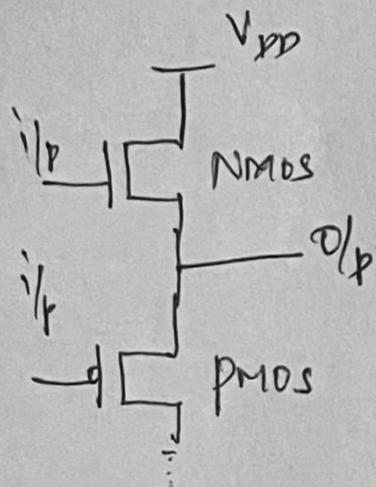


why NMOS is Preferred over PMOS?

Maj carriers - NMOS (\bar{e}), PMOS (h)

- Mobility $\approx 2.5 \mu p$
 - If mob more then Conductivity more
 - NMOS fast
 - " Small in size
 - As size is less the packing density is more
 - Speed
- Si $\rightarrow 1400 \text{ cm}^2/\text{v-sec}$
 μ_n
 $\mu_p \rightarrow 450 \text{ cm}^2/\text{v-sec}$
Con: $\mu_n \rightarrow 3900 \text{ cm}^2/\text{v-sec}$
 $\mu_p \rightarrow 1900 \text{ cm}^2/\text{v-sec}$
- } features



2nd term \rightarrow time varying drain current component that is linearly related to v_{gs} .

3rd term \rightarrow proportional to the square of signal voltage.

For sine i/p, This squared term produces undesirable harmonics, or non linear distortion in the o/p voltage.

To minimize the harmonics, we require

$$v_{gs} \ll 2(V_{gsQ} - V_{TN}) \rightarrow (4)$$

Eqn (4) represents the small signal condition that must be satisfied by all linear amplifiers.

Neglecting v_{gs}^2 term,

$$i_D = i_{DQ} + i_d$$

linearity \rightarrow total current can be separated into a dc & ac component. The ac component of drain current is given by

$$i_d = 2kn(V_{gsQ} - V_{TN}) v_{gs}$$

$$\frac{i_d}{v_{gs}} = g_m = 2kn(V_{gs} - V_{TN}) \rightarrow (5)$$

g_m - transconductance is a transfer coefficient summing output current to input voltage and can be thought of as the gain of the transistor

$$g_m = \frac{2I_D}{V_{gs}} / v_{gs} = V_{gsQ} = \text{constant} = 2kn(V_{gs} - V_{TN})$$

2nd term \rightarrow time varying drain current component that is linearly related to v_{gs} .

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$$v_{gs} \ll 2(V_{gsQ} - V_{TN}) \rightarrow (4)$$

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g_m = transconductance is a transfer coefficient relating output current to input voltage and can be thought of as the gain of the transistor

$$g_m = \frac{\partial I_D}{\partial v_{gs}} / v_{gs} = V_{gsQ} = \text{constant} = 2kn(V_{gsQ})$$

From (2) :- $i_D = kn(V_{GS} - V_{TN})$.

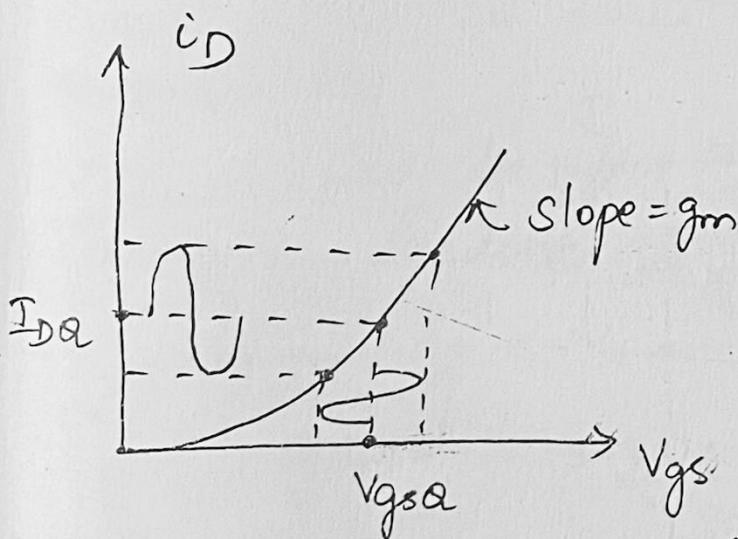
$$i_{DQ} = kn(V_{GSQ} - V_{TN})^2.$$

$$\therefore V_{GSQ} - V_{TN} = \sqrt{\frac{i_{DQ}}{kn}}.$$

Sub in (5)

$$g_m = 2kn \sqrt{\frac{i_{DQ}}{kn}} = 2\sqrt{kn} I_{DQ}.$$

$$\boxed{g_m = 2\sqrt{kn} I_{DQ}}.$$



If V_{GS} is small, g_m is constant. With a point in the saturation region, the transistor operates as current source that is linearly controlled by V_{GS} .

$\boxed{g_m \propto kn}$ (function of width to length ratio)

When the width of the transistor increases the gain increases.

