



SRM Institute of Science and Technology
College of Engineering and Technology

DEPARTMENT OF MATHEMATICS

SRM Nagar, Kattankulathur – 603203, Chengalpattu District, Tamilnadu

Academic Year: 2022-23 (ODD)

Slot C1

Set A

Test: CLAT-1

Course Code & Title: 18MAB302T- Discrete Mathematics for Engineers

Year & Sem: III & V

Date: 9.9.2022

Duration: 50 minutes

Max. Marks: 25

Course Articulation Matrix:

At the end of this course, learners will be able to:			Program Outcomes (PO)											
Course Outcomes (CO)		Learning Bloom's Level	1	2	3	4	5	6	7	8	9	10	11	12
CO1	Apply the concepts of set theory and its operations in data structures and mathematical modeling languages	4	3	3										
CO2	Solve problems using counting techniques and understanding the basics of number theory	4	3	3										
CO3	Comprehend and validate the logical arguments using concepts of inference theory	4	3	3										
CO4	Inculcate the curiosity for applying the concepts of algebraic structures to coding theory	4	3	3										
CO5	Apply graph theory techniques to solve wide variety of real world problems	4	3	3										
CO6	Acquire knowledge in mathematical reasoning, combinatorial analysis and discrete structures	4	3	3										

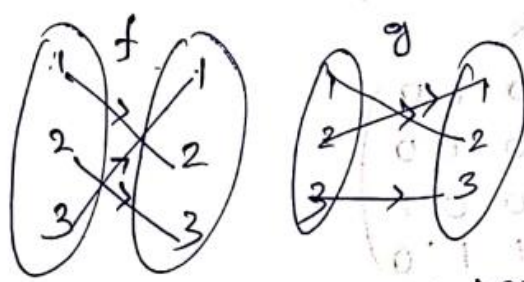
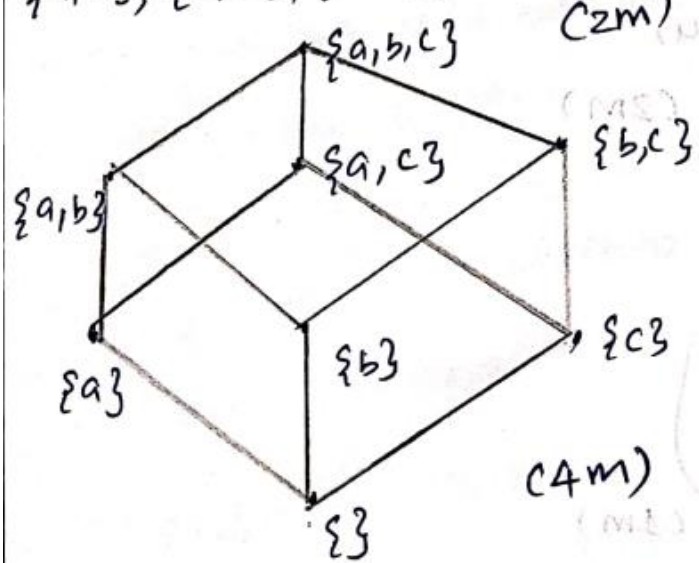
Part - A
(5 x 1 = 5 Marks)

Instructions: Answer all

Q. No	Answer with choice variable	Marks	BL	CO	PO	PI Code
1	a) $A \cup \phi = A$	1	1	1	2	1.2.1
2	a) Reflexive	1	1	1	2	1.2.1
3	c) $\begin{pmatrix} 1 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}$	1	2	1	2	1.2.1
4	d) 8	1	2	1	2	1.2.1
5	d) $\{\{1,2,3\}, \{4,5\}, \{6\}\}$	1	2	1	2	1.2.1

Part B
(2*4= 8 marks)

