

# # How to build Strong Programming Logic?

"If I had 1 hour to chop down a tree, I'd take 45 min to sharpening my Axe"

— Abraham Lincoln

- \* (1) Concepts  $\Rightarrow$  Contests  $\xrightarrow{\text{Rank Ratings}}$
- + min 375 Ques from excel sheet provided (till medium level questions)
  - + Practise & do them only then part for contests

## # (2) THINK $\Rightarrow$ CODING

- Read the Question carefully
- make algo with (pen + paper)
- corner Cases  
(ye sei kaha kaha fas sakte hai)
- Dry Run with 2 sample Inputs

## (3) STEP - BY- STEP

(i) Basic Approach



(ii) Time reduce (DSA apply)



(iii) Reduce space

## (4) PRACTISE

(i) 3 days Rule → Max. 3 days se jada don't leave for practise  
the concept / logic

(ii) 1 hr each day

## (5) MOVE - ON

Easy : 5-10 min

Medium : 15-20 min

Hard : 40-60 min

company expectation

# 5 Basic Principles

↓ X  
(SMART WORK)

## (1.) ODYSSEUS METHOD

- Cut off all your Distraction
- Remove all the things that makes u feel distracted

## (2.) PARETO PRINCIPLE

⇒ 20% Input result → 80% Output

⇒ Read the syllabus

↓  
Read the topic

↓  
But search from

↓  
class Notes



"Combine them  
"common"  
part

## (3.) SPACED REPETITION (POMODORO)

⇒ 1½ hr + 5-10 min  
(focus) (Break)

## (4.) PARKINSON'S LAW

- ⇒ Set deadline for your each work
- ⇒ Pre-plan your work

⇒ Pre-planned includes:

- What to study
- When to study

& follow your Deadline

### (5.) Active Recall

→ 1st Read your topic + Analyse them  
↓  
then go for notes making  
(think about that topic & write notes  
by yourself)

⇒ Long Term Planning

→ Redefine

→ Redefine

→ Redefine

→ Redefine

→ Redefine

② Working in groups with each other

→ Redefine

# # Coding Platforms #

## # Beginners :

- Hacker Rank
- HackerEarth
- Geeks for Geeks

## # Placement / Interview Prep :

- LeetCode
- InterviewBit

## # Competitive Programming

- Codeforces
- CodeChef

① GitHub

② IIT Bombay → AdX → Online course platform:

# Java Lecture

- Shradha Mam (Atpna College)

Lect - 1

## Introduction to Java Language

- \* Pseudocode : → sample code containing only logic part  
↓  
to represent flow of code in simple English language

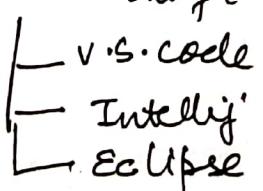
Pseudocode

- 1) start
- 2) Input 2 NO.
- 3) calculate sum = number 1 + number 2
- 4) Print sum
- 5) exit

## Installation

1) Java Development Kit (JDK)

2) Code Editor (IDE)  
Integrated development environment



"java"

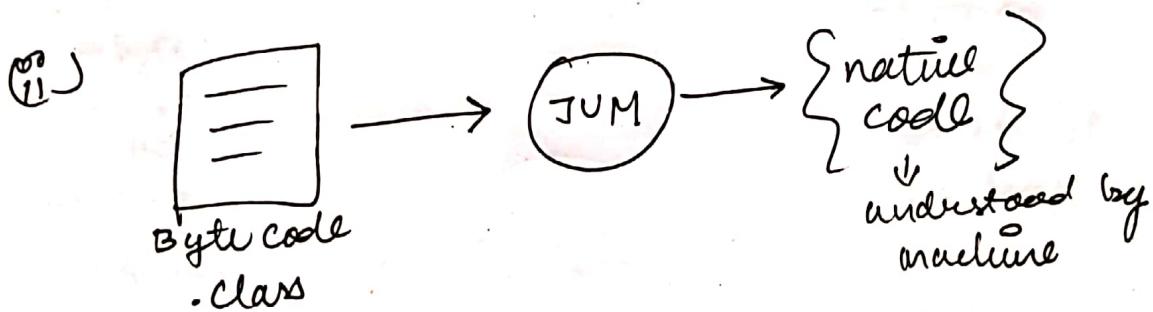
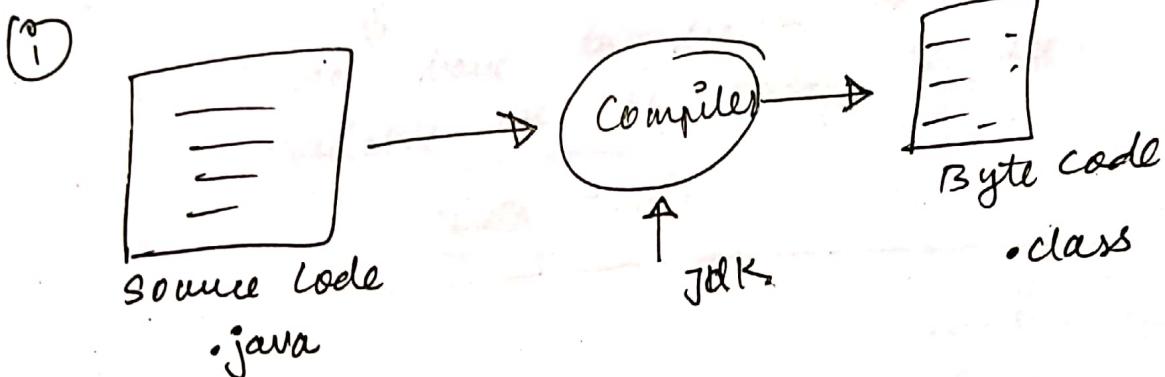
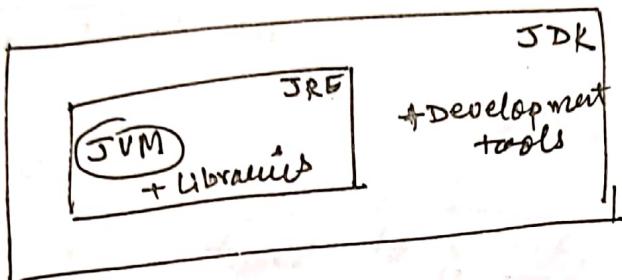
Q. How is my code running?

⇒ (i) Compilation

(ii) Execution

\* JDK contains JRE  
↓  
Java Runtime Environment

JVM : Java Virtual Machine



function

void main()  
{  
}

In main() the sequence to execute first  
compile & then .

## Lecture - 2

E - notes

### Output

System.out.print()



System class

- + **Border code** ⇒ go code by default editor  
see modifications ant this

### Variables

- \* Java is a **typed language**  
we have to declare the type of variable we are going to use.

**Data Type**

#### **Primitive**

- byte
- short
- int
- long
- double
- float
- char
- boolean

#### **Non-Primitive**

- String
- Array
- class
- object
- Interface

**1 byte = 8 bits**

- \* sc.next() → read only 1<sup>st</sup> word
- \* sc.nextLine() → read whole sentences / paragraph.

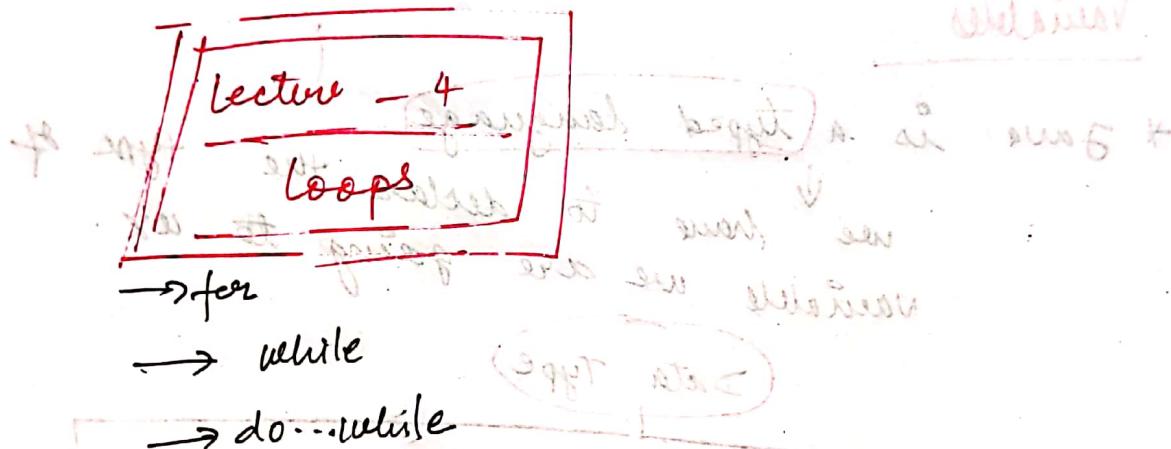
## Lecture - 3

### Conditionals statements

Keywords → if, else, elseif, switch, break, continue

% → calculate remainder (modulo)

break → terminate the condition or exit the condition



① for (initialise ; condition ; updation)

② while (condition)

③ do

    while (condition);

        if condition  
        breaks false

    executes once

## Lecture - 5

### 9 Best Pattern Questions in Java

#### (1) Pattern - 1

(Solid Rectangle)

$\tau = 4$        $s = c$

*	*	*	*	*
*	*	*	*	*
*	*	*	*	*
*	*	*	*	*

★  
★  
★  
★

$\tau = 4$

Nested loop:

```
for (i=1 ; i<=4 ; i++)
```

{

```
    for (j=1 ; j<=5 ; j++)
```

{

```
        sout("*");
```

```
    sout("\n");
```

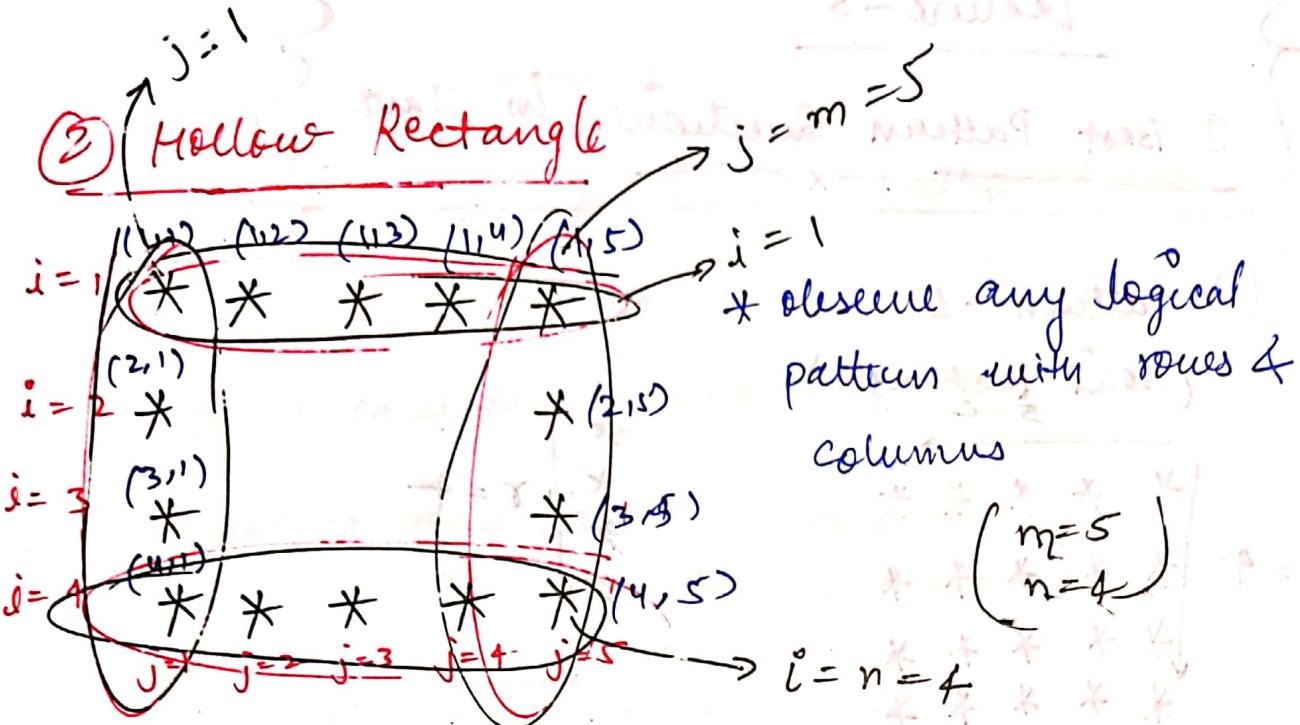
{

```
    ++i;
```

```
} m == i || i == 2 || j == 2 } if
```

$m = j$

```
; ("*") two
```



columns (innerloop)

row  
(outerloop)

\* Boundary

int  $n = 4, m = 5;$

for ( $i = 1 ; i \leq 4 ; i++$ )

{  
    for ( $j = 1 ; j \leq 5 ; j++$ )

{

        if ( $i == 1 || j == 1 || i == n ||$

$j == m$ )

{  
        cout ("\*");

{

```

else
{
    sout(" ");
}

3//for - inner
sout("\n");

3//for - outer

```

### (3) Half Pyramid Pattern

```

*
* *
* * *
* * * *

```

1<sup>st</sup> row  $\rightarrow$  1 star

2<sup>nd</sup>  $\rightarrow$  2 stars

3<sup>rd</sup>  $\rightarrow$  3 stars

4<sup>th</sup>  $\rightarrow$  4 stars

\* No. of row = No. of stars \*

for (i=1; i<=n; i++)

{ for (j=1; j<=i; j++)

{ sout("\*");

{ sout("\n");

}

#### (4) Inverted Half Pyramid

\*\*\*\*\*

$n=4$

\*\*\*

\*\*

\*

```
for(i=n; i>=1; i--)
```

{

```
    for(j=1; j<=i; j++)
```

{

```
        cout<"*";
```

{

```
        cout<"\n";
```

{

```
    }
```

```
    for(j=i+1; j>i; j--)
```

```
    {
```

```
        cout<"*";
```

```
    }
```

```
    cout<"\n";
```

```
}
```

## (5) Inverted Half Pyramid

(rotated by  $180^\circ$ )

$n=4$

$$\begin{array}{l}
 \text{space} \quad \left[ \begin{array}{l} \text{space} + \text{star} \\ \hline 3 \end{array} \right] = 4 \\
 - - * \quad \leftarrow 3 \text{ space} + 1 \text{ star} = 4 \\
 - - * * \quad \leftarrow 2 \text{ space} + 2 \text{ star} = 4 \\
 - * * * \quad \leftarrow 1 \text{ space} + 3 \text{ star} = 4 \\
 * * * * \quad \leftarrow 0 \text{ space} + 4 \text{ star} = 4
 \end{array}$$

\* Point Space \*

row	space	star
row 1	$3 = n - i$	$i = 1$
2	$2 = n - i$	$i = 2$
3	$1 = n - i$	$i = 3$
4	$0 = n - i$	$i = 4$

3 loop → no. of rows  
 1 loop → space  
 1 loop → star

// row

```

for (i=1; i<=n; i++)
{
    // space
    for (j=1; j<n-i; j++)
    {
        cout(" ");
    }
    // star
    for (j=1; j<=i; j++)
    {
        cout("*");
    }
    cout("\n");
}
    
```

## (6) Half Pyramid with Number

1 → row=1 no. 1 to 1  
1 2 → row=2 no. 1 to 2  
1 2 3 → row=3 no. 1 to 3  
1 2 3 4 → row=4 no. 1 to 4  
1 2 3 4 5 → row=5 no. 1 to 5

n=5

```
for (i=1; i<=n; i++)  
{  
    for (j=1; j<=i; j++)  
    {  
        cout << j++;  
    }  
    cout << endl;  
}
```

(\*+\* i <= n > i <= i) ref

(\*+\* i <= i <= n > i <= i) ref

(\*(" ") two)

ref

(\*+\* i <= i <= i) ref

(\*(" ") two)

ref

# (7.) Inverted Half Pyramid with Nos.

Diagram showing the structure of an inverted half pyramid with numbers:

1 2 3 4 5	$\rightarrow \text{row } = 1$	(i)	(j) 5 to 1
1 2 3 4	$\rightarrow r = 2$		1 to 4
1 2 3	$\rightarrow r = 3$		1 to 3
1 2	$\rightarrow r = 4$		1 to 2
1	$\Rightarrow r = 5$		1 to 1

$n=5$

```
//row  
for(i=1 ; i<=n ; i++)  
{  
    for(j=1 ; j<=(n-i+1) ; j++)  
        cout<(j+" ");  
    cout<endl;  
}
```

## (8.) Floyd's Triangle

Diagram of Floyd's Triangle:

1	2 3	4 5 6	7 8 9 10	11 12 13 14 15

Level 1 val (1)  
Level 2 val (2 3)  
Level 3 val (4 5 6)  
Level 4 val (7 8 9 10)  
Level 5 val (11 12 13 14 15)

→ r = 1  
→ r = 2  
→ r = 3  
→ r = 4  
→ r = 5

n=5 (total no. of rows)

int number = 1;  
// row  
for (i=1; i<=n; i++)  
{  
 for (j=1; j<=i; j++)  
 {  
 cout << number << " ";  
 number++;  
 }  
 cout << endl;  
}

(90)

0-1 Triangle

(j)

$$\rightarrow r = 1$$

1

$$\rightarrow r = 2$$

0 1

1 0 1

$$\rightarrow r = 3$$

0 1 0 1

$$\rightarrow r = 4$$

1 0 1 0 1

$$\rightarrow r = 5$$

(3)

Value (1)

2<sup>val</sup>

(0,1)

3<sup>val</sup>

(1,0,1)

4<sup>val</sup>

(0,1,0,1)

5<sup>val</sup>

(1,0,1,0,1)

n=5

		2				
		1	0	1	0	1
1		1	0	1	0	1
2		(2,1)	(2,2)			
3		(3,1)	(3,2)	(3,3)		
4		(4,1)	(4,2)	(4,3)	(4,4)	
5		(5,1)	(5,2)	(5,3)	(5,4)	(5,5)
		1	2	3	4	5

$(i+j) \Rightarrow \text{odd}$  sum = point  $\rightarrow 0$

$(i+j) \Rightarrow \text{even}$  sum = point  $\rightarrow 1$

for ( $i=1$  ;  $i \leq n$  ;  $i++$ )

{ for ( $j=1$  ;  $j \leq i$  ;  $j++$ )

{ int sum =  $i+j$ ;

if (sum % 2 == 0)

{ even

sout("1");

}

else

{

if odd

(cout < "0");

((e3))

3/1 for

(cout < "1n");

3/1 four - outer

i = 5 (base)

int m[5][5] = {

{0, 1, 2, 3, 4}

0	1	2	3	4
1	0	2	3	4
2	1	0	3	4
3	2	1	0	4
4	3	2	1	0

0 ← triag = m[0][block(i+1)]

1 ← triag = m[1][m[0][block(i+1)]]

(++j; i >= 0; i--) do

(++(i -> j); i = 0) do

(i = 0 = m[0][tri]

(0 = 0 = s.p(m[0])) b

## Lecture - 6

### # Advanced Pattern Questions #

#### (10) Butterfly Pattern

```

    *
   * *
  * * *
 * * * *
* * * * *
* * * * *
* * * * *
* * * * *
* * * * *

```

$N = m = 6$

Focus on this part  
just reverse the loop.

$i = 1$

$j = 1$

$k = 1$

(10)

row	1 <sup>st</sup> part star	Space	2 <sup>nd</sup> part star
1	1	6	1
2	2	4	2
3	3	2	3
4	4	0	4

# row no. = no. of stars in 1<sup>st</sup> part

$((n-i)) = \text{no. of stars in } 2^{\text{nd}} \text{ part}$

★ How to print spaces = ?