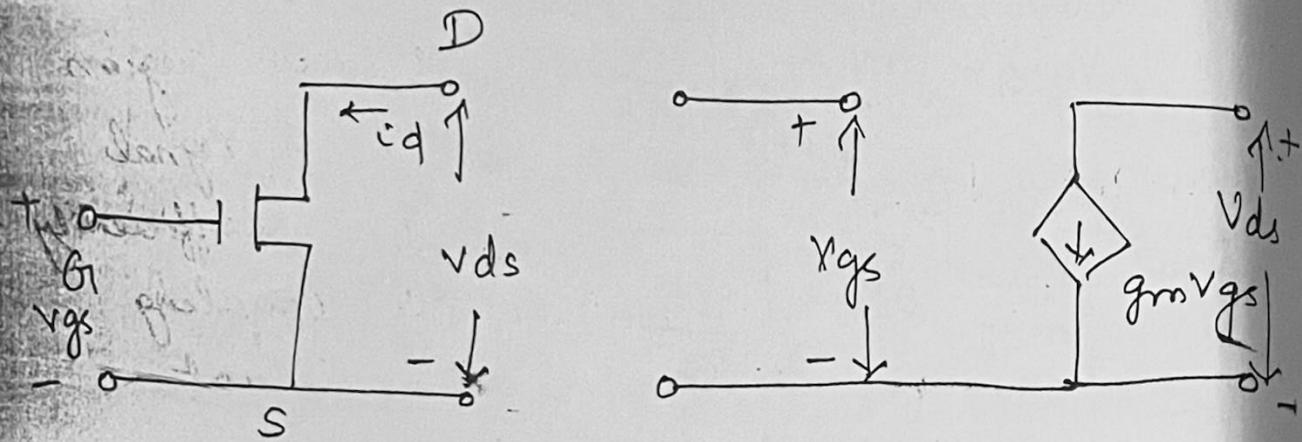
Small signal equivalent circuit :-

$$V_{DS} = V_{DD} - i_D R_D.$$

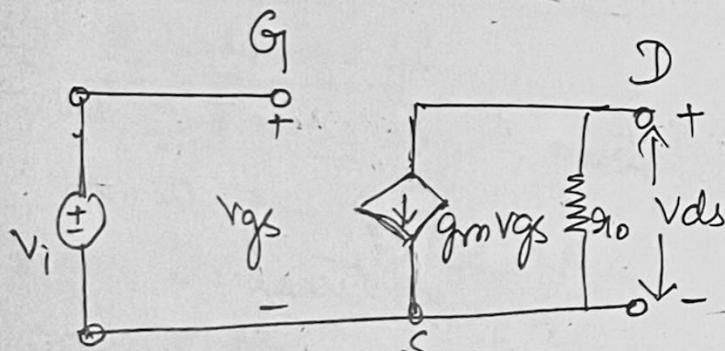
$$V_O = V_{DS} = -i_D R_D.$$

$$i_d = g_m v_{gs}$$

$$v_{gs} = v_c$$



Expanded Small signal equivalent circuit



N-channel MOSFET

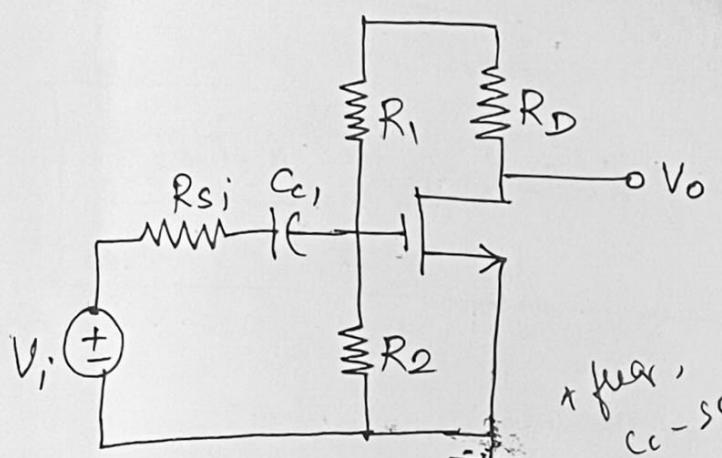
AC Analysis of Basic MOSFET Amplifier configuration using classical discrete circuit bias arrangement

MOSFET is a 3 terminal device. It has the

following configurations :

- Common Source
- Common Drain
- Common Gate

The Common Source Amplifier

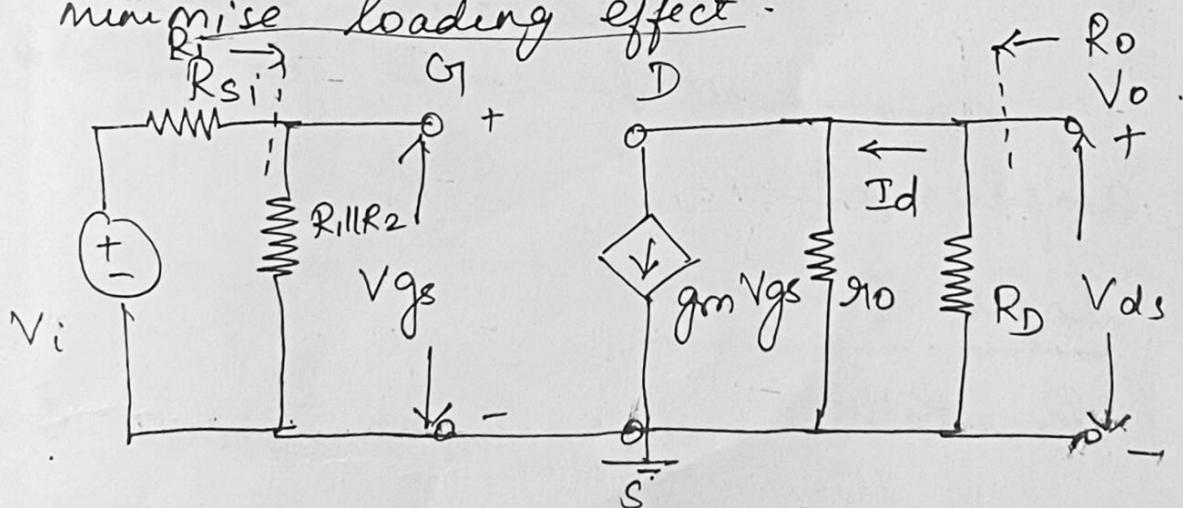


* Assume that the transistor is biased in saturation regions by $R_1 \parallel R_2$ & signal frequency is sufficiently large for coupling capacitor to act

essentially as a short circuit.

- * The signal source is represented by Thevenin's equivalent circuit, in which the signal voltage source V_i is in series with an equivalent resistor R_{si} .

R_{si} should be less than $R_i = R_1 \parallel R_2$ to minimise loading effect.



Voltage gain A_v

$$A_v = \frac{V_o}{V_i}$$

$$V_o = -g_m V_{gs} \times (R_D \parallel R_L)$$

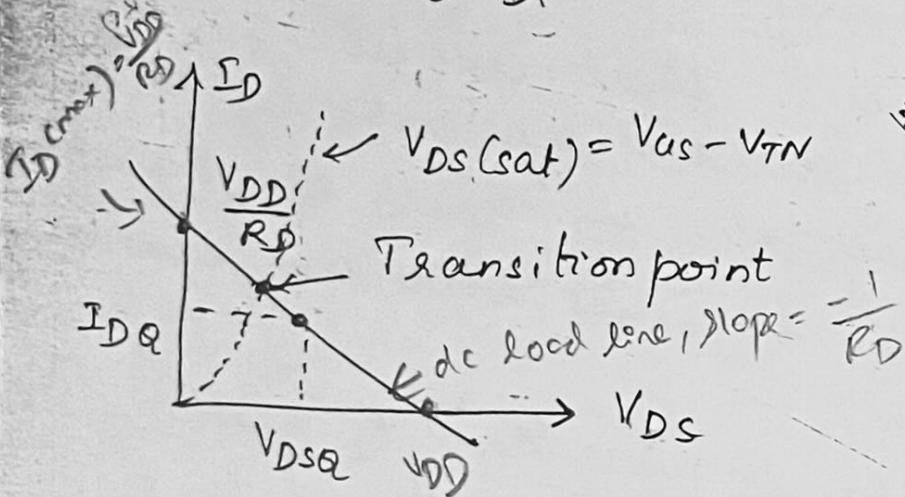
$$V_{gs} = \frac{V_i \times R_1 \parallel R_2}{R_{si} + R_1 \parallel R_2}$$

Sub in V_o

$$\therefore V_o = -g_m (\infty || R_D) \frac{V_i \times (R_1 || R_2)}{R_1 || R_2 + R_{S1}}$$

$$A_v = \frac{V_o}{V_i} = -g_m (\infty || R_D) \frac{(R_1 || R_2)}{R_1 || (R_2 + R_{S1})}$$

$$\Rightarrow V_{DS} = -I_d R_D$$



* transistor should be biased in saturation & Q-point must be near the middle of the saturation region.

* i/p signal must be small for linear amplification.

Input resistance

$$R_i = R_1 || R_2$$

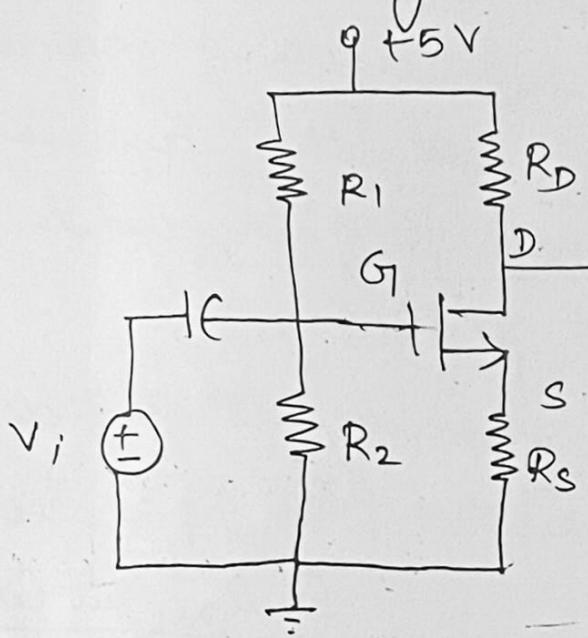
low frequency input resistance looking into the gate of MOSFET is ∞ .

