

ACOL 215

(24 Sept.)

|| Exercise Find the prime implicants of
 $F(w,x,y,z) = \sum (0,2,4,5,6,7,8,10,13,14,15)$

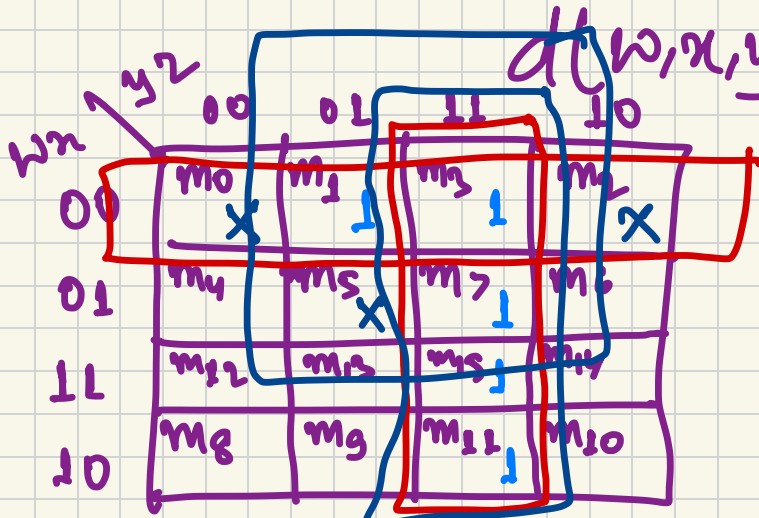
Don't care conditions

Simplify the Boolean function

$$F(w, x, y, z) = \sum (1, 3, 7, 11, 15)$$

which has don't care conditions

$$d(w, x, y, z) = \sum (0, 2, 5)$$



$$yz + w'x'$$
$$yz + w'z$$

Simplify

$$F(w, x, y, z) = \sum (4, 5, 6, 7, 12)$$

with

$$d(w, x, y, z) = \sum (0, 8, 13)$$

Ans

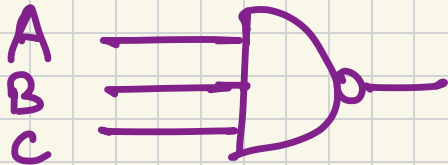
$$y'z' + w'x \quad (\text{check})$$

NAND and NOR implementation

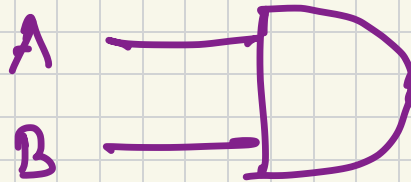
Digital circuits are frequently constructed with NAND and NOR gates.

Why? Easier to fabricate with electronic components.