Spaces

$2 * 3 \rightarrow (n-i) (4-1)$   
 $2 * 2 \rightarrow (n-i) (4-2)$   
 $2 * 1 \rightarrow (n-i) (4-3)$   
 $2 * 0 \rightarrow (n-i) (4-4)$

1<sup>st</sup> half  $\Rightarrow$  (1 to n)  $\Rightarrow$  row loop  
2<sup>nd</sup> half  $\Rightarrow$  (n to 1)  $\Rightarrow$  row loop

i = n = 4  
Space =  $2 * (n - i) = 2 * 0 = 0$

Star = 4 + 4

i = 3  
Space =  $2 * (n - i) = 2 * 1 = 2$

Star = 3 + 3 + 2 + 2 + 2

\* Condition gets flip by some number

```
int n = 5;
for(i=1; i<=n; i++) {
    // star -> 1st part
    for(j=1; j<=i; j++)
        cout<<"*";
}
```

for { } of row 2 from = on two \*

// space

int space =  $2 * (n - i)$ ;

for (j=1; j<=space; j++)

sout(" "));

// start - 2<sup>nd</sup> part

for(j=1; j <= i; j++)

{

cout ("\*");

3

cout ("\\n");

3 // for

// lower half pattern

for(i=n; i >= 1; i--)

{

cout ("\*");

cout ("\*");

remain same as above loop :-

3

cout ("\*");

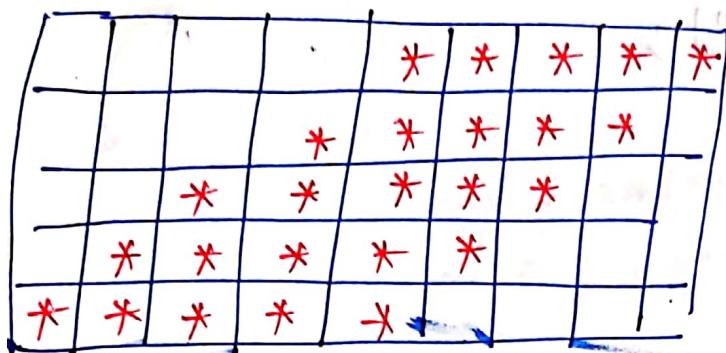
cout ("\*");

-2

cout ("\*");

## (II) Solid Rhombus

$n = 5$



row = 5

each row = 5 star

Matrix form  
Convert

$i$	Space	Star
1	4 space	5 star
2	3 space	5 star
3	2 space	5 star
4	1 space	5 star
5	0 space	5 star

$i = \text{row}$

$\downarrow$

$(n - i)$

const.

for ( $i = 1; i \leq n; i++$ )

{

11 spaces

for ( $j = 1; j \leq (n - i); j++$ )

{

```

cout("11*");
}
11 stars
for(j=1 ; j<=5 ; j++)
{
    cout("*");
}
cout("\n");

```

(13)

### Number Pyramid

```

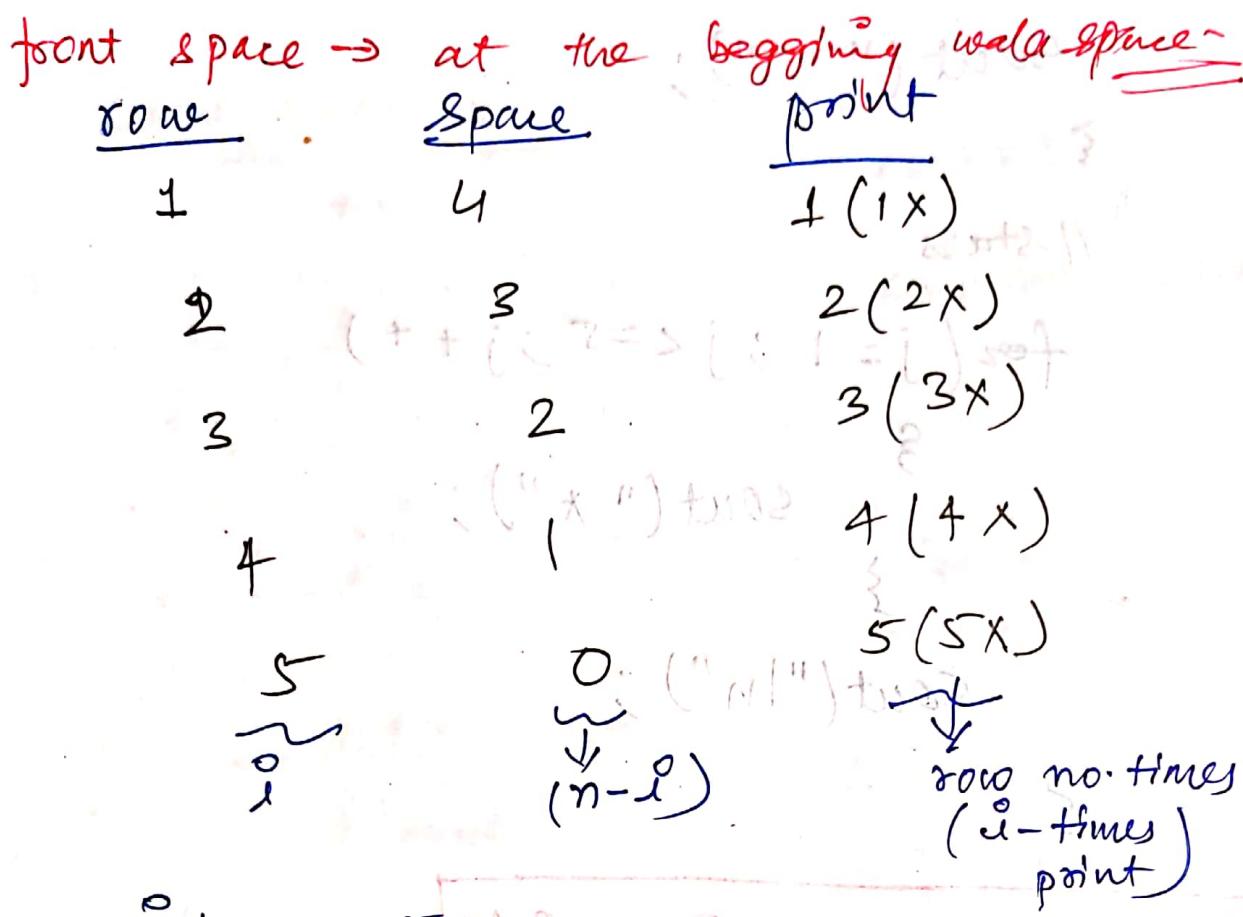
    1
   2 2
  3 3 3
 4 4 4 4
5 5 5 5 5

```

D  $\Rightarrow$  space

n = 5

<u>Step</u>	<u>Star</u>
1	1 $\rightarrow$ 1 time
2	2 $\rightarrow$ 2 time
3	3 $\rightarrow$ 3 time
4	4 $\rightarrow$ 4 time
5	5 $\rightarrow$ 5 time



```

int n = 5;
for (i=1 ; i<=n ; i++)
{
    // spaces
    for (j=1 ; j<=(n-i) ; j++)
    {
        cout << " ";
    }
    // numbers → print row no → row times
    for (j=1 ; j<=i ; j++)
    {
        cout << i << " ";
    }
    cout << endl;
}
// for

```

### (13') Palindromic Pattern

$\rightarrow$  BOB front + back same Edite  
 $\rightarrow$  121 hori

divide in 2 parts

1	1	1	1	1				
1	1	1	1	1				
1	1	2	1	2				
1	1	3	2	1	2	3		
1	4	3	2	1	2	3	4	5
5	4	3	2	1	2	3	4	5

i

space

1

2

3

(i)

4

3

2

1

n-i

1st half

No.

1 to 1

2 to 2

3 to 3

4 to 4

5 to 5

2nd half

No.

X

2.

2, 1, 0, 3

2, 1, 0, 4

2, 1, 0, 5

~~into +~~

~~j = i to 1~~

~~j = 1 to i~~

~~j = 1 to i~~

~~j = 2 to i~~

~~j = 2 to i~~

~~j = 2 to i~~

Print n=5;

// rows

for (i=1; i<=n; i++)

// spaces

for (j=1; j<= (n-i); j++)

sout(" ");

}

// 1st half Numbers

~~for(j=i ; j>=1 ; j--)~~

~~cout(j);~~

~~{~~

~~1/2nd half-numbers~~

~~for(j=2 ; j<=i ; j++)~~

~~{~~

~~cout(j);~~

~~for loop~~

~~-04~~

~~X~~

~~3/1 for~~

~~cout("n");~~

~~+01~~

~~for loop~~

~~+ at 2~~

#### (14\*) Diamond pattern

\* \* \* \* \*

\* \* \* \* \*

\* \* \* \* \*

\* \* \* \* \*

\* \* \* \* \*

\* \* \* \* \*

\* \* \* \* \*

\* \* \* \* \*

\* \* \* \* \*

\* \* \* \* \*

2 part

part 1

part 2

part 3

part 4

part 5

part 6

Upper half

1

2

(i) 3

Space

3

2

(n-i) 1

1

3

5

(2\*i-1)

lower half

$\Rightarrow$  just flip the row no.  $\rightarrow$  remaining will be same as upper half.

int n = 4;

//Upper Half

for (i=1; i<=n; i++)

{

// spaces

for (j=1; j<=(n-i); j++)

{

sout (" " );

{

for (j=1; j<=(n-i); j++)

{

{

{

for (j=1; j<=(2\*i-1); j++)

{

sout ("\*");

~~sout("n");~~

~~3//for~~

// lower half

for (~~i=0~~; i >= 1; i--)

~~last -> { last ->~~

// spaces

for (~~j=0~~; j <= ~~(n-i)~~; j++)

sout(" ");

space

// star

for (~~j=1~~; j <= ~~(2\*i - 1)~~; j++)

~~{ i = j } ref~~

sout("\*");

~~(++i; { } => i; i = i) ref~~

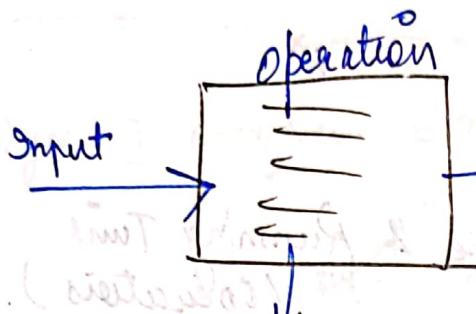
sout("n");

~~{ } two~~

note:- To replicate any pattern (flip)  
j's value par two depend for ratio (i/i)  
as value no opp flip kar do.

## Lecture - 7

### \* Functions & Methods +



syntax:

public static returnType functionName ( )  
{  
    }  
    }

void  $\Rightarrow$  no return type

functions

(we  
call them  
directly)

method

(we  
call  
by  
Class or object  
creating object)

## Lecture - 8

F - notes

### Time Complexity & Space Complexity

#### Time Complexity

Rel. b/w. Input size & Running Time  
(Operations)

\* Times less  
\* Space less

## Lecture - 9

### Array Introduction (1-D Array)

provide space

`type[] arrayName = new type[size];`

↑  
keyword  
non-pointing data type; ke  
space to store the data

⇒ index starts from ⇒ "0" (zero)

⇒ address of memory stored in hex decimal

// Input:  
`int [] marks = new int[5];`

// display array

```
for(i=0 ; i<arr.length ; i++)  
    {  
        System.out.println(arr[i]);  
    }
```

→ linear fashion memory allocation

(contiguous)

→ by default null values gets initialized

// input array

```
for(i=0; i<size; i++)  
    arr[i] = sc.nextInt();
```

// Linear Search

```
for(i=0; i<arr.length; i++)  
    if(arr[i] == val)  
        (ans) sout(i);
```

Linear Search

in best

Linear Search

Linear Search

(i+j < n) (i+j >= 0) (i+j)

((i+j) % n) % 2

whether

prime number search

whether digit below zero even triplet for

## Lecture - 10

### 2-D - Array

					row
					0 1 2 3 4
0					
1					
2					

↓ column

row = 3

column = 5

(row x column) x datatype

int [][] arr = new int [3][5];

row ↑      ↑ column

// Input :

```

for (i=0 ; i<row ; i++)
{
    for (j=0 ; j<column ; j++)
        arr[i][j] = sc.nextInt();
}

```

// Output of 2-d array → Matrix format

```

for (i=0 ; i<row ; i++)
{
    for (j=0 ; j<column ; j++)
        cout [arr[i][j]+ " "];
}

```

```

    cout ("\\n");
}
// linear search
for (i=0 ; i < row ; i++)
{
    for (j=0 ; j < column ; j++)
    {
        if (arr[i][j] == val)
        {
            cout (i + " " + j);
        }
    }
}

: topic II
( ++i ; row > i ; 0 = i ) not
( ++i ; column > i ; 0 = i ) not
{ cout (arr[i][j]);
}

transfer value + given by if transfer II
( ++i ; row > i ; 0 = i ) not
( ++i ; column > i ; 0 = i ) not
{ cout (arr[i][j]);
}

```

## Lecture - 22

### Java OOPS in 1 shot

\* "new" keyword  $\Rightarrow$  memory ke ander ;  
 $\Rightarrow$  memory heap me ek jagah  
 allocate ho jayegi us jagah ke  
 ander , hamari function - ki puri object  
 will get stored there .

Student s1 = new

Student();

constructor

to create something  
i.e., its objects

### Basic Java - Class

Eg:-

class Pen

{ string color;

public void printColor()

{ sout("Colour of this Pen" + this.color);

}

} // class

// main class

```

public class Main
{
    public static void main (String args[])
    {
        Pen p1 = new Pen();
        Pen p2 = new Pen();
        p1.color = "blue";
        p2.color = "black";
        p1.printcolor();
        p2.printcolor();
    }
}

```

- \* java has garbage collector  
(NO destructor unlike C++, C)
- \* Polymorphism
  - ↳ f<sup>n</sup> overloading
  - ↳ f<sup>n</sup> overriding
- \* see package → @ 39:00 min in this video -
- \* Main class → public → access to compiler
- \* if access modifier used ⇒ protected
  - ↳ we can use them only by creating its getter & setter in other class.

## Encapsulation

class - object (identity)  
(methods)  
(properties)

Data Hiding is possible with the help  
of encapsulation.

with the help of Access Modifier

Abstraction  $\Rightarrow$  user ko imp. cheez dikhaa  
& non-imp things chupaa lena.

f ~~instantiate~~ \* instantiation  $\Rightarrow$  to create

## Static - Keyword

$\Rightarrow$  it can be accessed anywhere  
the class or outside the class

$\Rightarrow$  properties common to all

$\Rightarrow$  static ko 1 baar memory di jati  
hui takin object ke liege baar baar  
memory create hote hai.

All objects will be given  
same id.

## Lecture 11

### String

String name = sc.next();

String name = sc.nextLine();

only 1<sup>st</sup> word of string

whole line / para

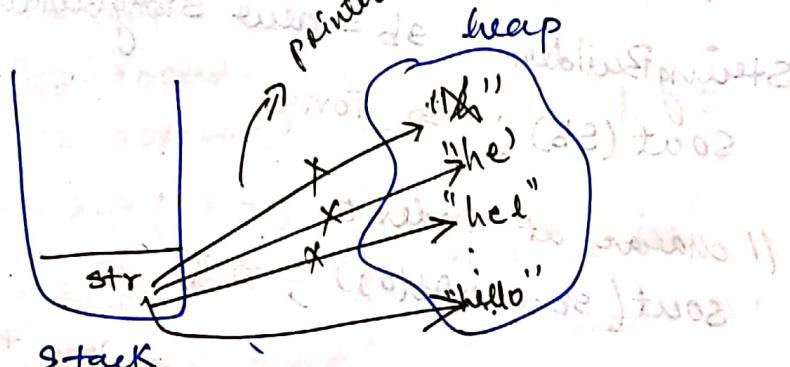
## Lecture 12

### String Builder

→ when we need to modify our string

→ String in Java are immutable.

String str = "h";



str + "e" → he

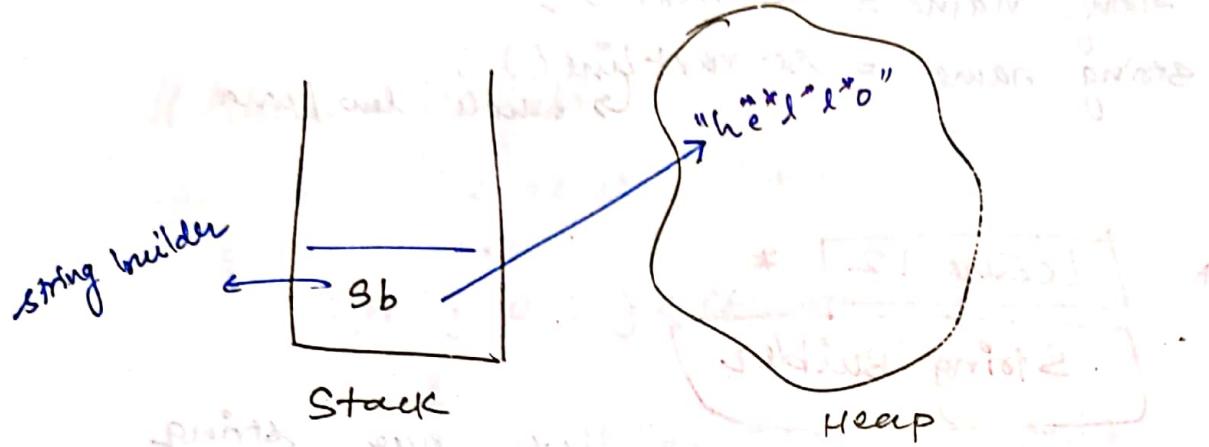
str + "l" → hel

str + "l" → hell

str + "o" → hello

\* Any process in heap is little time taking process ⇒ (User has to wait a little)

→ user experience managers  
so, to tackle it, string Builder class came into existence.



# In case of sb, it will add directly  
here only in the heap - in private

// Syntax :  
StringBuilder sb = new StringBuilder("Tony");  
cout(sb);  $\Rightarrow$  Tony.

// char at index 0  
cout(sb.charAt(0));  $\Rightarrow$  T

// set char. at index  $\rightarrow$  replace the prev made character with 'P'  
cout(sb.setCharAt(0, 'P'))  $\Rightarrow$  Pony  
cout(sb);  $\Rightarrow$  Pony

// insert any character  $\rightarrow$  insert karna hai  
sb.insert(0, 'S')  $\Rightarrow$  STony

cout(sb)

sb.insert(2, 'n');  $\Rightarrow$  Tonny

sout(sb);

// deleting any substring from string

sb.delete(2, 3);  $\Rightarrow$  Tony

sout(sb);

[2, 3)

sb.delete(2, 4);  $\Rightarrow$  Toy

sout(sb);

// add at the end

StringBuilder sb = new StringBuilder("h");

sb.append

sb.append("e");

sb.append("l");

sb.append("o");  $\Rightarrow$  hello

sout(sb);

Same string builder me change ho raha hai

but encad of string we have to make new string  
in each call.

// length of string

sout(sb.length());  $\Rightarrow$  4

{ (4) two

## // Reverse a String

"hello"  $\Rightarrow$  "olleh"  
I/P "O/P"

I/P: 

h	e	l	l	o
0	1	2	3	4

note  
back

leave the  
middle character  
string

front

O/P: 

o	l	l	e	h
0	1	2	3	4

String Builder .sb = new StringBuilder("hello");

for(i=0; i<sb.length()/2; i++)

{

int front = (i);

int back = sb.length() - i - 1;

char frontchar = sb.charAt(front);

char backchar = sb.charAt(back);

// setting the character

sb.setCharAt(front, backchar);

sb.setCharAt(back, frontchar);

}

cout(sb);

front index pe  
back wall char

to calculate  
front wall char.

# Lecture - 12

## Operators & Binary No. System

operator  $a + b$  → operand  
  |  
  operator

\* Symbols that tell compiler to perform some operations

### ① Arithmetic Operator

Binary (2 operands)

$+, -, *, /, \%$

↑  
modulo  
(remainder)

### Pre-Increment

$++a$

① change value

② use value / assign value

~~int a = 10;~~

~~int b = 0;~~

~~b = ++a;~~

~~sout(a); → 11~~

~~sout(b); → 11~~

~~g(a) = (101)~~

### Unary (1 operand)

$++, --$

↑  
number at p

### Post-Increment

$a++$

① one value

② change value / assign value

~~int a = 10;~~

~~int b = 0;~~

~~b = a++;~~

~~sout(a); → 11~~

~~sout(b); → 10~~

$p + q + r$

② Relational Operators  $\rightarrow$  output boolean value

$=, !=, >, <, \geq, \leq$

③ Logical Operators

$\&, ||, !$

Binary Number System

$\Rightarrow$  Base 2

0, 1, 2, 3, 4, 5, 6, 7, 8, 9  $\rightarrow$  decimal no. system

\* 4 to binary

$$\begin{array}{r} 2 | 4 \\ \hline 2 | 2 \\ \hline 1 \end{array}$$

Remainder

100

$$\begin{array}{r} 2 | 0 \\ \hline 2 | 1 \\ \hline 1 \end{array}$$
$$= 2^2 + 2^1 + 2^0 = 4$$

$$\begin{array}{r} 2 | 5 \\ \hline 2 | 1 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 2^2 \\ 2^1 \\ 2^0 \end{array}$$

$$(101)_2 = (5)_{10}$$

$$4 + 0 + 1 = 5$$

$$(101)_2 = (5)_{10}$$

- Octal  $\rightarrow$  Base 8
- Hexadecimal  $\rightarrow$  Base 16

## ④ Bitwise Operators

(i)  $\&$       (ii)  $|$       (iii)  $\wedge$       (iv)  $\sim$

Binary  
And

Binary  
OR

Binary  
XOR

Binary One's  
Complement

Binary left shift

(v)  $\ll$

(vi)

$\gg$

Binary Right  
shift

True  $\rightarrow$  1

false  $\rightarrow$  0

$$A = 0101$$

$$B = 0110$$

$$(i) \quad 0101$$

$$\& 0110$$

$$\hline 0100$$

$$A \& B = C$$

$$\therefore C = 0100$$

$$(ii) \quad 0101$$

$$| 0110$$

$$\hline 0111$$

$$A | B = C$$

$$\therefore C = 0111$$

$$(iii) \quad \text{xor } (\wedge)$$

similar value  $\rightarrow$  false  
diff values  $\rightarrow$  true

$$\begin{array}{r} 0101 \\ \wedge 0110 \\ \hline 0011 \end{array}$$

$$A \wedge B$$

$$\therefore C = 0011$$

#### (iv) Complement

$$0 \rightarrow 1$$

$$1 \rightarrow 0$$

$$\text{Ans} = 1010\ 00$$

$$A = 0101$$

$$\sim A = 1010$$

#### (v) Binary Right Shift

$$A \gg 1$$

$$\rightarrow (0101)$$

$$[0010]$$

$$B \gg 1$$

$$\Downarrow$$

$$[0011]$$

$$0110 = 6$$

Position

Syntax: Number operator

$$0010 A \ll 1$$

0101 (bit shift towards left)

$$\begin{array}{r}
 & \swarrow & \searrow & \swarrow & \searrow \\
 & 0 & 1 & 0 & 1 \\
 \overline{0} & \overline{0} & \overline{1} & \overline{1} & \overline{0} \\
 \hline
 & 1 & 0 & 1 & 0
 \end{array}$$

(i)  $\Rightarrow 1010$  (ii)  $\Rightarrow 0010$

$$\text{new No} = (1010)$$

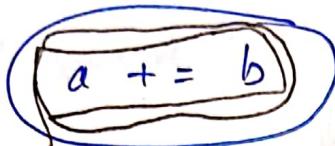
(i)  $\Rightarrow 1010$  (ii)  $\Rightarrow 0010$

shift  $\leftarrow$  with definite  
start  $\leftarrow$  with 0010

## ⑤ Assignment Operator

=; +=; (-=); \*=; /=

$$a = a + b$$



## Lecture - 13 Bit Manipulation in Java

True

False

→ current flow  $\Rightarrow 1$  (high state)

→ no current flow  $\Rightarrow 0$  (low state)

left shift

$N \ll i$

$3 \ll 1$

$(010 \ll 1)$

$(100)$

Right shift

$N \gg i$

$3 \gg 1$

$(010 \gg 1)$

$(001)$

- ① Get
- ② Set
- ③ Clear
- ④ Update

## ① Get Bit Operation

Ques) Get the 3rd bit (position = 2) of a number  
n. ( $n = 0101$ ) =  $(5)$  in decimal

$n = 0 \underset{3}{1} \underset{2}{0} \underset{1}{1} \underset{0}{0}$  (position)  
?  $\downarrow \downarrow \downarrow \downarrow$

- \* Bit Mask :  $1 \ll i$
- \* Operation : AND (&)

$i = 2$  (here)  $\Rightarrow$  position

(i)  $1 \ll 2$  (left shift)

$\text{H.P.} \leftarrow 0001 \ll 2$   $\rightarrow$  bit mask  
 $0100 \rightarrow \text{O.P.}$

(ii)  $0100 \text{ AND } 0101$

=  $0100$

(001)

final no.

if final no.  $\neq$  zero  $\Rightarrow$  bit = 1  
final no. = zero  $\Rightarrow$  bit = 0

## Code :

```

int n = 5 ;
int pos = 2 ;
int bitMask = n << pos ;
if ((bitMask & n) == 0)
    sout("bit was zero") ;
else
    sout("bit was non-zero") ;

```

## (2) Set Bit Operation

Ques.) Set the 2nd bit ( $pos = 1$ ) of a no.  $n$

(i) Bit mask :  $1 \ll 1$

(ii) Operation : OR

(iii)  $1 \ll 1$

~~00000000~~

$0001 \ll 1$

$0010 \rightarrow 0/1$

$\gg 1000$

(iv)  $0010$  OR  $0101$

$0101$

$= (7)_{10}$

Code:-

```
int n = 5;
```

```
int pos = 1;
```

```
int bitMask = n << pos;
```

```
int newNo = (bitMask) | (n);
```

```
cout << newNo;
```

### (3) clear Bit

Ques) clear the 3<sup>rd</sup> bit ( $pos=2$ ) of a number.