Output Resistance :- is found by setting $V_{GS} = 0$

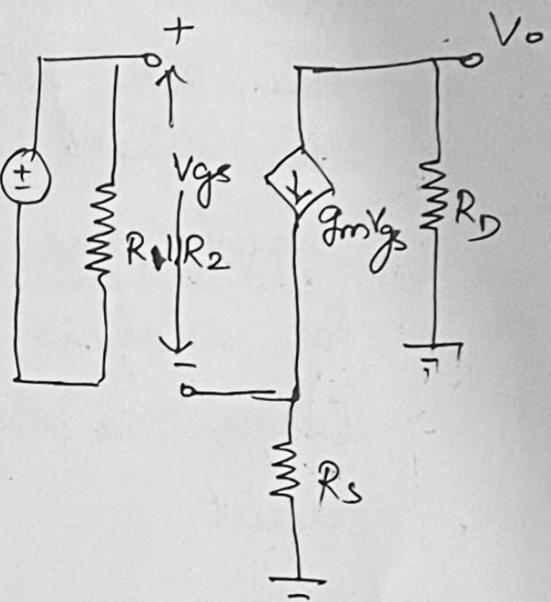
$$\therefore R_o = R_D || \infty$$

Common Source Amplifier with Source Resistor

R_s tends to stabilize the Q-point against variations in transistor parameters. But it reduces the gain.



Equivalent Circuit



Voltage Gain Av

$$A_v = \frac{V_o}{V_i}$$

$$A_v \approx \left(\frac{g_m R_D}{1 + g_m R_s} \right) = \infty$$

$$V_o = -g_m V_{gs} R_D$$

$$V_i = V_{gs} + g_m V_{gs} R_s$$

$$= V_{gs} (1 + g_m R_s)$$

$$V_{gs} = \frac{V_i}{1 + g_m R_s}$$

$$V_o = \frac{V_i}{1 + g_m R_s} (-g_m R_D)$$

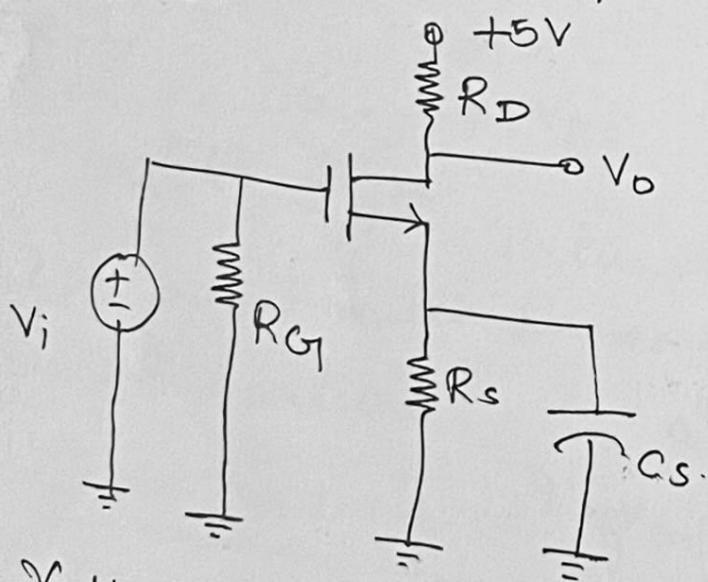
$$\therefore A_v = \frac{V_o}{V_i} = \frac{-g_m R_D}{1 + g_m R_s}$$

Common Source Circuit with Source

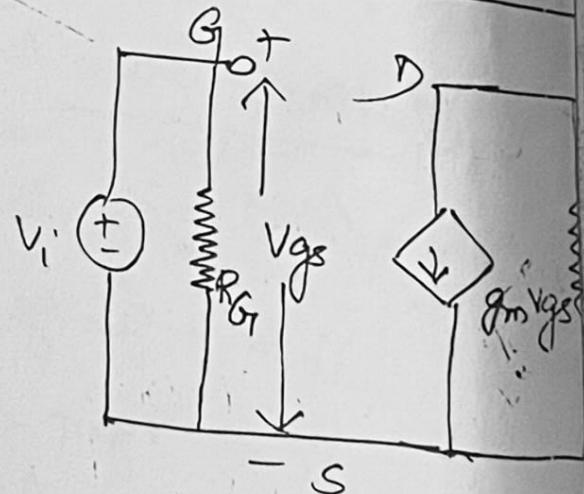
Bypass Capacitor

A source capacitor added to the common source circuit with a source resistor will minimise the loss in the small signal voltage gain, while maintaining Q-point stability.

For analysis, if the frequency is sufficient, the bypass capacitor acts as a short circuit.



Equivalent Circuit



Voltage Gain Av

$$Av = \frac{V_o}{V_i}$$

$$V_o = -g_m V_{gs} R_D$$

$$V_i = V_{gs}$$

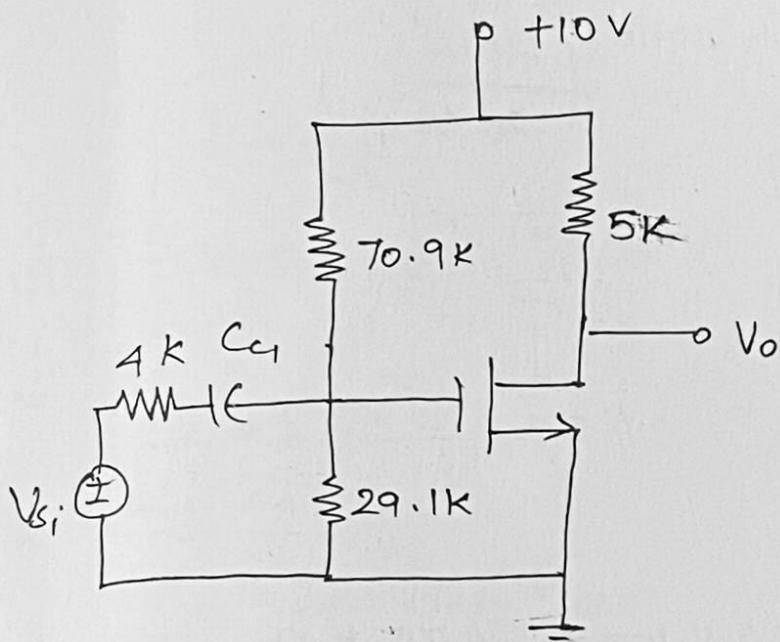
$$\therefore Av = \frac{V_o}{V_i} = -g_m R_D$$

$$Av = -g_m R_D$$

$$\lambda = 0$$

Examples :-

- ① Determine the small signal voltage gain and input & output resistances of CS amplifier.



