

4 Sum

18. 4Sum

Medium

10.3K

1.2K



Companies

Given an array `nums` of `n` integers, return an array of all the **unique** quadruplets `[nums[a], nums[b], nums[c], nums[d]]` such that:

- $0 \leq a, b, c, d < n$
- `a, b, c, and d` are **distinct**.
- `nums[a] + nums[b] + nums[c] + nums[d] == target`

You may return the answer in **any order**.

Example 1:

Input: `nums = [1,0,-1,0,-2,2]`, `target = 0`

Output: `[[-2,-1,1,2], [-2,0,0,2], [-1,0,0,1]]`

Example 2:

Input: `nums = [2,2,2,2,2]`, `target = 8`

Output: `[[2,2,2,2]]`

nums[] = { 1, 0, -1, 0, -2, 2 } target = 0

{ 1, -1, -2, 2 } , { 1, -1, 0, 0 } , { -2, 2, 0, 0 }
↓
0

Brute force:

nested loops → distinct → set → store the values

for (i=0, i<n, i++)

f(i) = i+1, j<n, j++)

for (k = j+1, k<n, k++)

f(g = k+1, g<n, g++)

if (sum == target)

set push(nums[i], c, d)

T.C. = $O(N^4)$

S.C. = $O(2^N)$

We have to return distinct array of the 4 element we
sum = target.

As distinct is asked we store the array in set ~~and~~ to make it
distinct. We push the array in sorted form in set to
easily distinguish betⁿ distinct array.

As we are doing we are iterating at every element in array and summing them up to match the target

Set <vector<int>> st \rightarrow Store the distinct elements

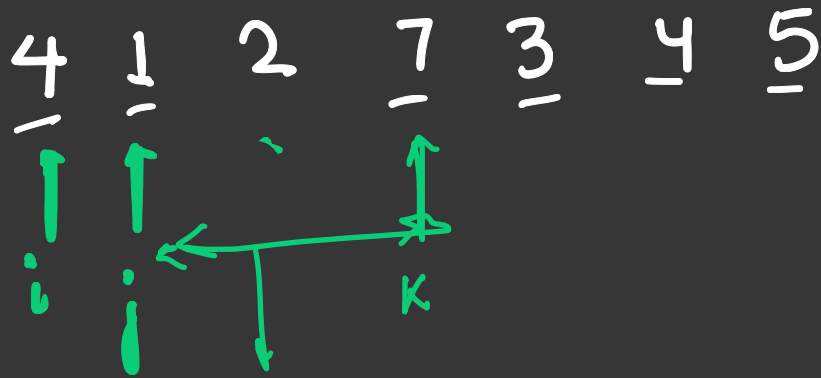
T.C. $\sim O(N^4) \rightarrow \underline{\underline{O(N^3)}}$

What we can do is

$$\underbrace{a + b + c}_{\text{loop}} + \underbrace{d}_{\text{}} = \text{target}$$

$$d = \text{target} - \underbrace{(a + b + c)}_{\text{val 1}}$$

val 1 \rightarrow check if present in hashmap



target = 16

hashmap → Because we need distinct element

for (i = 0; i < n; i++)

for (j = 0; j < n; j++) hashmap < int, int > map

for (k = j + 1; k < n; k++)

needed value = target - (arr[i] + arr[j] + arr[k]).

if (map.find(needed value) != map.end())

~~vector~~ temp = { arr[i], j, k, needed value};

sort.

map.insert(arr[k], set.temp);

$$T.C = O(N^3 \log K)$$

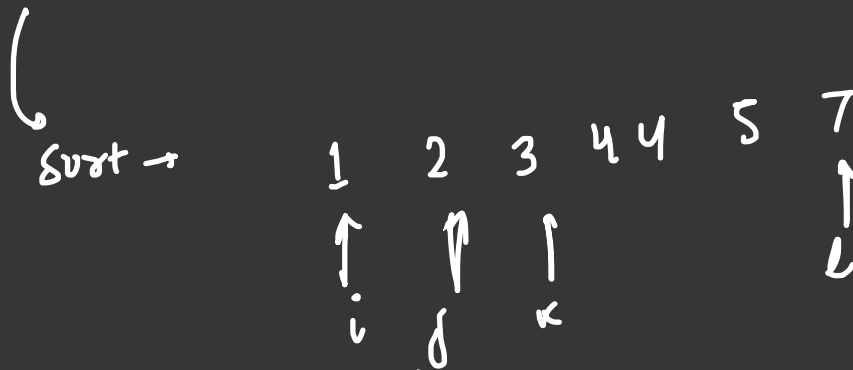
$$S.C = O(N) + O(2 \times Q_{max})$$

D primed \rightarrow T.C. $O(N^3 \log K)$

hashset
 $\left(\begin{array}{l} \text{set} < \text{int} > \\ \text{set} < \text{vector} > \end{array} \right.$