$$(n = 0101)$$

(i) Bit Mask :  $1 \ll 2$

(ii) Operation : AND with NOT

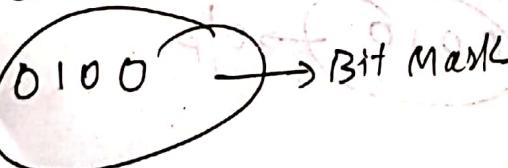
Sol)

$$n = \begin{array}{r} 0 \\ 1 \\ 0 \\ 1 \end{array} = (5)_{10}$$

$$0/p \text{ find } \Rightarrow 0001 = (1)_{10}$$

(i)  $1 \ll 2$

$$0001 \ll 2$$



(ii)  $\sim(0100) \Rightarrow (1011)$

$$(1011) + (0101) \Rightarrow (0001) = (1)_{10}$$

## Code :

```

int n = 5;
int pos = 2;
int bitMask = 1 << pos;
int notbitMask = ~bitMask;
int newNO = (notbitMask) & (n);
cout(newNO);

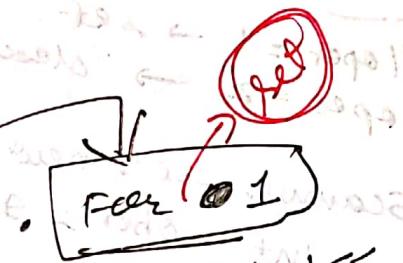
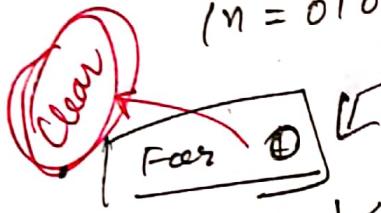
```

### (+) Update Bit

Ques) update the 2nd bit ( $pos=1$ ) of a number  $n$

to 1. (n, notbitMask)

$$(n = 0101)$$



(i) Bit Mask :  $1 << i$

(ii) Operation : OR

(i) Bit Mask :  $1 << i$

(ii) Operation : NOT

$$\textcircled{1} \quad 1 << 1$$

$$0001 << 1$$

$$0010$$

$$\textcircled{2} \quad (0010) \text{ | } (0101)$$

$$0111$$

O/P

$$\textcircled{3} \quad 1 << 2$$

$$0001 << 2$$

$$0100$$

BM

$$\textcircled{4} \quad (0100) \text{ & } (0101)$$

$$0001$$

O/P

## Code

```

int n=5;
int pos = 1;
int oper = 1;
// update bit to 1 else update bit to 0
// set operation
int bitMark = 1<<i;
int newNo = (bitMark) | (n);

```

## Code

```

if oper == 1 → set
if oper == 2 → clear
Scanner sc = new Scanner(System.in);
Scanner sc = new Scanner(System.in);
oper = sc.nextInt();
int n = 5;
int pos = 1;
int bitmark = N < pos;
if (oper == 1)
    int newNo = (bitMark) | (n);
    sout(newNo);
else
    int new_mark = ~bitMark;
    int newNo = (new_mark) & (n);
    sout(newNo);

```

## Lecture - 14

### Sorting in Java

#### (1) Bubble Sort

7	8	3	1	2
7	8	3	1	2

(Unsorted array)

$$\text{length} = n$$

$$\text{no. of pass} = (n-1)$$

①

7 8 3 1 2

7 3 8 1 2

7 3 1 8 2

7	3	1	2	8
---	---	---	---	---

(largest element  $\Rightarrow$  end)

②

2<sup>nd</sup> loop 7 1 2 8

3 1 2 7 2 8

3	1	2	7	8
---	---	---	---	---

③

1 3 2 7 8

1	2	3	7	8
---	---	---	---	---

④

1	2	3	7	8
---	---	---	---	---

- \*  $n = \text{length of array}$
- \* no. of comparisons =  $(n-1) \rightarrow \binom{n}{2}$

Code :

```

int arr[] = {7, 8, 3, 1, 2};
int n = arr.length;
for (i=0; i < (n-1); i++) // (n-1)
{
    for (j=0; j < (n-i-1); j++)
        if (arr[j] > arr[j+1])
    {
        int temp = arr[j];
        arr[j] = arr[j+1];
        arr[j+1] = temp;
    }
}

```

$$Tn = O(n^2)$$

# (20) Selection Sort

7	8	3	12
---	---	---	----

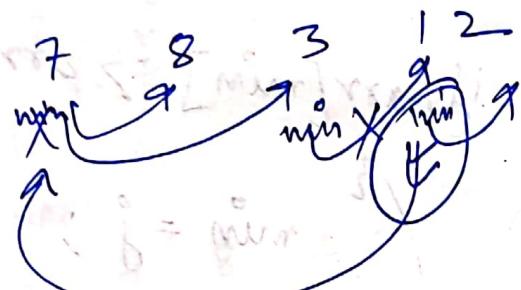
Unsorted array

→ 1 swap per iteration

→ select any 1 as min / smallest element and then compare it with other array element

(1)

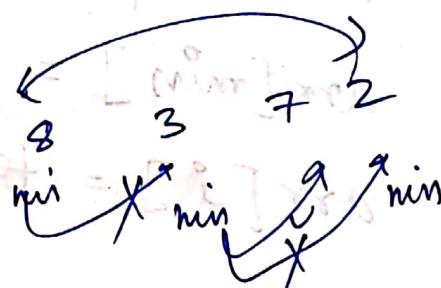
i = 0



1	8	3	7	2
---	---	---	---	---

(2)

i = 1



1	2	3	7	8
---	---	---	---	---

(3) i = 2

No swap  
7 is min

1	2	3	7	8
---	---	---	---	---

(4) i = 3

3	7	8	min
1	2	3	7

## Code

```
int arr[] = {7, 8, 3, 1, 2};  
int n = arr.length;  
for (i=0; i < n; i++)  
    {  
        int min = i;  
        for (j=i+1; j < n; j++)  
            {  
                if (arr[min] > arr[j])  
                    min = j;  
            }  
        int temp = arr[min];  
        arr[min] = arr[i];  
        arr[i] = temp;  
    }  
}
```

*for loop*  
*min element to min*  
*fix one & compare*  
*with rest*

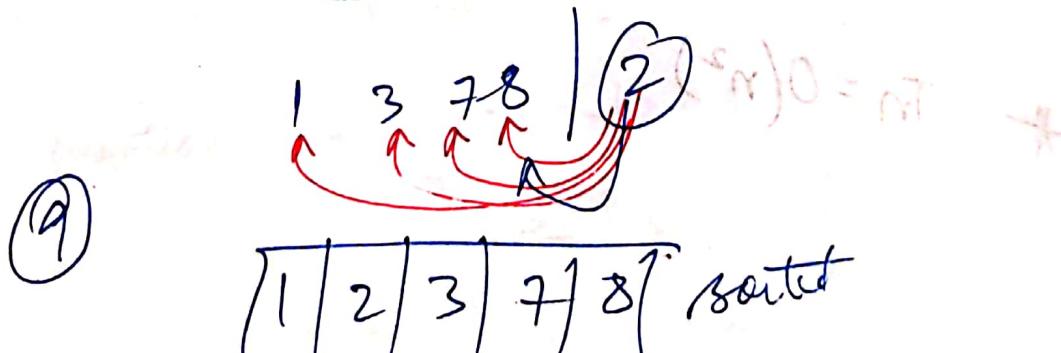
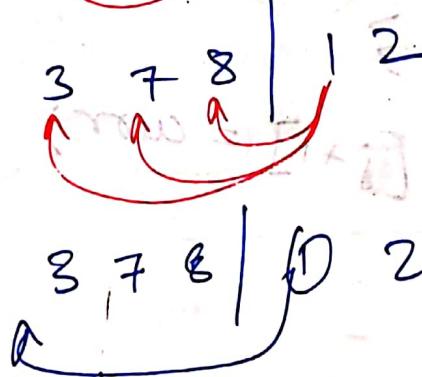
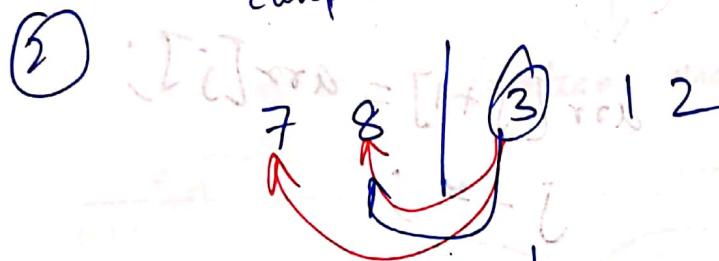
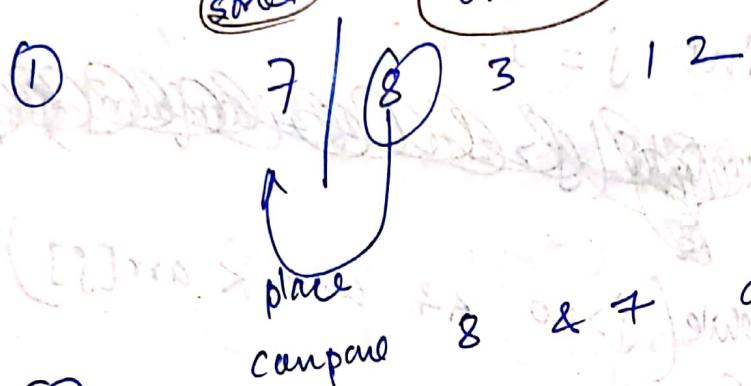
$$T_n = O(n^2)$$

### ③ Insertion Sort

7	8	3	1	2
---	---	---	---	---

Divide Array into 2 parts

Sorted      Unsorted



Code

int arr[] = {7, 8, 3, 1, 2};

int n = arr.length;

for (int i=1; i < n; i++)

{

    int curr = arr[i];

    int j = i-1;

    while (j >= 0 && curr < arr[j])

{

    arr[j+1] = arr[j];

    j--;

}

    arr[j+1] = curr;

}

\*  $Tn = O(n^2)$

## Lecture -19

### Quick Sort

Unsorted array :

6	3	9	5	2	8
---	---	---	---	---	---

#

#### Pivot & Partition

To choose Pivot ?

- 1) random
- 2) median
- 3) 1<sup>st</sup> element
- ✓ 4) last element

6	3	9	5	2	8
---	---	---	---	---	---

pivot

Karim:

element < pivot  $\Rightarrow$  left  
element  $>$  pivot  $\Rightarrow$  send then Right

6	3	5	2
---	---	---	---

Pivot

smaller

larger

pivot

2

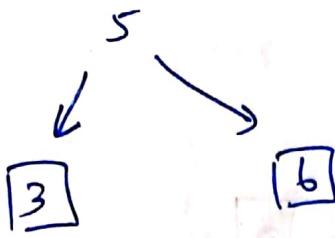
pivot

6

3

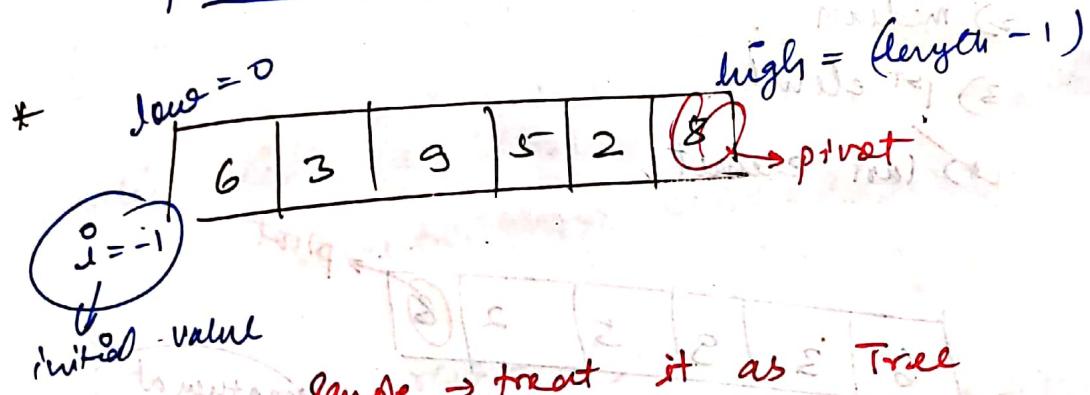
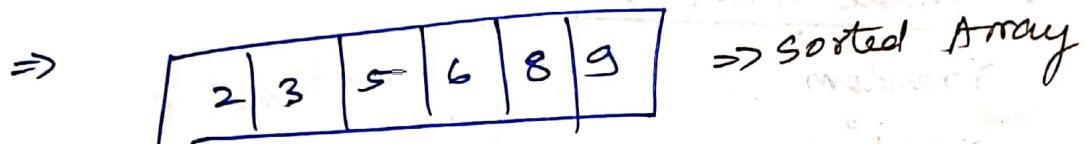
5

apply recursive quick sort for each pivot

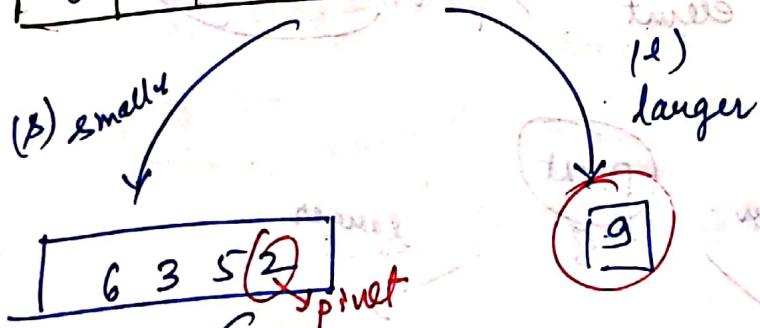
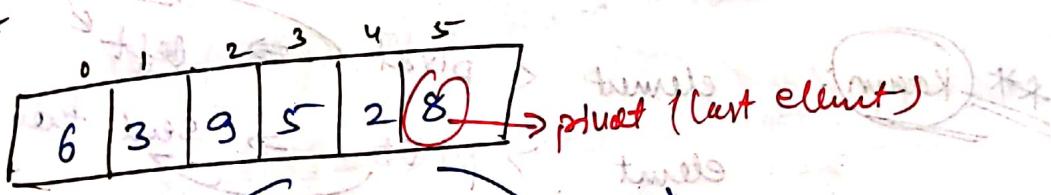


\* Single element is always sorted

\* See from left to right in this recursive tree



**Note**



(d) larger



decrease  
no action  
done not  
empty

→ Move from left to right in tree  
we get:

(ans 2, 3, 5, 6, 8, 9)

0 1 2 3 4 5

2 3 5 6 8 9 → sorted array

⇒

Code in Java

low = 0

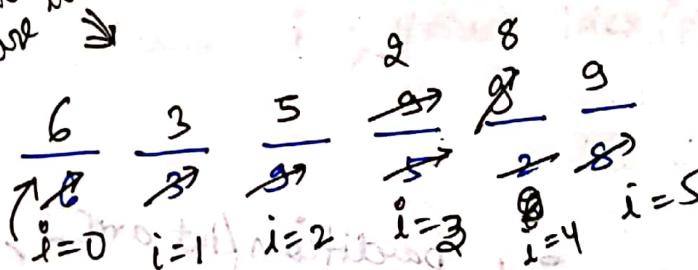
6	3	9	5	2	8
0	1	2	3	4	5

high = 5

→ pivot

$i = -1$  (no elements less than pivot  
initially bcz pivot not selected)

swap method  
this we use

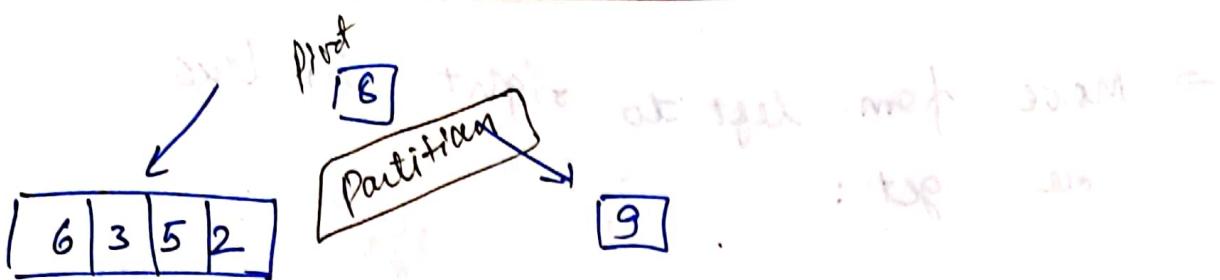


\* Compare 6 with pivot, then  $(6 < \text{pivot})$   
 $i$  will create space for '6'.  
 $(i++)$

pivot

6	3	5	2	8	9
---	---	---	---	---	---

Now we get:



apply again same quick sort (recursive vs know)

### Code

```
public static void quick(int arr[], int low, int high)
```

{

if (low < high)

{

int pidx = partition(arr, low, high);

(values less than pivot pat  
less than pivot pat) i = 0

more than pivot pat ← quick(arr, pidx + 1, high);

{

{

```
public static int partition(int arr[], int low, int high)
```

{

int pivot = arr[high];

int i = low - 1; // track for empty space

```
for (int j = low; j < high; j++)
```

{

```
if (arr[j] < pivot) // element < pivot
```

```
{  
    i++; // space create to store smaller  
    // swap → place j to its position and store element  
    int temp = arr[i]; // with all j & small  
    arr[i] = arr[j]; // element will be zero.  
    arr[j] = temp;  
}  
} // if
```

{ // for

i++; // add 1 more space for pivot.

// swap pivot → b/c pivot end me hai abhi to  
int temp = arr[i]; // swap sali position  
arr[i] = pivot; // pare same ke liye

arr[high] = temp;

return i; // pivot index (position)

} // fn

Main()

{

int arr[] = {6, 3, 9, 5, 2, 8};

int n = arr.length;

\* quick(arr, 0, n-1);

}

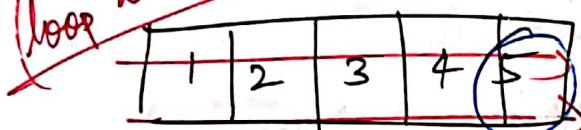
## Time Complexity $\Rightarrow$ Quicksort

\* Worst Case occurs when pivot is always the smallest or the largest element.

$$\text{Worst Case : } T_n = O(n^2)$$

$$\text{Avg. Case : } T_n = (n \log n)$$

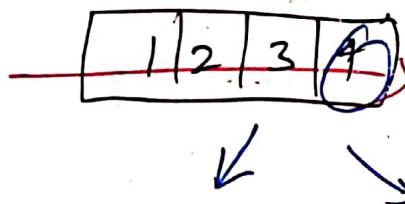
→ when our array is completely sorted  
 either ascended (either ascending or descending) in root  
at each level



$$T_n$$

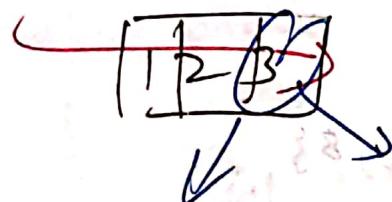
(n)

level 1 (n - levels)



$$n-1$$

level 2



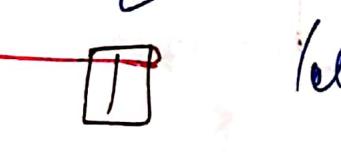
$$n-2$$

level 3



$$n-3$$

level 4



$$n-4$$

level 5

⇒ Hier level par loop chalane time

$$T_n = O(n)$$

$$\Rightarrow n + (n-1) + (n-2) + \dots + 1 \quad (\text{A.P.})$$

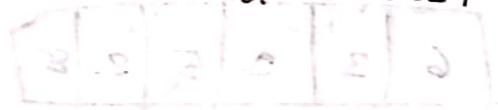
$$= \frac{n(n+1)}{2}$$

$$T_n = O(n^2)$$



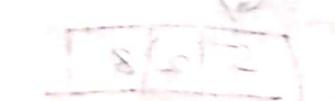
$$T_n = O(n^2)$$

at most case.

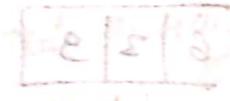


↑ after swap

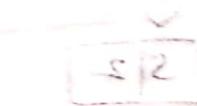
swap



swap



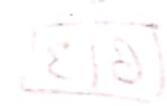
swap



swap



swap



swap



→ to the  
next

new position will forward step \*

new stream. If we next request, add \*

## Lecture - 20

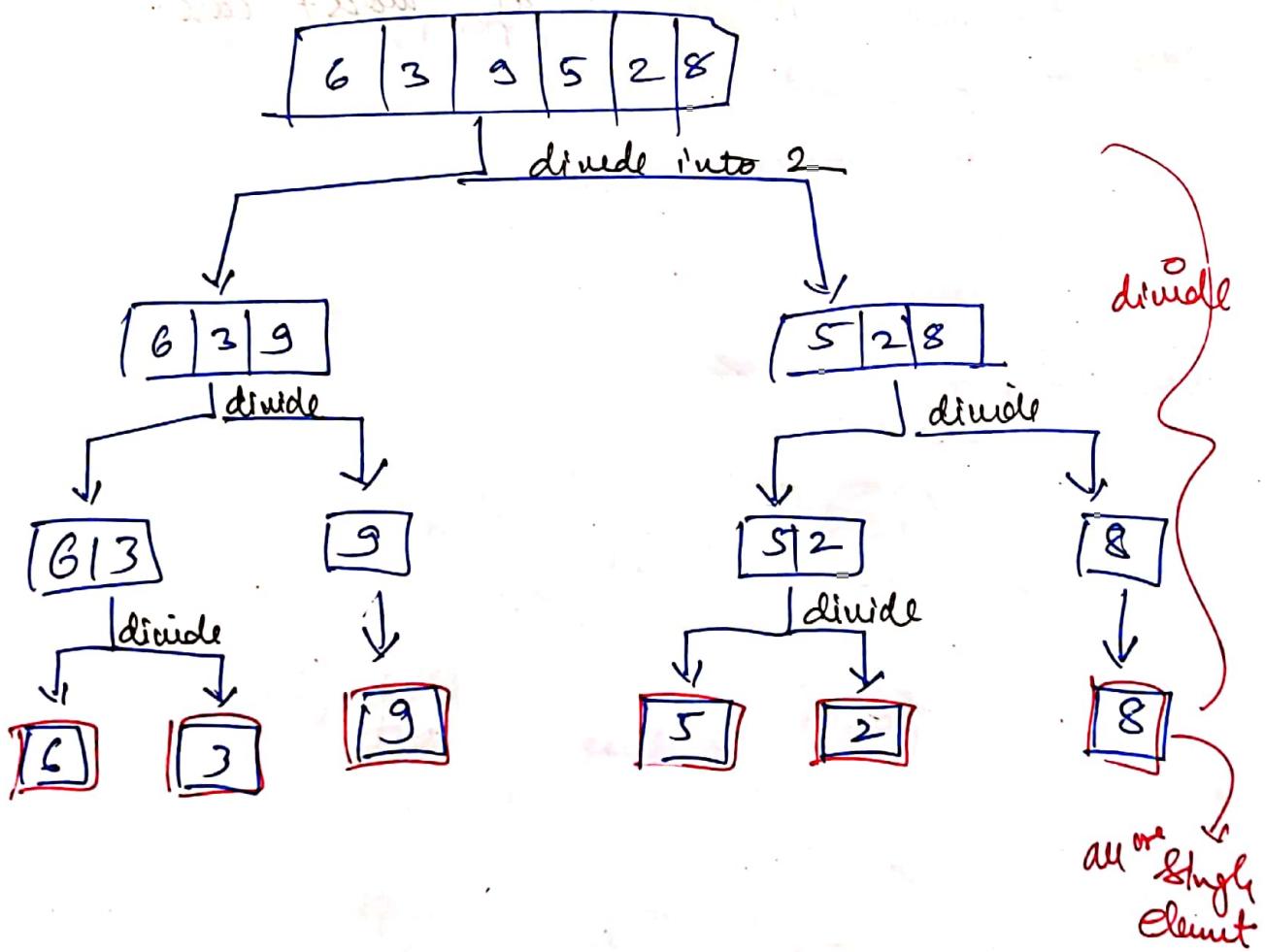
### Merge - Sort

Unsorted

6	3	9	5	2	8
---	---	---	---	---	---

\* Based on :