$$V_{TN} = 1.5 \text{ V}$$

$$k_n = 0.5 \text{ mA/V}^2$$

$$\alpha = 0.01 \text{ V}^{-1}$$

Solution :-

$$A_v = -g_m (\alpha_0 || R_D) \frac{R_i}{R_i + R_{si}}$$

$$g_m = 2k_n (V_{ASQ} - V_{TN})$$

$$\alpha_0 = [d I_{DQ}]^{-1}$$

To find V_{ASQ} & I_{DQ}

$$V_{ASQ} = \left(\frac{R_2}{R_1 + R_2} \right) V_{DD} = \left(\frac{29.1}{70.9 + 29.1} \right) (10) = 2.91 \text{ V}$$

$$I_{DQ} = k_n (V_{ASQ} - V_{TN})^2 = (0.5)(2.91 - 1.5)^2 = 1 \text{ mA}$$

To find g_m & α_0 :

$$g_m = 2k_n (V_{ASQ} - V_{TN})$$

$$= 2(0.5)(2.91 - 1.5) = 1.41 \text{ mA/V}$$

$$\alpha_0 = [d I_{DQ}]^{-1} = [(0.01)(1)]^{-1} = 100 \text{ k}\Omega$$

To calculate A_v :

$$A_v = -g_m (\text{r}_o \parallel R_D) \left(\frac{R_i}{R_i + R_{si}} \right)$$

$$= (-1.41)(100 \parallel 15) \left(\frac{20.6}{20.6 + 4} \right)$$

$$A_v = -5.62$$

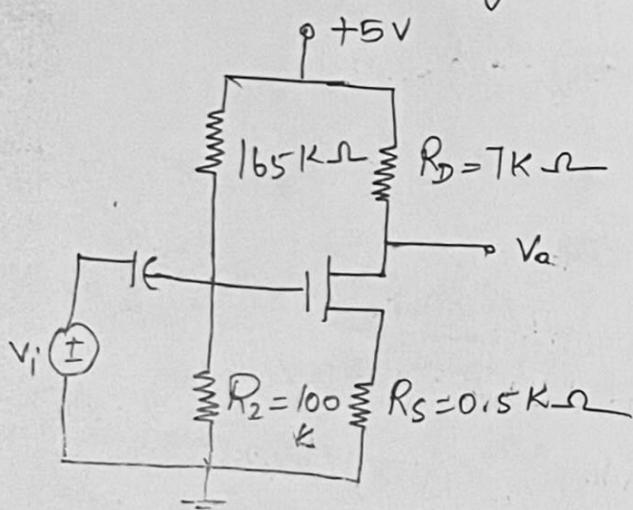
Input resistance

$$R_i = R_1 \parallel R_2 = 70.9 \parallel 29.1 = 20.6 \text{ k}\Omega$$

O/P resistance

$$R_o = R_D \parallel \text{r}_o = 5 \parallel 100 = 4.76 \text{ k}\Omega$$

② Determine a small signal voltage gain of circuit containing a source resistor. ①



$$V_{TN} = 0.8 \text{ V}$$

$$k_n = 1 \text{ mA/V}^2$$

$$\lambda = 0$$

$$V_{DSQ} = 1.5 \text{ V}$$

$$I_{DQ} = 0.5 \text{ mA}$$

$$V_{GSQ} = 6.25 \text{ V}$$

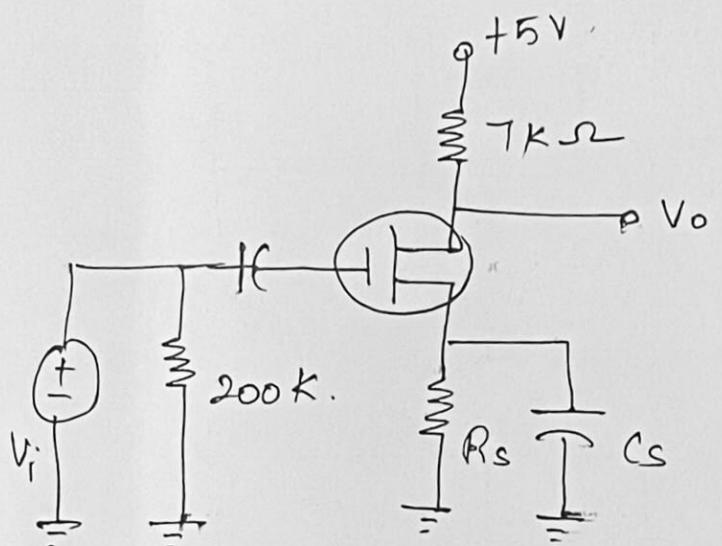
$$g_m = 2k_n (V_{GSQ} - V_{TN})^2 = 2(1)(1.5 - 0.8)^2 = 1.4 \text{ mA}$$

$$\text{r}_o = [2I_{DQ}]^{-1} \approx \infty$$

To find A_v :

$$A_v = \frac{-g_m R_D}{1 + g_m R_S} = \frac{-(1.4)(7)}{1 + (1.4)(0.5)} = -5.7$$

③ Determine the small signal voltage gain of CS circuit with source bypass capacitor.



$$V_{TN} = 0.8 \text{ V}$$

$$K_n = 1 \text{ mA/V}^2$$

$$\lambda = 0.$$

$$I_{DQ} = 0.5 \text{ mA}$$

Solution :-

$$I_{DQ} = I_Q = K_n (V_{GSQ} - V_{TN})^2$$

$$0.5 = (1)(V_{GSQ} - 0.8)^2 = 1.51 \text{ V}$$

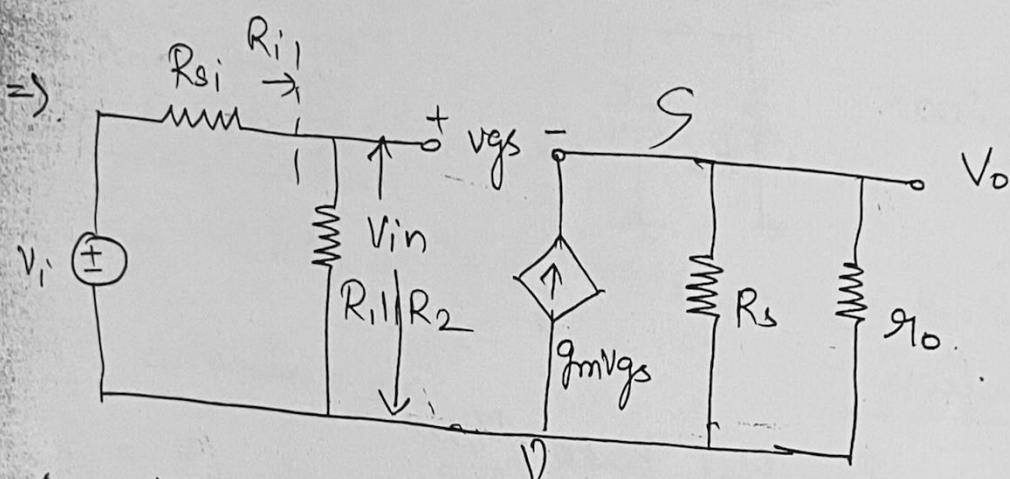
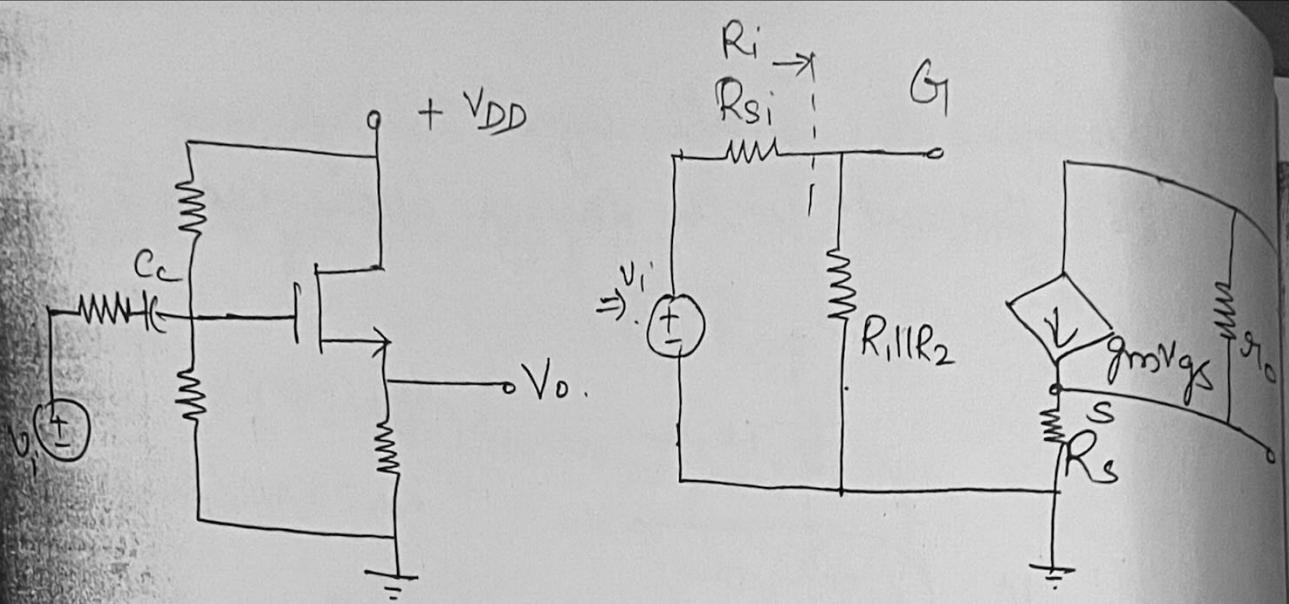
$$g_m = 2K_n (V_{GS} - V_{TN}) = 1.4.$$

