

```
% Task 1: For loop use
```

```
% define variables
```

```
true_pi = pi;
```

```
N_values = [1000, 10000, 100000, 500000, 1000000]; % Different numbers of  
random points
```

```
computed_pi = zeros(size(N_values)); % Array to store computed Pi values
```

```
deviation = zeros(size(N_values)); % Array to store deviations from true Pi
```

```
execution_times = zeros(size(N_values)); % Array for execution times
```

```
% For loop over each number of points in N_values
```

```
for j = 1:length(N_values)
```

```
    N = N_values(j);
```

```
    inside_circle = 0;
```

```
    % measuring execution time
```

```
    tic;
```

```
    % Generate random points and check if they are inside the quarter circle
```

```
    for i = 1:N
```

```
        x = rand;
```

```
        y = rand;
```

```
        if x^2 + y^2 <= 1
```

```
            inside_circle = inside_circle + 1;
```

```
        end
```

```
    end
```

```
    % Estimate Pi
```

```
    computed_pi(j) = 4 * inside_circle / N;
```

```
    % deviation from the true Pi value
```

```
    deviation(j) = abs(computed_pi(j) - true_pi);
```

```
    % Record execution time
```

```
    execution_times(j) = toc;
```

```
    % Print details for each iteration
```

```
    fprintf('N = %d, Computed Pi = %.10f, Deviation = %.10f, Execution Time  
= %.5f seconds\n', ...
```

```
        N, computed_pi(j), deviation(j), execution_times(j));
```

```
end
```

```
N = 1000, Computed Pi = 3.1120000000, Deviation = 0.0295926536, Execution Time = 0.01176 seconds  
N = 10000, Computed Pi = 3.1304000000, Deviation = 0.011926536, Execution Time = 0.00135 seconds  
N = 100000, Computed Pi = 3.1518400000, Deviation = 0.0102473464, Execution Time = 0.00647 seconds  
N = 500000, Computed Pi = 3.1448080000, Deviation = 0.0032153464, Execution Time = 0.03239 seconds  
N = 1000000, Computed Pi = 3.1389120000, Deviation = 0.0026806536, Execution Time = 0.06608 seconds
```

```
% Plot the computed value of Pi as the number of points increases
```

```
figure;
```

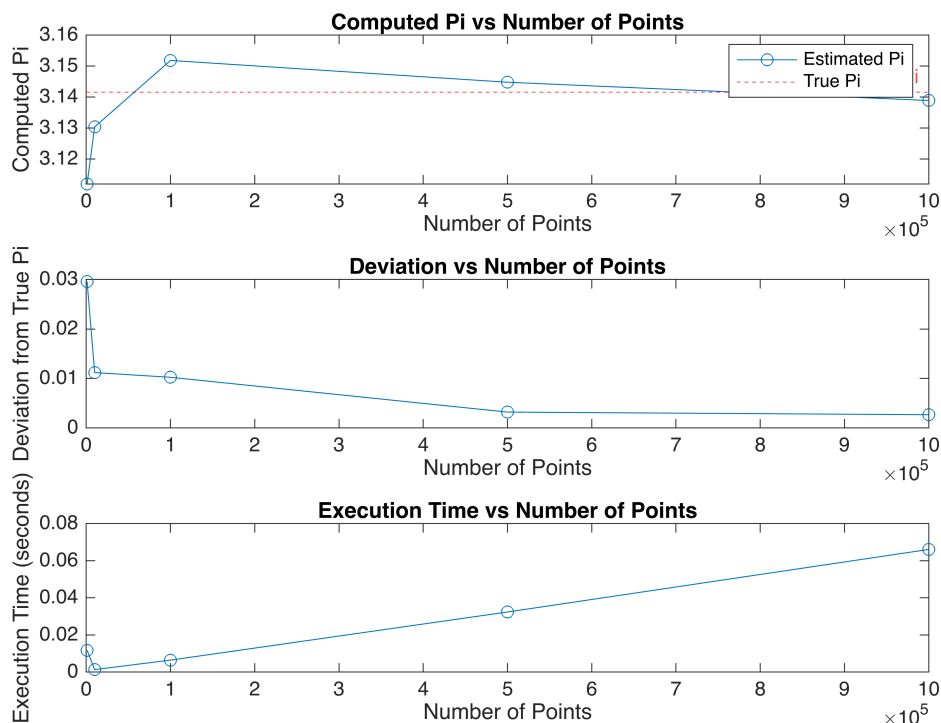
```

subplot(3,1,1);
plot(N_values, computed_pi, '-o');
hold on;
yline(true_pi, '--r', 'True Pi');
xlabel('Number of Points');
ylabel('Computed Pi');
title('Computed Pi vs Number of Points');
legend('Estimated Pi', 'True Pi');
hold off;

% Plot the deviation from true Pi as the number of points increases
subplot(3,1,2);
plot(N_values, deviation, '-o');
xlabel('Number of Points');
ylabel('Deviation from True Pi');
title('Deviation vs Number of Points');

% Plot the execution time as the number of points increases
subplot(3,1,3);
plot(N_values, execution_times, '-o');
xlabel('Number of Points');
ylabel('Execution Time (seconds)');
title('Execution Time vs Number of Points');