divide & conquer Property

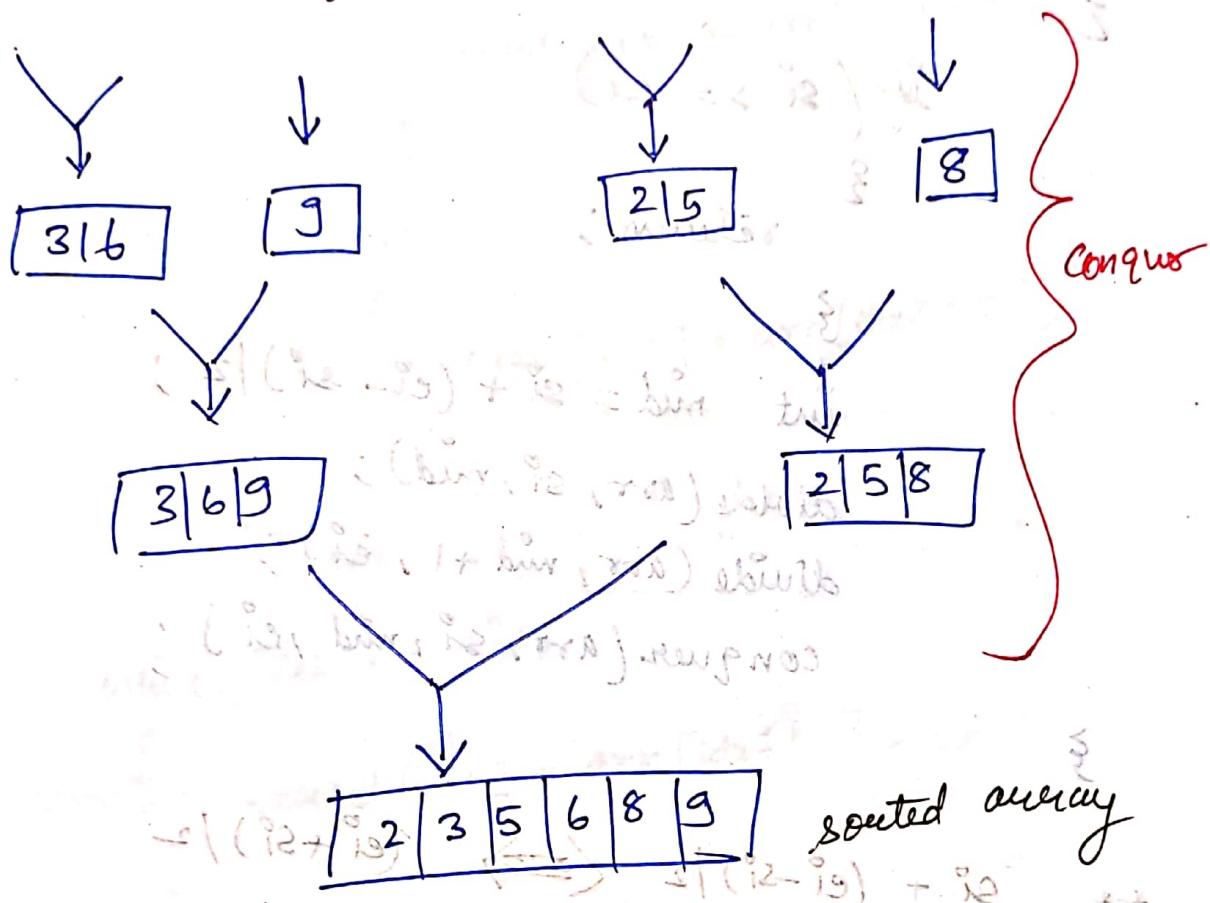


\* Single elements are already sorted.

+ Now, Conquer these single elements and

while doing so make it the comparison  
(i.e., sort them)

Now, extending prev. Tree structure:-



sorted 1

3	6	9
0	1	2

sorted 2

2	5	8
0	1	2

merged array

2	3	5	6	8	9	
0	1	2	3	4	5	

new array (sorted Array)

## Code

$si = \text{starting index}$   
 $ei = \text{ending index}$

public static void divide(int arr[], int si, int ei)

{

if ( $si >= ei$ )

{  
    return;

int mid =  $si + (ei - si) / 2$ ;

divide(arr, si, mid);

divide(arr, mid + 1, ei);

conquer(arr, si, mid, ei);

\*\*  $si + (ei - si) / 2 \Leftrightarrow (ei + si) / 2$

But we are using this to reduce  
space complexity.

public static void conquer(int arr[], int si, int  
mid, int ei)

{

int merged[] = new int[ei - si + 1];

int idx1 = si;

int idx2 = mid + 1;

int x = 0;

```

while (idx1 <= mid & idx2 <= ei)
{
    if (arr[idx1] <= arr[idx2])
    {
        merged[x++] = arr[idx1++];
    }
    else
    {
        merged[x++] = arr[idx2++];
    }
}

// while

```

$(\text{right})_0 = \text{pt}$

---

```

while (idx1 <= mid)
{
    merged[x++] = arr[idx1++];
}

while (idx2 <= ei)
{
    merged[x++] = arr[idx2++];
}

for (int i=0; i<merged.length; i++)
{
    arr[j] = merged[i];
}

// for

```

$(\text{right})_0 = \text{pt}$

Main()

{

int arr[] = {6, 3, 9, 5, 2, 8};

Let n = arr.length;

divide(arr, 0, n-1);

} // main

$$T_n = O(n \log n)$$

+  $\lg n$  (divide)

+ n (conquer)

( $\lg n$  is  $\lg n \cdot \log n > 1$ ) ref

( $\lg n$  before =  $\lg n$ ) ref

# Lecture 15

## Recursion - 1

### Recursion

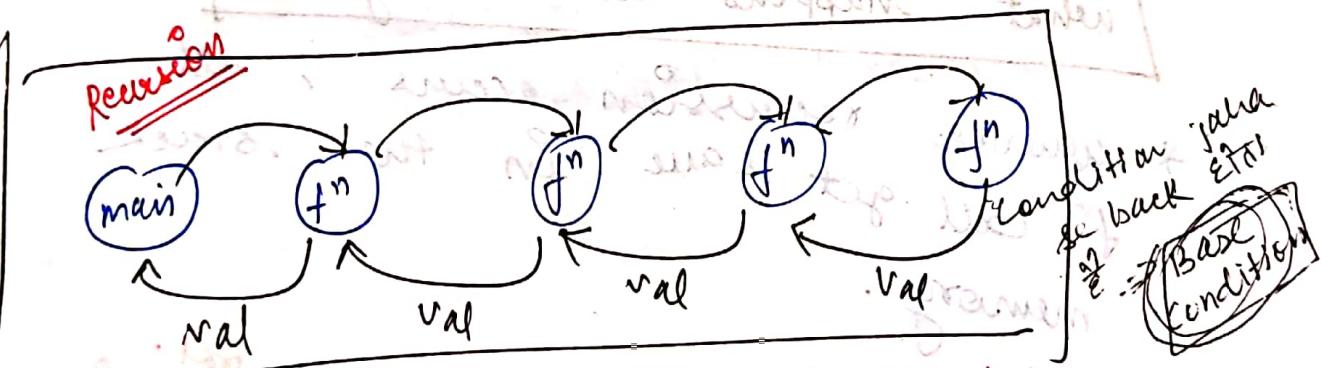
#### # Prerequisites #

- i) iteration / loop
- ii) function

$$f(n) = n^2 \rightarrow \text{given}$$
$$f(f(n)) = f(n^2)$$

↓  
Recursion

function that calls itself



Ques: Use Recursion to print numbers from 5 to 1.

Iteration : `for (i=5; i>0; i--)  
cout <i<"> ;`

Recursive :

```

public static void pointNums (int n)
{
    if (n == 0)
        cout << n;
    else
        pointNums (n - 1);
}

```

public static void pointNums (int n)

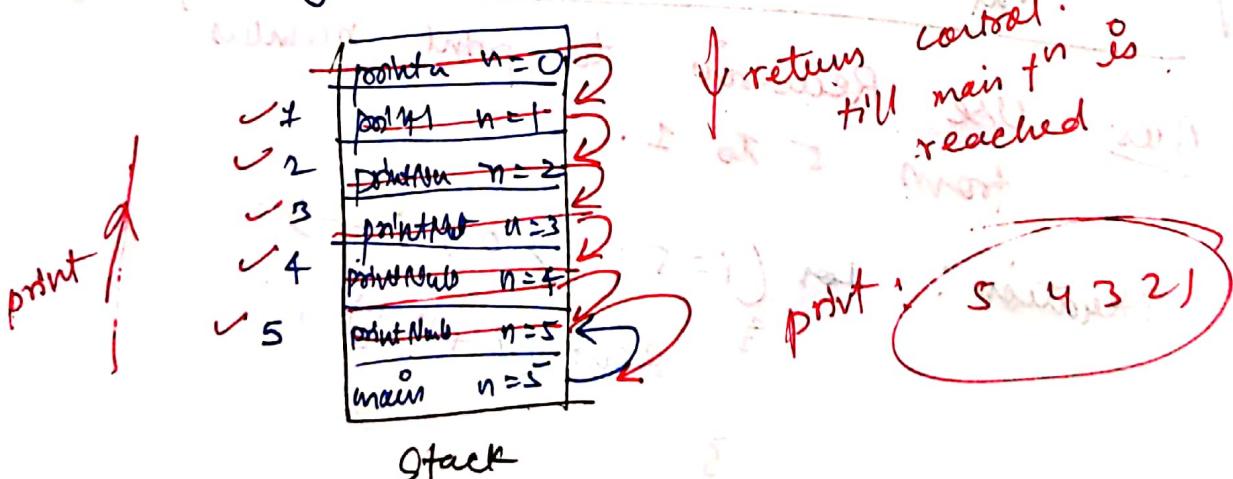
{  
if ( $n == 0$ ) {  
 return;  
} Base condition

cout << n; // point

pointNums ( $n - 1$ ); // recursion

what happens in Memory ?

\* whenever recursion occurs ; all  
fn call get save in the stack  
memory.



\* Recursion uses more memory.

Variably gets created again & again

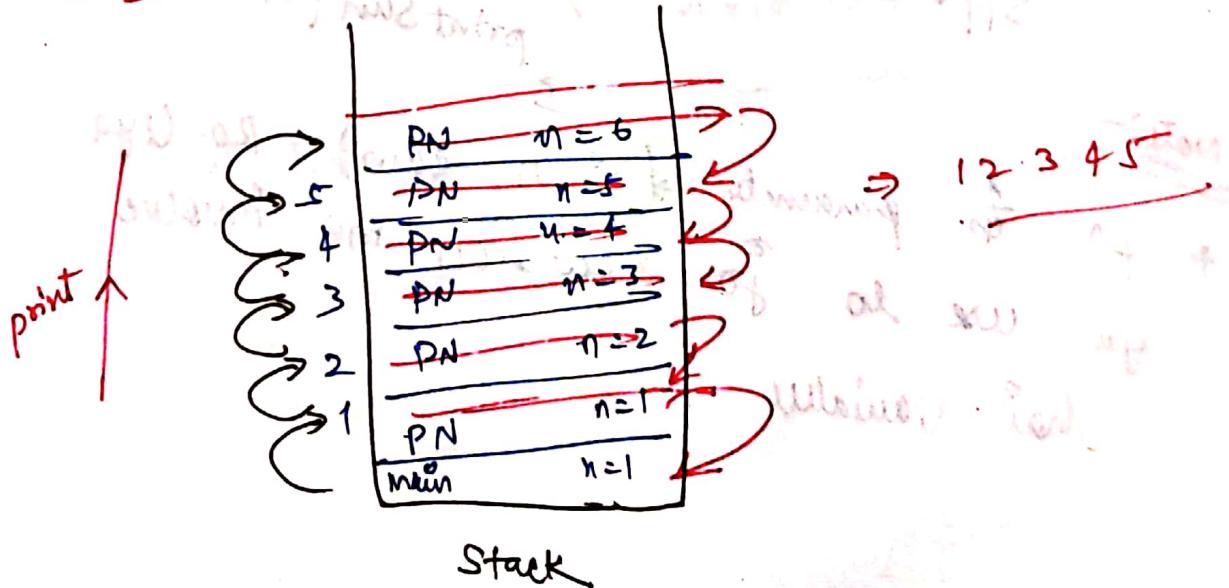
in the memory.

+ when base condition is not true, then after some time of execution when our memory gets full stack overflow.  
( $\infty$  recursion in case  $n$ )

# (Ans 2)

```
Point Numbers from 1 to 5 static void printNums(int n) {  
    public static void printNums(int n) {  
        if (n == 6) {  
            return;  
        } else {  
            cout << n; // print  
            pointNums(n+1); // recursion  
        }  
    }  
}
```

### Memory Space



Ques: Print sum of n-natural No.

- ① main fn  $\Rightarrow$  1
- ② base condition  $\Rightarrow$   $i = n$  (sum)
- ③ work  $\Rightarrow$  calculate sum

Code:

```
public static void pointSum(int i, int n, int sum)  
{  
    if (i == n) {  
        sum = sum + i;  
        cout << sum;  
        return;  
    }  
    pointSum(i + 1, n, sum);  
    sum = sum + i; // sum calculate  
    pointSum(i + 1, n, sum); // recursion
```

3/1 Pm

```
main()  
{  
    pointSum(1, 5, 0);  
}
```

Note:-  
\* fn  $\frac{1}{4}$  parameter  $\rightarrow$   $i, n, sum$  ko kya  
ya we do jo recursion me involve  
hai variable

Recursion			
Base case	15	PS i=5 n=5 s=1	$\Rightarrow \text{sum} = 15$
		PS i=4 n=5 s=10	
		PS i=3 n=5 s=15	
		PS i=2 n=5 s=20	
		PS i=1 n=5 s=25	
		main i=1 n=5 s=0	

Stack

Stack (Function) stack

Ques: Point Factorial of a Number 'n'

$$n! = n \times (n-1) \times (n-2) \times \dots \times 1$$

$$3! = 3 \times 2 \times 1$$

$$1! = 1$$

$$0! = 1$$



Q1 info.  $\Rightarrow n=5$

Q2 param  $\Rightarrow$  i)  $(n-1)! \text{ if } n > 1$   
ii)  $n \times (n-1)! \text{ if } n < 1$

$\Rightarrow \text{return}$

Q3 Base  $\Rightarrow (n=1)$

$\Rightarrow \text{return 1}$

```

public static void factorial(int n) {
    if (n == 0)
        cout << fact;
    return;
}

fact = fact * n;
factorial(n-1, fact);

```

~~return~~

for (int i = 1; i <= n; i++)

factorial(5, 1);

1 \* 2 \* 3 \* 4 \* 5 = 120

OR

```

public static int factorial(int n)

```

```

    if (n == 1 || n == 0)

```

```

        return 1;
    else

```

~~else~~

main()

```

    int f = factorial(5);
    cout << f;
}

```

```

    fact-nm1 = factorial(n-1);

```

```

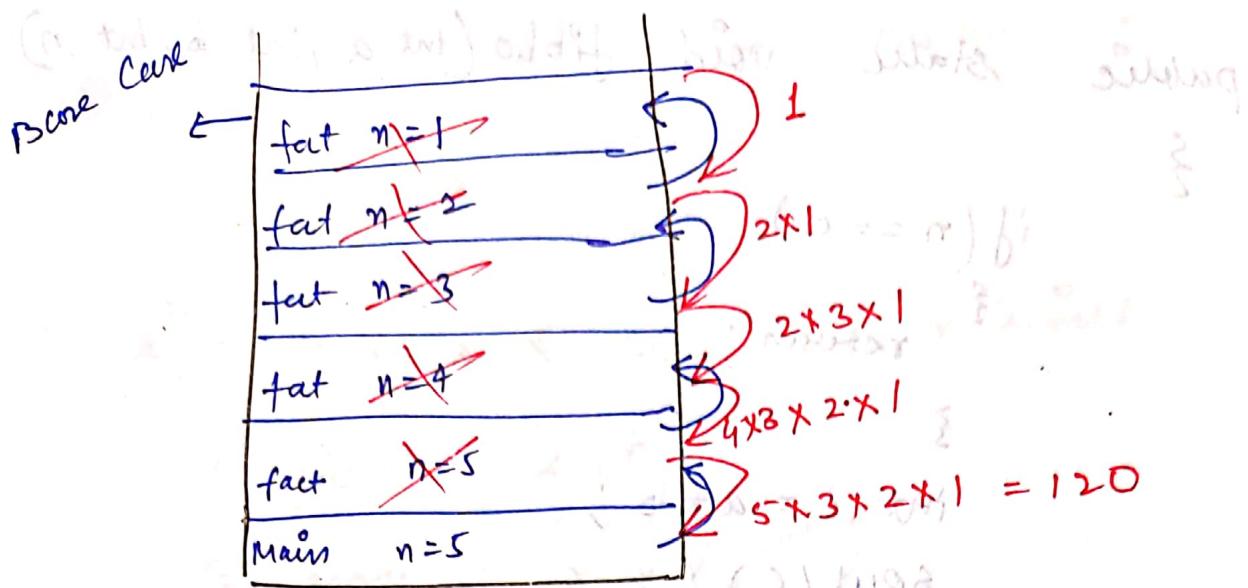
    fact-n = n * fact-nm1;

```

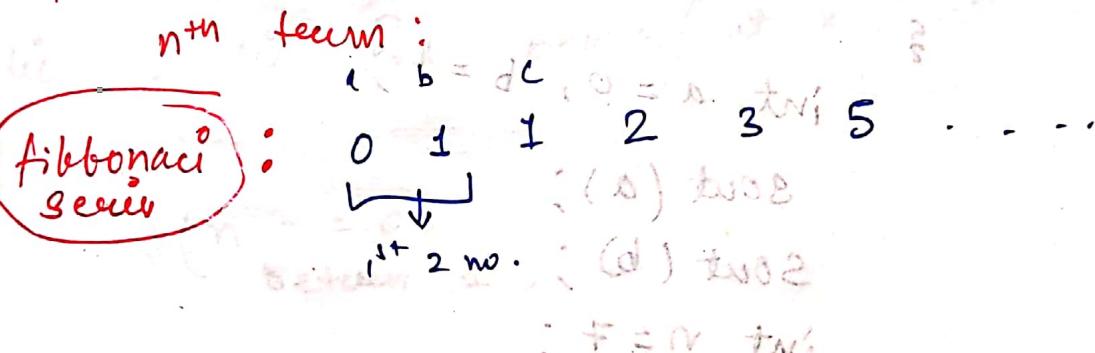
```

    return fact-n;
}

```



Ques. Print the fibonacci sequence. HU



① Given  $\Rightarrow$   $1^st = 0$  }  $a+b=c$  odd if  
 $2^{nd} = 1$  }  $b=a$

② Recur  $\Rightarrow$  create the next term  
 $c = a+b$

③ Base Case  $\Rightarrow$   $n^{th}$  term

```

public static void fibbo(int a, int b, int n)
{
    if (n == 0)
        return;
    {
        cout = int c = a + b;
        sout(c);
        fibbo(b, c, n-1);
    }
}

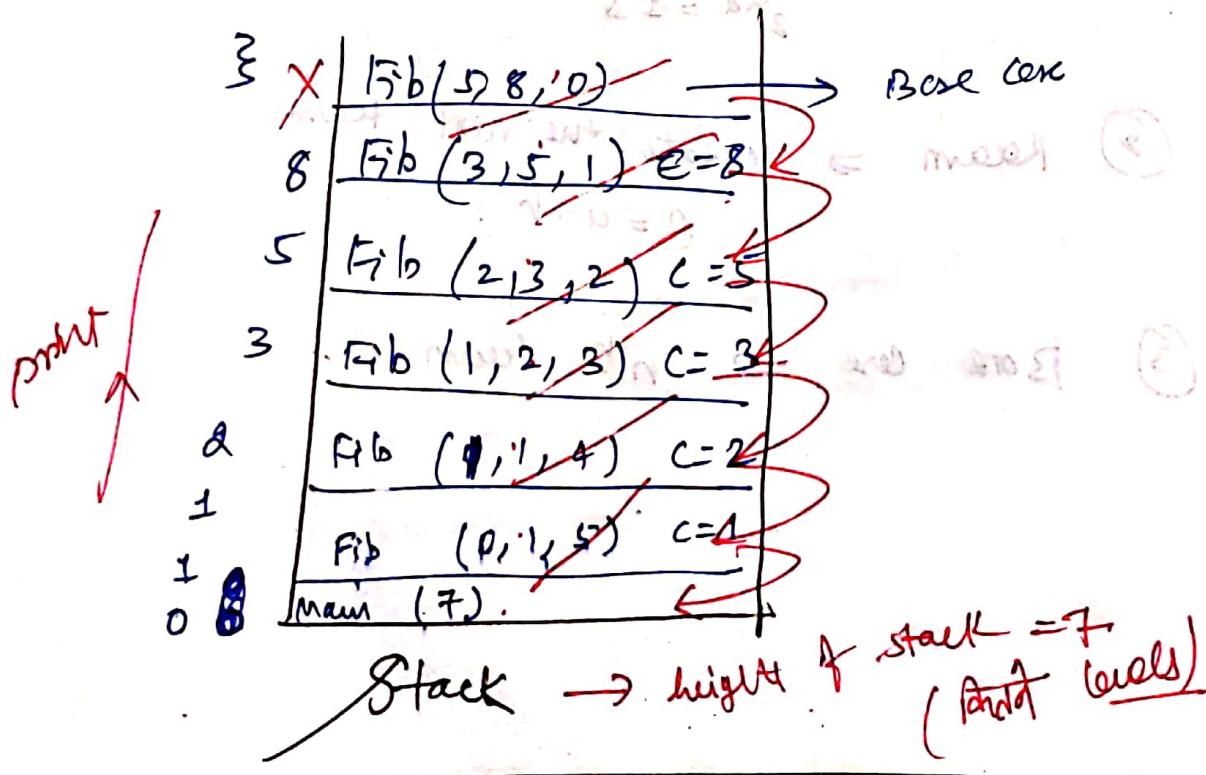
```

~~WTF happened instead of int thing~~

```

main()
{
    int a = 0, b = 1;
    sout(a);
    sout(b);
    int n = 7;
    fibbo(a, b, n-2);
}