To find A_v .

$$A_v = \frac{V_o}{V_i} = -g_m R_D = -(1.4)(7) = -9.8$$

Common Drain Circuit: The Source Follower

The output is taken off the source with respect to ground and the drain is connected to V_{DD} directly. Since V_{DD} becomes ground in ac analysis we have the name common drain. The more common name is source follower.



$$A_v = \frac{V_o}{V_i}$$

$$V_o = g_m V_{gs} (R_s || r_o)$$

$$V_{in} = \frac{V_i \times R_L || R_2}{R_{si} + R_L || R_2} \rightarrow ①$$

But

$$V_{in} = V_{gs} + (g_m V_{gs}) (R_s || r_o)$$

$$V_{gs} = \frac{V_{in}}{1 + g_m (R_s || r_o)}$$

$$V_o = \frac{g_m V_{in} (R_s || r_o)}{1 + g_m (R_s || r_o)} \rightarrow ②$$

Substitute ① in ②

$$V_o = \frac{g_m V_i (R_1 || R_2) (R_s || \infty)}{(R_s i + R_1 || R_2)(1 + g_m (R_s || \infty))}$$

$$\boxed{A_v = \frac{V_o}{V_i} = \frac{g_m (R_s || \infty)}{1 + g_m (R_s || \infty)} \cdot \frac{R_1 || R_2}{R_s i + R_1 || R_2}}$$

(or)

$$A_v = \frac{\frac{R_s || \infty}{g_m}}{1 + \frac{R_s || \infty}{g_m} R_s i + R_1 || R_2} \cdot \frac{R_1 || R_2}{R_s i + R_1 || R_2}$$

- * magnitude of voltage gain is always less than unity.
- * O/P resistance is less than that of common source circuit.

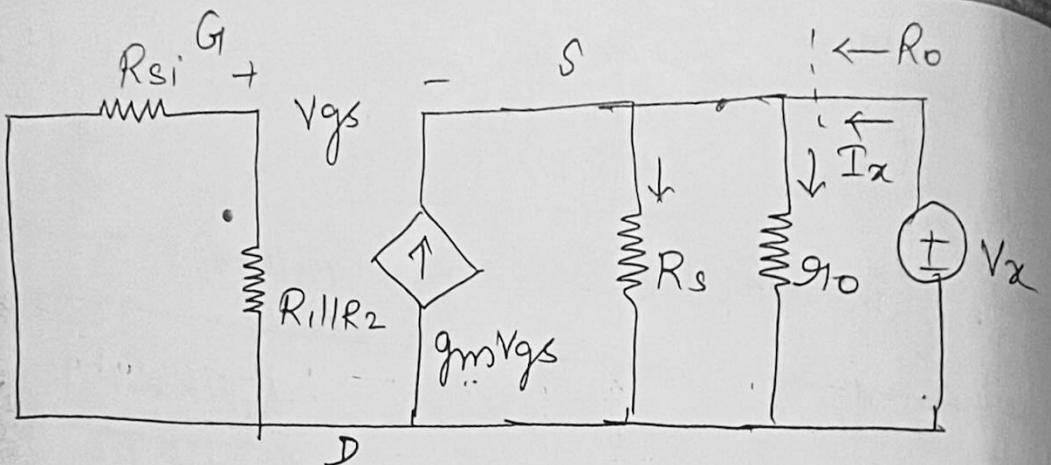
Input Impedance

$$R_i = R_1 || R_2$$

Output Impedance

A small O/P resistance is desirable when the circuit is to act as ideal voltage source & drive load circuit without suffering loading effects.

To find the O/P resistance let $V_i = 0$ & test voltage is applied to the O/P.



$$R_o = \frac{V_x}{I_x} \quad V_x + V_{gs} = 0 \quad \therefore V_x = -V_{gs} \text{ or} \\ V_{gs} = -V_x.$$

Apply KCL at the output terminal.

