

Count the no. of subarray with xor k.

Problem Statement

[Suggest Edit](#)

Given an array 'A' consisting of 'N' integers and an integer 'B', find the number of subarrays of array 'A' whose bitwise XOR (\oplus) of all elements is equal to 'B'.

A subarray of an array is obtained by removing some (zero or more) elements from the front and back of the array.

Example:

Input: 'N' = 4 'B' = 2

'A' = [1, 2, 3, 2]

Output: 3

Explanation: Subarrays have bitwise xor equal to '2' are: [1, 2, 3,
2], [2], [2].

arr[] = { 4, 2, 2, 6, 4 } K = 6

Brute / Naive approach:

Generate all Subarray and xor them to get K = 6

$$\begin{aligned} 4 &\leftarrow 4 \\ 6 &\leftarrow 4 \wedge 2 \end{aligned}$$

$$4 \leftarrow 4 \wedge 2 \wedge 2$$

$$2 \leftarrow 4 \wedge 2 \wedge 2 \wedge 6$$

$$6 \leftarrow 4 \wedge 2 \wedge 2 \wedge 6 \wedge 4$$

$$\text{Ans} = 4$$

$$2 \leftarrow 2$$

$$0 \leftarrow 2 \wedge 2$$

$$6 \leftarrow 2 \wedge 2 \wedge 6$$

$$2 \leftarrow 2 \wedge 2 \wedge 6 \wedge 4$$

$$6 \leftarrow 6$$

$$2 \leftarrow 6 \wedge 4$$

$$4 \leftarrow 4$$

$$2 \leftarrow 2$$

$$4 \leftarrow 2 \wedge 6$$

$$0 \leftarrow 2 \wedge 6 \wedge 4$$

eg: 1 2 3 2

K=2

2 ← 1

1 ← 1

3 ← 1 2

1 ← 2 >

3 ← 2 > 2

> ← 3

1 ← 3 2

2 ← 2

0 ← 1 2 3

2 ← 1 2 3 2

Ans = 3

So, Brute force is simple. but. Time Complexity is $O(N^2)$.

Optimal Approach:

$$K = 2$$

4 2 2 6 4

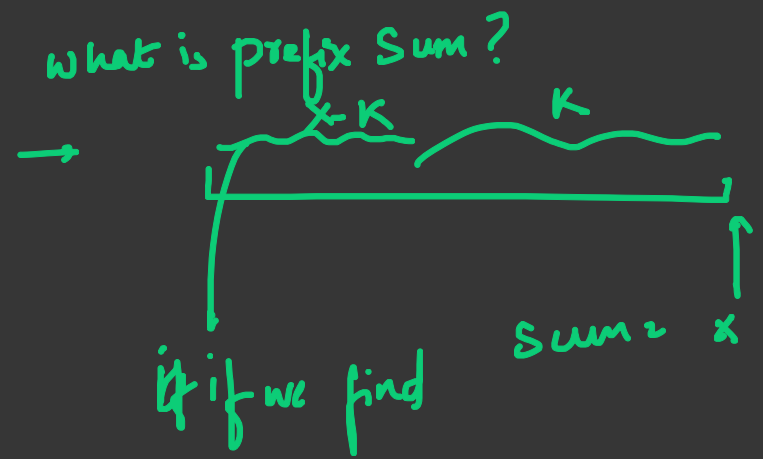
$$X^K = XR$$

$$X^{K \wedge K} = X R^K$$

$$X = X R^K$$

4 2 2 6 4

$$R = 2$$



Hashmap to keep the track of XOR

There is
 x
 for

4 2 2 6 4

↑ ↑ ↑ ↑ ↑
 6 6 6 6 6

$$xR = 4 \oplus 6 \oplus 2 \oplus 6$$

$$\text{count} = 1 \oplus 3 \oplus 4$$

Ans = 4

$$K = 6$$

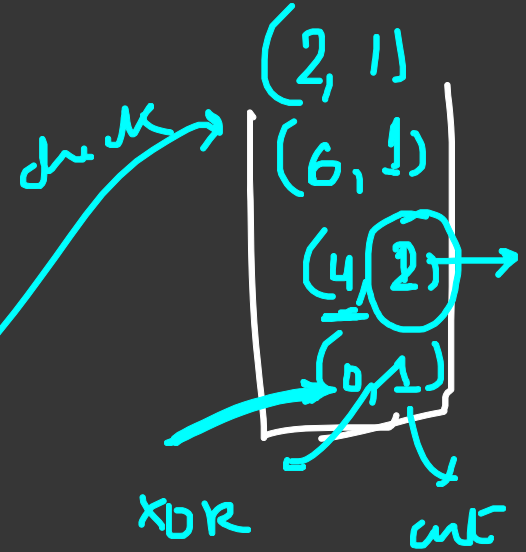
$$\begin{array}{c} x \oplus xR \oplus K \\ \hline x \oplus 4 \oplus 6 = 2 \end{array}$$