NAND



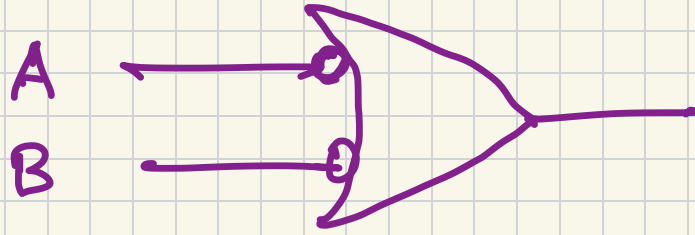
$(ABC)'$



$(A \text{ NAND } B)$
 $\text{NOT } (A \text{ AND } B)$

AND-invert

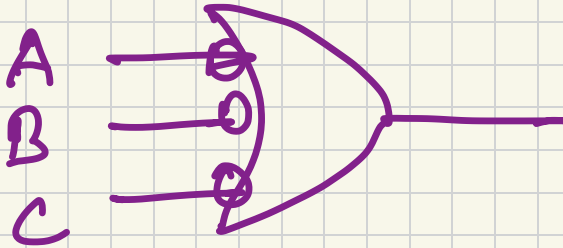
Other graphical representation



NOT A OR NOT B

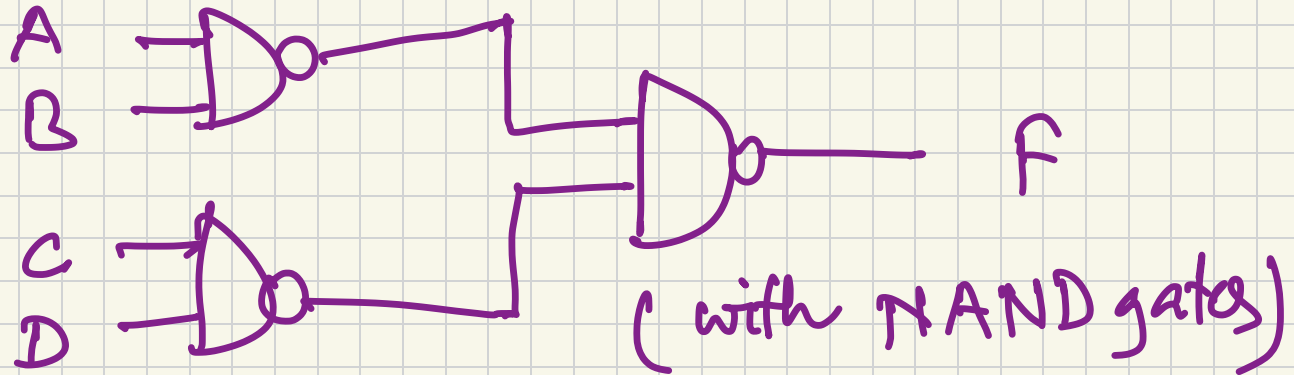
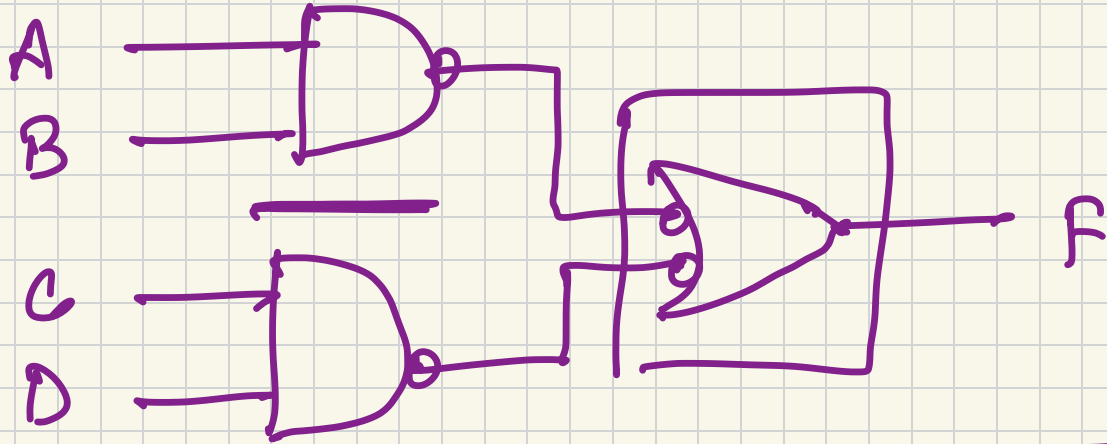
NOT (A AND B)

