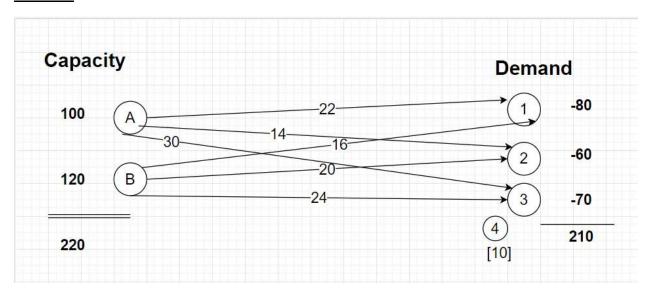
Assignment 4

Question 1:

Solution:



Decision Variable:

Let,

 X_{ij} = AED distribution from plant i to warehouse j i = Plants; i = A, B j = Warehouse; j = 1, 2, 3

Objective Function:

To minimize the transportation cost of AEDs.

Constraints:

i. Supply/Capacity Constraints:

$$X_{A1} + X_{A2} + X_{A3} + X_{AD} = 100;$$

 $X_{B1} + X_{B2} + X_{B3} + X_{BD} = 120;$

ii. Demand Constraints:

$$X_{A1} + X_{B1} = 80;$$

 $X_{A2} + X_{B2} = 60;$
 $X_{A3} + X_{B3} = 70;$

iii. Dummy Variable:

```
Production Capacity = 100 + 120 = 220
Demand = 80 + 60 + 70 = 210
```

Thus, create a dummy variable in demand section to equate the supply and demand. Dummy Variable D = 10;

```
X_{AD} + X_{BD} = 10;
```

Mathematical Formulation of Linear Programming Problem:

```
Let,
                        X<sub>ij</sub> = AED distribution from plant i to warehouse j
                       i = Plants; i = A, B
                       j = Warehouse; j = 1, 2, 3
                          Min = 22 X_{A1} + 14 X_{A2} + 30 X_{A3} + 16 X_{B1} + 20 X_{B2} + 24 X_{B3} + 600 X_{A1} + 600 X_{A2} + 600 X_{A3} + 625 X_{B1} + 625 X_{B1} + 625 X_{B2} + 600 X_{A3} + 600
                        X_{B2} + 625 X_{B3} + 0 X_{AD} + 0 X_{BD};
                          Subject To
                                                  X_{A1} + X_{A2} + X_{A3} + X_{AD} = 100;
                                                  X_{B1} + X_{B2} + X_{B3} + X_{BD} = 120;
                                                  X_{A1} + X_{B1} = 80;
                                                  X_{A2} + X_{B2} = 60;
                                                  X_{A3} + X_{B3} = 70;
                                                  X_{AD} + X_{BD} = 10;
                          And
                                                                            X_{ij} >= 0;
                                                                            i = A, B; j = 1, 2, 3;
```

Question 2:

Solution:

Decision Variable:

```
Let,

X_{ij} = Oil flow from well i to pump j in TBH.

X_{jk}= Oil flow from pump j to refineries k TBH.

i = Wells; i = 1, 2, 3

j = Pumps; j = 4, 5, 6

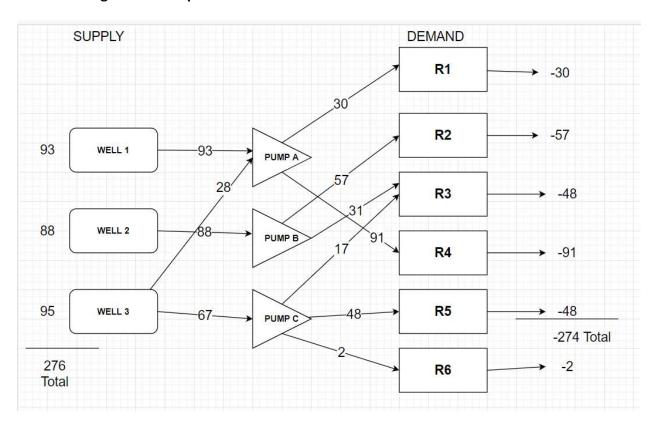
k = Refineries; k = 7, 8, 9
```

Objective Function:

To find the minimum providing cost of oil to the refineries.