4 1 2 7 3 4 5

target = 16

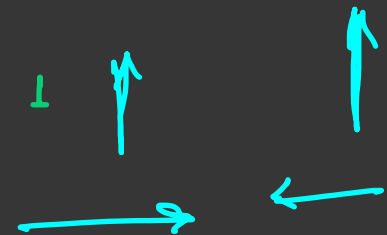
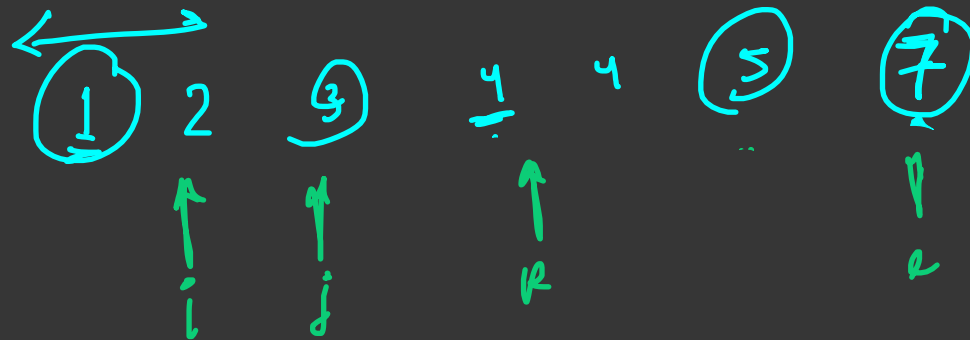


{7, 1, 4, 4}

4th value

{5, 3, 4, 4}

{7, 1, 5, 3}



$$7 + 4 = 11$$

$$7 + 5 = 12$$

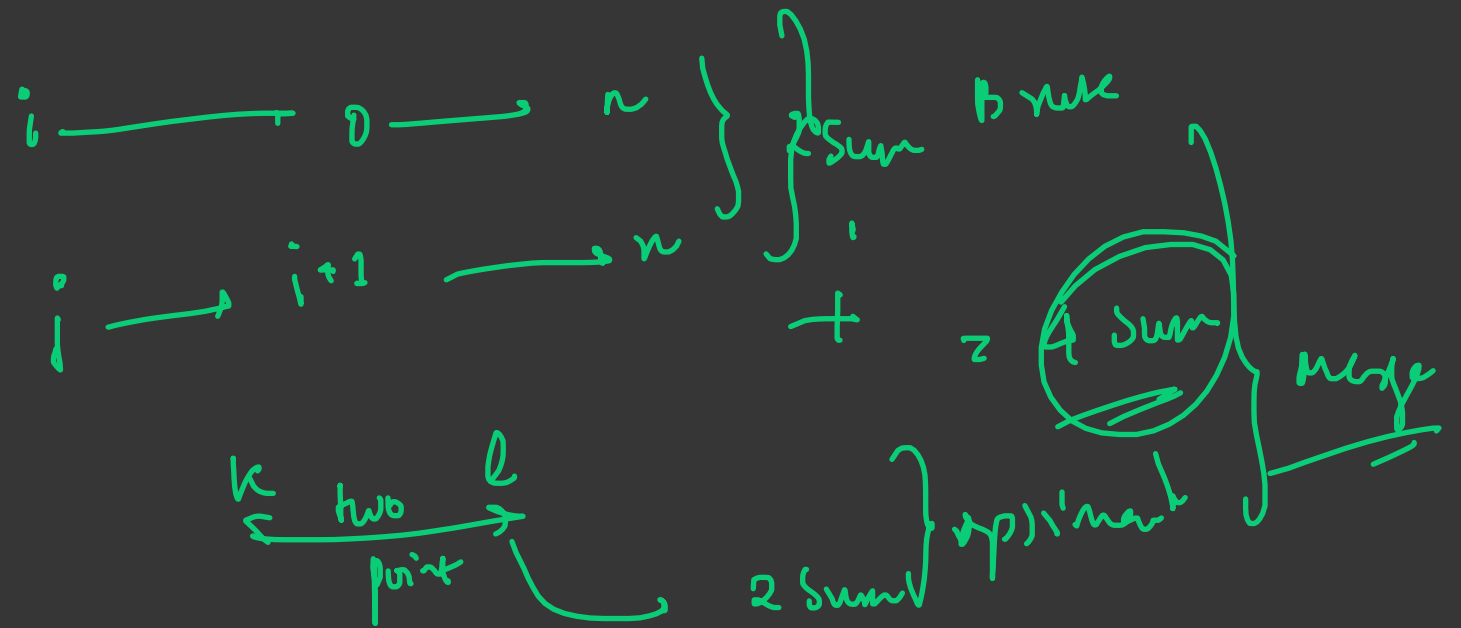
$$\text{for Sum} = 1 + 2 = \underline{3} + \frac{10}{(k+1)}$$

