

Find Majority element $> n/3$

Problem Statement

[Suggest Edit](#)

Given an array 'A' of 'N' integers, find the majority elements of the array.

A majority element in an array 'A' of size 'N' is an element that appears more than $\text{floor}(N / 3)$ times.

Note: The floor function returns the number rounded down to the nearest integer.

Note: Return the array of majority elements in sorted order.

Example:

Input: 'N' = 9 'A' = [2, 2, 1, 3, 1, 1, 3, 1, 1]

Output: 1

Explanation: The frequency of '1' is 5, which is greater than $\text{floor}(N / 3)$, hence '1' is the majority element.

Explanation of Question

Q:

$arr[] = \{1, 1, 1, 2, 2, 2\}$

$n = \underline{\underline{6}}$

element find and store $arr[] = \{ \quad \}$
 $\xrightarrow{\text{freq.} > n/3}$

$n/3 = \frac{6}{3} = 2 \rightarrow \text{freq.} \geq 2$

$arr[] = \{ \textcircled{1} \textcircled{1} \textcircled{1}, 2, 2, 2 \}$
 \uparrow

$1 \rightarrow 3 > 2$
 $2 \rightarrow 3 > 2$

$arr[] = \{1, 2\}$

sorted Sorted array

Observation.

$$n = 8 \rightarrow \left\lceil \frac{8}{3} \right\rceil = \underline{\underline{3}}$$

$$3 > 2 \quad 3$$

At max how many element
can be there in an array?

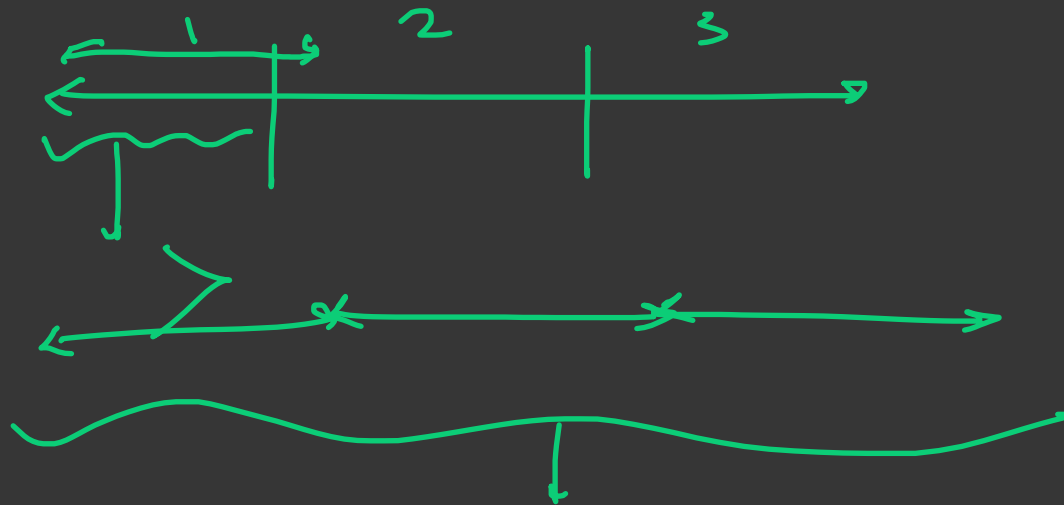
- At minimal a element would have 3 occurrence so, if $3+3+3 = \underline{\underline{9}} > \text{size of array}$.
- We to assume at 3 element of 3 occurrence the size of the array is 9 but it is greater than original size of array
- So, At max we will have only 2 element.

$$\text{eg: } 99 = \left\lceil \frac{99}{3} \right\rceil = \underline{\underline{33}}$$

$$34 + 34 = \begin{array}{r} 68 \\ 34 \\ \hline 102 \end{array} > 99 \quad \text{X}$$

Intuition behind it:

