

Distinct Subsequences

s1 = "babgbag"

b a b g b a g

s2 = "bag"

We have to count the no. of ways ?

→ Recursion.

→

	b a b g b a g	b a g
↑		↑
i		j

Recursion Approach

- We have 2 strings. so,

match
and
non match
concept

$f(\text{ind1}, \text{ind2}) \rightarrow$ Express in Index

Base Case
 $\text{if } (\underline{j} < 0) \text{ return } 1,$

$\text{if } (i < 0) \text{ return } 0,$

match
 $\text{if } (s1[i] == s2[j]) \rightarrow f(i-1, j-1) + f(i-1, j)$

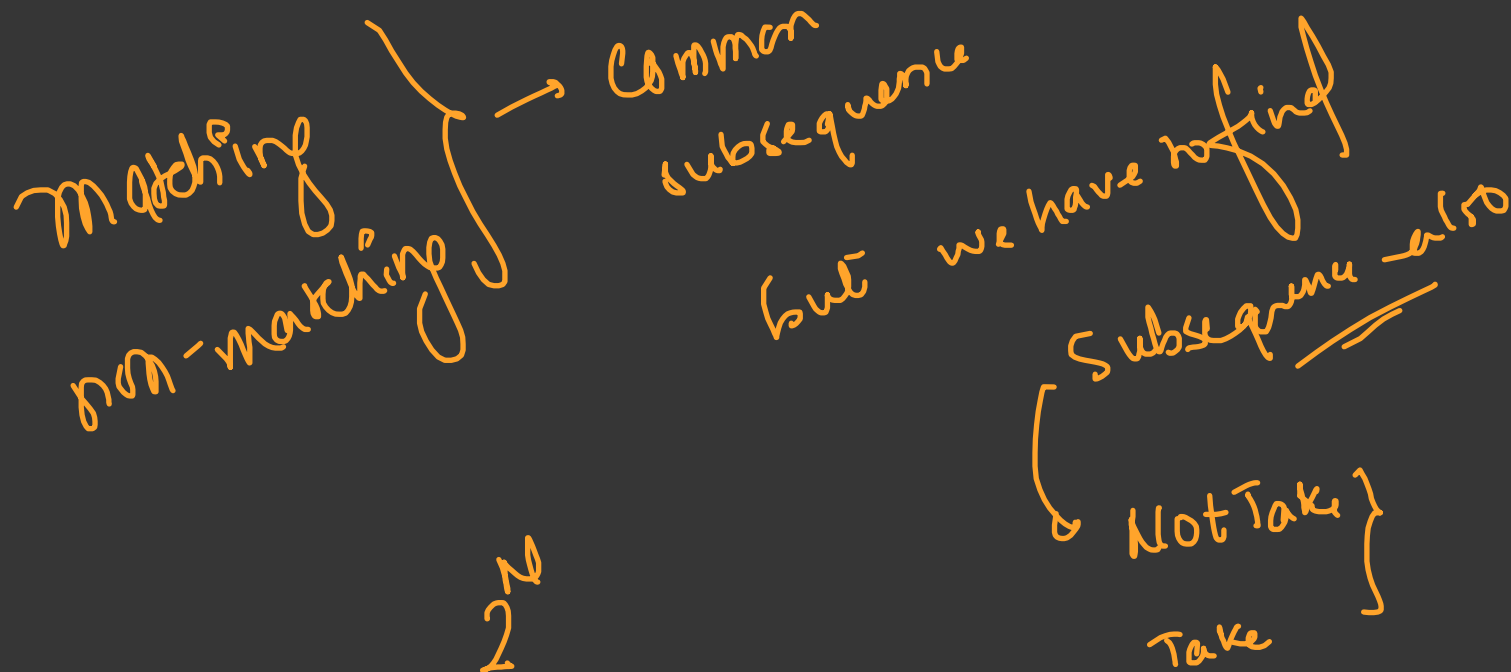
not match
else
 $f(i-1, j)$

Summation of
ways

Exploze

Base Case

When do I return 1? \rightarrow When all char of S2
then I return 1.



Recursion Tree:

0-based index if

b a b a b
 ↑ ↑ ↑ ↑ ↑

b a b
 ↑ ↑ ↑

$f(6, 2) \rightarrow$ match
 take \ not

$f(5, 2)$

$f(5, 1)$

3
 match $f(4, 0)$
 1 $f(3, -1)$
 2 $f(3, 0)$ not match
 2 $f(3, 1)$

$f(2, 0)$ match
 1 $f(1, -1)$
 1 $f(1, 0)$
 1 $f(0, 0)$
 1 0

$$f(-1, 1) \quad f(-1, 0)$$

There would be overlapping sub problems.

→ So, we use Memoization

$$dp \rightarrow dp[n][m];$$

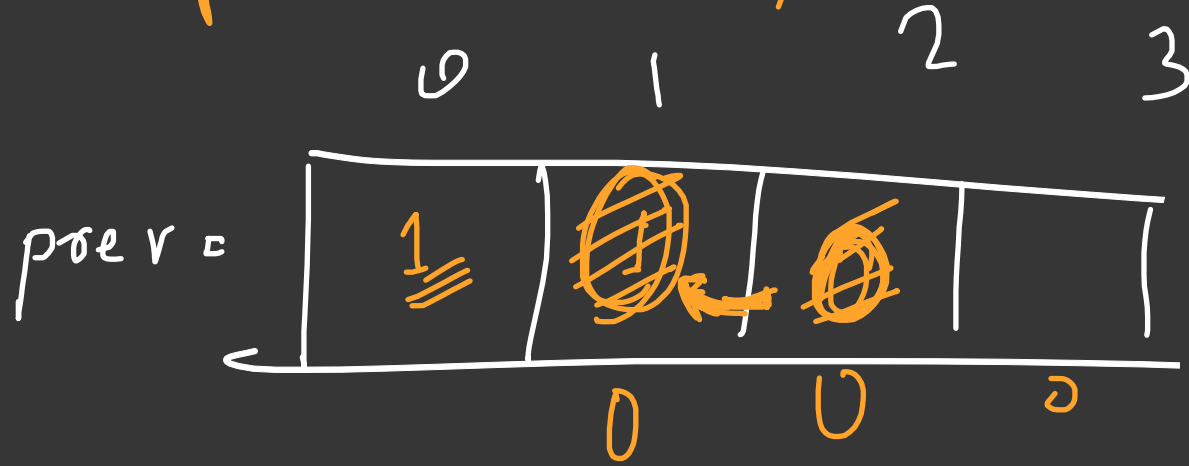
Tabulation:

Base Case: $if(i \geq 0) \rightarrow$ means for every $i \geq 0$
 $if(j \geq 0)$ we have b

Space Optimization

In 1D array.

Observe Space Optimization



$i = 2$
 $prev[0] = 1$

babg bag
 ↑

bag
 ↑↑

$prev[i] = prev[j]$
 or

$j = 1$
 $dp[i]$
 if (
 $dp[i-1][j-1] + dp[i-1][j]$
 ↓ prev