$$I_x + g_m V_{gs} = \frac{V_x}{r_o} + \frac{V_x}{R_s}$$

Sub $V_{gs} = -V_x$ in the above equation

$$I_x = \frac{V_x}{r_o} + \frac{V_x}{R_s} + g_m V_x$$

$$I_x = V_x \left[\frac{1}{r_o} + \frac{1}{R_s} + g_m \right]$$

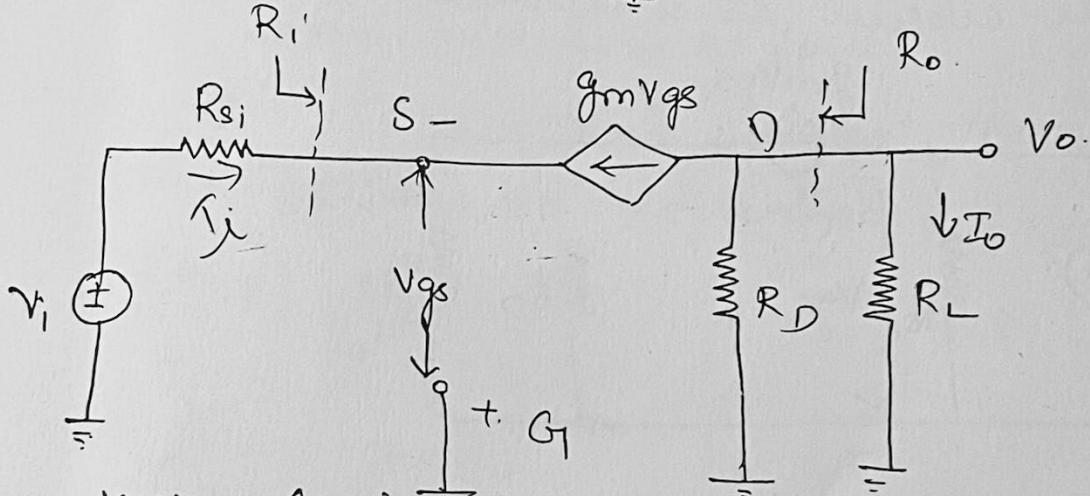
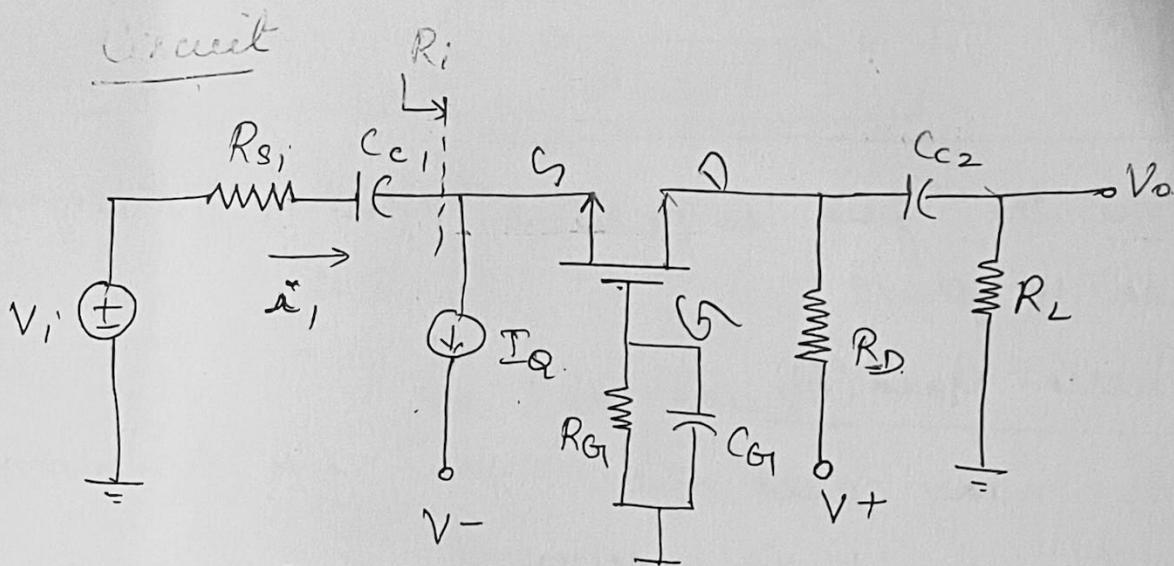
$$V_x = I_x \left(r_o || R_s || \frac{1}{g_m} \right)$$

$$R_o = \frac{V_x}{I_x} = (r_o || R_s || \frac{1}{g_m})$$

Common Gate Configuration $\Delta V_{CEQ} = V_{CEQ} - 0$

- * The input is applied to the source terminal and gate is at signal ground.
- * Biasing current I_Q .

Circuit Diagram



Voltage Gain:

$$A_v = \frac{V_o}{V_i} \quad V_o = -g_m V_{gs} (R_D || R_L)$$

$$V_i' = I_i' R_{S_i} - V_{gs}$$

$$I_i' = -g_m V_{gs}$$

$$V_i' = -g_m V_{gs} R_{S_i} - V_{gs}$$

$$V_i = -V_{gs} [1 + g_m R_{S_i}]$$

$$V_{gs} = \frac{-V_i'}{1 + g_m R_{S_i}}$$

$$\text{Sub in } V_o: \quad \frac{V_o}{1 + g_m R_{S_i}}$$

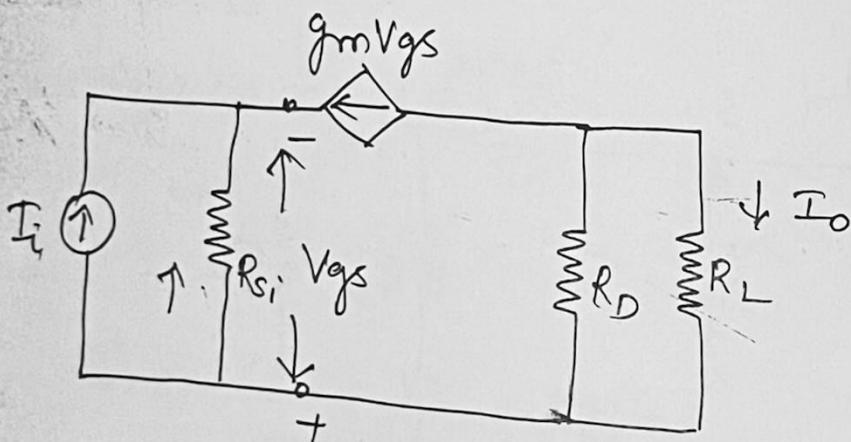
$$V_o = \frac{-g_m V_i (R_D || R_L)}{1 + g_m R_{S_i}}$$

$$A_V = \frac{V_O}{V_I} = \frac{g_m(R_D || R_L)}{1 + g_m R_{S_i}}$$

Since the gain is positive input & output signals are in phase.

Current Gain (A_i)

In many cases the signal i/p to comm. gate circuit is a current.



$$A_i = \frac{I_o}{I_i} \quad I_o = -g_m V_{GS} \times \frac{R_D}{R_L + R_D} \quad \text{---(1)}$$

Apply KCL to the i/p:

$$I_i + \frac{V_{GS}}{R_{S_i}} + g_m V_{GS} = 0$$

$$V_{GS} \left(\frac{1}{R_{S_i}} + g_m \right) = -I_i$$

$$V_{GS} \left(\frac{1 + g_m R_{S_i}}{R_{S_i}} \right) = -I_i \Rightarrow V_{GS} = -\frac{I_i \times R_{S_i}}{1 + g_m R_{S_i}}$$

$$I_o = \frac{g_m R_D}{R_D + R_L} \frac{R_{S_i}}{1 + g_m R_{S_i}} I_i$$

Sub in

$$A_i = \frac{I_o}{I_i} = \frac{g_m R_D R_{si}}{(R_D + R_L)(1 + g_m R_{si})}$$

when $R_D \gg R_L$ &

$$g_m R_{si} \gg 1$$

$$A_i \approx 1 \text{ for CG circuit.}$$

Input Impedance

- * The input resistance is low.
- * If the i/p signal is current, then low i/p resistance has an advantage.