```



(Ques)) Print  $x^n$  (stack height = n)

$$* (x)^n *$$

$$x^n = x \times x \times x \times \dots \text{ n times}$$

① given :  $x, n$

② work :  $x * (x^{n-1})$

③ base :  $x^0 = 1$

$$x = 0 \Rightarrow 0$$

base case

public static int power(int x, int n)

{

if ( $n == 0$ )  
return 1;

if ( $x == 0$ )  
return 0;

int xPownm1 = power(x, n-1);

int xPoco = ~~x~~ \* xPownm1;

return xPoco;

}

main()

{

int x=2, n=7;

int ans = power(x, n);

} cout(ans);

W1

$$x=2 = \text{Base Case } 2^0 = 1$$

$$x^n = (2)^5 = \underline{\underline{32}}$$

Recursion Tree	
	Power : $x=2, n=0 \rightarrow \text{Base Case } 2^0 = 1$
1	Power : $x=2, n=1 \rightarrow 1 \times 2^1 = 2$
2	Power : $x=2, n=2 \rightarrow 2 \times 2^2 = 8$
3	Power : $x=2, n=3 \rightarrow 4 \times 2^3 = 32$
4	Power : $x=2, n=4 \rightarrow 8 \times 2^4 = 16$
5	Power : $x=2, n=5 \rightarrow 16 \times 2^5 = 32$
6	Main : $x=2, n=5$

Stack

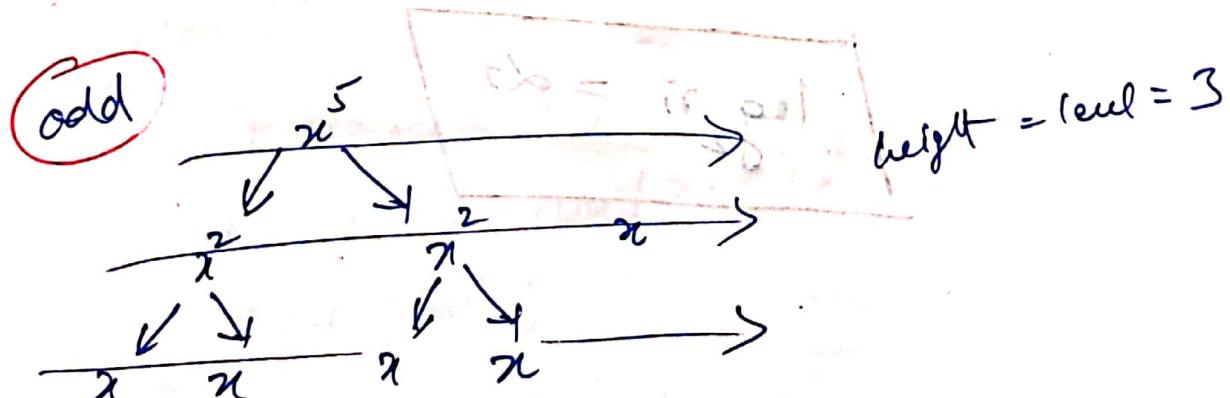
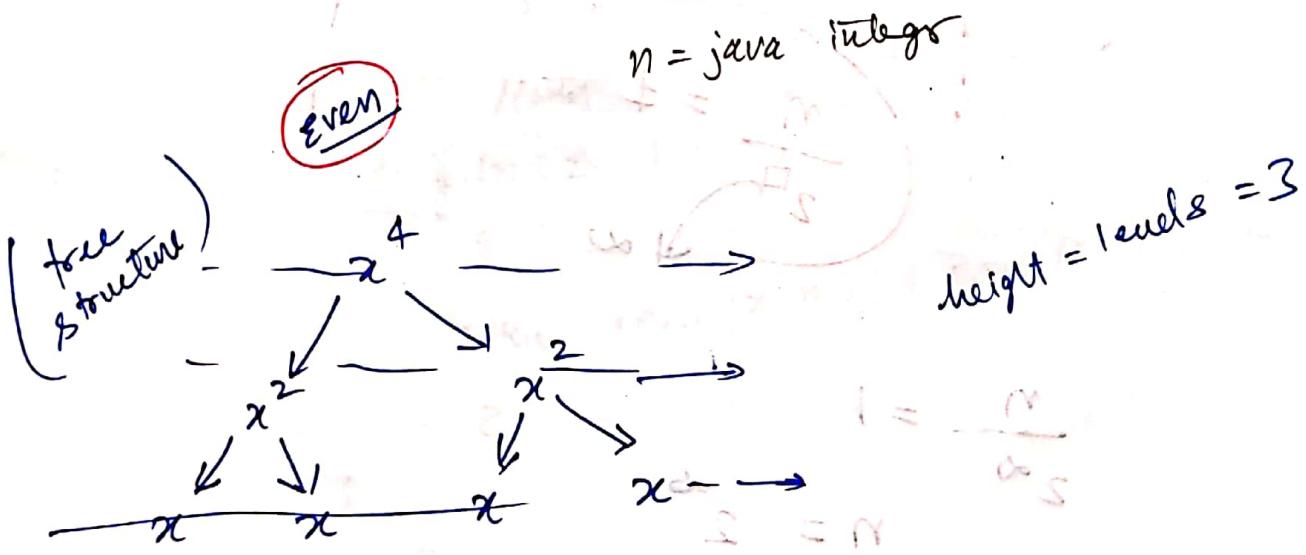
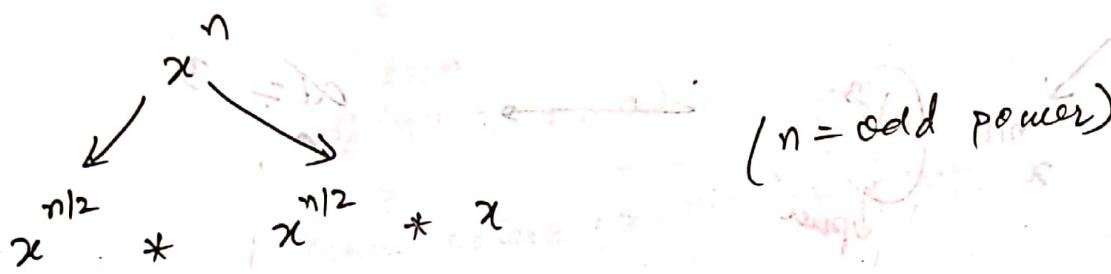
$32 \rightarrow \text{return}$

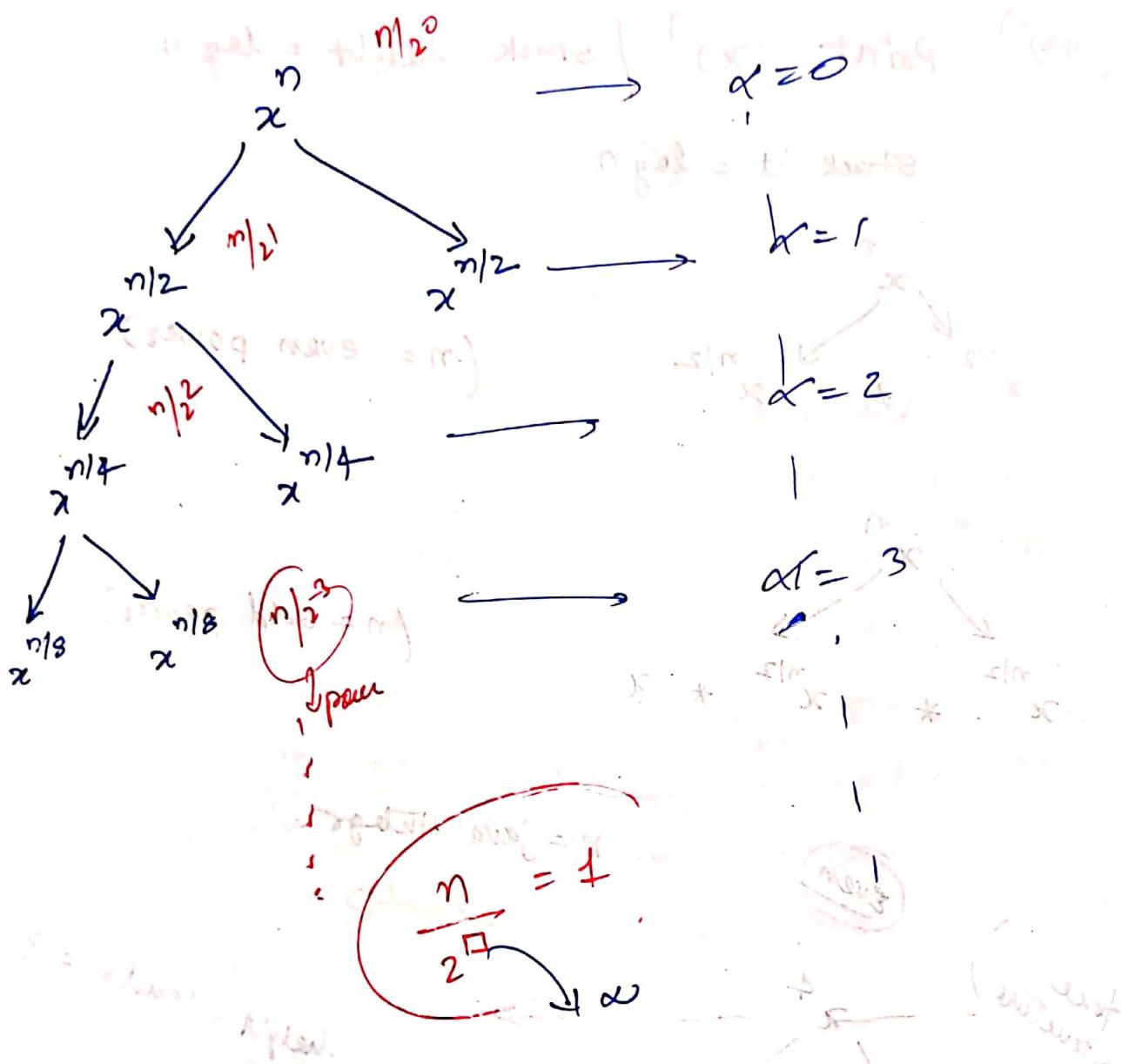
$$\left\{ \begin{array}{l} n=5 \\ \text{level} = 6 \end{array} \right\}$$

$$T_n = O(n)$$

Ques<sup>o</sup>) Point  $(x)^n$  [stack height =  $\log n$ ]

stack ht =  $\log n$





$$\frac{n}{2^\alpha} = 1$$

$$n = 2^\alpha$$

$$\boxed{\log_2 n = \alpha}$$

public static int power(int x, int n)

{

if (n == 0)

    return 1;

}

base case

if (x == 0)

    return 0;

}

// even

if (n % 2 == 0)

    return power(x, n / 2) \* power(x, n / 2);

}

// odd

if (n % 2 != 0)

    return power(x, n / 2) \* power(x, n / 2) \* x;

\*

Main()

{  
    int x = 2, n = 5;

    int ans = power(x, n);

    cout << ans;

}

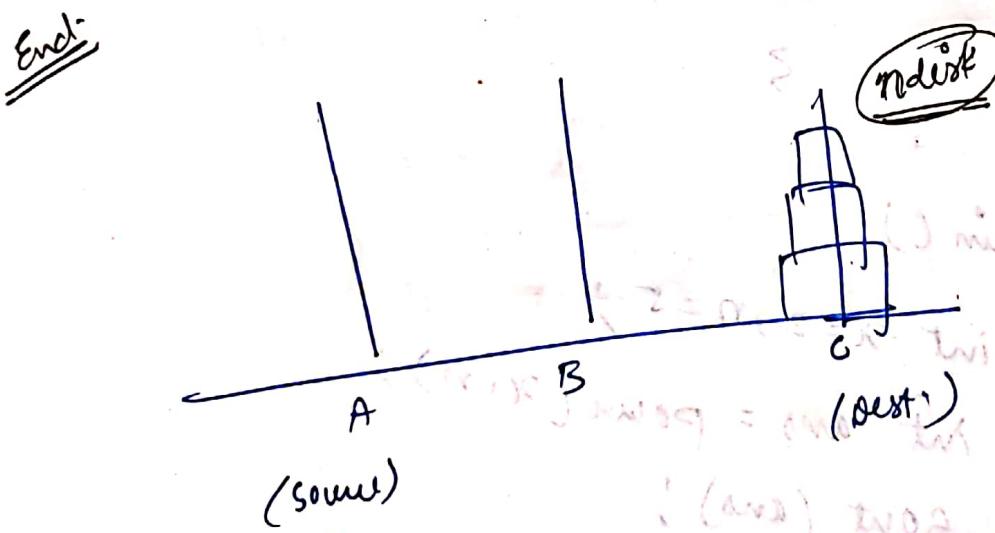
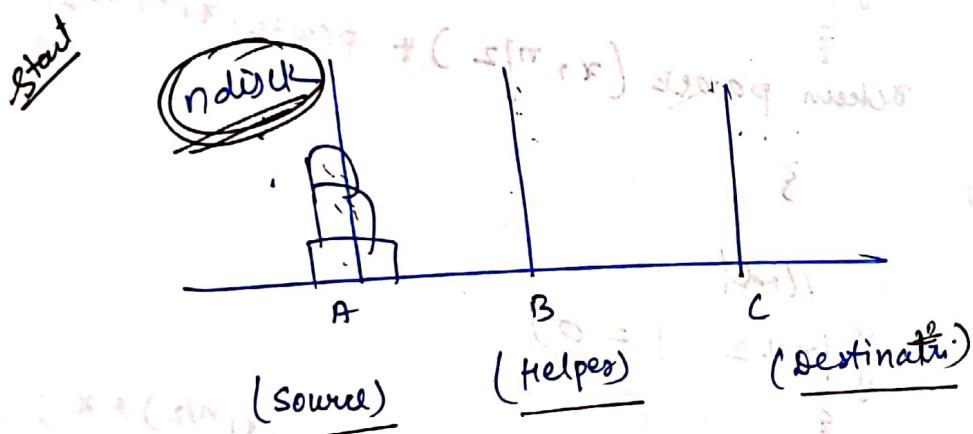
$$T_n = O(\log n)$$

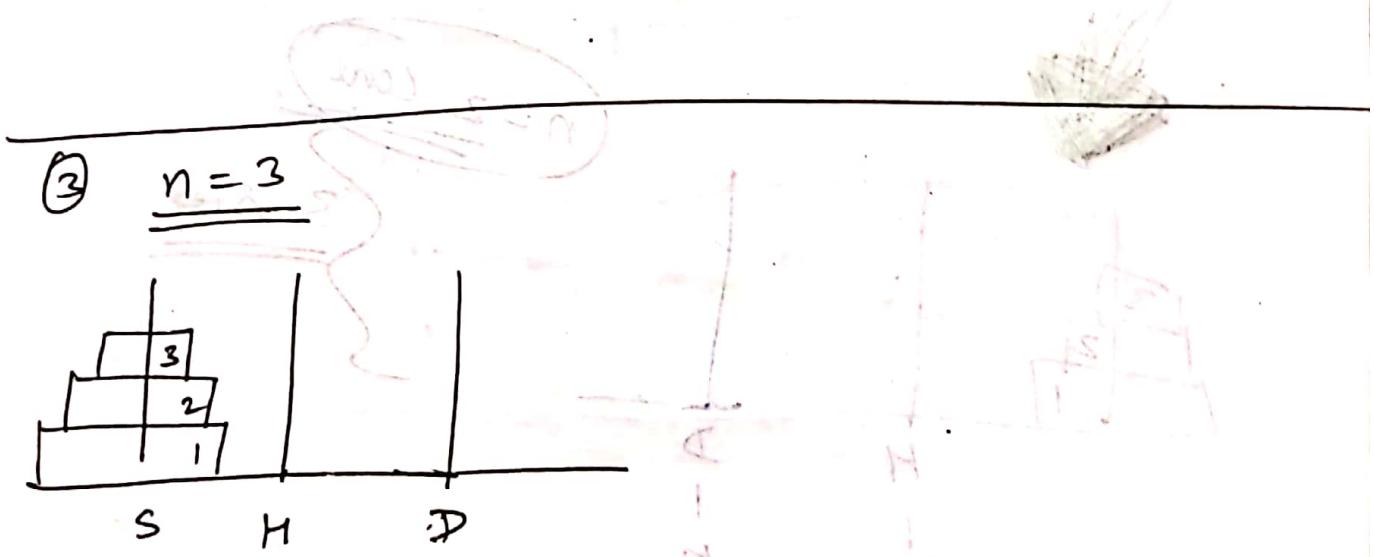
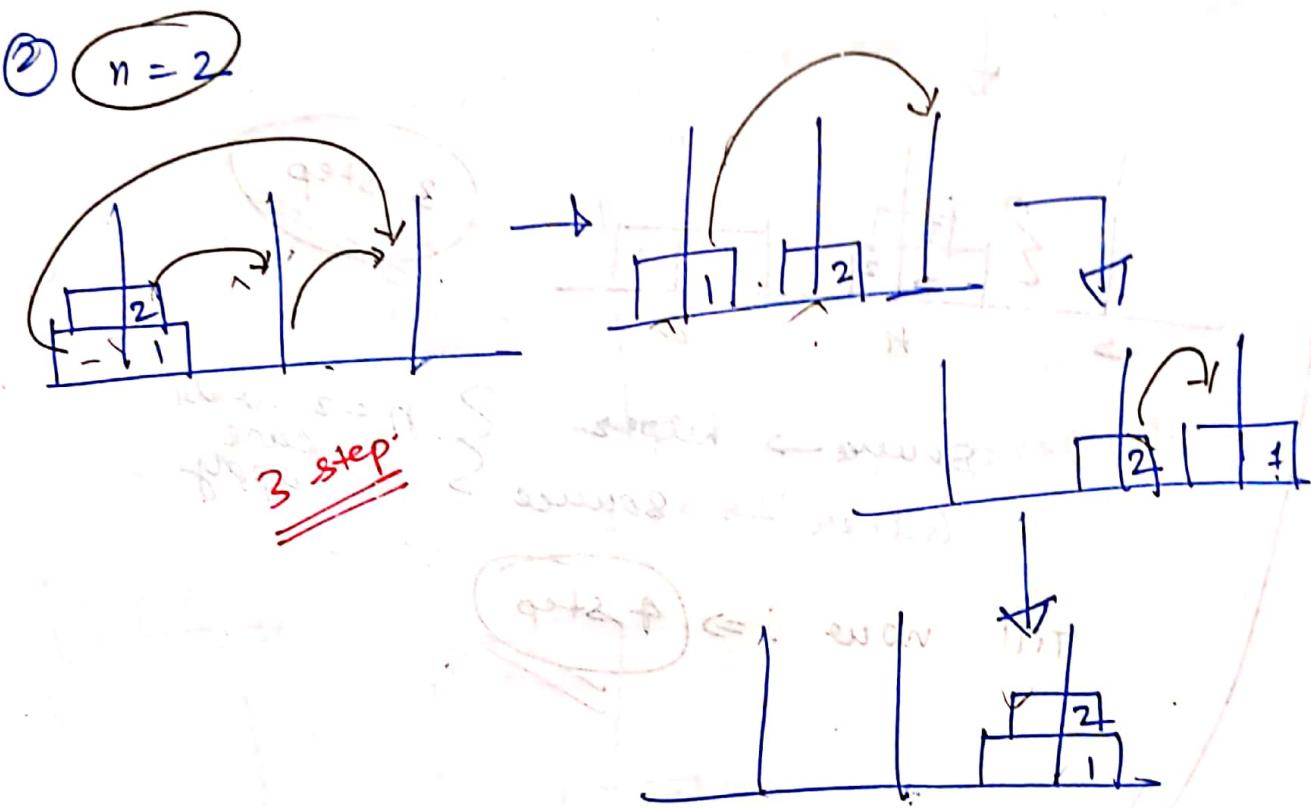
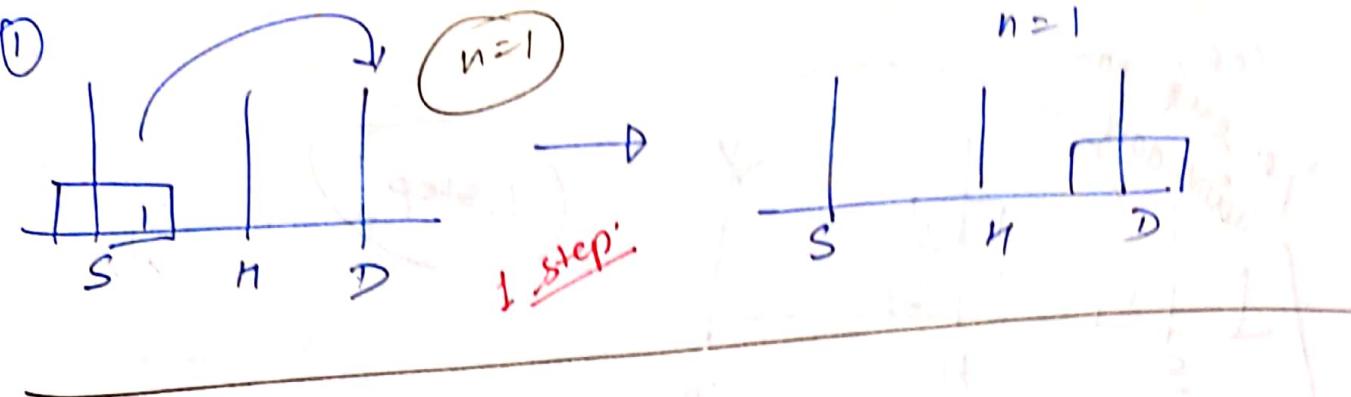
## Lecture - 16

### Recursion - 2

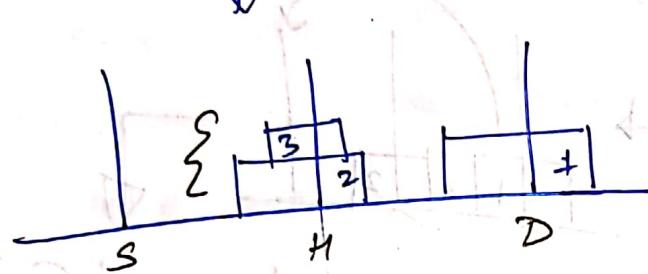
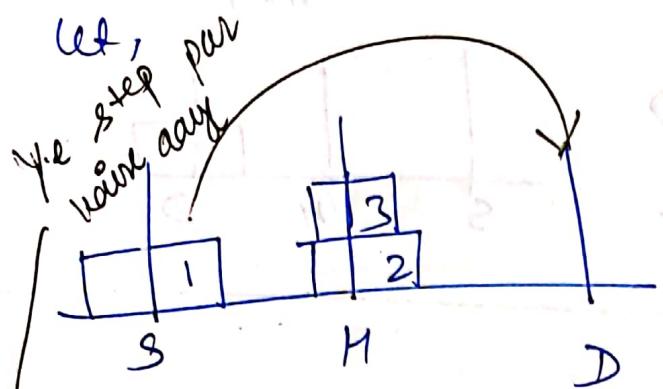
#### (a) Tower of Hanoi

- Rules
- \* only 1 disk transferred in 1 step
  - \* Smaller disk are always kept on top of larger disks





