# **Homework 4: Permutation Testing**

CSC 495, Prof. Robin Burke Spring 2015 Due: 5/21/2015<sup>1</sup>

## **Objective:**

To gain experience with CUG and QAP tests.

## What to do:

- Download the archive file hwk4.zip and uncompress. This archive contains several graph data files: dolphin.graphml, krack-advice.graphml, and krack-friend.graphml. It also contains two utilities which are my reimplementations of the CUG and QAP routines from the SNA library: mycugtest.R and myqaptest.R. There is also a starter file hwk4.R that loads the utilities.
- 2. Run RStudio.

## Part I: Dolphin Network

- 3. Load the dolphin network from dolphin.graphml. This is an undirected network. The Sex attribute is 0 for female, 1 for male, and 2 for a few dolphins where this variable was not known.
- 4. Compute the (global) transitivity of this graph. It should come out around 0.31.
- 5. Our first task is to test if this transitivity is significantly different from what would be expected in a random network of the same density. In other words, can we reject the null hypothesis that the level of transitivity here could be due to chance edge formation?
  - a. Use the mycugtest routine to test the transitivity of the graph against density-conditioned random neworks. You will need to pass "edges" as the cmode parameter and you'll need to supply type= "global" so that transitivity will be calculated correctly each time.
  - b. Use print.cug.text and plot.cug.test to examine the results of the test.
  - c. Can we reject the null hypothesis (p=0.05)? Why or why not?
- 6. Next, test the degree centralization of the network. Recall that centralization is the extent of concentration of degree in nodes in a network.
  - a. Define a function that takes a graph, computes degree centralization and returns just the centralization value. (Remember that centralization.degree returns a named list.)
  - b. Using this function, compute a CUG test for degree centralization.
  - c. Use print.cug.text and plot.cug.test to examine the results of the test.
  - d. What is the null hypothesis in this test? Can it be rejected? Why or why not?
- 7. Next, test the assortativity of the network by sex. (Are male dolphins more likely to be found in the company of other male dolphins?)
  - a. You need to use assortativity.nominal, but note: the types parameter for assortativity.nominal does not allow zero as a value. You will need to add 1 to the Sex attribute before passing it to mycugtest.
  - b. Use print.cug.text and plot.cug.test to examine the results of the test.
  - c. What is the null hypothesis in this test? Can it be rejected? Why or why not?
- 8. Using your degree centralization function from step 6, perform a QAP test on the dolphin network.
  - a. Use the summary gaptest and plot gaptest to examine the results.
  - b. Explain why QAP is not a valid test for degree centralization. How do the results demonstrate this?
- 9. Next, test the assortativity of the dolphin network by sex using the QAP method.
  - a. Use the summary.qaptest and plot.qaptest to examine the results.
  - b. What is the null hypothesis in this test? Can it be rejected? Why or why not?

<sup>&</sup>lt;sup>1</sup> Due dates are before class: 5:30 pm CDT

## Part II

- 10. In this part, we will look at the Krackhardt data from Lab 1. I have already created the networks and stored them in graphml files.
- 11. Load the advice and friend graphs.
- 12. Make the friend graph undirected by collapsing the edges (weak version).
- 13. Use the leading eigenvector method to find communities in the undirected network.
- 14. Plot the friend network with the edges colored according to their community membership.
- 15. Using the CUG test, examine the assortativity of the advice network by the friend communities. (Are the managers more likely to ask advice from those in their friend group?) As before, state the null hypothesis and what your test finds relative to that hypothesis.
- 16. Using the CUG test, examine the assortativity of the advice network by the tenure attribute.
  - a. Note that this is scalar assortativity, so you will use the assortativity function, not assortativity.nominal. The assortativity function requires two parameters: types1 and types2, because it is possible to use different values on each end of a directed edge. For this question, set types1 to be the tenure attribute and types2=NULL.
  - b. What is the null hypothesis in this test? Can it be rejected? Why or why not?
- 17. Repeat the analysis in step 15, but using the OAP test instead.
- 18. Repeat the analysis in step 16, but using the QAP test instead.
- 19. Create an R markdown file hwk4.Rmd and copy your R code into it with appropriate annotations. Include your answers to the hypothesis testing questions in steps 5-9 and 15-18.
- 20. Run hwk4.Rmd and save the resulting HTML as hwk4.html.
- 21. Combine hwk4.R, hwk4.Rmd, and hwk4.html into a zip archive. No need to include the utility files or the data files.

#### What to turn in

Upload your zip archive to the Homework 4 dropbox on D2L before class on 5/21.

### Rubric

- Step 5, 1 pt (0.5 mechanics, 0.5 explanation)
- Step 6, 1 pt
- Step 7, 1 pt
- Step 8, 1 pt
- Step 9, 1 pt
- Step 14, 1 pt
- Step 15, 1 pt
- Step 16, 1 pt
- Step 17, 1 pt
- Step 18, 1 pt