

DP on Strings:

Longest Common Subsequence } with we have to

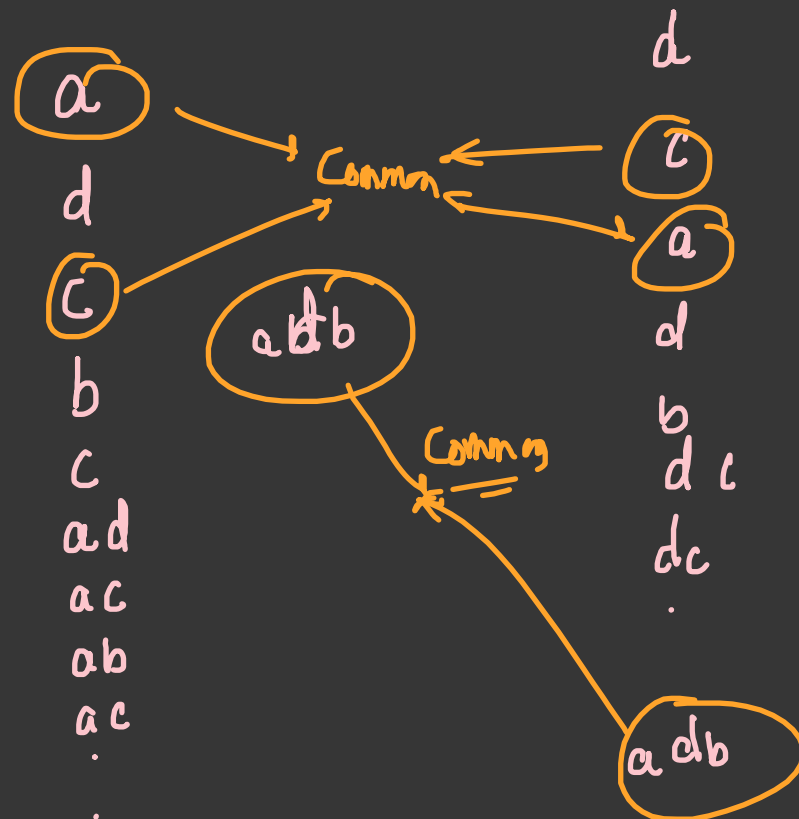
$s_1 = \text{"a d c b c"}$
 $s_2 = \text{"d c a d b"}$

Can generate 32 subsequence

find the length of
Longest subsequence

So, Output is 3

Common Subsequence:



Which the Longest Common Subsequence

$adb \rightarrow$ size/length of "adb"

string is 3

Problem Statement!

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[Suggest Edit](#)

Given two strings, 'S' and 'T' with lengths 'M' and 'N', find the length of the 'Longest Common Subsequence'.

For a string 'str'(per se) of length K, the subsequences are the strings containing characters in the same relative order as they are present in 'str,' but not necessarily contiguous. Subsequences contain all the strings of length varying from 0 to K.

Example :

Subsequences of string "abc" are: ""(empty string),
a, b, c, ab, bc, ac, abc.

Comm:ic

match
not match

Detailed approach of the problem:

Let say, we have 2 strings.

$$\left. \begin{array}{l} s_1 = \text{acd} \\ s_2 = \text{ced} \end{array} \right\} \text{ so longest Common Subsequence is } \text{cd} = 2$$

Brute approach would be generate all subsequence of s_1 and s_2 and find the common between them and then find the longest subsequence.

So, by this approach the time complexity: is $O(2^N) + O(2^N)$ which is exponential

The approach is somewhat correct but, either by generate subsequence differently why not simultaneously generate and check common subsequence between subsequence.

So, Now.

We know that we will use recursive as we have to try all possible ways

So, Question arises ~~with~~ how we generate subsequence

There is a simple concept of take and not take

here let see,

We have $s_1 = a c d$ $s_2 = c e d$

In recursive what we take indx.

here we have 2 string of different length so,

There would be 2 index

$f(\text{ind1}, \text{ind2})$

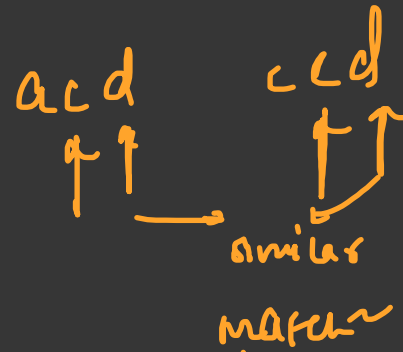
Question is when we will consider the character and when not?

When we find common character means we consider it its

obvious -

So, let say.

$f(2, 2)$



if $s_1[\text{ind1}] == s_2[\text{ind2}]$

$1 + f(\text{ind1} - 1, \text{ind2} - 1)$

After first indx

a c d c e d
↑ ↑ ↑
not match

but in future there can be a character which matches
that is concept of subsequence

So, there are 2 cases ~~one~~

1st Case It
move ind 1 by

1

2nd Case

we move ind 2 by 1

a c d c e d
↑ ↑ ↑
Once ind 1
and ind 2

if not match

not match $\rightarrow 0 + \max(f(\text{ind } 1-1, \text{ind } 2), f(\text{ind } 1, \text{ind } 2-1))$

why? \rightarrow Because we want longest common subsequence

return $\max(\text{match}, \text{not match})$,

Base Case

if (indx1 > 2)

Recursive function.