A NAND B



Invert - OR

$$F = AB + CD$$

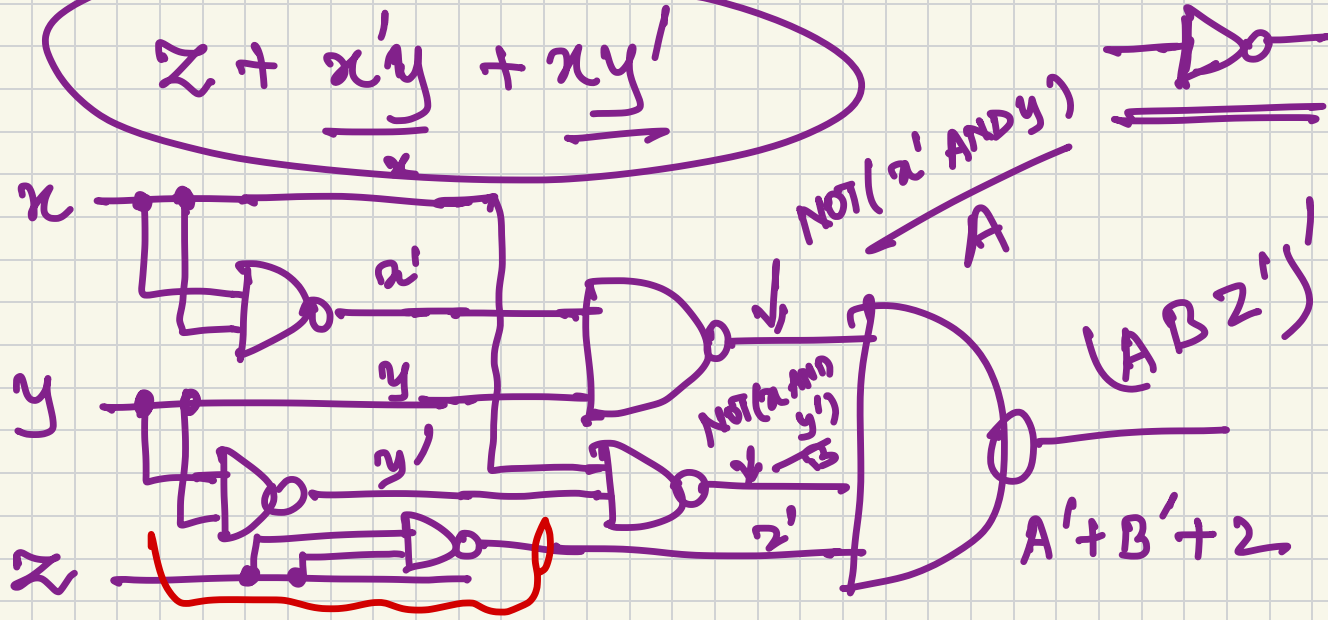


Exercise

Implement the following with
NAND gates.

$$F(x, y, z) = \sum (1, 2, 3, 4, 5, 7)$$

$$z + \frac{x'y}{x} + \underline{xy'}$$



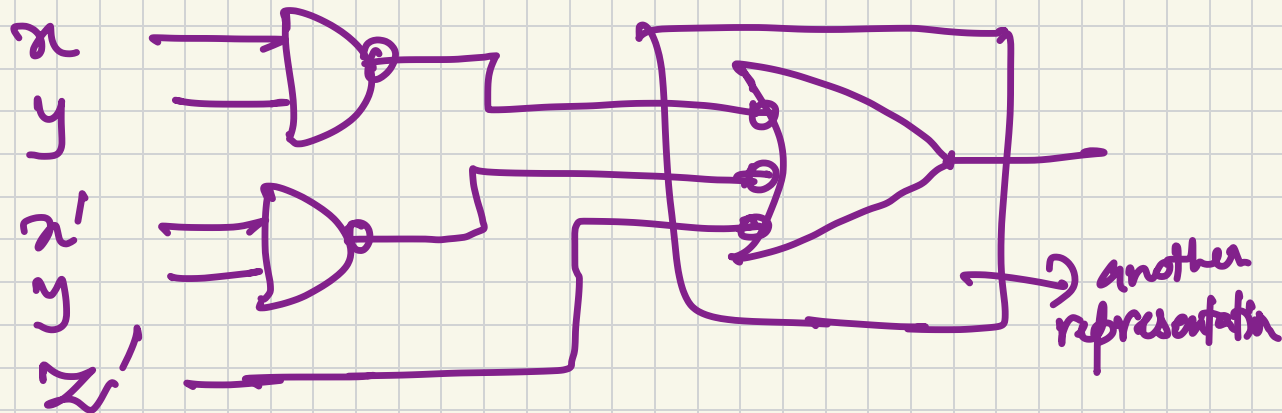
Exercise

Implement $F(x, y, z)$

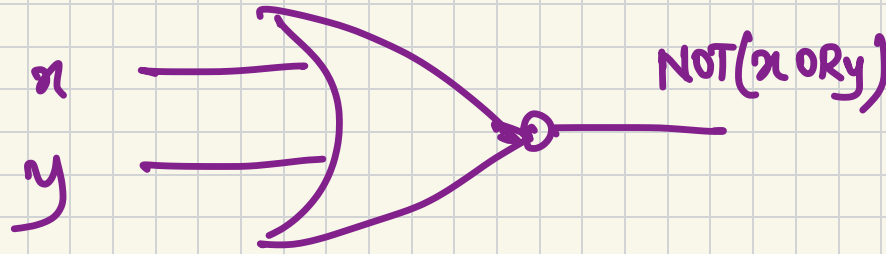
$$= \sum (0, 1, 3, 5, 6, 7)$$

with NAND gates.

