- 1. Are $\lfloor x \rfloor + \lfloor y \rfloor$ and $\lfloor x + y \rfloor$ always equal? Why or why not?
- 2. Is $\lfloor \frac{n+1}{2} \rfloor = \lceil \frac{n}{2} \rceil$ true? Explain.
- 3. A perfect number is a positive integer n that has the following property: n is equal to the sum of all positive integers k < n that evenly divide n. For example, 6 is a perfect number, because 1, 2, and 3 are the positive integers less than 6 that evenly divide 6, and 6 = 1 + 2 + 3. Find the next perfect number after 6. You may find it easy to write a program that finds the next perfect number after 6.
- 4. Compute the value of the summation: $\sum_{i=1}^{6} i \cdot 2^{i}$
- 5. Rewrite the following set by exhaustively listing its elements.

$$\{n\in\mathbb{Z}\ \mid\ 0\leq n\leq 20\quad \text{ and }\quad n\bmod 5\ =\ n\bmod 7\}$$

6. [4 marks] Prove that set intersection distributes over set union, i.e.

$$A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$$