$f(\text{ind1}, \text{ind2})$

Base case
if $(\text{ind1} < 0 \parallel \text{ind2} < 0)$ return 0;

if $(s1[\text{ind1}] == s2[\text{ind2}])$

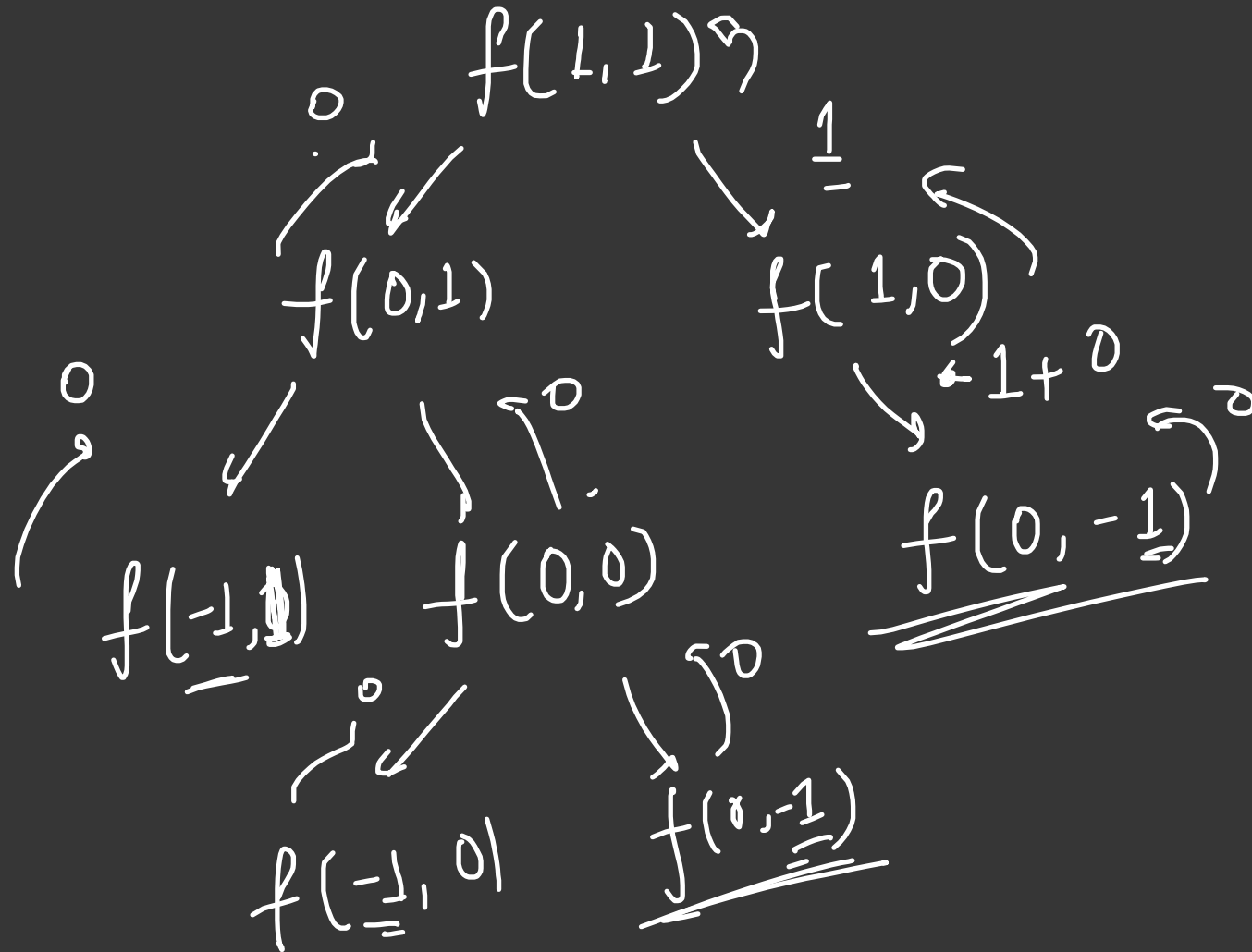
return $1 + f(\text{ind1}-1, \text{ind2}-1)$;

return $\max(f(\text{ind1}-1, \text{ind2}), f(\text{ind1}, \text{ind2}-1))$

Recursive Tree:

$$f(2, 2) \xrightarrow{1+1} 2 \xrightarrow{2} 2$$

a c d
c e d



ans = 2

large input
 there would
 be overlapping
 subproblems

Memorization.

for memorization we observe changing variable

(ind1, ind2)

vector < vector<int>> dp(ind1, vector<int>(ind2, 1))

T.C: $O(N \times M)$ S.C: $= O(N \times M) + O(N + M)$

Tabulation:

Base Case: Shifting of index

Base Case changes to $\text{if } (i \geq 0 \text{ || } j \geq 10)$

\downarrow $\text{dp}[0][i]$

\downarrow return 0;

\downarrow $\text{dp}[i][0]$

for ($i = 0$; $i < n$; $i++$) $\text{dp}[i][0] = 0$

for ($j = 0$; $j < m$; $j++$) $\text{dp}[0][j] = 0$