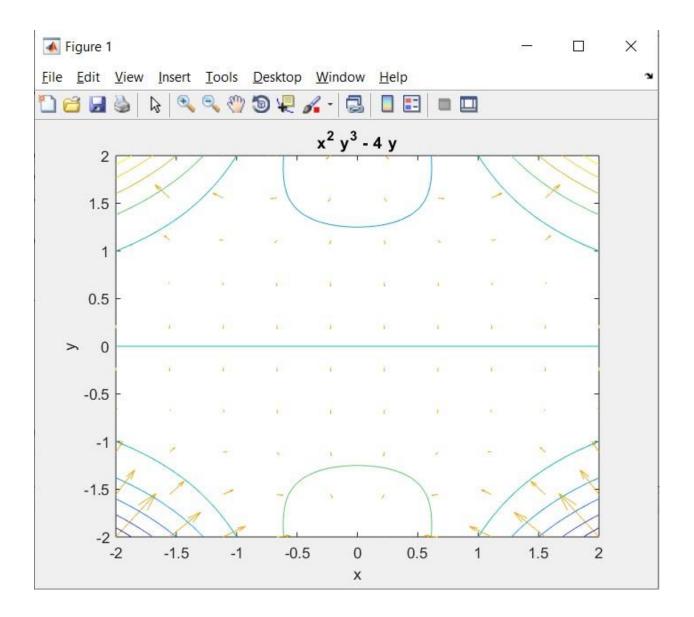
## Find the Gradient of the function $f = x^2y^3 - 4y$ .

```
Editor - C:\Matlab data\Untitled1.m
Untitled1.m × Untitled2.m × +
1 -
       syms x y
2 -
       f = input( 'Enter the function f(x,y): ');
       grad = gradient(f,[x,y]);
      f1 = diff(f,x);
       f2 = diff(f,y);
 6 -
      P = inline(vectorize(f1), 'x', 'y');
7 -
      Q = inline(vectorize(f2), 'x', 'y');
      x = linspace(-2, 2, 10);
8 -
9 -
      y = x;
10 -
      [X,Y] = meshgrid(x,y);
11 -
      U = P(X,Y);
12 -
     V = Q(X,Y);
13 -
      quiver(X,Y,U,V,1)
14 -
      axis on
15 -
      xlabel('x')
16 -
      ylabel('y')
17 -
      hold on
18 -
       ezcontour(f,[-2 2])
19 -
      fprintf('Gradient of f(x,y) is :\n');
20 -
      fprintf('%s\n',grad);
Command Window
  >> Untitled1
  Enter the function f(x,y): (x^2)*(y^3)-4*y
  Gradient of f(x,y) is:
  2*x*y^3
  3*x^2*y^2 - 4
fx >>
```

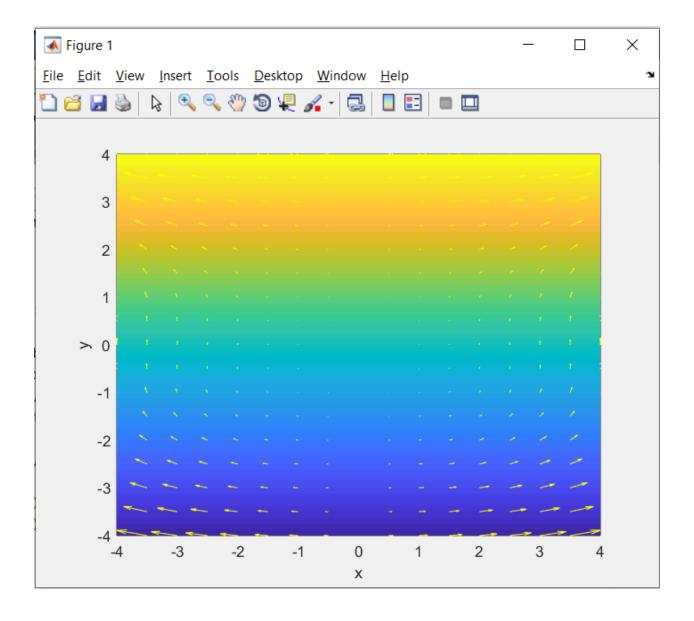


Find the divergence of a vector field  $f = [xy, x^2]$ .

```
Editor - C:\Matlab data\Untitled2.m
   Untitled1.m × Untitled2.m ×
                               +
 1 -
        clear all
        clc
 2 -
 3 -
        syms x y
        x = -4:0.5:4;
 4 -
 5 -
        y = x;
        [X,Y] = meshgrid(x,y);
 6 -
 7 -
        Div = divergence(X, Y, X.*Y, X.^2);
 8 -
       pcolor(X,Y,Div);
       shading interp
 9 -
        hold on;
10 -
        quiver(X,Y, X.*Y.^2, X.^2,'Y');
11 -
12 -
       hold off;
13 -
        xlabel('x')
14 -
        ylabel('y')
15 -
        disp(Div)
```

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Command Window
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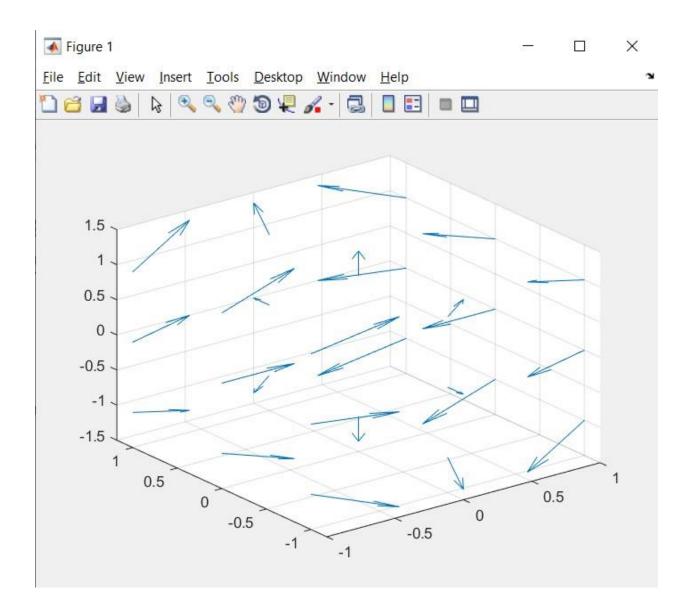
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f_{x} >>
```



Visualize the curl of a vector function f = [yz, 3zx, z].

```
Editor - C:\Matlab data\Untitled3.m
  Untitled1.m × Untitled2.m × Untitled3.m × +
 1 -
      clear all
 2 -
      clc
      syms x y z
    V = [y*z, 3*z*x, z];
     X = [x y z];
      disp(curl(V,X))
    [x,y,z] = meshgrid([-1 0 1]);
    u = -3*x;
      v = y;
10 - w = 2*z;
11 - quiver3(x,y,z,u,v,w);
Command Window
   -3*x
```

2\*z



Find the work done for the force  $\vec{F}(x,y,z) = yz\vec{i} + xz\vec{j} + (xy+2z)\vec{k}$  along the line segment from (1,0,-2) to (4,6,3).

Find the work done for the force  $\vec{F}(x,y,)=x^2\vec{t}+y^2\vec{j}$  along the arc of the parabola  $y=2x^2$  from (-1,2) to (2,8).