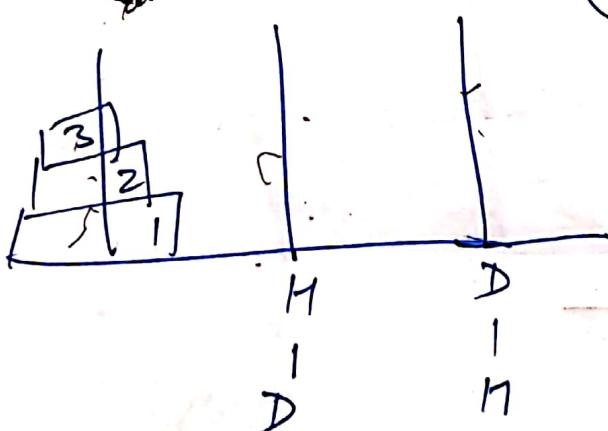
$$\begin{aligned} & \text{①} + \text{②} + \text{③} : q^2 \\ & \text{④} + \text{⑤} + \text{⑥} : q^4 \\ & \text{⑦} + \text{⑧} + \text{⑨} : q^6 \end{aligned}$$



source  $\rightarrow$  helper  
helper  $\rightarrow$  source

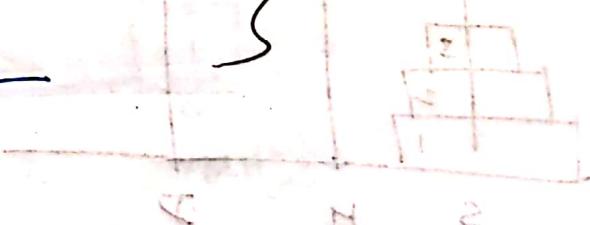
$n=2$  walk  
care  
apply

Till now  $\Rightarrow$  4 step



$n=2$  care

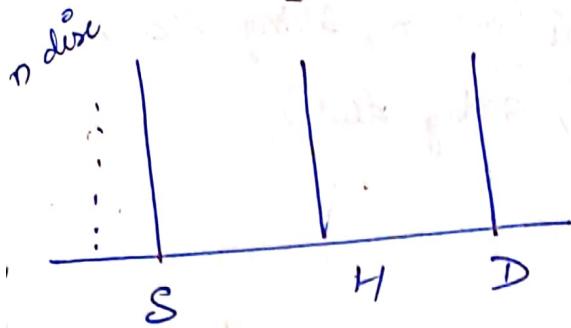
3 step



$$\begin{aligned}\therefore \text{Total Step} &= 3 + 1 + 3 \\ &= 7 \text{ step}\end{aligned}$$

①

### For General Case

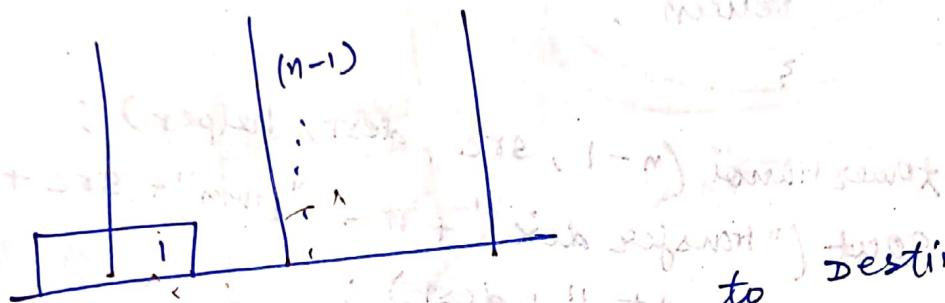


Step 1:

$(n-1)$  disk

Helper takes paluch a dc

②

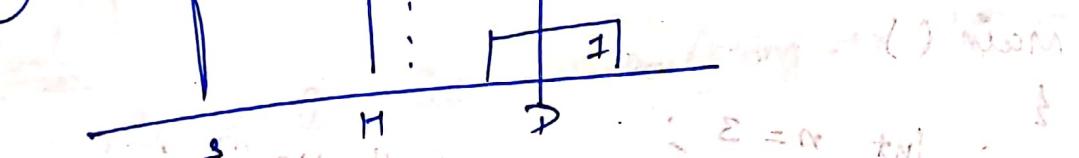


Step 2:

"1" disk

source to destination

③



$(n-1)$  disk

H  $\rightarrow$  D

Using source as helper

## Code

```
public static void towerHanoi(int n, String src,
                               String helper, String dest)
```

```
{ if (n == 1)
```

```
    {
        sout("transfer disk " + n + " from " + src
             + " to " + dest);
    }
```

```
    return;
```

```
}
```

```
    towerHanoi(n - 1, src, dest, helper);
```

```
    sout("transfer disk " + n + " from " + src +
         " to " + dest);
```

```
    towerHanoi(n - 1, helper, src, dest);
```

```
}
```

```
main()
```

```
{ int n = 3;
    towerHanoi(n, "S", "M", "D"); }
```

Time Complexity  $\Rightarrow T_n = O(2^n) \approx O(2^n)$

$$T_n = 2(T_{n-1} + 1) = 2(2T_{n-2} + 1) + 1$$

$$T_{n-1} = 2T_{n-2} + 1$$

$$T_{n-2} = 2T_{n-3} + 1$$

$$T_1 = 1$$

$$n-2 = 7$$

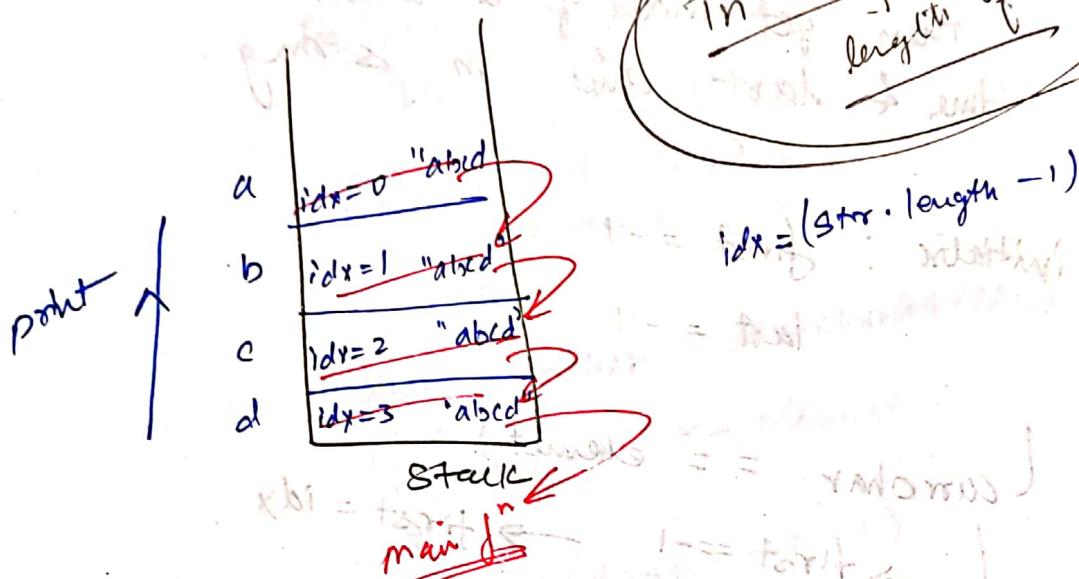
$$n-3 = 6$$

$$x = n-7$$

$$2^{n-1} T(1) + 2^{n-2} + 2^{n-3} + \dots$$

$$= -2^n$$

## (a2) Point a String in Reverse



### Code

```

public static void printRev(string str, int idx)
{
    if (idx == 0)
    {
        sout(str.charAt(0));
        return;
    }
    sout(str.charAt(idx));
    printRev(str, idx - 1);
}

Main()
{
    string str = "abcd";
    printRev(str, str.length() - 1);
}

```

Ques 3) Find the 1<sup>st</sup> & last occurrence of an element in string.

"abacabadabach"

String

Let, element = a  
then get index of a when it's 1<sup>st</sup> time & last time in string.

initialise : first = -1

last = -1

currchar == element

first == -1  $\rightarrow$  first = idx

else  $\Rightarrow$  last = idx

\* value of first & last ( $\Rightarrow$  remains stack changes)  
only idx values in stack changes

$Tn = O(n)$   
(length of string)

## Code

```
public static int first = -1;
public static int last = -1;
public static void findOccur(string str, int idx, char element)
```

if (idx == str.length())

sout(first);

sout(last);

return;

```
{ first = -1; last = -1; }
```

char currchar = str.charAt(idx);

if (currchar == element)

if (first == -1)

first = idx;

else

last = idx;

}

}

findOccur(str, idx + 1, element);

}

Main()

```
{ string str = "abbaacdababd"; }
```

findOccur(str, 0, 'a');

}

(Q4)

Check if an Array is sorted  
(strictly increasing)

$$\text{Arr}[ ] = \{1, 2, 3, 4, 5\}$$

Code:-

```
public static boolean isSorted(int arr[], int idx)
{
    if (idx == arr.length - 1)
        return true;
    if (arr[idx] < arr[idx + 1])
        if (isSorted(arr, idx + 1))
            return isSorted(arr, idx + 1);
    else
        return false;
}
Main()
{
    int arr[] = {1, 3, 5};
    sout(isSorted(arr, 0));
}
```

~~CR.~~  
 { Inside ~~f<sup>n</sup>~~  
 if ( $\hat{idx} == \text{arr.length} - 1$ )  
 { return true;  
 (Following becomes)  $\text{arr}[\hat{idx} + 1]$   
 if ( $\text{arr}[\hat{idx}] >= \text{arr}[\hat{idx} + 1]$ )  
 { array is sorted  
 return false;  
 return ~~isSorted(arr, idx + 1)~~;

$T(n) = O(n)$   
 length of array

$(x_1, x_2) \in \text{AND}$   $x_1 = \text{XOR}$   $x_2 = \text{XOR}$   
 $(x_1' \oplus x_2') \in \text{AND}$   
 $x_1' \oplus x_2' = \text{XOR}$   
 and  $x_1 \oplus x_2$   
 problem (two, 1 + two, one)

$x_1 \oplus x_2 = \text{XOR}$   
 $(x_1 \oplus x_2) \oplus x_1 = x_2$   
 $(x_1 \oplus x_2) \oplus x_2 = x_1$

(Q5) move all 'n' to the end of  
the string

I/P  $\Rightarrow$  "a b c z x d"

↓

O/P  $\Rightarrow$  "a b c d z x x"

currChar (current character)  
idx  $\rightarrow$   
count  $\rightarrow$  track no. of 'x'

newString  $\rightarrow$

Code:

```
public static void moveAll(string str, int idx,  
                           int count, string newString)
```

```
{  
    // Base Case  
    if (idx == str.length())  
        cout << newString;  
}
```

```
char currChar = str.charAt(idx);
```

```
if (currChar == 'x')
```

```
{  
    count++;
```

```
    moveAll(str, idx + 1, count, newString);
```

```
}
```

```
else
```

```
{  
    newString += currChar;
```

```
    moveAll(str, idx + 1, count, newString);
```

main()

string str = "abcd";  
moveAll(str, 0, 0, 4);

empty string

3

### // Base Case of f-Recursion:

if (idx == str.length())

{  
for (i = 0; i < count; i++)  
newString += 'x';

cout << newString;

return;

start address  
of answer

what will our  
answer be

$$T_n = O(n + \text{count})$$

$$= O(2n)$$

$$= O(n)$$

$$T_n = O(n)$$

length of string

last = start + l

length will be l

(Q6)

## Remove Duplicates in a String

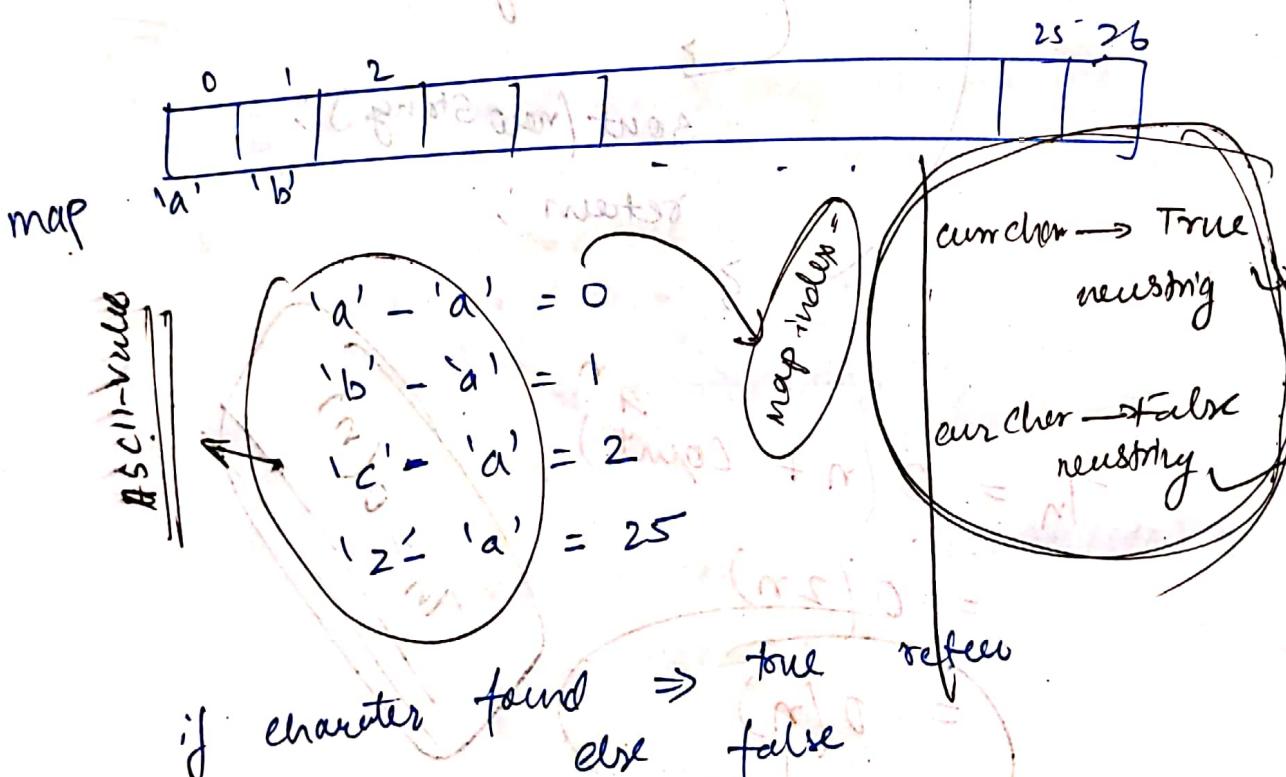
I/P  $\Rightarrow$  str = "a b b c c d d"

O/P  $\Rightarrow$  "abcd"

(i) \* create array to track - keep of duplicate - element

(ii) \* size of array =  $2^6 = 64$

no of alphabet =  $2^6$



curr character = True

new string me add 'nah' kaun

curr character = false

add in new string

$\downarrow$   
map[pas] = True  
to keep track  
of whenever we  
have got  
character

Code.

public static boolean[] map = new boolean[26];

public static void removeDup(String str, int idx, String newString)

{ Base Case

if (idx == str.length())

cout(newString);

return;

{

char currChar = str.charAt(idx);

if (map[currChar - 'a'] == true)

removeDup(str, idx + 1, newString);

{

else

{

newString += currChar;

map[currChar - 'a'] = true;

removeDuplicates(str, idx + 1, newString);

{

} If

characters - character  
gives integer value:

Main()

String str = "abbccda";

removedup(str, 0, "");

$$T_n = O(n)$$

n = length of string

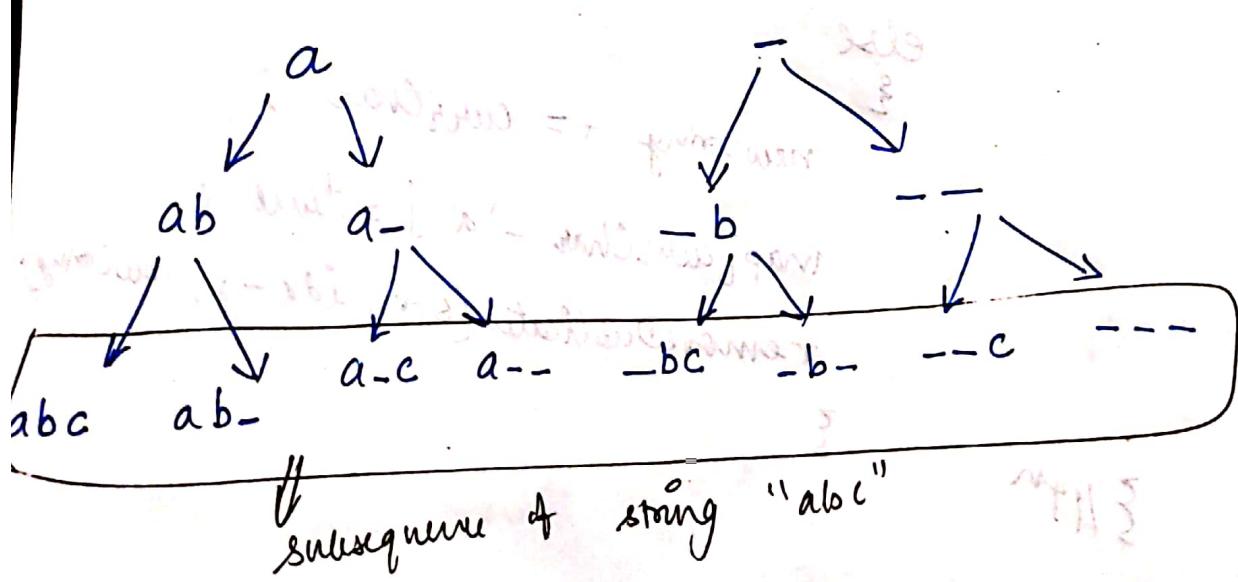
(Q7)

Important Ques:

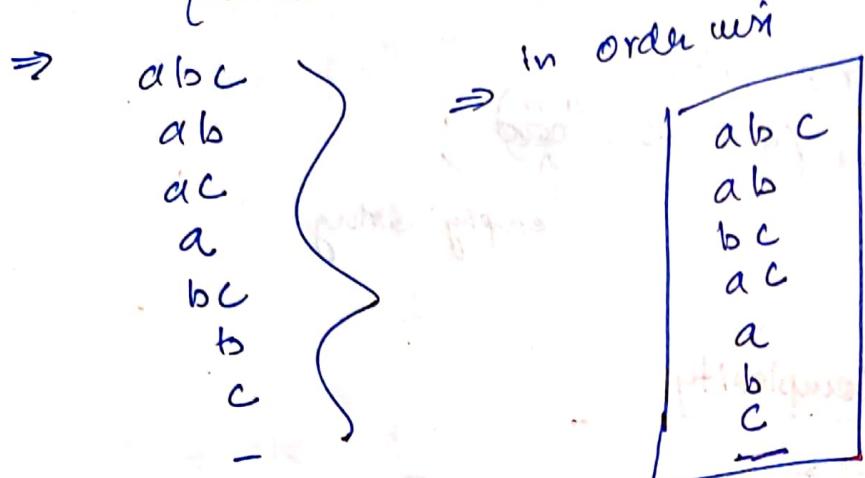
\* Print all the subsequences of a string

"abc"

\* Subsequence  $\Rightarrow$   
 $\Rightarrow$  a sequence that can be derived from the given string by deleting zero or more elements without changing the order of the remaining elements



!- Subsequences we got:-



ut, newString = "" (empty)

"abc" call 1 : newString + curChar (a aayega)  
idx call 2 : newString (a nahi aayega)

### Code

```
public static void subsequence (string str, int idx,  
string newString)
```

{ // Base Case

if (idx == str.length())

{ cout (newString);

return;

{

char curChar = str.charAt (idx);

choose curChar

// to be (take it) → choose to be

Subsequence (str, idx+1, newString + curChar);

// Not to be (not take it) → choose not to be

Subsequence (str, idx+1, newString);

{

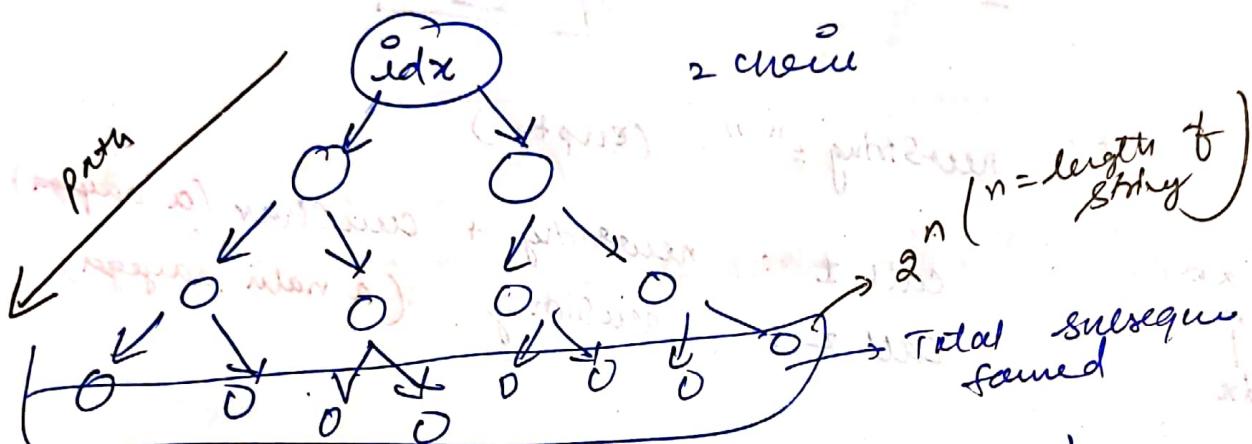
Main()

3

String str = "abc"  
subsequences (str, 0, "") ;  
empty string

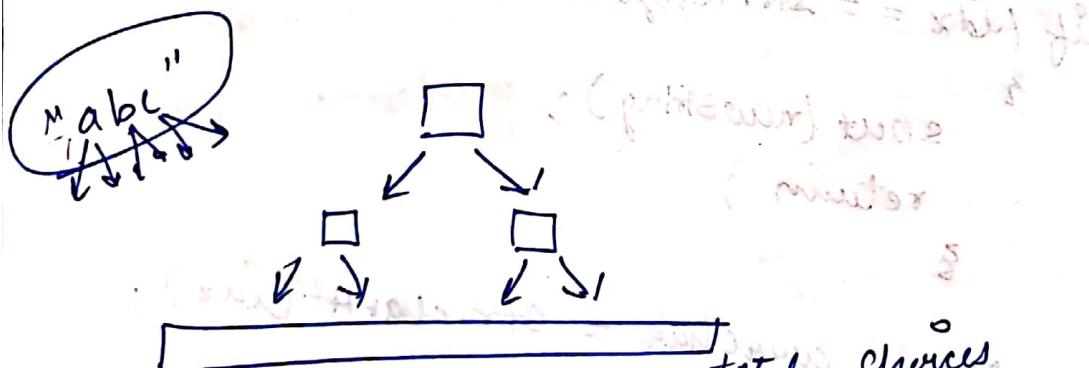
3

### Time Complexity



(At each par getting 2 choices)

"abc"  $\rightarrow$  3 characters or  $3 = 1 \text{ result}$   
 $\therefore \text{subseq no.} = 2^3 = 8$



total choices  
(total subsequences)

$$\text{Subs} = 2^n$$

$$= 2 \times 2 \times 2 = 2^n$$

$$\text{(last level (node)} = 2^n = 2 \times (2^{n-1})$$

$$\text{2nd last level (node)} = 2^{n-1} = 2 \times (2^{n-2})$$

$$= 2 \times (2^{n-3})$$

$$= 2 \times (2^{n-4})$$

↓  
↓  
↓  
↓  
↓  
↓

↓  
↓  
↓  
↓  
↓  
↓

# Add the  $f^n$  calls

G.P  $\rightarrow$  Geometric progression

$$2^n + 2^{n-1} + 2^{n-2} + 2^{n-3} + \dots + 1$$

$$= \frac{a(r^n - 1)}{(r-1)} = \frac{(2^{n+1} - 1)}{(2 - 1)}$$

$$= (2^{n+1} - 1)$$

time complexity

$$T_n = O(2^n) \quad \text{in terms of asymptotic notation}$$

(In terms of time complexity)

(In terms of space complexity)

(In terms of time complexity)

(In terms of space complexity)

(In terms of time complexity)

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(In terms of time complexity)

(In terms of space complexity)

(In terms of time complexity)

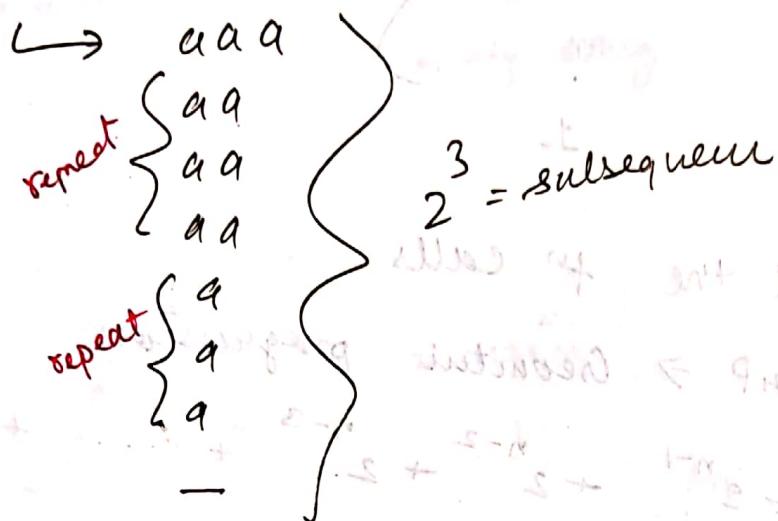
(In terms of space complexity)

(In terms of time complexity)

(In terms of space complexity)

(Q8) Point all the subsequences of a string unique.