We have said that the occurrence should be more than $\frac{1}{3}$ rd of array size n . $\approx \frac{n}{3}$



more than $\frac{1}{3}$ rd

$$\frac{1}{3} + \frac{1}{3}$$

$$\frac{2}{3}$$

$$\frac{1}{3} \approx 0.33$$
$$\approx \underline{\underline{0.43}}$$

$$\begin{array}{r} 0.4 \\ 0.4 \\ 0.4 \\ \hline 1.2 \end{array}$$

$$\begin{array}{r} 0.33 \\ 0.33 \\ 0.33 \\ \hline 1 \end{array}$$

Brute force:

arr[] = { 1, 1, 1, 2, 2, 2 }

n = 6

count freq. = ans push
↳ int n = n

ans[2] = { _, }
ans[3] = { _, }

```
for (i = 0, i < n, i++)
```

```
int count = 0;
```

```
if (ans[i] != arr[i] || ans.size() == 0)
```

```
for (j = 0; j < n; j++)
```

```
if (arr[i] == arr[j]) {  
    count++;  
}
```

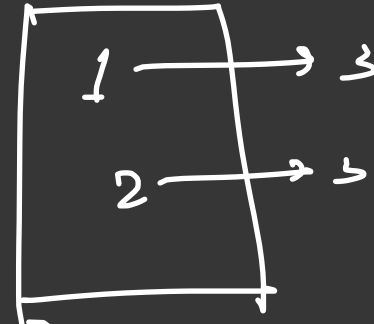
```
if (count % 3 == 0) ans.push
```

T.C. = $O(N^2)$

S.C. = $O(1)$

Better Approach:

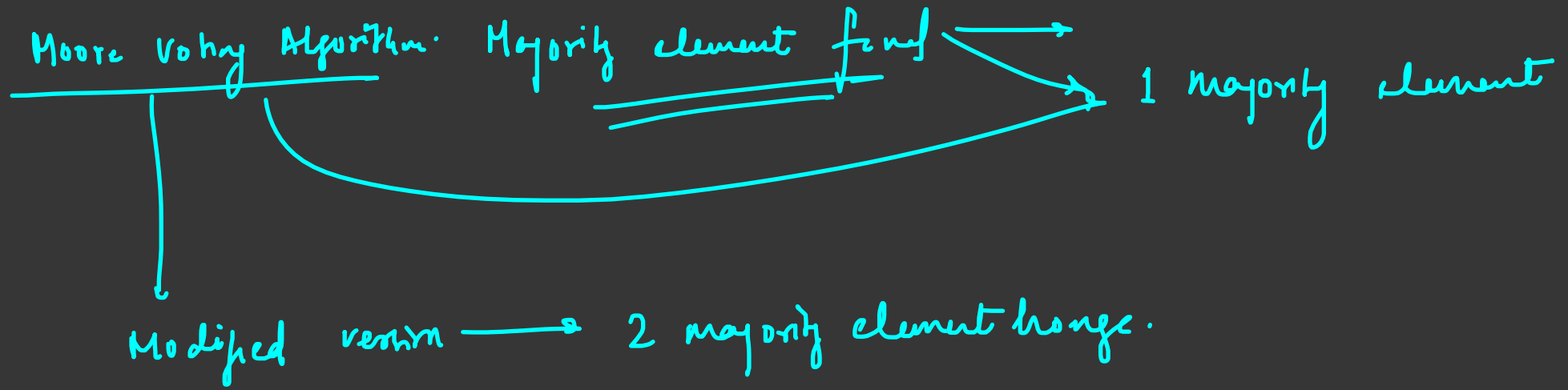
Using hashmaps to store freq



```
for (auto it: hashmap)
    if (it.second > n/3)
        ans = it.first;
```

return ans;

Optimal Approach:



So, we know that we can have only 2 elements which can be more than $n/3$ times.

So, Idea is to find 2 majority element in the array and check if the 2 majority elements are greater than $n/3$ time.

Pseudocode:

ele1, ele2, count1 = 0, count2 = 0.

for (i = 0, i < n, i++)

if (count1 == 0 && arr[i] != ele2)

ele1 = arr[i].

count1 = 1

similar for ele2.

} Moore Voting Algo

To avoid overlapping of majority element.

Cont

$$\underline{\underline{T.C.}} \Rightarrow O(N) + O(N) = O(2N) \hat{=} O(N)$$

$$S.C. : \rightarrow \underline{O(1)} \rightarrow \cdot$$