6		4	3	1	2	1.2.1
	$\begin{aligned} & \overline{A} \cup \overline{B} \cup (A \cap B \cap \overline{C}) \\ &= (\overline{A \cap B}) \cup ((A \cap B) \cap \overline{C}) \\ &\quad \text{by De Morgan's law} \\ &= ((\overline{A \cap B}) \cup (A \cap B)) \cap (\overline{A \cap B} \cup \overline{C}) \\ &\quad \text{by Distributive law} \\ &= U \cap (\overline{A \cap B} \cup \overline{C}) \\ &\quad \text{by Inverse law} \\ &= \overline{A \cap B} \cup \overline{C} \\ &\quad \text{by Identity law} \\ &= \overline{A} \cup \overline{B} \cup \overline{C} \\ &\quad \text{by De Morgan's law} \\ &\quad (4m) \end{aligned}$					
7		4	3	1	2	1.2.1
	<p>$(aa) \in R$ as a^2 is a perfect square $\therefore R$ is Reflexive (1m)</p> <p>When ab is a perfect square, ba is also a perfect square. $\therefore R$ is Symmetric (1m)</p> <p>Let $aRb \Rightarrow ab = x^2$ & $bRc \Rightarrow bc = y^2$ $\Rightarrow (ab)(bc) = x^2 y^2$ $\therefore ac = \left(\frac{xy}{b}\right)^2 = \text{a perfect square}$ $\therefore R$ is Transitive (1m)</p> <p>Since R is Reflexive, Symmetric and Transitive, R is an equivalence relation (1m)</p>					

	<p style="text-align: center;">Part - C (12 x 1 = 12 Marks)</p>					
8a	 <p>Both f and g are 1-1 and onto. so f^{-1} and g^{-1} exists. (1m)</p> <p>$f^{-1} = \{(2,1), (3,2), (1,3)\}$ (1m)</p> <p>$g^{-1} = \{(2,1), (1,2), (3,3)\}$ (1m)</p> <p>$f \circ g = \{(1,3), (2,2), (3,1)\}$ (1m)</p> <p>$(f \circ g)^{-1} = \{(3,1), (2,2), (1,3)\}$ (1m)</p> <p>$f^{-1} \circ g^{-1} = \{(1,1), (2,3), (3,2)\}$ (1m)</p> <p>Hence $(f \circ g)^{-1} \neq f^{-1} \circ g^{-1}$. (1m)</p>	6	4	1	2	1.2.1
8b	<p>$P(S) = \{ \{ \}, \{a\}, \{b\}, \{c\}, \{a,b\}, \{b,c\}, \{c,a\}, \{a,b,c\} \}$ (2m)</p>  <p>(4m)</p>	6	4	1	2	1.2.1

9	<p>$A = 4$. Compute till W_4 (2 marks)</p> <p>K P_i q_j (P_i, q_j) W_k</p> <p>1. 1,4 1,3 $(1,1)(1,3)$ $(4,1)(4,3)$ $\begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{pmatrix}$ (2m)</p> <p>2. 4 3 $(4,3)$ $\begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{pmatrix}$ (2m)</p> <p>3. 1,2,4 4 $(1,4)(2,4)$ $(4,4)$ $\begin{pmatrix} 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \\ 1 & 1 & 1 & 1 \end{pmatrix}$ (2m)</p> <p>4. 1,2,3,4 1,2,3,4 $(1,1)(1,2)$ $(1,3)(1,4)$ $(2,1)(2,2)(2,3)$ $(2,4)(3,1)(3,2)$ $(3,3)(3,4)(4,1)$ $(4,2)(4,3)(4,4)$ $\begin{pmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \end{pmatrix}$ (2m)</p> <p>Transitive closure</p> <p>$R^\infty = \{ (1,1)(1,2)(1,3)(1,4)(2,1)(2,2)$ $(2,3)(2,4)(3,1)(3,2)(3,3)(3,4)$ $(4,1)(4,2)(4,3)(4,4) \}$ (2m)</p>	12	4	1	2	1.2.1
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