**Example 12.1** Consider the design of a typical digital fiber-optic link which has to transmit at a data rate of 20 Mbits/s with a BER of 10<sup>-9</sup> using the NRZ code. The transmitter uses a GaAlAs LED emitting at 850 nm, which can couple on an average 100 μw (–10 dBm) of optical power into a fiber of core size 50 μm. The fiber cable consists of a graded-index fiber with the manufacture's specification as follows:  $\alpha_f = 2.5 \text{ dB/km}, (\Delta T)_{\text{mat}} = 3 \text{ ns/km}, (\Delta T)_{\text{modal}} = 1 \text{ ns/km}. \text{ A silicon } p\text{-}i\text{-}n \text{ photodiode}$ has been chosen, for detecting 850-nm optical signals, for the front end of the receiver. The detector has a sensitivity of -42 dBm in order to give the desired BER. The source along with its drive circuit has a rise time of 12 ns and the receiver has a rise time of 11 ns. The cable requires splicing every 1 km, with a loss of 0.5 dB/splice. Two connectors, one at the transmitter end and the other at the receiver end, are also required. The loss at each connector is 1 dB. It is predicted that a safety margin of 6 dB will be required. Estimate the maximum possible link length without repeaters and the total rise time of the system for assessing the feasibility of the desired system.

## Solution

Using Eq. (12.2), the total channel loss  $C_L$  may be calculated as follows:

$$C_L = \alpha_f L$$
 + (splice loss per km) ×  $L$  + (loss per connector) × no. of connectors  
= (2.5 dB/km) ×  $L$  (km) + (0.5 dB/splice) × (1 splice/km) ×  $L$  (km) + (1 dB) × 2  
= (3 $L$  + 2) dB

Here,  $P_{tx} = -10$  dBm,  $P_{rx} = -42$  dBm, and  $M_S = 6$  dB. Substituting the values of  $P_{tx}$ ,  $P_{rx}$ ,  $C_L$ , and  $M_S$  in Eq. (12.1), we get

$$-10 = -42 + (3L + 2) + 6$$
$$L = 8 \text{ km}$$

or

Therefore,

Therefore, a maximum transmission path of 8 km is possible without repeaters.

Let us now calculate the total rise time  $t_{\rm sys}$  using Eqs (12.8) and (12.9). It is given that  $t_{tx} = 12$  ns,  $t_{rx} = 11$  ns. In the case of multimode fibers, intramodal dispersion, is primarily due to material dispersion, and hence  $t_{\rm intramodal} \approx t_{\rm mat}$ .

$$t_{\text{mat}} = (3 \text{ ns/km}) \times L = (3 \text{ ns/km}) \times (8 \text{ km}) = 24 \text{ ns}$$
  
 $t_{\text{intermodal}} = (1 \text{ ns/km}) \times L = (1 \text{ ns/km}) \times (8 \text{ km}) = 8 \text{ ns}$   
 $t_{\text{sys}} = [(12)^2 + (24)^2 + (8)^2 + (11)^2]^{1/2} = 30 \text{ ns}$ 

The maximum allowable rise time  $t_{\rm sys}$  for our 20-Mbits/s NRZ data stream [from Eq. (12.11)], is

$$t_{\text{sys}} \le \frac{0.70}{B} = \frac{0.70}{20 \times 10^6} \text{s} = 35 \,\text{ns}$$

Since  $t_{sys}$  (= 30 ns) for the proposed link is less than the maximum allowable limit, the choice of components is adequate to meet the system design criteria.

**Example 12.2** A type-I intensity-modulated analog fiber-optic link employs a laser transmitter which couples a mean optical power of 0 dBm into a multimode optical fiber cable. The cable exhibits an attenuation of 3.0 dB/km with splice losses estimated at 0.5 dB/km. A connector at the receiver end shows a loss of another 1.5 dB. The *p-i-n* photodiode receiver has a sensitivity of -25 dBm for a CNR of -50 dB with a modulation index of 0.5. A safety margin of 7 dB is required. The rise times of the ILD and p-i-n diode are 1 ns and 5 ns, respectively, and the intermodal and intramodal rise times of the fiber cable are 9 ns/km and 2 ns/km, respectively. (a) What is the maximum possible link length without repeaters? (b) What is the maximum permitted 3-dB bandwidth of the system?

## Solution

## (a) Link power budget

The mean optical power coupled into the fiber cable by the laser transmitter  $(P_{tx}) = 0$  dBm, the mean optical power required at the *p-i-n* receiver  $(P_{rx}) = -25$  dBm, and the total system margin  $(P_{tx} - P_{rx}) = 25$  dB.

Assume that the repeaterless link length is L. Then, using Eq. (12.2), the total channel loss  $C_L$  may be calculated as follows:

$$C_L$$
 = (attenuation/km) ×  $L$  + (splice loss/km) ×  $L$  + connector loss  
= (3 dB/km) ×  $L$  + (0.5 dB/km) ×  $L$  + 1.5 dB  
= (3.5 $L$  + 1.5) dB

Therefore, from Eq. (12.1), we have

$$P_{tx} - P_{rx} = C_L + M_S$$

$$\Rightarrow 25 \text{ dB} = [(3.5L + 1.5) + 7] \text{ dB}$$
Thus
$$L = \frac{16.5}{3.5} \approx 4.7 \text{ km}$$

(b) Rise-time budget

$$t_f^2 = [(9 \text{ ns/km} \times 4.7 \text{ km})^2 + (2 \text{ ns/km} \times 4.7 \text{ km})^2] = 1877.65 \text{ ns}^2$$
  
 $t_{\text{sys}} = (t_{tx}^2 + t_f^2 + t_{rx}^2)^{1/2}$   
 $= [(1 \text{ ns})^2 + 1877.65 \text{ ns}^2 + (5 \text{ ns})^2]^{1/2}$   
 $= 43.63 \text{ ns}$ 

Therefore, the system bandwidth

$$\Delta f = \frac{0.35}{t_{\text{sys}}} = \frac{0.35}{43.6 \times 10^{-9}} \text{ Hz}$$
  
=  $8 \times 10^6 \text{ Hz} = 8 \text{ MHz}$ 

Thus the proposed link length without repeaters is 4.7 km with a 3-dB bandwidth of 8 MHz.