 $\begin{aligned} &\text{Min}_z = 1.52 \ X_{14} + 1.60 \ X_{15} + 1.40 \ X_{16} + 1.70 \ X_{24} + 1.63 \ X_{25} + 1.55 \ X_{26} + 1.45 \ X_{34} + 1.57 \ X_{35} + 1.30 \ X_{36} \\ &+ 5.15 \ X_{47} + 5.69 \ X_{48} + 6.13 \ X_{49} + 5.63 \ X_{410} \ + 5.80 \ X_{411} + 5.12 \ X_{57} + 5.47 \ X_{58} + 6.05 \ X_{59} + 6.12 \ X_{510} + 5.71 \ X_{511} + 5.32 \ X_{67} + 6.16 \ X_{68} + 6.25 \ X_{69} + 6.17 \ X_{610} + 5.87 \ X_{611}; \end{aligned}$

Network Diagram for the problem:



Constraints:

i. Oil flow from wells to the pump

$$X_{14} + X_{15} + X_{16} = 93;$$

 $X_{24} + X_{25} + X_{26} = 88;$
 $X_{34} + X_{35} + X_{36} = 95;$

ii. Oil flow from pumps to the refineries

$$X_{47} + X_{57} + X_{67} = 30;$$

 $X_{48} + X_{58} + X_{68} = 57;$
 $X_{49} + X_{59} + X_{69} = 48;$
 $X_{410} + X_{510} + X_{610} = 91;$
 $X_{411} + X_{511} + X_{611} = 48;$
 $X_{412} + X_{512} + X_{612} = 2;$

iii. Dummy variable

Thus, create a dummy variable in demand section to equate the supply and demand.

Dummy Variable D = 2;

$$X_{412} + X_{512} + X_{612} = 2;$$

Equality constraint

$$X_{14} + X_{24} + X_{34} = X_{47} + X_{48} + X_{49} + X_{410} + X_{411} + X_{412};$$

 $X_{15} + X_{25} + X_{35} = X_{57} + X_{58} + X_{59} + X_{510} + X_{511} + X_{512};$
 $X_{16} + X_{26} + X_{36} = X_{67} + X_{68} + X_{69} + X_{610} + X_{611} + X_{612};$

Mathematical Formulation of Linear Programming Problem:

```
Let,
    X_{ij} = Oil flow from well i to pump j in TBH.
    X_{jk}= Oil flow from pump j to refineries k TBH.
    i = Wells; i = 1, 2, 3
    j = Pumps; j = 4, 5, 6
    k = Refineries; k = 7, 8, 9
```

 $Min_z = 1.52 X_{14} + 1.60 X_{15} + 1.40 X_{16} + 1.70 X_{24} + 1.63 X_{25} + 1.55 X_{26} + 1.45 X_{34} + 1.57 X_{35} + 1.30 X_{36}$ $+5.15\ X_{47}+5.69\ X_{48}+6.13\ X_{49}+5.63\ X_{410}\ +5.80\ X_{411}+5.12\ X_{57}+5.47\ X_{58}+6.05\ X_{59}+6.12\ X_{510}+1.00$ $5.71 X_{511} + 5.32 X_{67} + 6.16 X_{68} + 6.25 X_{69} + 6.17 X_{610} + 5.87 X_{611}$;

Subject To

bject To
$$X_{14} + X_{15} + X_{16} = 93;$$

$$X_{24} + X_{25} + X_{26} = 88;$$

$$X_{34} + X_{35} + X_{36} = 95;$$

$$X_{47} + X_{57} + X_{67} = 30;$$

$$X_{48} + X_{58} + X_{68} = 57;$$

$$X_{49} + X_{59} + X_{69} = 48;$$

$$X_{410} + X_{510} + X_{610} = 91;$$

$$X_{411} + X_{511} + X_{611} = 48;$$

$$X_{412} + X_{512} + X_{612} = 2;$$

$$X_{14} + X_{24} + X_{34} = X_{47} + X_{48} + X_{49} + X_{410} + X_{411} + X_{412};$$

$$X_{15} + X_{25} + X_{35} = X_{57} + X_{58} + X_{59} + X_{510} + X_{511} + X_{512};$$

$$X_{16} + X_{26} + X_{36} = X_{67} + X_{68} + X_{69} + X_{610} + X_{611} + X_{612};$$

And

$$X_{ij} >= 0;$$

$$X_{jk} \ge 0;$$

 $i = 1, 2, 3; j = 4, 5, 6; k = 7, 8, 9;$

Solution Network Diagram:

