Assignment 4

Question 1:

Heart Start produces automated external defibrillators (AEDs) in each of two different plants (A and B). The unit production costs and monthly production capacity of the two plants are indicated in the table below. The AEDs are sold through three wholesalers. The shipping cost from each plant to the warehouse of each wholesaler along with the monthly demand from each wholesaler are also indicated in the table. How many AEDs should be produced in each plant, and how should they be distributed to each of the three wholesaler warehouses so as to minimize the combined cost of production and shipping?

```
Unit Shipping Cost Unit Monthly
Warehouse 1 Warehouse 2 Warehouse 3 ProductionCost
ProductionCapacity
```

Plant A \$22 \$14 \$30 \$600 100

Plant B \$16 \$20 \$24 \$625 120

Monthly 80 60 70 Demand

library('lpSolveAPI')

To read the LP file.

```
HeartStart <- read.lp("HeartStart.lp");</pre>
HeartStart
## Model name:
##
                XA1
                       XA2
                              XA3
                                     XB1
                                            XB2
                                                   XB3
                                                          XAD
                                                                 XBD
## Minimize
                622
                       614
                              630
                                     641
                                            645
                                                   649
                                                            0
                                                                    0
## R1
                  1
                         1
                                1
                                       0
                                              0
                                                      0
                                                            1
                                                                    0
                                                                           100
## R2
                  0
                         0
                                0
                                       1
                                               1
                                                      1
                                                            0
                                                                    1
                                                                           120
## R3
                  1
                         0
                                0
                                       1
                                               0
                                                      0
                                                            0
                                                                    0
                                                                            80
                                                                       =
                  0
                                0
                                               1
                                                      0
                                                            0
## R4
                         1
                                       0
                                                                    0
                                                                            60
## R5
                  0
                         0
                                1
                                       0
                                               0
                                                      1
                                                            0
                                                                    0
                                                                            70
                                              0
                                                            1
## R6
                  0
                         0
                                0
                                       0
                                                      0
                                                                    1
                                                                            10
                Std
                       Std
                              Std
                                     Std
                                            Std
                                                   Std
                                                          Std
## Kind
                                                                 Std
## Type
               Real
                      Real
                             Real
                                    Real
                                           Real
                                                  Real
                                                         Real
                                                                Real
## Upper
                Inf
                       Inf
                              Inf
                                     Inf
                                            Inf
                                                   Inf
                                                          Inf
                                                                 Inf
## Lower
                                       0
                                              0
```

##To solve the LP.

```
solve(HeartStart)
```

##To compute the objective function value.

get.objective(HeartStart)

[1] 132790

##To compute the values of decision variables.

get.variables(HeartStart)

[1] 0 60 40 80 0 30 0 10

##To compute the values of constraints.

get.constraints(HeartStart)

[1] 100 120 80 60 70 10

##Question 2: Oil Distribution TexxonOil Distributors, Inc., has three active oil wells in a west Texas oil field. Well 1 has a capacity of 93 thousand barrels per day (TBD), Well 2 can produce 88 TBD, and Well 3 can produce 95 TBD. The company has five refineries along the Gulf Coast, all of which have been operating at stable demand levels. In addition, three pump stations have been built to move the oil along the pipelines from the wells to the refineries. Oil can flow from any one of the wells to any of the pump stations, and from any one of the pump stations to any of the refineries, and Texxon is looking for a minimum cost schedule. The refineries' requirements are as follows.

Refinery R1 R2 R3 R4 R5 Requirement (TBD) 30 57 48 91 48

The company's cost accounting system recognizes charges by the segment of pipeline that is used. These daily costs are given in the tables below, in dollars per thou-sand barrels.

| То | | Pump A | | Pump B | Pun | Pump C | |
|------|--------|--------|------|--------|------|--------|--|
| | Well 1 | 1.52 | | 1.60 | 1. | 1.40 | |
| From | Well 2 | 1.70 | | 1.63 | 1. | 1.55 | |
| | Well 3 | 1.45 | | 1.57 | 1. | 1.30 | |
| | ı | | | | | | |
| То | | R1 | R2 | R3 | R4 | R5 | |
| | Pump A | 5.15 | 5.69 | 6.13 | 5.63 | 5.80 | |
| From | Pump B | 5.12 | 5.47 | 6.05 | 6.12 | 5.71 | |
| | Pump C | 5.32 | 6.16 | 6.25 | 6.17 | 5.87 | |

1)What is the minimum cost of providing oil to the refineries? Which wells are used to capacity in the optimal schedule? Formulation of the problem is enough.

2)Showthenetworkdiagramcorresponding to the solution in (a). That is, labeleach of the arcs in the solution and verify that the flows are consistent with the given information.

##To read the LP file.

```
OilRefineries <- read.lp("OilRefineries.lp");

OilRefineries

## Model name:

## a linear program with 27 decision variables and 12 constraints

##To solve the LP.

solve(OilRefineries)

## [1] 0

##To compute the objective function value. ##Minimal Optimal solution

get.objective(OilRefineries)

## [1] 1966.68
```

##To compute the values of decision variables.

```
get.variables(OilRefineries)

## [1] 93 0 0 0 88 0 28 0 67 30 0 0 91 0 0 57 31 0 0 0 0 17 0 48 0  
## [26] 0 2
```

##To compute the values of constraints.

```
get.constraints(OilRefineries)
## [1] 93 88 95 30 57 48 91 48 2 0 0 0
```

##The Well 2 will obtain us the optimal solution for the transportation problem.

