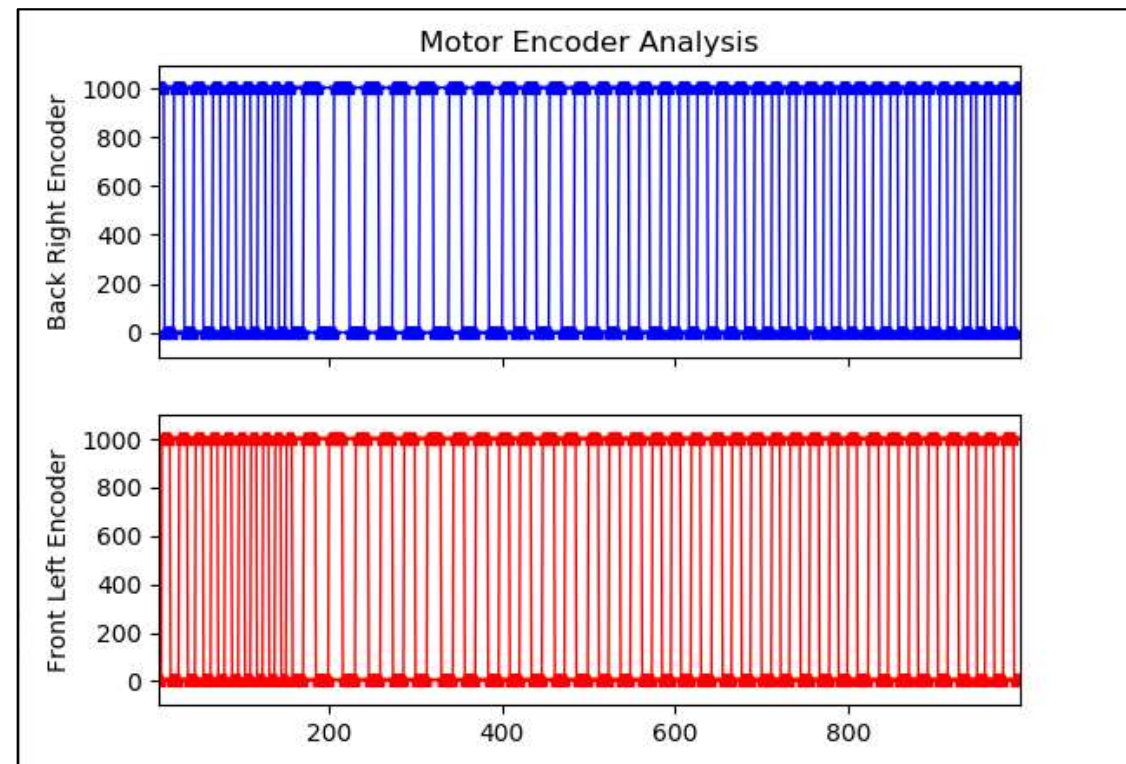
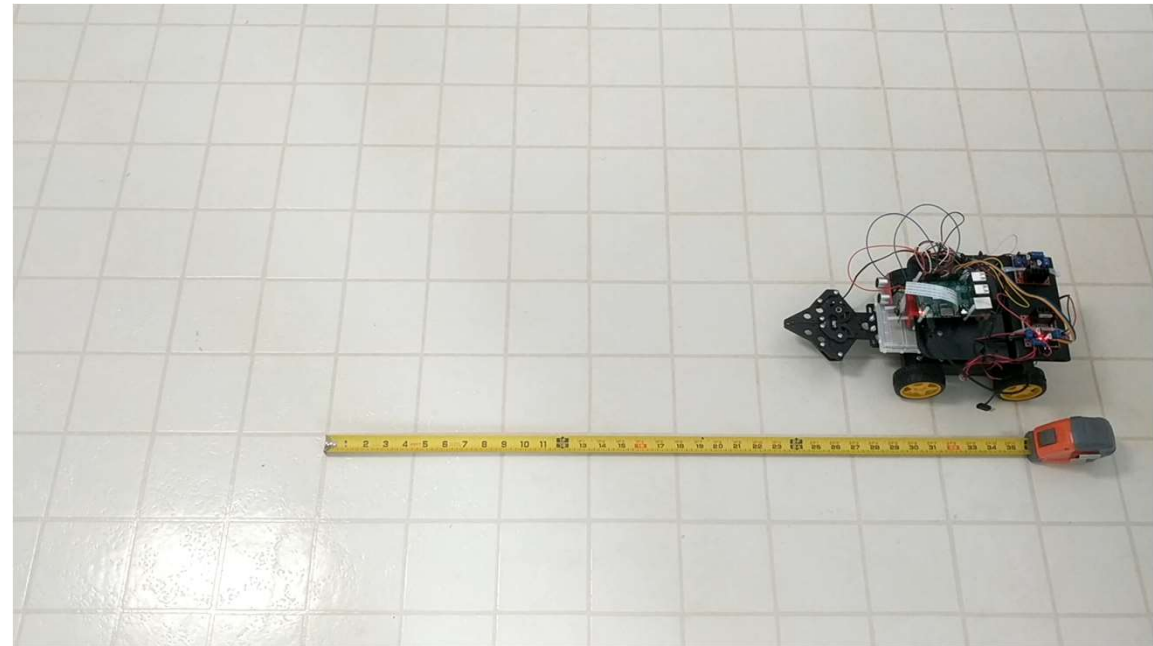
Kinematics & Localization



In-Class Exercise

- Create new Python script *encodercontrol05.py*
- Script must:
 1. Drive robot in straight line for a user-defined distance
 2. Record encoder data from both encoders
- Open & subplot all data in Matplotlib

$$\left(\frac{1 \text{ wheel rev}}{2\pi(0.0325)\text{meter}} \right) (x \text{ meters}) = \# \text{ wheel rev}$$



References

- *Introduction to Autonomous Mobile Robots*, Siegwart
 - Chapter 5
- *Wheel Encoder Kit*, Sparkfun
 - <https://www.sparkfun.com/products/12629>
- RedBot Assembly Guide
 - https://learn.sparkfun.com/tutorials/redbot-assembly-guide-rev-02/wheel-encoder?_ga=2.100473117.2032092491.1562591960-231095067.1560280769
- Rpi.GPIO
 - <https://pypi.org/project/RPi.GPIO/>
- Resolution, Accuracy, and Precision of Encoders
 - <https://cdn.usdigital.com/assets/general/usd-encoder-precision.pdf>