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Sieve of Eratosthenes

Date: 48

Optimization

Prime No \rightarrow

T	T	T	T	T	T				T	T	T
0	1	2	3	4	5				22	23	24

2 \rightarrow 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30, ...

3 \rightarrow 6, 9, 12, 15, 18, 21, 24, 27, ...

4 \rightarrow Not Prime

5 \rightarrow 10, 15, 20, 25, ...

① \rightarrow optimization = 1 (Inner Loop)

$$i \rightarrow 2 \times 2 = 4$$

$$2 \times 3 = 6$$

$$2 \times 4 = 8$$

$$2 \times 5 = 10$$

$$i = 3 \times 2 = 6$$

$$3 \times 3 = 9$$

$$3 \times 4 = 12$$

$i \rightarrow$ Pehle Teri start $\rightarrow i \times i$

ex \rightarrow 2 \times 2 = 4, 6, 8, 10, 12, 14, 16, ...

3 \times 3 = 9

ab 3 se phle jo bhi

5 \times 2

vo aagye
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loga

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$$5 \times 5 = 25$$

1) se plate $\rightarrow 10$, 15, 20

$$\begin{array}{c} 5 \times 3 \\ \downarrow \\ 5 \times 4 \\ \downarrow \\ \times 2 \end{array}$$

so, start from $i \neq i$

② Optimization-2 (Outer Loop)

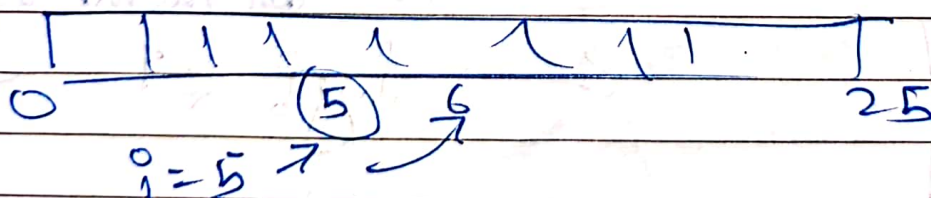
inner loop \Rightarrow int $j = i \neq i$
 while $(j \leq N)$ &
 $arr[j] = false$
 $j = j + 1$

already mark because
 $M = 7, 14, 21, \dots, 49$

$\rightarrow i \neq i = 49$ so

best while $(49 \leq N)$

\rightarrow Outer loop extra chal rha h
 ab $i = 0 \rightarrow \sqrt{n} \rightarrow$ why?
 $n = 25, \sqrt{n} = 5$



inner loop $j = 5 \times 5 = 25$

so \sqrt{n} tak loop chalo

$i = 6$

inner loop $j = 6 \times 6 = 36 \rightarrow$ out of

bound

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Worst $T.C \approx n \log(\log n)$

Same algo

↳ but Avg achi ho jayegi

→ L, R

L = 13956

R = 198935

No of Primes

0 | T | T | F | 1 | 19835
13956
Count kr lugaa

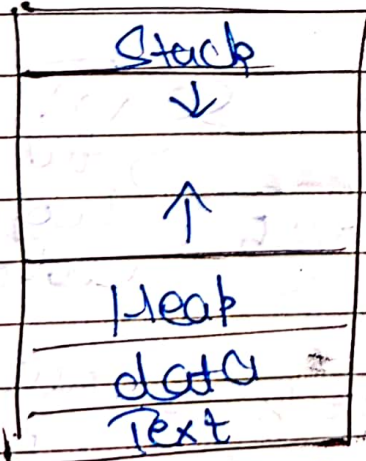
But if L = 13956

R = 10^9

Cannot allocate 10^9 on memory

← why? ←

fun() of
int a[1000]



↳ Memory

low mem size

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32-bit Linux

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int, double, char array, max size $\rightarrow 10^6$

★ bool array $\rightarrow 10^7$

Global \rightarrow int, double, char $\rightarrow 10^7$ bool $\rightarrow 10^8$

\hookrightarrow Diff for diff computer Architecture
for online contest

$$\Rightarrow 1 \leq (L, R) \leq 10^9$$

$$\hookrightarrow (R-L) \leq 10^6$$

Ex: $L=110$

$R-L=20$

$R=130$

110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130
T	T	T	T	T	T	T	T	T	T	T	T	T	T	T	T	T	T	T	T	T
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20

Segmented Sieve \uparrow

Steps \rightarrow i) Generate all primes responsible to mark seg sieve

ex: find all the prime NO from 0 to \sqrt{R}
 \hookrightarrow using Normal sieve

Sieve $\rightarrow \sqrt{R} = 11$

11 13 17 19

Prime

These prime will help to mark in segmented sieve

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(8-2) →

Base prime = {2, 3, 5, 7, 11}

find first index to start marking

→ index 0 → Resembles 110

index 20 → Resembles 130

start → first Multiple

$$\text{prime} = 2 \quad \begin{array}{r} \text{low} \\ 110 \\ \underline{2} \end{array} \times 2 = 110$$

↓
start marking with this

$$\text{prime} = 3 \quad \rightarrow \quad 110 \times 3 = (36.6) \times 3$$

↓
Int

$$\downarrow \quad 36 \times 3 = 108$$

If (value < low)

first Multiple + prime

$$108 + 3 = 111$$

$$\text{First Multiple} = \left(\frac{\text{low}}{\text{prime}} \right) * \text{prime}$$

$$\text{int } j = \max(\text{first Multiple}, \text{prime} * \text{prime})$$

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$i=3$ first mul = $(111) \rightarrow$ main
 $i \neq i = 9$

but for $i=11$ first mul = $110 \times 11 = (110)$
 $i \neq i = 121$
 \rightarrow take this
at Krazy Market

req Sieve $[j-L] = \text{false}$
 $j = \text{prime}$

why Not $j = 111 - L = 110 = (1) \rightarrow \text{Index}$
but array is from 0 to $R-L+1$

Ans $\rightarrow 118127$