\* "aaa"



\* Use: Special Data Structure  $\Rightarrow$  HashSet

### Code

```
public static void subsequences(string str, int idx, string newString, HashSet<string> set)
{
    // Base Case
    if (idx == str.length())
    {
        if (set.contains(newString))
        {
            return;
        }
    }
    else
    {
        cout (newString);
        set.add (newString);
        return;
    }
}
```

char curChar = str.charAt(idx);

if to be subsequences(str, idx+1, newString + curChar, set);

if not to be subsequences(str, idx+1, newString, set);

3 || fn

Main()

{

String str = "aaa";

HashSet<String> set = new HashSet();

subsequences(str, 0, "", set);

3 || main

Output

↓,

aaa
aa
a
-

→ Unique Subsequence

Yabg

## (Q9) Point Keypad Combination

0 → .

let say:

1 → abc

"23"

2 → def

find possible keypad

3 → ghi

combination of 23.

4 → jkl

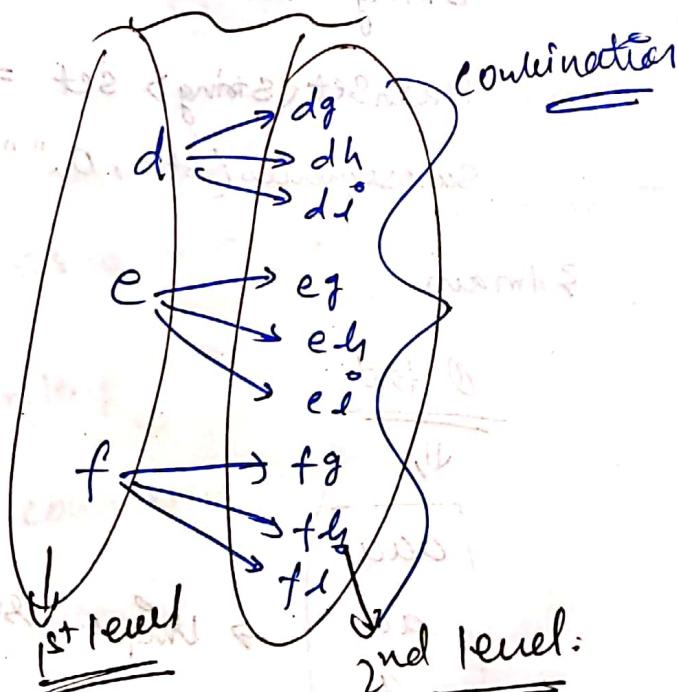
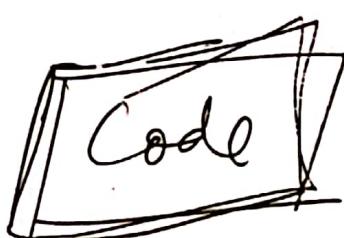
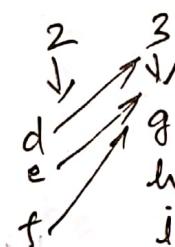
5 → mno

6 → pqrs

7 → tu

8 → vwxyz

9 → yz



public static String[] Keypad

```
= { "", "abc", "def", "ghi", "jkl", "mno", "pqrs",
    "tuv", "vwxyz", "yz" }
```

```

public static void printKey(string str, int idx,
                           string comb) {
    // Base Case
    if (idx == str.length()) {
        cout << comb;
        return;
    }
    char currChar = str.charAt(idx);
    string mapping = keypad[currChar - '0'];
    for (int i = 0; i < mapping.length(); i++) {
        printKey(str, idx + 1, comb + mapping.charAt(i));
    }
}

main() {
    string str = "23";
    printKey(str, 0, "");
}

```

$$T_n = 4^n \rightarrow \text{time complexity}$$

## Lecture - 17

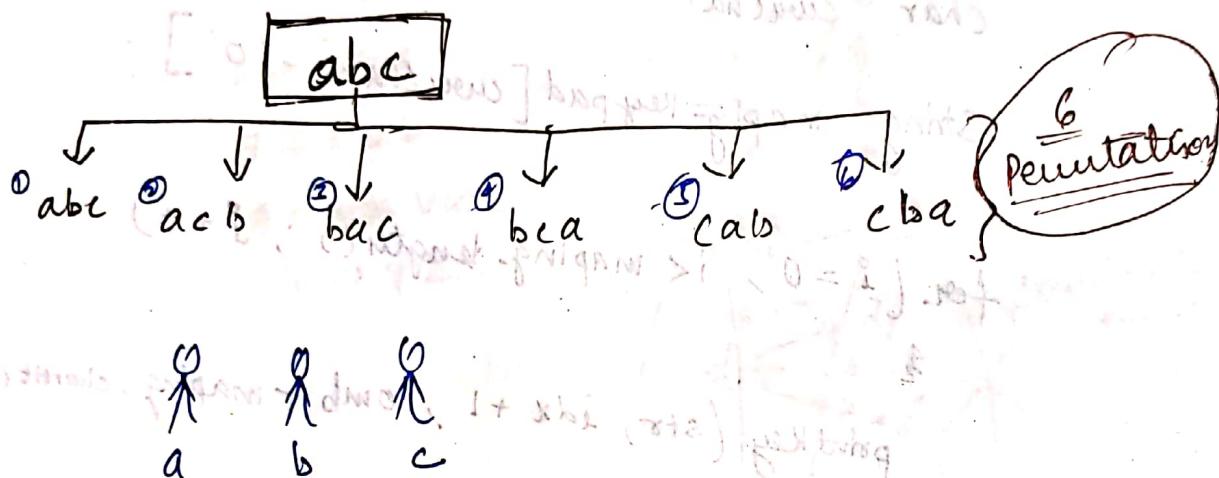
### Recursion - 3

Adv. level

(Q1) Print all permutation of a string.

"abc"

↓  
all possible combination of letters



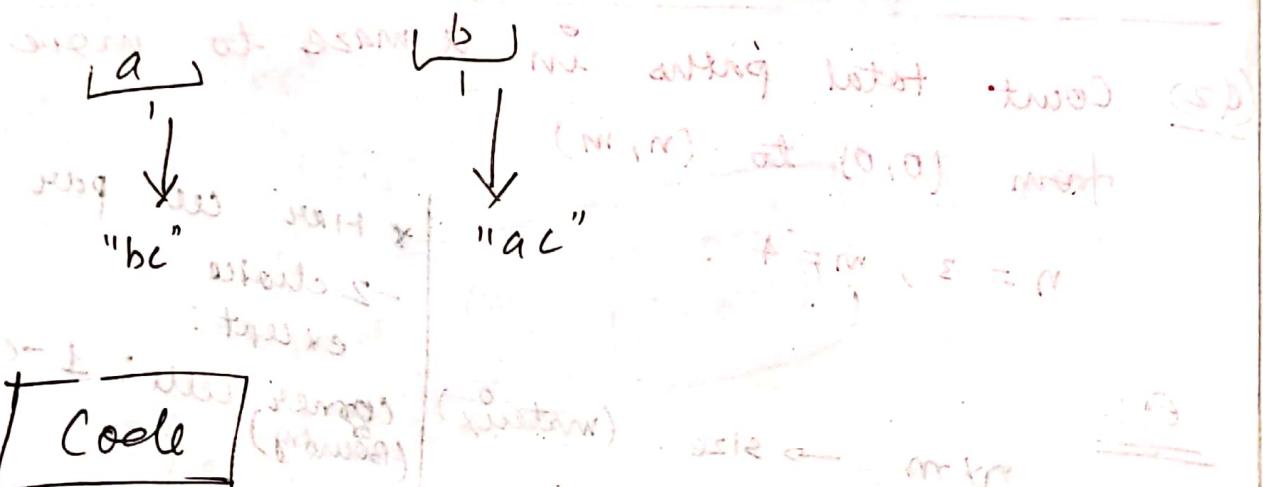
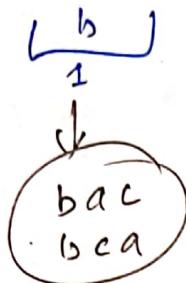
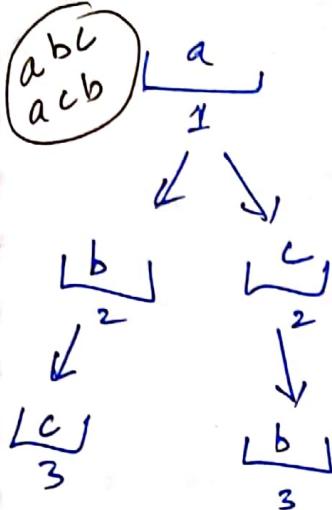
1	2	3
a	b	c
a	c	b
b	a	c
b	c	a
c	a	b
c	b	a

$$\Rightarrow \text{total no} = 6$$

$$+ 3P_3 = 3! = 6$$

$$(3P_3) = 6$$

abc



```
Code
```

```
public static void printPerm(string str, string permutation)
{
    // Base case
    if(str.length() == 0)
    {
        cout (permutation);
        return;
    }

    for (i=0 ; i<str.length() ; i++)
    {
        char currChar = str.charAt(i);

        string newStr = str.substring(0,i) +
                        str.substring(i+1);

        printPerm (newStr, permutation + currChar);
    }
}
```

31/FM

Main()

```
{  
    string str = "abc";  
    printPerm(str, "");  
}
```

$$T_n = O(n!)$$

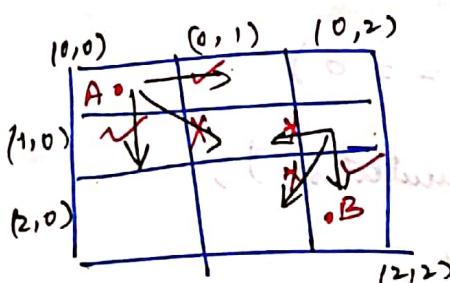
(Q2) Count total paths in a maze to move from  $(0,0)$  to  $(n,m)$

$$n=3, m=4$$

Eg:-

$n \times m \rightarrow$  size (matrix)

$$\text{if, } n=m=3$$



\* Max cell pair  
- 2 choice "sd"  
except:  
corner cell: 1-choice  
(Boundary) (2,2)

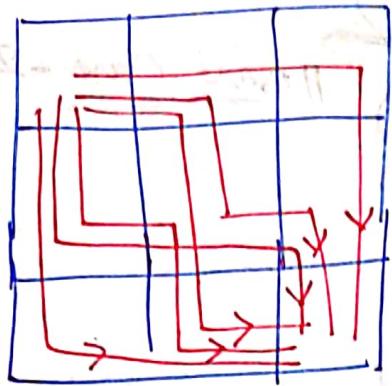
$3 \times 3$

\* go from A to B & find no. of total path

bottom row

Condition:  
(i) right move      (ii) + diagonal & back  
not allowed

(iii) downward move

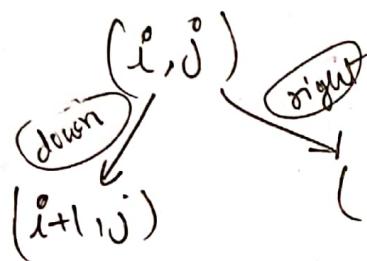


\* 6 paths possible

total path = 6

moving allowed

\* each cell  $\rightarrow$  2 choices := right / down



base cond:  $(i = n-1)$   
 $(j = m-1)$

$\downarrow$   
 $\text{Count}(i+1, j) + \text{Count}(i, j+1)$  } total path



public static int countPath (int i, int j, int n, int m)

{ // Base Case ->

if ( $i = n$  ||  $j = m$ )

{ return 0;

}

$$((n+m)-2)0 = 0$$

```

if ( $i == n-1 \text{ and } j == m-1$ ) {
    return 1;
}

```

$\Rightarrow$  // Base Case - 2

// move downward  
int downPath = countPath( $i+1, j, n, m$ );

// move right  
int rightPath = countPath( $i, j+1, n, m$ );

return downPath + rightPath;

$\} // i^{th}$

main()

{

int  $n = 3, m = 3$ ;  
int totalPath = countPath(0, 0, n, m);  
cout < totalPath;

$\} // main$

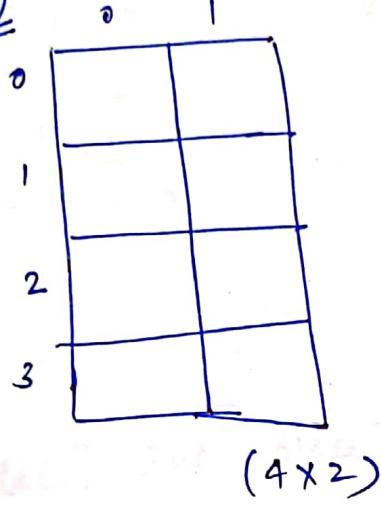
$$T_n = O(2^{n+m})$$

(d3) Place Tiles of size  $1 \times m$  in a floor  
of size:  $n \times m$

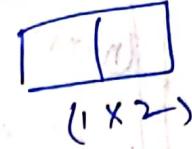
$$n = 4, m = 2$$

Eq:-

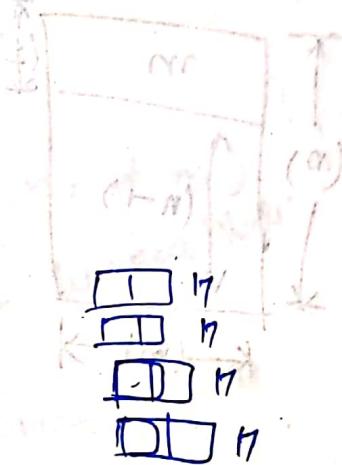
floor



size of Tile



$$(1 \times 2)$$



ways

(i) place tiles horizontally

(ii)

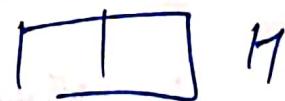
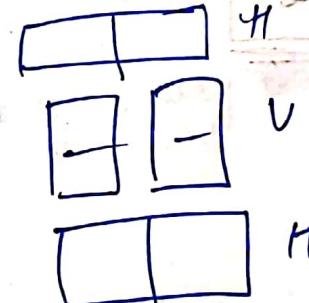


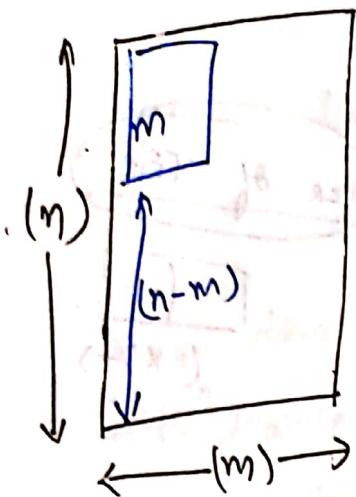
$m = n = 2$  (ii)



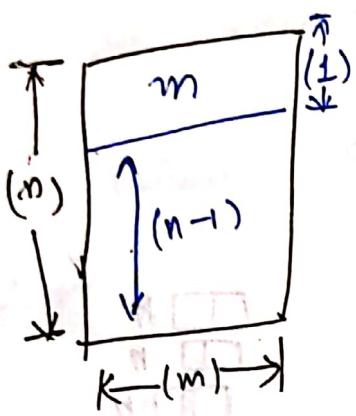
$m = n = 2$  (ii)

(iii)





Tile with size ( $n \times m$ )  
 $\downarrow$   
 $m$   $\rightarrow$   $H$   
 $\downarrow$   
 $n$   
 $\downarrow$   
place  $(n-m)$   $\rightarrow$   $(n-1)$  place



$(n \times n)$

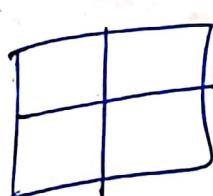
Code

Base Case

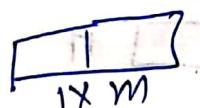
(i)  $n = m$

= 2 way

$n=2, m=2$

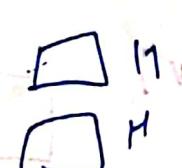
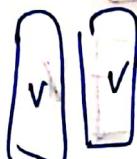


$n \times m$



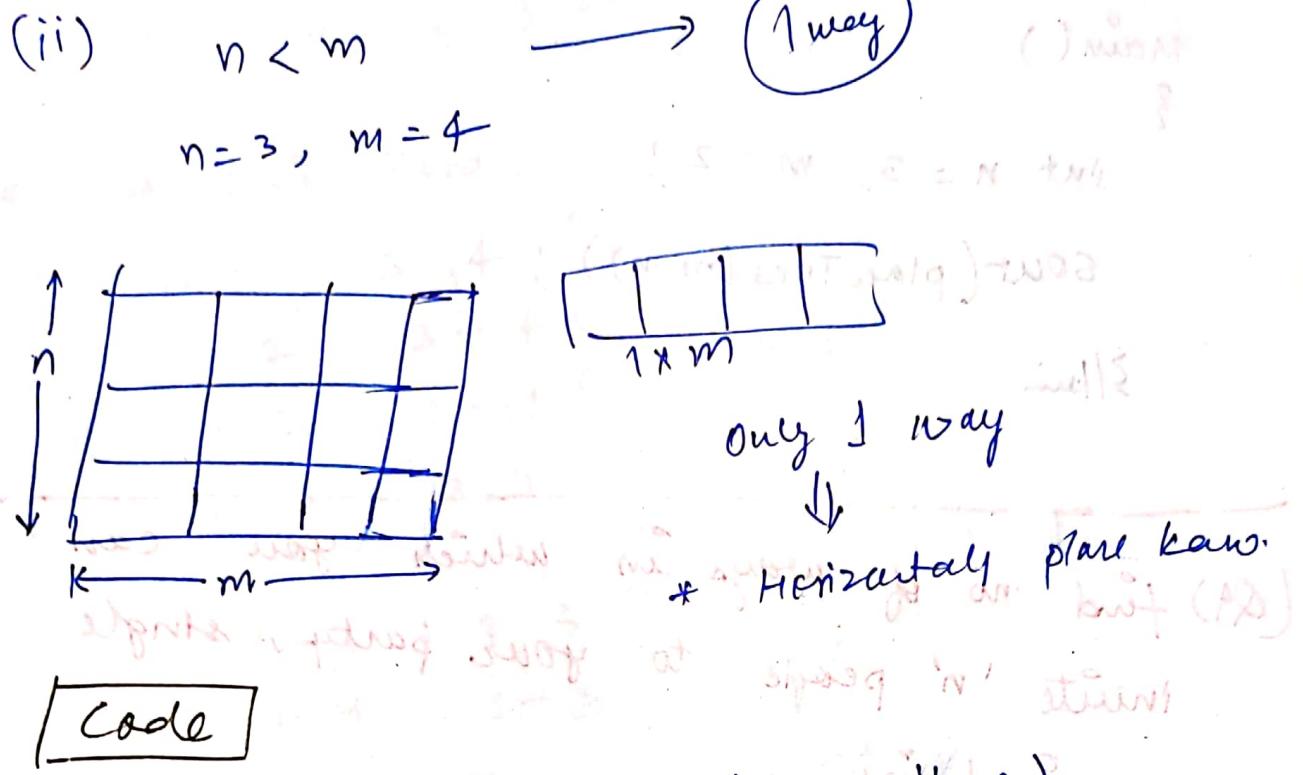
$1 \times m$

$L_2 Y$



$L_1 Y$





```
public static int placeTiles(int n, int m)
```

{ //Base case

if ( $n == m$ )  $\rightarrow$  either place vert or horiz

return 2; // Only 2 ways possible

3

if ( $n < m$ )

return 1; // Only 1 way possible

3

//Vertically  $\Rightarrow$  placeTiles ( $n-m, m$ );

int vertPlace =

//Horizontally

int horPlace = placeTiles ( $n-1, m$ );

return vertPlace + horPlace;

{ // fn

main()

{

int n = 3, m = 2;

sout(placeTiles(n, m));

3/km

place tiles

place tiles

(Q4) find no of ways in which you can invite 'n' people to your party, single or in pairs.

~~Ex: when~~

$n=4 \Rightarrow$  1 way

$n=3 \Rightarrow$  single (1-2), (1-2) pair (1-2)  $\Rightarrow$  2 ways

$n=3 \Rightarrow$  1-2 3  $\rightarrow$  1 way

1-2 3  $\rightarrow$  2 ways

1-3 2  $\rightarrow$  3 ways

1 2-3  $\rightarrow$  4 ways

$n=4 \Rightarrow$  1 2 3 4  $\rightarrow$  4 ways

1 two allele

1 2 3 4 }  
1 2-3 4 }  
1 2 3-4 }

1 2-4 3 } 4 way

\* 110 pair karo : ways of ways

1-2      3 4 }  
1-2      3-4 } 4 way  
1-3      2-4 }  
1-3      2 4 }

1-4      2 3 } 2 way  
1-4      2-3 }

$$\text{ways} = 4 + 4 + 2 = 10$$

ways

guest call(n)

pair call(n-2)

(n-1) \* call(n-2)

Calling

public static int callGuest(int n)

{ // base case

if (n <= 1)

{ return 1;

} else

{ return 1 +

callGuest(n-1);

callGuest(n-1);

callGuest(n-1);

callGuest(n-1);

// single

int ways =

callGuest(n-1);

4 pair  
int ways2 = (n-1) \* callGust(n-2);

return ways1 + ways2;

3/11/11

main()

{

    int n = 4;

    cout << callGust(n);

3/11/11

(Q5) Point all the subsets of a set of  
natural numbers.

\* n=3 \*

{1, 2, 3}

(1, 2, 3)

↓ ↓ ↓

(1, 2, 3), (1, 2) and (1, 3),

(2, 3)

(1)

(2)

(3)

empty()

Code

public static void printSubset (ArrayList<Integer> subset)

{

    for (i=0; i < subset.size(); i++)

        cout << subset.get(i) + " ";

    cout << endl;

}

```
public static void findSubset (int n,  
                           ArrayList<Integer> subset)
```

{ // Base Case :

if (n == 0)

{ printSubset (subset);

return;

}

// add hoga

subset.add(n);

findSubsets (n-1, subset);

// add nahin hoga

subset.remove (subset.size() - 1);

findSubsets (n-1, subset);

3 / / + n

main()

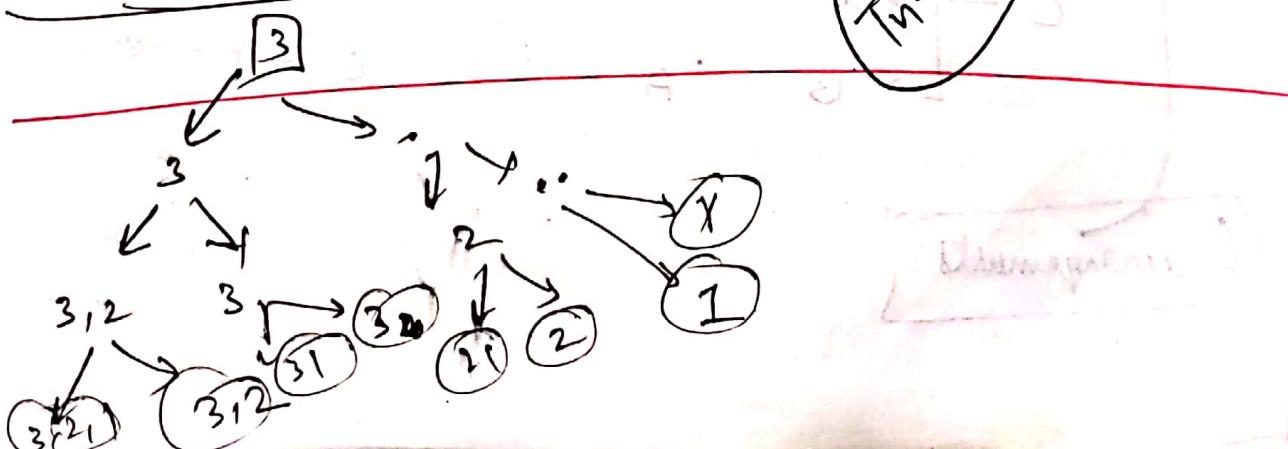
{

int n = 3;

ArrayList<Integer> subset = new ArrayList<>();

findSubsets (n, subset);

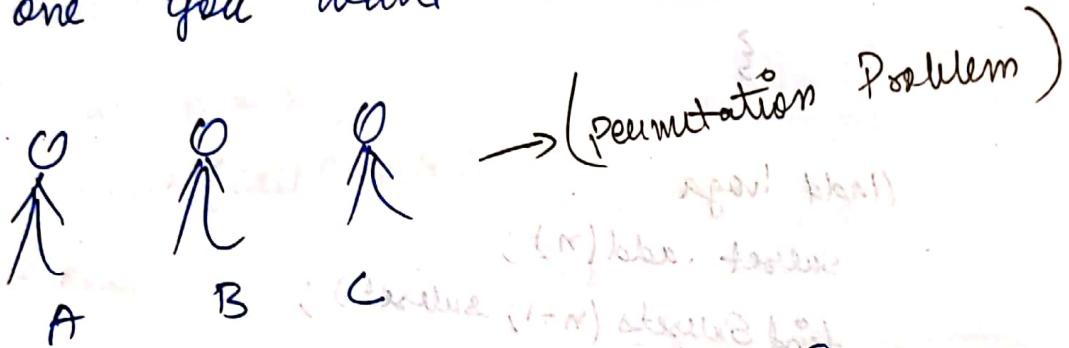
} / / n



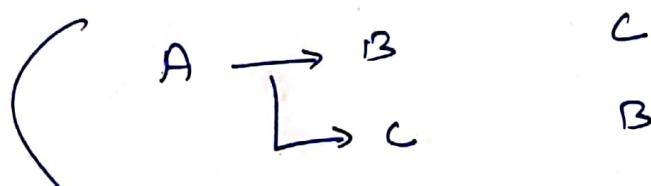
## Lecture -18

### Back-Tracking

\* Find all possible solutions & use the one you want.



\* Arrange them in a single line +



$A \ B \ C \rightarrow (i)$

$A \ C \ B \rightarrow (ii)$

$B \ A \ C \rightarrow (iii)$

$B \ C \ A \rightarrow (iv)$

$C \ A \ B \rightarrow (v)$

$C \ B \ A \rightarrow (vi)$

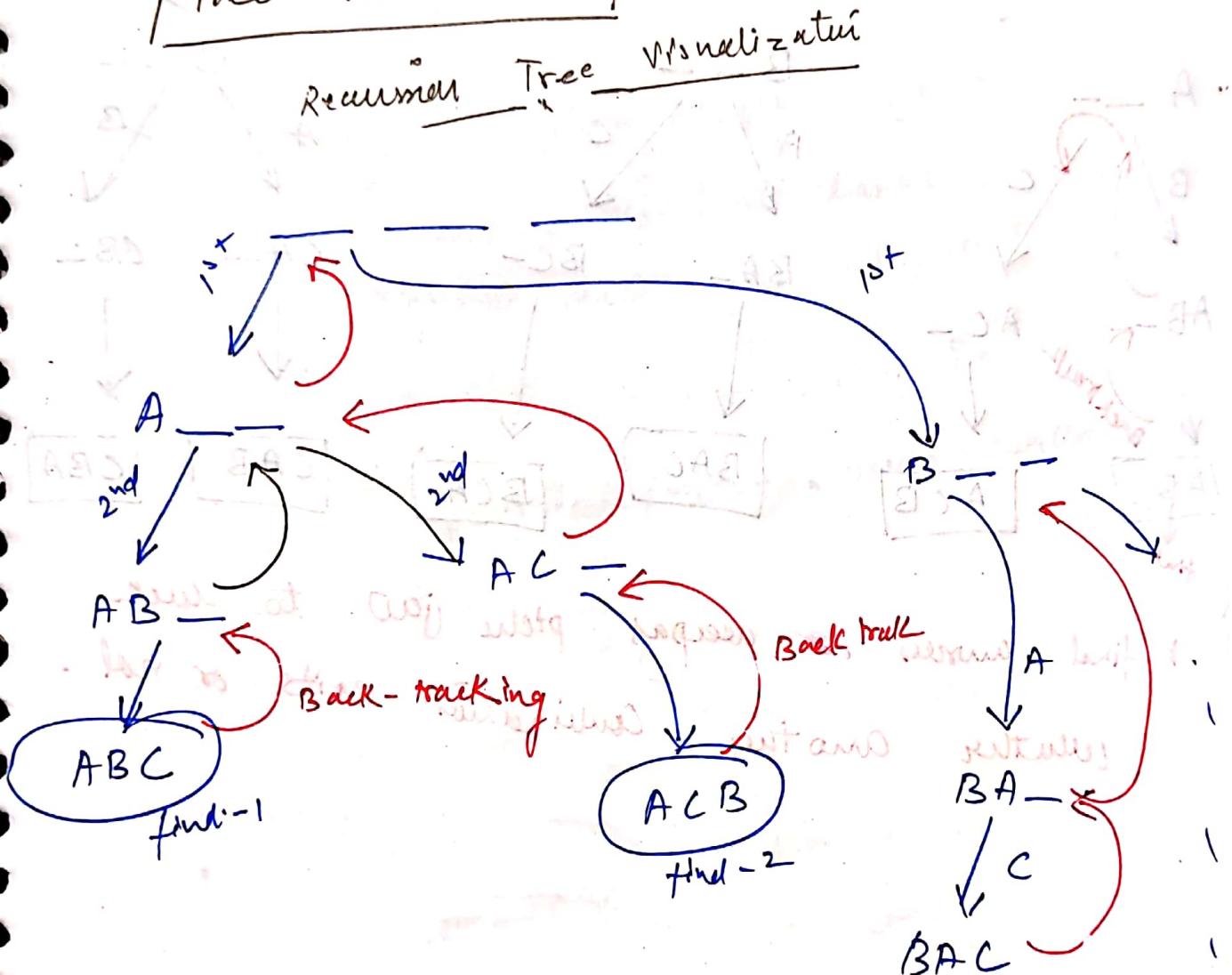
6 arrangements

total permutation =  $n!$

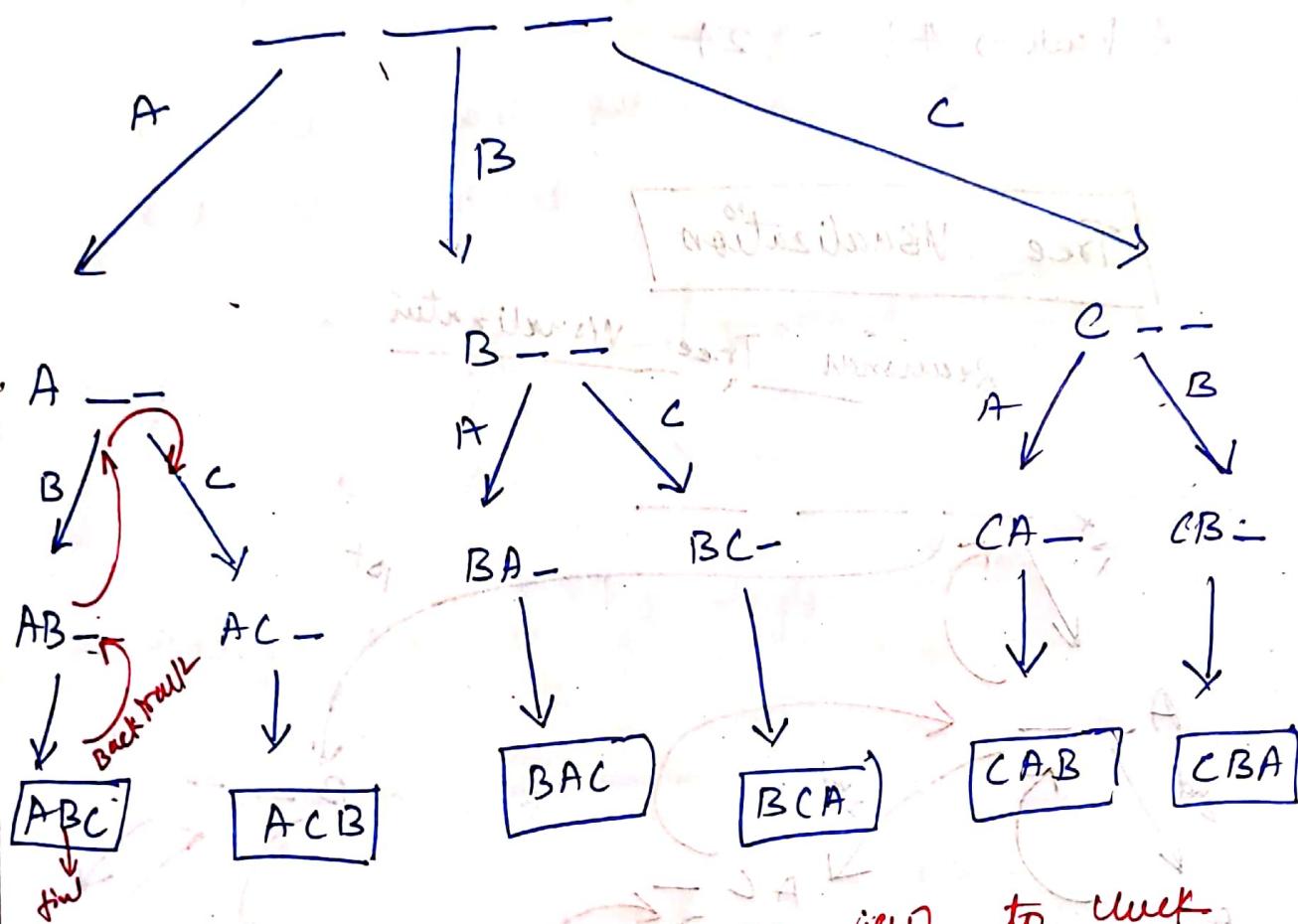
$$3 \text{ books} \rightarrow 3! = 6$$

$$4 \text{ books} \rightarrow 4! = 24$$

### Tree Visualization



## Free Visualization



+ find sources see we pass pitch jew to chick

whether another continuation exists or not.

## Code

```
public static void printPerm(String str, String perm,
                             int idx)
{
    // Base - case
    if (str.length() == 0)
        cout(perm);
        return;
}

for (i = 0; i < str.length(); i++)
{
    char curChar = str.charAt(i);
    String newStr = str.substring(0, i)
                    +
                    str.substring(i+1);
    printPerm(newStr, perm + curChar, i+1);
}

main()
{
    String str = "ABC";
    printPerm(str, "", 0);
}
```

## Time Complexity

$$T_n = O(n + n!)$$

steps

## N - Queens

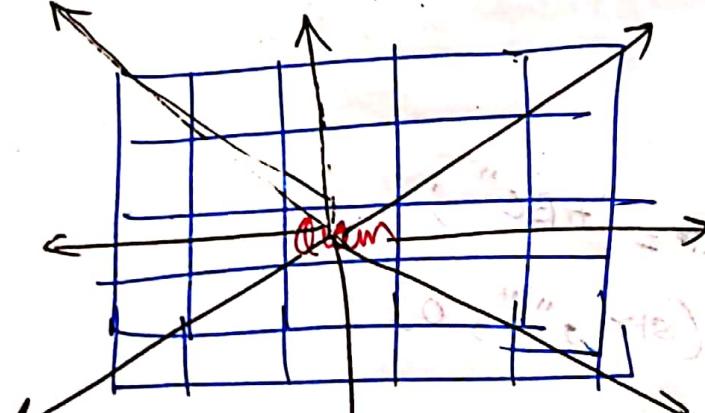
~~\*\*~~  $N \times N$  : Chess Board

$N$  : Queen

Print all  $Sol^n$  where queens are safe.

Eg:

$5 \times 5$  ( $n=5$ )

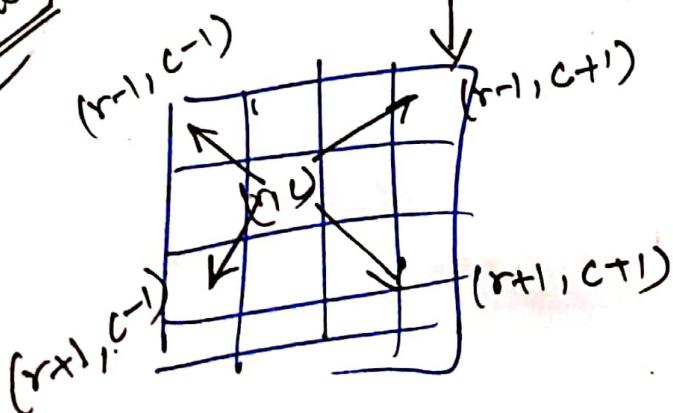


(5  $\rightarrow$  Queen)

( ) missing

path of Queen seen  
here

~~formula~~



$Q_1, Q_2, Q_3, Q_4$  ( $Q = \text{Queen}$ )

Place them in diff. columns (safely) (Qu X)

$Q_1$	↖	↖		
	↖			
		↖		
			↖	

$Q_1$	↖	↖	↖	
	↖			
		$Q_3$	↖	
			↖	

- $Q_3$  not possible to place
- Backtrack & change pos of  $Q_1$  &  $Q_2$
- Arrangement wrong

→  $Q_4$  not poss. to place  
 → Backtrack  
 →  $Q_2$  will say I'm at last pos.  
 → Now change  $Q_1$  position

	↖	$Q_3$	↖	
$Q_1$	↖		↖	
	↖		$Q_4$	
	$Q_2$			

		$Q_3$		
$Q_1$	(Q=initial)			
				$Q_4$

Result 1 (all Queen placed safely pos.)

$Q_1$				

	$Q_2$			
$Q_1$				

(Row  $\rightarrow 2$ )

and so on & so forth

Code

⇒ N-Queen Puzzles

↓  
Return answer in the form of

⇒ List of list of string

\* jaha par Queen ho sakti hai ⇒ Q

other wise put "o" in other places

[["..Q..", "...Q"], [ ]]

Only

Code

# public boolean isSafe(int row, int col, char board[8][8])

{

// horizontal

for (int j=0; j < board.length; j++)

{

if (board[row][j] == 'Q')

{

return false;

}

}

// vertical

for (int i=0; i < board.length; i++)

{

if (board[i][col] == 'Q')

{

return false;

}

//upper left

```
int r = row; if (row >= 0 & r >= 0; c = col; c >= 0 & r >= 0; c++, r--)  
for (int c = col; c < board.length & & r >= 0; r--, c++)  
    if (board[r][c] == 'Q')  
        return false;  
    else  
        continue;
```

//upper right

```
int r = row; if (row >= 0 & r >= 0; r >= 0; r--, c++)  
for (int c = col; c < board.length & & r >= 0; r--, c++)  
    if (board[r][c] == 'Q')  
        return false;  
    else  
        continue;
```

//lower left

```
int r = row; if (row >= 0 & r < board.length; c = col; c >= 0 & r < board.length; r++, c--)  
for (int c = col; c >= 0 & r < board.length; r++, c--)  
    if (board[r][c] == 'Q')  
        return false;  
    else  
        continue;
```

// lower right

```
for (int c = col ; c < board.length && r < board.length ;  
     c++, r++)
```

{

```
    if (board[r][c] == 'Q')
```

{

```
        return false;
```

}

{

// for repeat

```
return true;
```

3/1st

```
# public void saveBoard (char [][] board ,  
list<list<string>> allBoards)
```

{

```
    string row = " ";
```

```
    list<string> newBoard = new ArrayList<>();
```

```
    for (int i = 0 ; i < board.length ; i++)
```

{

```
    row = " ";
```

{

```
    if (board[i][j] == 'Q')
```

{

```
        row += 'Q' ;
```

}

## N-Queens ... Conti-nues

W (West Kansas) woodpecker

else

5

row + =

2

```
newBoard.add(row);
```

۲۳

all Board add (new Board);

三

\* public void helper(char[][] board, int col, list<list<String>>)

۳

// Base case

if (col == board.length)

三

SaveBoard(board, allBoard);

return;

三

```
for(int row = 0; row < board.length;  
    row++)
```

92

i)  $(isSafe(row, col, board))$

۳

board [row][col] = 'Q';

helper (board, allBoard, col + 1)

board [row][col] = ".";

3/1 for

{ (row) board, allBoard }

3/1 fn

{ (row) board, allBoard }

class Solution {  
 boolean isSolved (String[] board) {  
 for (int i = 0; i < 9; i++) {  
 for (int j = 0; j < 9; j++) {  
 if (board[i][j] != '.') {  
 if (!isValid (board, i, j)) return false;  
 }  
 }  
 }  
 return true;  
 }  
}

(if you see null  
if board == null)

{ (row) board, allBoard }

{ int row }

{ (row). board > row <= row tri) ref  
(+row)

{ (row, col, word) sfp2(i) }

## Lecture - 21

### Java Sudoku Solver

\* A sudoku soln must satisfy all the

following :-

(1) each digit 1-9 must occur exactly once

in each row

(2) each of the digit 1-9 must occur exactly once in each column

(3) each of the digit 1-9 must occur exactly once in each of the  $3 \times 3$  sub-boxes

tri of the grid

\* The '.' character indicates empty cells

\* Sample Input :

5	3		7					
6			1	9	5			
.	9	8						
8				2				
4					3			1
7				2				6
6						2	8	
4	1	9						5
			8			7	9	

9x9

board =  $\begin{bmatrix} "5", "3", "5" \\ "5", "3", "5" \\ "5", "3", "5" \end{bmatrix}$

**Code**

a) \* Starting Row =  $3 * (\text{row} / 3)$   
 Starting Column =  $3 * (\text{col} / 3)$

b) \* Starting Row =  $\text{row} - \text{row} \% 3$   
 Starting Column =  $\text{col} - \text{col} \% 3$

isSafe

① row

② column

③ grid

**Code**

public boolean isSafe(char board[][], int row, int col, int number)

{

// column

for (int i = 0; i < board.length; i++) {

{

if (board[i][col] == (char)(number + '0'))

{

return false;

}

};

EX:

5	3	5	5	3	5	5	3	5
5	3	5	5	3	5	5	3	5
5	3	5	5	3	5	5	3	5

```
//row
for (int j=0 ; j< board.length ; j++)
{
    if (board [row] [j] == (char)(number + '0'))
        return false;
}
```

---

~~```
//grid
for (int j=0 ; j< board.length ; j++)
{
    if (board [row] [j] == (char)(number + '0'))
        return false;
}
```~~

---

```
//grid
int sr = 3 * (row / 3) ; // starting row
int sc = 3 * (col / 3) ; // starting column
for (int i=sr ; i<sr+3 ; i++)
{
    for (int j=sc ; j<sc+3 ; j++)
        if (board [i] [j] == (char)(number + '0'))
            return false;
}
```

```

return true;

} // fn

* public boolean helper(char board[][], int row,
    int col)

{
    if (row == board.length)
        return true;

    int nrow = 0;
    int ncol = 0;

    if (col == board.length - 1)
        nrow = row + 1;
        ncol = 0;

    else
        nrow = row;
        ncol = col + 1;

    if (board[nrow][ncol] != '0')
        if (helper(board, nrow, ncol))
            return true;
}

```

```
else {
```

```
    // fill the places (empty)
```

```
    for (int i=1; i<=9; i++)
```

```
        if (isSafe (board, row, col, i))
```

```
            board [row] [col] = (char) (i+'0');
```

```
        if (helper (board, row, ncol))
```

```
            return true;
```

(Truebot)

else

```
    board [row] [col] = '0';
```

```
    if
```

```
    for
```

```
    return false;
```

```
if
```

```
main ()
```

```
    helper (board, 0, 0);
```

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