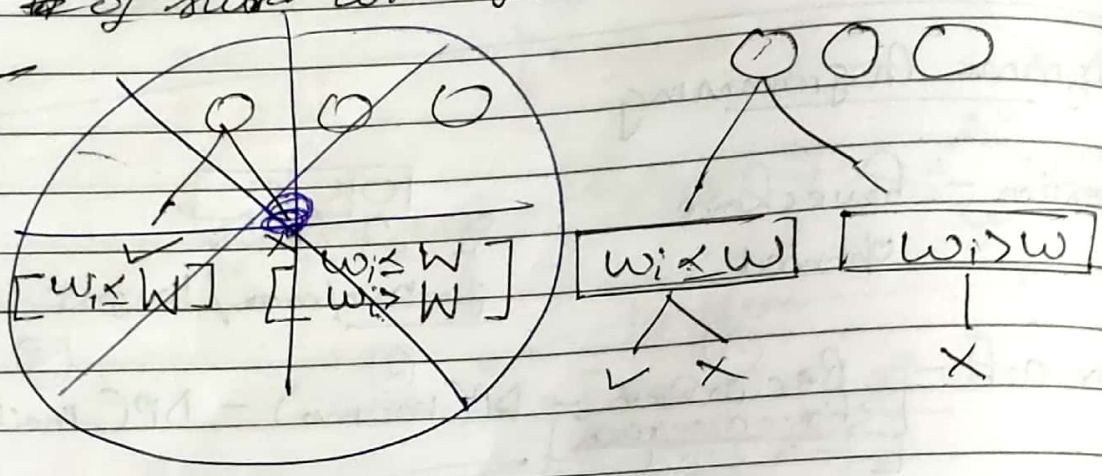
0-1 knapsack

- ✓ Subset sum
- ✓ equal sum partition
- count of subset sum
- ✓ min subset sum diff
- ✓ target sum
- # of subset with given diff

Recursive



Base Condn

```
if (n == 0 or w == 20)
    return 0
```

wt [| | |] n == 0

val [| | |]

w w = 0

choice diagram

```
if wt[n-1] <= w:
    return max( val[n-1] + solve( w-wt[n-1], ... ),
                solve( ... ) )
else:
    return solve( ... )
```

memoization

Base cond^n

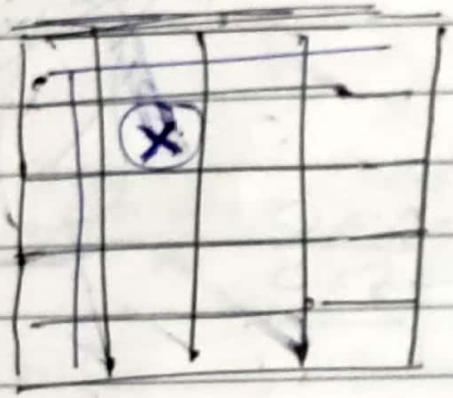
```
if memo[][] != None
    return memo[][]
```

choice tree

```
memo[][] = ans
return memo[x]
```

[disadvantage: Stack overflow | little slower]

tabulation



if (wt[j] -

① initialization → base cond^n

② solve → memo

i —

j —

0-1 knapsack bottom-up

Recursive → bottom-up

take item according to matrix

(1) Solve (n, w)

{

(2) # base condition
if (n == 0 or w == 0)
return 0

(3) # choice diagram
w - wt[n-1]
if ~~wt[n-1] - w~~ >= 0:
return max(
val[n-1] + solve(w - wt[n-1]),
solve(n-1, w)
)

else:
return solve(n-1, w)

memo = [[None for (n+1)]
for (w+1)]

# base cond^n
for (i = (0 → n+1))
for (j = (0 → w+1))
if i == 0 or j == 0
memo[i][j] = 0

choice diagram
for n in range (1, n+1)
for w in range (1, w+1)

~~if wt[n-1] - w >= 0~~
if (w - wt[n-1]) >= 0
memo[n][w] = max(
val[n-1] + t[n-1][w - wt[n-1]],
t[n-1][w]
)

else:
memo[n][w] =
memo[n-1][w]