$$R_i = -\frac{V_{gs}}{I_i}$$

$$I_i = -g_m V_{gs}$$

$$\therefore R_i = \frac{-V_{gs}}{-g_m V_{gs}} = \frac{1}{g_m}$$

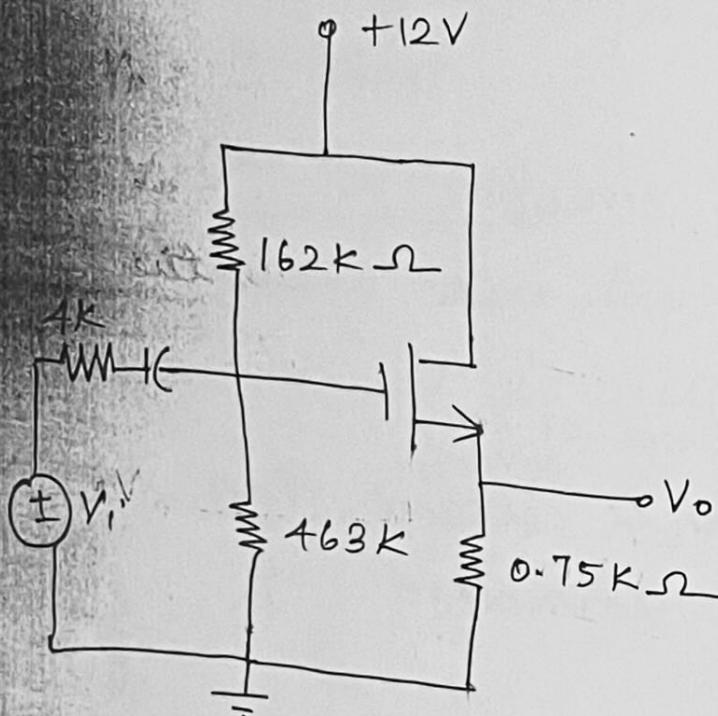
$$R_i = \frac{1}{g_m}$$

Output Resistance

$$R_o = R_D$$

Source Follower Amplifier

1) Calculate the small signal voltage gain, input & O/P resistance of the source follower circuit



$$\begin{aligned}V_{TN} &= 1.5V \\ k_n &= 4 \text{ mA/V}^2 \\ d &= 0.61V^{-1}\end{aligned}$$

Solution :-

$$I_{DQ} = 7.97 \text{ mA}$$

$$V_{ASA} = 2.91V$$

$$g_m = 2k_n(V_{ASA} - V_{TN}) = 2(4)(2.91 - 1.5) = 11.3 \text{ mS}$$

$$r_o \approx [d I_{DQ}]^{-1} = [0.01(7.97)]^{-1} = 12.5 \text{ k}\Omega$$

$$R_i = R_1 // R_2 = 162 // 463 = 120 \text{ k}\Omega$$

Voltage gain Av

$$Av = \frac{g_m(R_s // r_o)}{1 + g_m(R_s // r_o)} \frac{R_i}{R_i + R_s}$$

$$= \frac{(11.3)(0.75 // 12.5)}{1 + (11.3)(0.75 // 12.5)}$$

$$R_i = R_1 // R_2 = 120 \text{ k}\Omega \quad \frac{120}{120 + 4} = 0.86$$

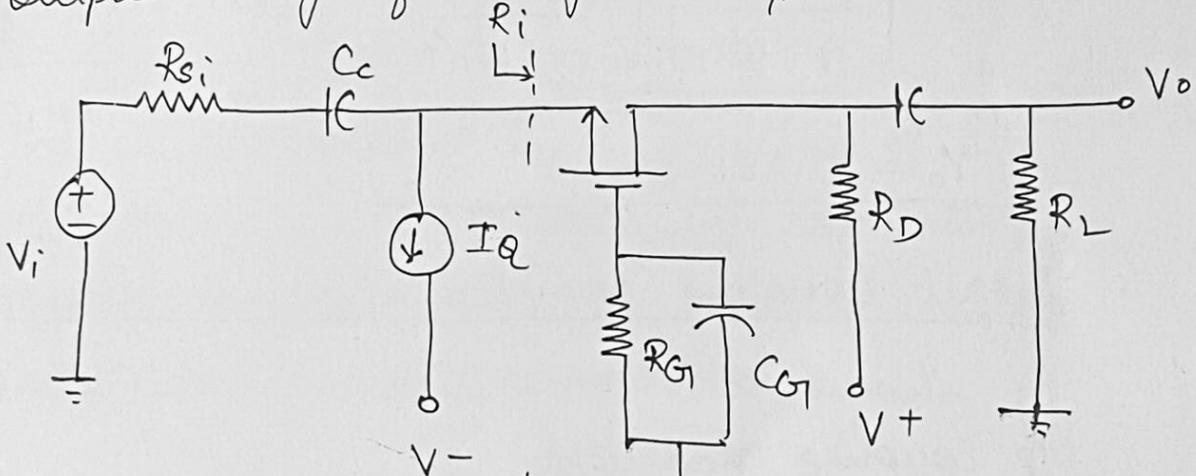
$$R_o = \frac{1}{g_m} / |R_s| / r_0 = \frac{1}{11.3} / |0.75| / 12.5$$

$$R_o = 0.0787 \text{ k}\Omega = 78.7 \text{ k}\Omega$$

Since R_o is less, source follower acts like a voltage source.

Common Gate Amplifier

- ① For the common gate circuit, determine the output voltage for a given i/p current.



The circuit parameters are:

$$I_Q = 1 \text{ mA}, V+ = +5 \text{ V}, V- = -5 \text{ V}, R_G = 100 \text{ k}\Omega, R_D = 4 \text{ k}\Omega$$

$$R_L = 10 \text{ k}\Omega, \text{ The transistor parameters are } V_{TN} = 1 \text{ V}$$

$k_n = 1 \text{ mA/V}^2$, and $d = 0$. Assume the i/p current is $100 \sin \omega t \mu\text{A}$ & $R_{si} = 50 \text{ k}\Omega$.

Solution:

$$I_Q = I_{DQ} = k_n (V_{GSQ} - V_{TN})^2$$

$$I = I (V_{GSQ} - 1)^2$$

$$V_{GSQ} = 2 \text{ V}$$

$$g_m = 2kn(V_{GSQ} - V_{TN}) = 2(1)(2-1) = 2 \text{ mA/V}$$

From A_i, we can write —

$$I_0 = I_i \left(\frac{R_D}{R_D + R_L} \right) \left(\frac{g_m R_{Si}}{1 + g_m R_{Si}} \right)$$

$$V_o = I_0 R_L$$

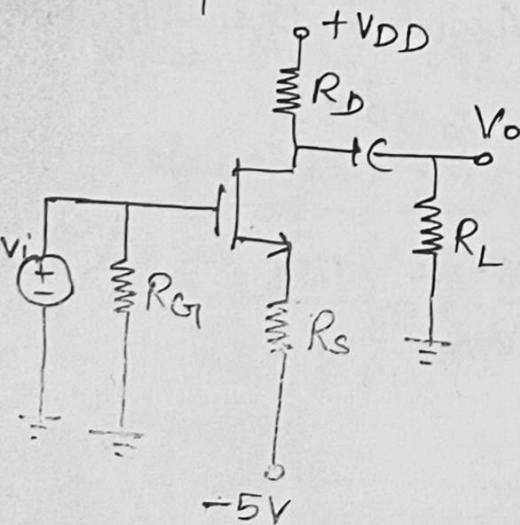
$$\begin{aligned} V_o &= I_i \left(\frac{R_D}{R_D + R_L} \right) \left(\frac{g_m R_{Si}}{1 + g_m R_{Si}} \right) \times R_L \\ &= \left[\frac{(10)(4)}{4+10} \right] \left[\frac{(2)(50)}{1+(2)(50)} \right] (0.1) \sin \omega t. \end{aligned}$$

$$V_o = 0.283 \sin \omega t \quad V$$

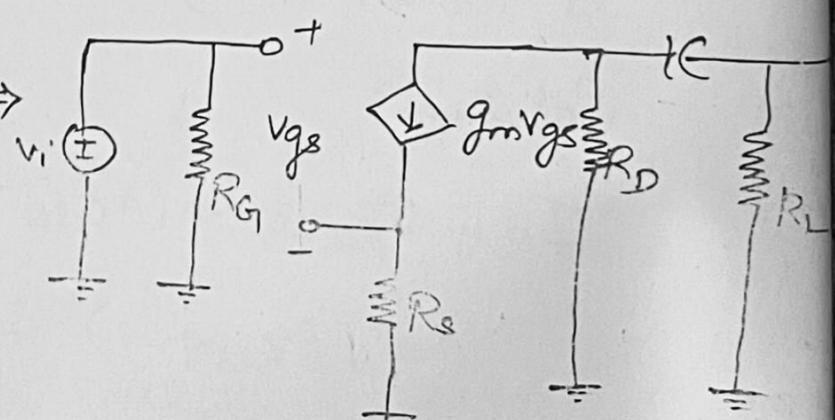
Output Coupling Capacitor : Common Source CK

Fig shows a common source MOSFET with O/P coupling capacitor.