```

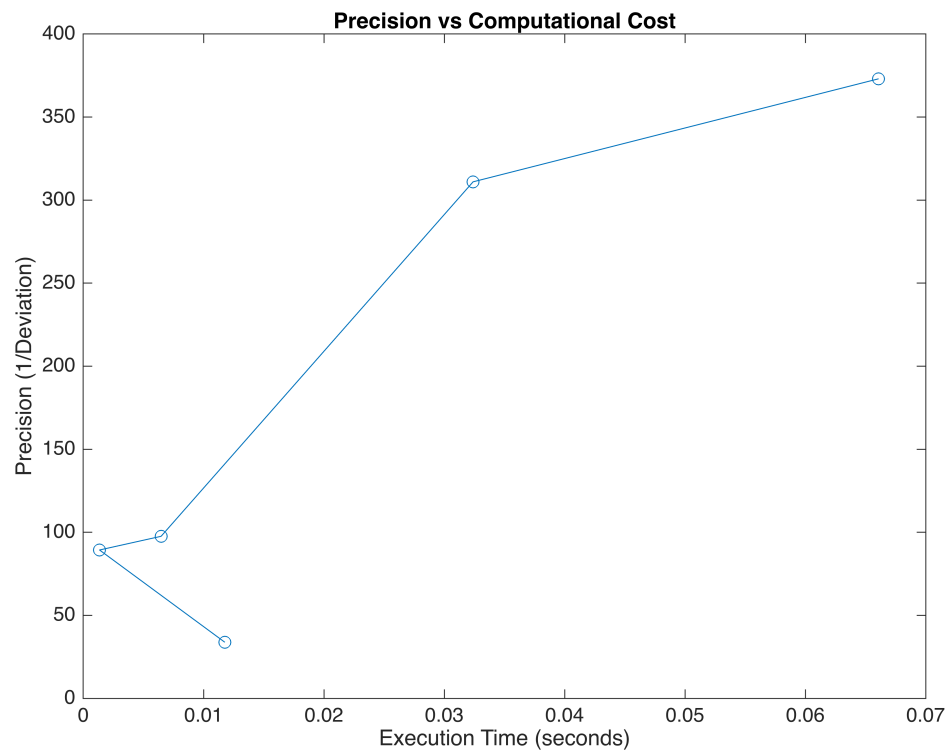


```

% Create a plot comparing precision (1/Deviation) to computational cost
(Execution Time)

```

```
figure;  
plot(execution_times, 1./deviation, '-o');  
xlabel('Execution Time (seconds)');  
ylabel('Precision (1/Deviation)');  
title('Precision vs Computational Cost');
```



% Task 2: Compute Pi using While Loop for a Specified Precision

% Define the desired precision

```
precision_levels = [2, 3, 4];
```

% Initialize arrays to store results for each precision level

```
computed_pis = zeros(1, length(precision_levels));
```

```
iterations = zeros(1, length(precision_levels));
```

```
execution_times = zeros(1, length(precision_levels));
```