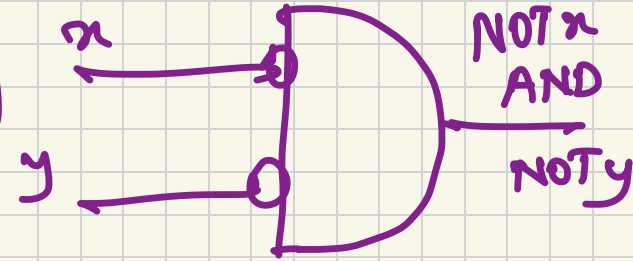
$$F = \underline{z + x'y' + xy}$$



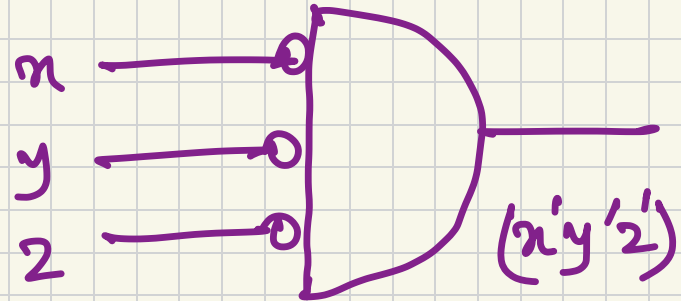
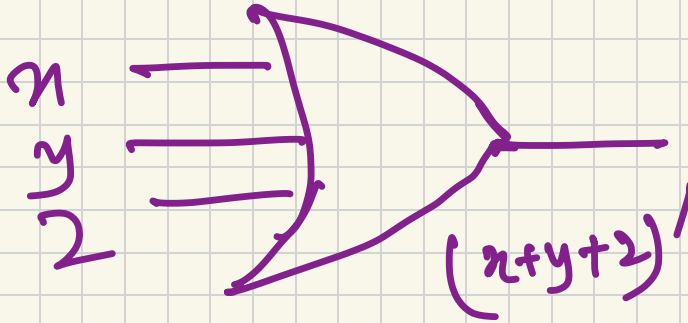
NOR implementation



