

# Advanced Recursion

# Steps Revisited:

## **1. Base Case:**

First try to make a base case in order to set up a termination condition.

## **2. Edge Case (Optional):**

This is used to avoid accessing array at the outliers.

## **3. Solving Smaller Sub-Problem:**

Relax, this will be taken care by the recursive call. :)

## **4. Solving the Final Step:**

Recall PMI, we have to work on our final step of calling.

# Replace Character Recursively

Given an input string S and two characters c1 and c2, you need to replace every occurrence of character c1 with character c2 in the given string.

Do this recursively.

## Input Format :

Line 1 : Input String S

Line 2 : Character c1 and c2 (separated by space)

## Output Format :

Updated string

## Constraints :

$1 \leq \text{Length of String S} \leq 10^6$

## Sample Input :

abacd

a x

## Sample Output :

xbxcd

# **Return Subsets of an array**

# Merge Sort

Sort an array A using Merge Sort.

## Input format :

Line 1 : Integer n i.e. Array size

Line 2 : Array elements (separated by space)

## Output format :

Array elements in increasing order (separated by space)

## Constraints :

$1 \leq n \leq 1000$

## Sample Input:

6

2 6 8 5 4 3

## Sample Output:

2 3 4 5 6 8

# Quick-Sort

Sort an array A using Quick Sort.

## **Input format :**

Line 1 : Integer n i.e. Array size

Line 2 : Array elements (separated by space)

## **Output format :**

Array elements in increasing order (separated by space)

## **Constraints :**

$1 \leq n \leq 1000$

## **Sample Input:**

6

2 6 8 5 4 3

## **Sample Output:**

2 3 4 5 6 8

# Return Keypad Code

Given an integer n, using phone keypad find out and print all the possible strings that can be made using digits of input n.

**Note : The order of strings are not important. Just print different strings in new lines.**

**Input Format :**

Integer n

**Output Format :**

All possible strings in different lines

**Constraints :**

$1 \leq n \leq 10^6$

**Sample Input:**

23

**Sample Output:**

ad  
ae  
af  
bd  
be  
bf  
cd  
ce  
cf

# Break - Question

## Staircase

A child is running up a staircase with N steps, and can hop either 1 step, 2 steps or 3 steps at a time. Implement a method to count how many possible ways the child can run up to the stairs. You need to return number of possible ways W.

### Input format :

Line 1 : Integer N (No. of steps)

### Output Format :

Line 1 : Integer W i.e. Number of possible ways

### Constraint :

$(1 \leq N \leq 30)$

### Sample Input 1:

4

### Sample Output :

7



# **Introduction to Dynamic Programming**

# Fibonacci Numbers Revisit

**Break Question-  
Min Steps Revisit**

# Minimum Count

Given an integer N, find and return the count of minimum numbers, sum of whose squares is equal to N. That is, if N is 4, then we can represent it as :  $\{1^2 + 1^2 + 1^2 + 1^2\}$  and  $\{2^2\}$ . Output will be 1, as 1 is the minimum count of numbers required.

**Note :**  $x^y$  represents x raise to the power y.

**Input Format :**

Integer N

**Output Format :**

Required minimum count

**Constraints :**

$1 \leq N \leq 1000$

**Sample Input 1 :**

12

**Sample Output 1 :**

3

**Sample Output 1 Explanation :**

12 can be represented as :

$1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 1^1$

$1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 1^1 + 2^2$

$1^1 + 1^1 + 1^1 + 1^1 + 2^2 + 2^2$

$2^2 + 2^2 + 2^2$

As we can see, the output should be 3.

# Minimum Cost Path

Given an integer matrix of size  $m \times n$ , you need to find out the value of minimum cost to reach from the cell (0, 0) to (m-1, n-1).

From a cell (i, j), you can move in three directions : (i+1, j), (i, j+1) and (i+1, j+1).

Cost of a path is defined as the sum of values of each cell through which path passes.

## Input Format :

Line 1 : Two integers, m and n

Next m lines : n integers of each row (separated by space)

## Output Format :

Minimum cost

## Constraints :

$1 \leq m, n \leq 20$

## Sample Input 1 :

```
3 4
3 4 1 2
2 1 8 9
4 7 8 1
```

## Sample Output 1 :

```
13
```

# Lowest Common Subsequence

A subsequence is a sequence that can be derived from another sequence by deleting some elements without changing the order of the remaining elements. Longest common subsequence (LCS) of 2 sequences is a subsequence, with maximal length, which is common to both the sequences.

Given two strings, S and T, find the value of longest common subsequence and print it as a line of space-separated integers.

## Input Format

The first line contains two space separated integers n and m, the sizes of sequences S and T.

The next line contains string S.

The next line contains string T.

## Constraints

$1 \leq n \leq 100$

$1 \leq m \leq 100$

## Output Format

Print the length of the longest common subsequence as a string on one line.

## Sample Input

```
5 6
abcde
cadbce
```

## Sample Output

```
4
```

## Explanation

The longest common subsequence is “abce” so the length is 4.