$$\text{Sum} = 1 + 3 = \underline{4}$$

(16)

{1, 3, 5, 7}

{1, 4, 4, 7}

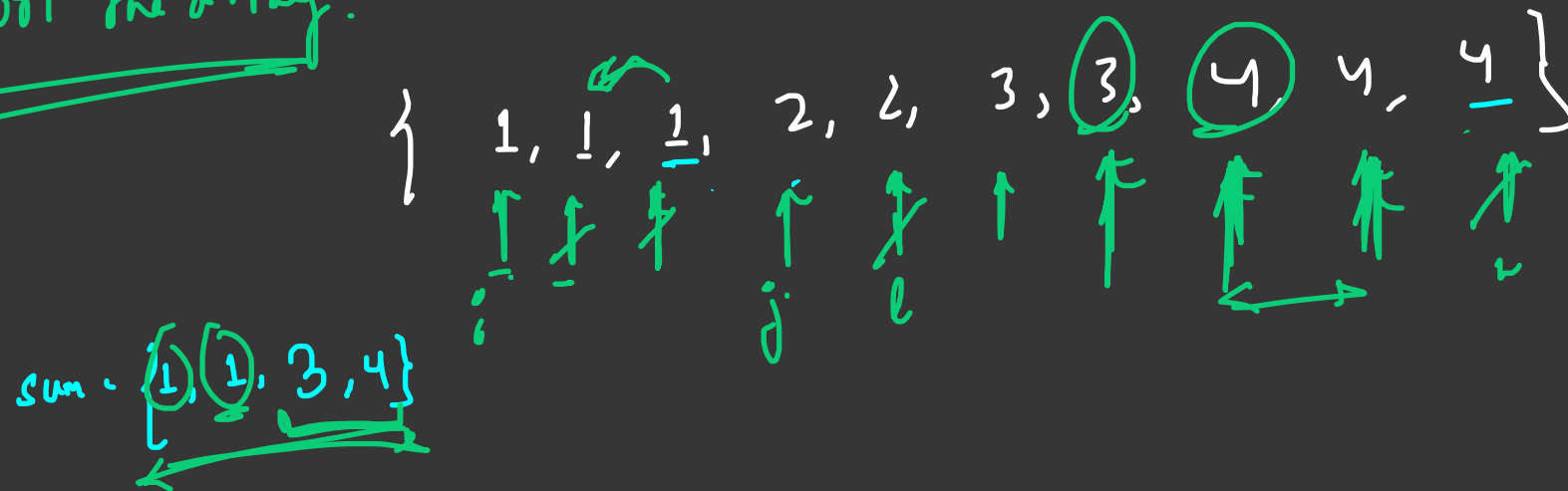


eg. arr[]: { 4, 3, 3, 4, 4, 2, 1, 2, 1, 1 }

target = 9

Optimal Approach.

- Sort the array:



$\{1, 2, 2, 4\}$

- To have distinct array we skip the duplicate element in every iterator

$$2 + 4 + 1 = 7$$

$$2 + 2 + 4 + 1 = 9$$

$$1 + 2 + 2 + 4 = 9$$

$$1 + 2 + 3 + 4 = 10$$

Pseudocode

```
for (i = 0, i < n; i++)  
    if (i > 0 && arr[i] == arr[i-1]) continue,
```

T.C. = $O(N^3)$

S.C. = $O(1)$

```
for (j = i+1, j < n; j++)  
    if (j > i+1 && arr[j] == arr[i]) continue,
```

```
int low = i+1, high = n-1,
```

```
for while (low < high)
```

```
    sum =           
```

```
    if (sum == target)
```

```
        ans.push_back(a, b, c, d)
```

```
        low++, high--
```

```
        // skip duplicate
```

```
        while (low < high && arr[low] == arr[low-1])  
            low++
```

```
        while (low < high && arr[high] == arr[high+1])  
            high--
```