OR - invert

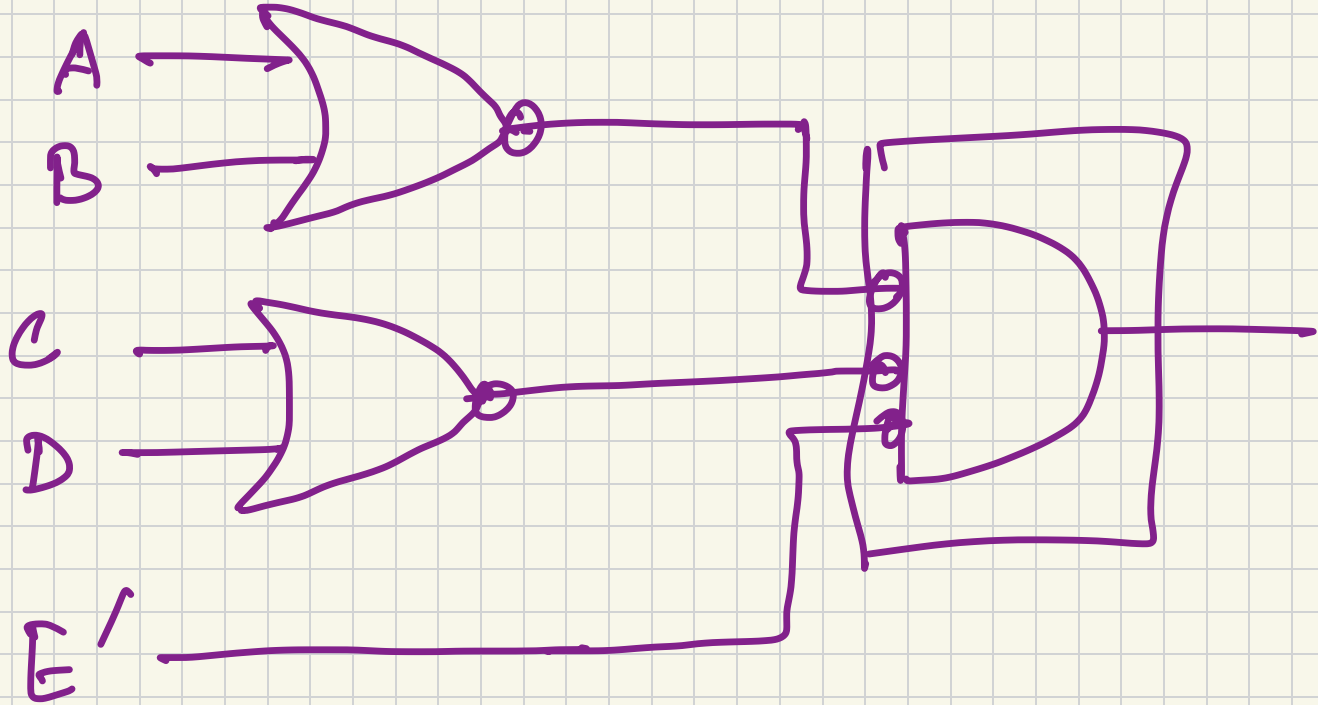


invert - AND



Example

$$F = (A+B)(C+D)E$$

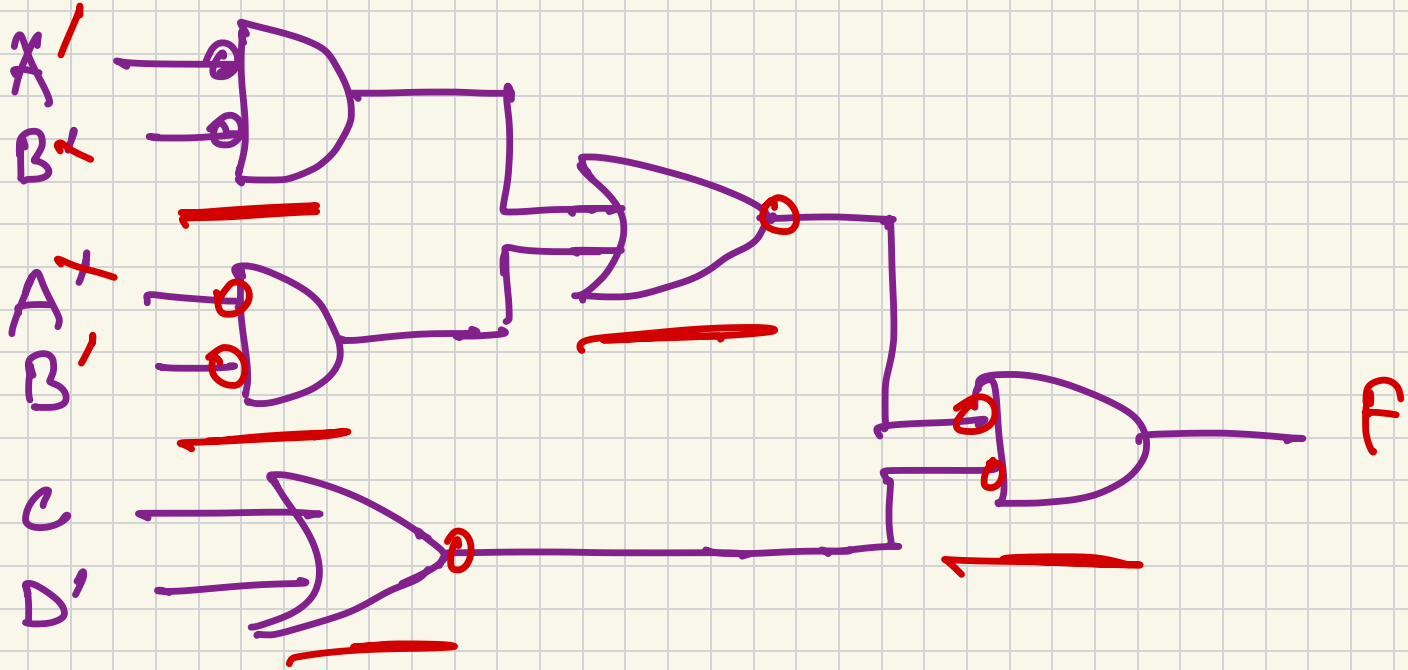


Exercise

Implement

$$F = (AB' + A'B)(C + D')$$

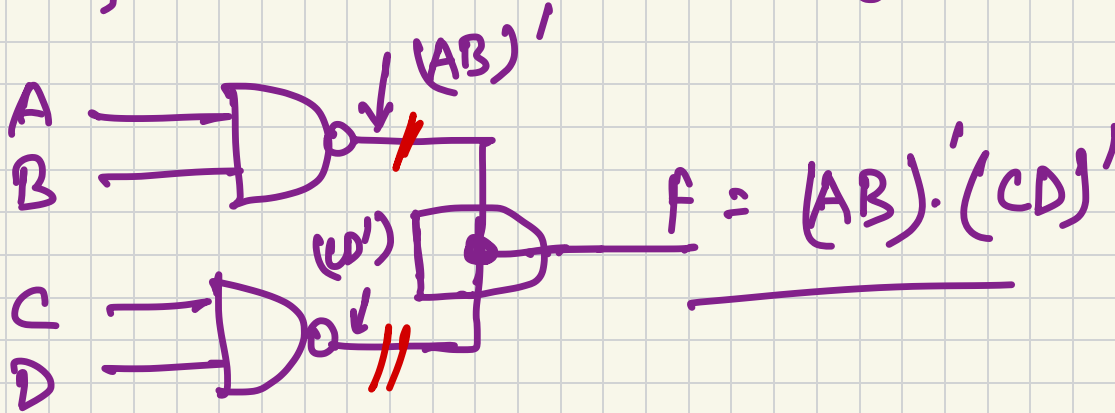
with NOR gates.