- * $R_{Si} \ll R_{Gf} \therefore R_{Si}$ is neglected.
- * O/P is connected to the load through a coupling capacitor.



r_o is assumed to be ∞



The maximum O/P voltage assuming Cc is a short circuit is,

$$|V_o|_{\max} = g_m V_{gs} (R_D \parallel R_L)$$

$$V_i = V_{gs} + g_m V_{gs} R_s$$

$$V_i = V_{gs}(1 + g_m R_s) \Rightarrow V_{gs} = \frac{V_i}{1 + g_m R_s}$$

$$V_o = g_m \frac{V_i}{1 + g_m R_s} (R_D \parallel R_L)$$

$$\boxed{\frac{V_o}{V_i} = A_{v\max} = \frac{g_m (R_D \parallel R_L)}{1 + g_m R_s}}$$

The time constant is a function of the effective resistance seen by capacitor C_C , which is determined by setting independent sources equal to zero.

$$V_i = 0, g_m V_{gs} = 0 \text{ then}$$

$$\tau_s = C_C (R_D + R_L)$$

$$\boxed{f_L = \frac{1}{2\pi\tau_s}}$$

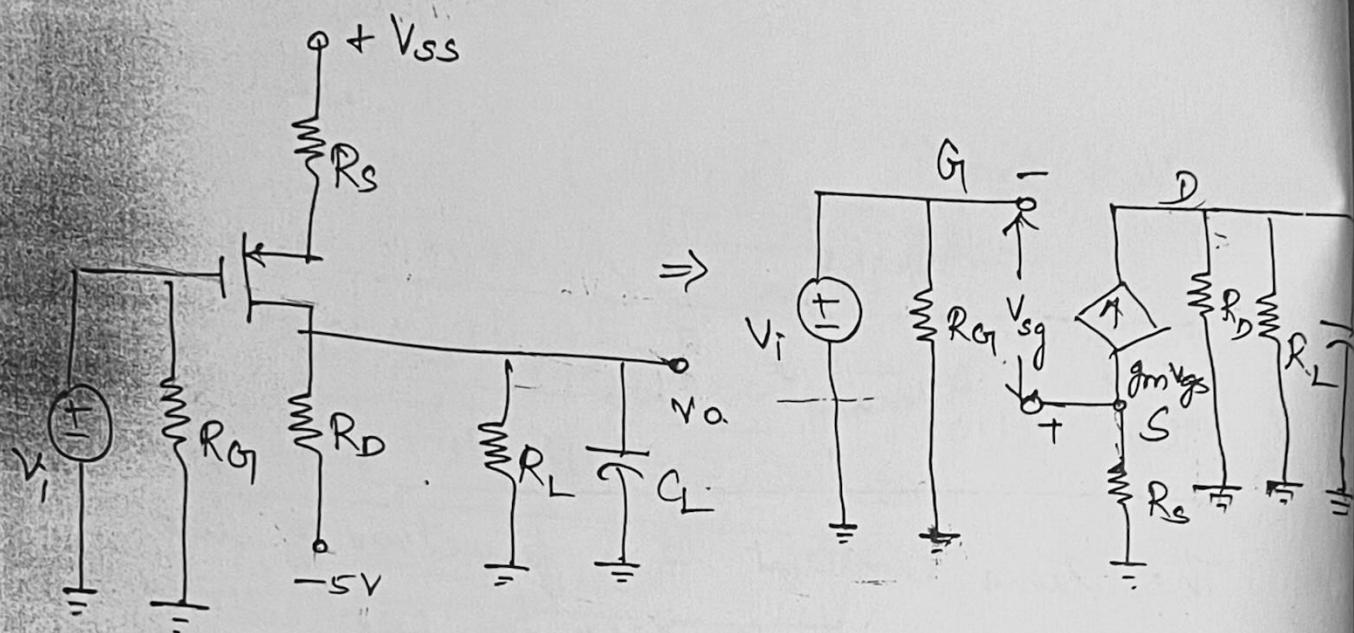
Load capacitor Effects:-

* Fig shows a MOSFET Common Source Amplifier with a load resistor R_L & a load capacitor C_L connected to the O/P.

* For the ac equivalent circuit V_o is assumed to be as.

* The circuit is like a low pass filter.

- * At high frequencies C_L decreases & acts as a shunt between OP & ground, & the output voltage is zero.



- * The equivalent resistance seen by load capacitor C_L is $(R_D || R_L)$.
 - * Since we set $V_i = 0$ then $gmV_{gs} = 0$ which means that the dependant current source does not affect the equivalent resistance
- Time constant

$$\tau_p = (R_D || R_L) C_L$$

The maximum gain asymptotic with C_L is open circuit, i.e.

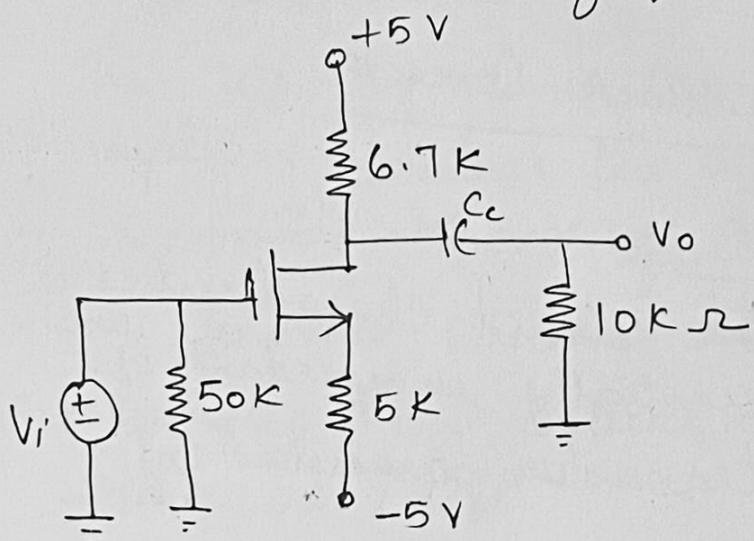
$$(A_v)_{\max} = \frac{gm(R_D || R_L)}{1 + gmR_s}$$

(Note : derivation done already. Refer.)

Same
but

Example:

- ① The circuit shown below is to be used as a simple audio amplifier. Design the circuit such that the lower corner frequency $f_L = 20\text{Hz}$.



Solution:

$$f_L = \frac{1}{2\pi\tau_s} \Rightarrow \tau_s = \frac{1}{2\pi f} = \frac{1}{2\pi(20)} = 7.96\text{ms}$$

$$C_c = \frac{\tau_s}{R_D + R_L} = \frac{7.96 \times 10^{-3}}{6.7 \times 10^3 + 10 \times 10^3} = 4.77 \times 10^{-7}\text{F}$$

$$\boxed{C_c = 0.477\mu\text{F}}$$

- ② Determine the corner frequency & max. gain asymptote of a MOSFET amplifier