

Experiment 8 : Support Vector Machines (SVMs) and the Kernel Trick

Total Marks: 100

1. Learning Objectives

Upon successful completion of this assignment, students will be able to:

Articulate the core concepts of Support Vector Machines, including the **maximal margin hyperplane**, **support vectors**, and the **soft margin** (C) parameter.

Understand and implement the **kernel trick** to solve non-linear classification problems.

Implement and compare the performance of different SVM kernels (**Linear**, **Polynomial**, and **RBF**).

Understand the role of key hyperparameters like C , γ , and degree .

Use `GridSearchCV` to systematically tune hyperparameters for an SVM.

Visualize 2D decision boundaries to intuitively understand how different kernels and hyperparameters work.

Rigorously evaluate and interpret the performance of a highly-tuned SVM on a hold-out test set.

2. Introduction

Support Vector Machines (SVMs) are a powerful class of supervised machine learning models. The core idea is to find an optimal "hyperplane" that best separates the classes in your data.

However, many real-world datasets are **not linearly separable**. You can't draw a single straight line to separate the classes. This is where the **kernel trick** comes in. A kernel function can project your data into a much higher-dimensional space where a linear separator *can* be found, without the massive computational cost.

In this assignment, you will work with a classic non-linear "moons" dataset. You will see firsthand why a linear SVM fails and how kernelized SVMs (RBF, Polynomial) can easily

solve the problem. You will also tune the key hyperparameters (C , γ) that govern the model's behavior.

3. Prerequisites

Ensure your Python environment has the following libraries installed:

```
pip install numpy pandas scikit-learn matplotlib seaborn
```

4. Experiment Tasks

You will use a synthetically generated "moons" dataset, which is a classic example of a non linearly separable problem.

Task 1: Data Loading and Preprocessing (10 Marks)

1. **Load Data:** Generate the `make_moons` dataset from scikit-learn.

```
from sklearn.datasets import make_moons
# Generate 500 samples with noise to make it challenging
X, y = make_moons(n_samples=500, noise=0.25, random_state=42)
```

2. **Create Hold-Out Set:** Perform a single **70/30 split** on the data.

```
X_train, y_train = train_test_split(X, y, test_size=0.3, random_state=42)
```

```
X_val, y_val = train_test_split(X, y, test_size=0.3, random_state=42)
```

Use `train_test_split` with `random_state=42`.

3. **Standardize Features:** This step is **critical** for SVMs, as they are sensitive to the scale of input features.

Fit a `StandardScaler` from `sklearn.preprocessing` on `X_train` only.

Transform both `X_train` and `X_val` using the *fitted* scaler.

You will use `X_train_scaled` and `X_val_scaled` for all model training and evaluation.

Task 2: Model 1 - The (Failing) Linear SVM (15 Marks)

1. **Train Model:**

Import `from sklearn.svm import SVC` (Support Vector Classifier).

Instantiate a linear SVM: `linear_model = SVC(kernel='linear', C=1.0, random_state=42)` .

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fit the model on `X_train_scaled` and `y_train` .

2. Evaluate:

Make predictions on `X_val_scaled` .

Print the `classification_report` and `accuracy_score` .

3. Analyze:

Briefly explain why the accuracy is not perfect. (Hint: Look at the data you generated).

Explain what the `c` parameter represents. What would happen if you set `c` to a very small value (e.g., 0.01)?

Task 3: Model 2 & 3 - The Kernel Trick (25 Marks)

You will now explore non-linear kernels to solve the problem.

1. RBF Kernel Model:

Instantiate a new `SVC` using the **RBF (Radial Basis Function)** kernel: `rbf_model = SVC(kernel='rbf', random_state=42)` . (Use default `C=1.0` and `gamma='scale'`).

fit the model on `X_train_scaled` and `y_train` .

Evaluate on `X_val_scaled` and print the `classification_report` .

2. Polynomial Kernel Model:

Instantiate a new `SVC` using the **Polynomial** kernel: `poly_model = SVC(kernel='poly', degree=3, random_state=42)` . (Use the default `degree=3`).

fit the model on `X_train_scaled` and `y_train` .

Evaluate on `X_val_scaled` and print the `classification_report` .

3. Analyze:

Create a simple table comparing the **Validation Accuracy** of the `linear` , `rbf` , and `poly` models.

Which kernel performed best with default settings? Why does this make sense for the 'moons' dataset?

Task 4: Hyperparameter Tuning with GridSearchCV (30 Marks)

The RBF model was likely the best, but its performance depends heavily on the `C` (regularization) and `gamma` (kernel influence) parameters. You will now find the *optimal*

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combination.

1. Define Search Space:

Create a parameter grid to search. A good starting point is:

```
param_grid = {
    'C': [0.1, 1, 10, 100],
    'gamma': [0.1, 1, 10, 100],
    'kernel': ['rbf']
}
```

2. Setup Grid Search:

Import `from sklearn.model_selection import GridSearchCV`.

Instantiate `GridSearchCV`:

```
grid = GridSearchCV(SVC(random_state=42), param_grid, refit=True, verbose=2,
                    cv=5, scoring='accuracy')
```

`refit=True` ensures the best model is retrained on all `X_train_scaled` data.

`cv=5` specifies 5-fold cross-validation.

3. Run Grid Search:

fit the `grid` object on your *entire* training set (`X_train_scaled`, `y_train`).

4. Analyze Results:

Print the `grid.best_params_` to see the best `C` and `gamma`.

Print the `grid.best_score_` to see the best cross-validated accuracy.

Task 5: Final Evaluation and Visualization (20 Marks)

1. Evaluate Final Model:

The `grid` object now holds the best model. Use it to make predictions on your **hold**

`out set (X_val_scaled).`

`final_predictions = grid.predict(X_val_scaled)`

Print the `classification_report(y_val, final_predictions)` .

Generate and plot a `confusion_matrix` for these final predictions.

2. Visualize Decision Boundaries:

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This is the most important part for understanding *how* the kernels work.

You need to plot the decision boundary for the `linear_model` , the default `rbf_model` , and your final `grid` (best) model.

Hint: Create a 2D mesh grid (`np.meshgrid`), make predictions for *every point* on the grid, and use `plt.contourf` to plot the resulting decision regions. Plot the `X_train_scaled` data points on top.

Create a 1x3 subplot to show the three decision boundaries side-by-side.

5. Submission Guidelines

Submit a single `.zip` archive containing:

1. **Source Code:** A single Jupyter Notebook (`.ipynb`) containing all your code, outputs, and plots.
2. **PDF Report:** A formal report (`StudentID_Report.pdf`) that includes:

Model Comparison: A table showing the **Validation Accuracy** for the four

models: 1. `SVC (kernel='linear', C=1)`

2. `SVC (kernel='rbf', default params)`

3. `SVC (kernel='poly', degree=3)`

4. `GridSearchCV Best Model`

Decision Boundary Plots: The 1x3 subplot from Task 5 showing the decision boundaries for the `linear` , default `rbf` , and final `tuned rbf` models.

Final Performance: Include the **Classification Report** and **Confusion Matrix** for the final tuned model on the 30% hold-out validation set.

Conclusion: Briefly answer the following:

Why did the linear SVM fail, and why did the RBF kernel succeed? (Refer to

your plots).

What did the `GridSearchCV` tell you? What were the best `C` and `gamma` ?

What happens if `gamma` is set *too high* (e.g., 1000)? What happens if `C` is set *too low* (e.g., 0.01)? How would this change the decision boundary?