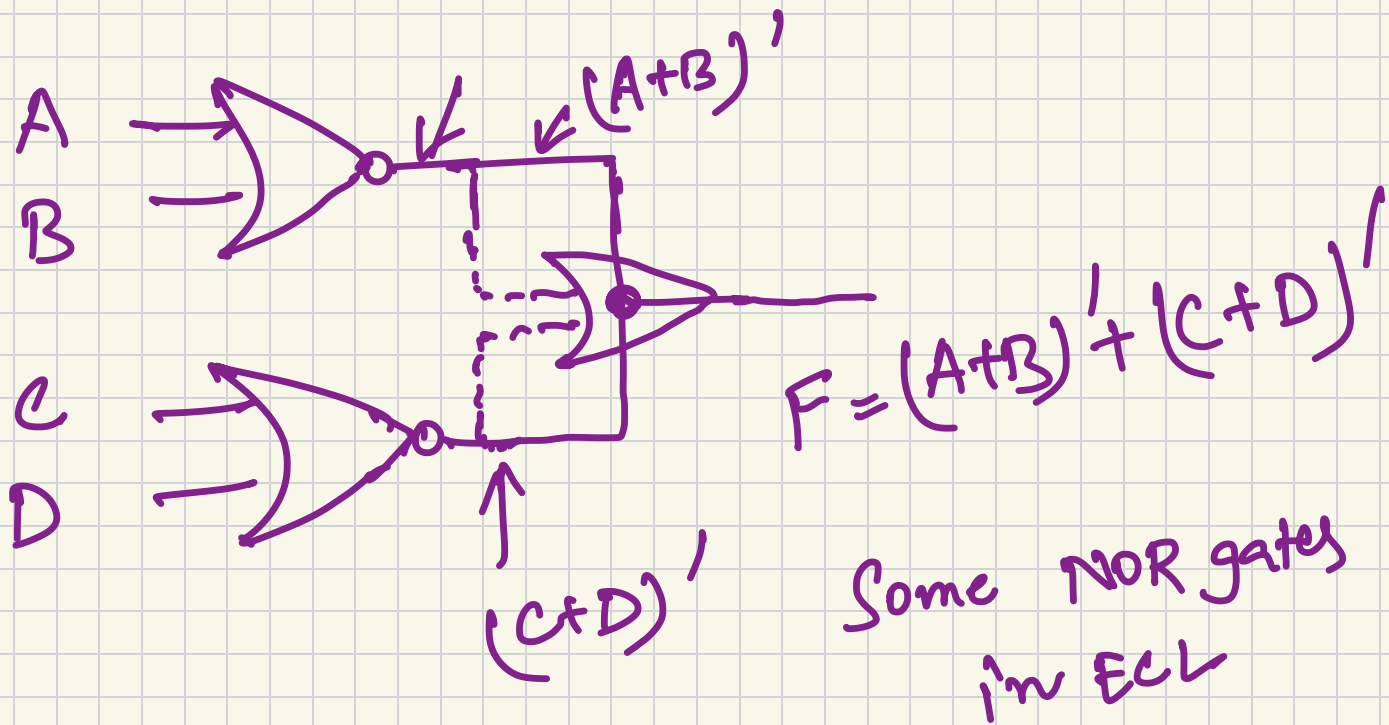
Two-level implementations

TTL

Some NAND and NOR gates allow a wired connection between the outputs of two gates to implement a specific logic function (wired logic).



AND-OR-Invert function



OR-AND-Invert Function