% for loop over each precision level

```
for k = 1:length(precision_levels)
```

```
    desired_precision = precision_levels(k);
```

```
    tolerance = 10^-(desired_precision); % Tolerance based on desired precision
```

```
    % Initialize variables
```

```
    inside_circle = 0; % points inside the quarter circle
```

```
    N = 0; % Number of points
```

```
    computed_pi = 0; % Initial estimate of Pi
```

```
    previous_pi = NaN; % To store the previous computed value of Pi
```

```
    min_iterations = 5000; % Minimum number of iterations to avoid
```

```
premiature stopping
```

```
    % Start timing
```

```
    tic;
```

```
    % While loop to compute Pi
```

```
    while true
```

```
        N = N + 1;
```

```
        x = rand;
```

```
        y = rand;
```

```
        % Check if the point is inside the quarter circle
```

```
        if x^2 + y^2 <= 1
```

```
            inside_circle = inside_circle + 1;
```

```
        end
```

```
        % Estimate Pi based on the number of points
```

```
        previous_pi = computed_pi; % Store the previous Pi value
```

```
        computed_pi = 4 * inside_circle / N; % Monte Carlo estimation of Pi
```

```
        % Ensure a minimum number of iterations to avoid premature stopping
```

```
        if N > min_iterations
```

```
            % Check if the computed Pi value is stable to the desired significant figures
```

```
            if abs(round(computed_pi, desired_precision) - round(previous_pi, desired_precision)) < tolerance
```

```
                break; % Exit the loop if the desired precision is achieved
```

```
            end
```

```

        end
    end

    % Stop timing
    execution_times(k) = toc;

    % Store the results for the current precision level
    computed_pis(k) = round(computed_pi, desired_precision);
    iterations(k) = N;

    % Display the results for the current precision level
    fprintf('Precision level: %d significant figures\n', desired_precision);
    fprintf('Computed Pi = %.10f\n', computed_pis(k));
    fprintf('Number of iterations = %d\n', N);
    fprintf('Execution time = %.5f seconds\n\n', execution_times(k));
end

```

```

Precision level: 2 significant figures
Computed Pi = 3.1200000000
Number of iterations = 5001
Execution time = 0.00279 seconds
Precision level: 3 significant figures
Computed Pi = 3.1430000000
Number of iterations = 5001
Execution time = 0.00206 seconds
Precision level: 4 significant figures
Computed Pi = 3.1466000000
Number of iterations = 5006
Execution time = 0.00235 seconds

```

% Task 3: Compute Pi with User-Defined Precision

```
function computed_pi = compute_pi()

    % Ask user for the desired precision level
    desired_precision = input('Enter the desired precision level (for
example: 1 or 2 or 3): ');

    % Initialize variables
    tolerance = 10^-(desired_precision); % Tolerance based on user-
specified precision
    inside_circle = 0;
    N = 0;
    computed_pi = 0; % Initial estimate of Pi
    previous_pi = NaN; % To store the previous computed value of Pi
    min_iterations = 5000; % Minimum iterations to prevent early stopping

    % figure for graphical display
    figure;
    hold on;
    axis equal;
    axis([0 1 0 1]);
    title(sprintf('Estimating Pi with Precision: %d ', desired_precision));
    xlabel('X');
    ylabel('Y');

    % Start the Monte Carlo simulation
    tic; % Start timer

    while true
        N = N + 1;
        x = rand;
        y = rand;

        % Check if the point is inside the quarter circle
        if x^2 + y^2 <= 1
            inside_circle = inside_circle + 1;
            plot(x, y, 'g. '); % Plot points inside the circle in green
        else
            plot(x, y, 'r. '); % Plot points outside the circle in red
        end

        % Estimate Pi based on the number of points
        previous_pi = computed_pi; % Store the previous Pi value
        computed_pi = 4 * inside_circle / N; % Monte Carlo estimation of Pi

        % Ensure a minimum number of iterations
        if N > min_iterations
            % Check if the computed Pi value is stable to the desired
            significant figures
        end
    end
```

```

        if abs(round(computed_pi, desired_precision) -
round(previous_pi, desired_precision)) < tolerance
            break; % Exit the loop if the desired precision is achieved
        end
    end

    if mod(N, 100) == 0
        drawnow;
    end
end

% Stop timer and calculate execution time
execution_time = toc;

% print the results
fprintf('Computed Pi = %.10f\n', computed_pi);
fprintf('Number of iterations = %d\n', N);
fprintf('Execution time = %.5f seconds\n', execution_time);

% final result on the plot
text(0.5, 0.5, sprintf('\pi \approx %.10f', computed_pi), 'FontSize',
14, 'HorizontalAlignment', 'center');

end

```