$$x \oplus 6 \oplus 6 = 0$$

$$x \oplus 4 \oplus 6 = 2$$

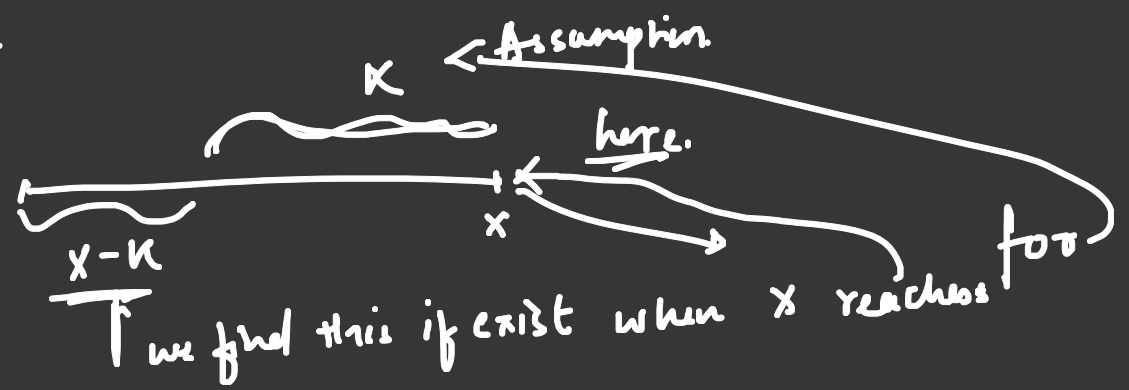
$$x \oplus 2 \oplus 6 = 4$$

$$x \oplus 6 \oplus 6 = 0$$



Explanation of the intuition and Algo:

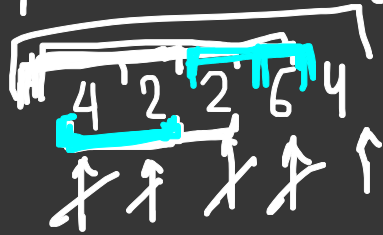
• Idea is to use prefix Sum Concept



eg: 4 2 2 6 4

Dry Run

→ To keep the track of the pre XOR value we use map.



XOR: ~~4~~ ~~6~~ ~~2~~ 6

cnt: ~~2~~ ~~1~~ ~~3~~ 4

4 2 2

$$x = x \oplus K$$

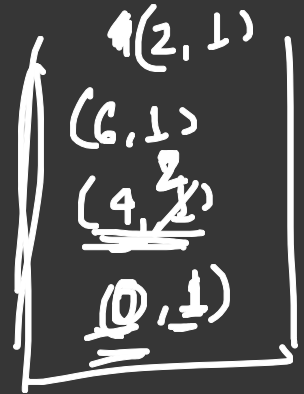
$$4 \oplus 6 = 2$$

$$6 \oplus 6 = \underline{\underline{0}}$$

$$4 \oplus 6 = 2$$

$$2 \oplus 6 = 4$$

$$6 \oplus 6 = \underline{\underline{0}}$$



preXOR
val

cnt

why?

Explain

100
010
110

Pseudocode:

Initial the map.

$xR = 0$

$map[xR]++;$

means.



for ($i = 0; i < n; i++$)

$xR \oplus arr[i];$

$x = xR^k;$

$count \oplus mp[x] \oplus i;$

$mp[xR]++;$

}

return count;

Time Complexity:

if we have $\langle \text{int}, \text{int} \rangle \longrightarrow$ operation $O(\log N) \longrightarrow$ Worst Case.

Unordered $\langle \text{int}, \text{int} \rangle \longrightarrow$ operation Best Case $O(1)$
Worst Case $O(N)$ \nearrow if there is many collisions

$$T.C. = \underbrace{O(N)}_{\text{iteration}} * \underbrace{O(\log N)}_{\text{map}}$$

$$\text{or } O(N) * \underbrace{O(1)}_{\text{unordered map}} \longrightarrow \underline{\underline{O(N^2)}}$$

S.C. \sim $O(N)$ \longrightarrow at worst it will store all array elements