

# Assignment - I

$$S/I = \frac{(D/R)^n}{i_0} = \frac{2}{1}$$

en data:

$$\frac{S}{I} = 15 \text{ dB (minimum required)}$$

$$S/I = 12.04 \text{ dB}$$

Path loss exponent (a)  $n=4$ , (b)  $n=3$

$$n_0 \cdot \text{co-channels } i_0 = 6$$

Soln:-

$$\text{Frequency reuse factor } Q = \frac{D}{R} = \sqrt{3N}$$

(a) Considering 7 cell reuse pattern,  $n=4$ ,  $N=7$

$$N=7$$

$$Q = \sqrt{3 \times 7} = \sqrt{21} = 4.5826 \approx 4.58$$

$$\frac{S}{I} = \frac{(D/R)^n}{i_0} = \frac{(4.5826)^4}{6} = \frac{440.01}{6} = 73.33$$

$$\frac{S}{I} = 18.65 \text{ dB}$$

As the  $S/I$  is greater than the minimum requirement,

$N=7$  can be used.

(b)  $n=3$ ,  $N=7$  (7 cell reuse pattern)

$$\frac{S}{I} = \frac{(D/R)^n}{i_0} = \frac{(4.58)^3}{6} = \frac{96.07}{6} = 16.01$$

$$\frac{S}{I} = 12.04 \text{ dB}$$

As the  $S/I$  is less than the minimum requirement, have to

use  $N=12$ .

By checking  $i=2, j=2$  next possible value of  $N = i^2 + j^2 + ij = 12$ ;

$N=12$  (12 cell reuse pattern)

For  $N=12$

$$Q = \frac{D}{R} = \sqrt{3N} = \sqrt{36} = 6$$

$$\frac{S}{I} = \frac{(D/R)^n}{i_0} = \frac{(6)^3}{1} = 36$$

$$\frac{S}{I} = 15.56 \text{ dB}$$

As  $S/I$  is greater than the minimum requirement,

$N=12$  can be used.

2) system

	A	B	C
No. of cells	394	98	49
channels/cell	19	54	100

Blocking probability = 5% = 0.05

Request rate  $\lambda = 2$  hour

holding time  $H = 3 \text{ mins} = (3/60) \text{ hours}$

System A

no. of channels/cell (C) = 19

traffic intensity per user =  $A_u = \lambda H = 2 \times (3/60) = 0.1 \text{ Erlangs}$

For  $GOS = 0.05$ ,  $C=19$ . From Erlang B chart/table

total traffic  $A = 14.32 \approx 14 \text{ Erlangs}$

$\therefore$  The number of users can be supported per cell is

$$U = A/A_u = 14/0.1 = 140 \text{ users.}$$

$\therefore$  For total 394 cells, total no. of subscribers that

be supported by system A is  $140 \times 394 = 55,160$



### system B

$$\text{No. of channels/cell } (C) = 57$$

$$\text{Traffic intensity per user} = A_u = \lambda H = 2 \times 3/60$$

$$A_u = 0.1 \text{ Erlangs}$$

For  $GOS = 0.05$ ,  $C = 57$ . From Erlang B chart/table

$$\text{total traffic } A = 51.55 \approx 51 \text{ Erlangs}$$

$$\therefore \text{no. of users that can be supported per cell } U = A/A_u = 51/0.1 = 510$$

$\therefore$  As there are 98 cells, the total no. of subscribers that can be supported by system B is,  $510 \times 98 = 49,980$

### System c

$$\text{no. of channels/cell } (C) = 100$$

$$\text{traffic intensity per user} = A_u = \lambda H = 2 \times (3/60)$$
$$A_u = 0.1 \text{ Erlangs}$$

For  $GOS = 0.05$ ,  $C = 100$ , from Erlang B chart/table,

$$\text{total traffic } A = 95.24 \approx 95$$

$\therefore$  the no. of users that can be supported per cell

$$U = A/A_u = 95/0.1 = 950$$

$\therefore$  As there are 49 cells, the total no. of subscribers that can be supported by system c is,  $950 \times 49 = 46,550$

3) Given data:

Total city coverage = 1300 sq. miles

cell radius  $R = 4$  miles

allocated spectrum = 40 MHz = 40,000 kHz

each channel bandwidth = 60 kHz

Frequency reuse factor = 7

Erlang B sys  $\rightarrow GOS = 2\% = 0.02$

traffic per user = 0.03 Erlangs

Soln

(a) no. of cells in the service area.

cell radius  $R = 4$  miles

cell coverage area =  $2.598 \times R^2 = 2.598 \times 4^2$

= 41.57 sq. miles

total no. of cells ( $N_c$ ) =  $\frac{\text{total city coverage}}{\text{one cell coverage}}$

$N_c = \frac{1300}{41.57}$

= 31.27  $\approx 31$

$N_c = 31$  cells

(b) no. of channels per cell ( $C$ )

$C = \frac{\text{allocated spectrum}}{\text{channel BW} \times \text{freq. reuse factor}}$

$C = \frac{40000}{60 \times 7} = 95.24 \approx 95$  channels/cell



(c) traffic intensity of each cell

For  $GOS = 0.02$ ,  $C = 95$ . From Erlang B chart (table),

traffic intensity  $A = 83.13 \approx 83$

$$A = 83 \text{ Erlangs/cell}$$

(d) maximum traffic carried

$$= \text{no. of cells} \times \text{traffic intensity per cell}$$

$$= 31 \times 83 = 2573 \text{ Erlangs.}$$

(e) the total no. of users that can be served for  $2.7\% GOS$

$$\text{traffic per user} = 0.03 \text{ Erlangs}$$

$$\text{total no. of users} = \frac{\text{Total traffic}}{\text{traffic per user}}$$

$$\text{total no. of users} = \frac{2573}{0.03} = 85766 \text{ users}$$

$$(f) \text{ No. of channels} = \frac{40 \text{ MHz}}{60 \text{ kHz}} = 666$$

$$\text{the no. of mobiles per channel} = \frac{\text{no. of users}}{\text{no. of channels}} = \frac{85766}{666}$$

$$\text{no. of mobiles per channel} \approx 128.78$$

(g) the theoretical maximum number of users that could be served at one time by the system

$$= C \times N$$

$$= 95 \times 31 = 2945 \text{ users.}$$

which is 3.41% of the occupied customer base.



A) Given data:

$$\text{Total BW} = 24 \text{ MHz}$$

$$\text{Channel BW} = 30 \text{ KHz} \rightarrow 2 \text{ simplex channels}$$

$$= 60 \text{ KHz}$$

$$\text{Traffic intensity per user} = 0.1 \text{ Erlangs}$$

Erlang B is used.

Soln:

(a) no. of channels in each cell for 4 cell reuse system

$$\text{no. of channels} = \frac{24 \text{ MHz}}{2 \times 30 \text{ KHz}} = 400 \text{ channels}$$

$$\text{no. of channels/cell} = \frac{400 \text{ channels}}{4 \text{ cells}} = 100 \text{ channels/cell}$$

(b) 90% capacity for perfect scheduling

$$\text{Total traffic} = 90\% \text{ of } 100 \text{ Erlangs} = 90 \text{ Erlangs}$$

$$A = U A_u$$

$$\text{no. of users (U)} = \frac{A}{A_u} = 90 / 0.1 = 900 \text{ users}$$

$$\text{maximum no. of users supported per cell} = 900$$

(c) blocking probability of system in (b) when maximum users available in user pool

$$C = 100, A = 90 \text{ Erlangs from Erlang B chart/table,}$$

$$AOS = 3\% = 0.03$$

- (d) If each cell now uses  $120^\circ$  sectoring instead of omnidirectional for each base station. What is the new total no. of users that can be supported per cell for same blocking probability in (c) ?

total 100 channels/cell.

→ now by  $120^\circ$  sectoring → 33.3 channels/cell

$$GOS = 3^{-1}.$$

From Erlang B chart/table.

traffic intensity  $A = 25$  Erlangs/sector

no. of users/sector =  $A/A_u = 250$  /sector

no. of users/cell =  $250 \times 3 = 750$  users

$$U = 750 \text{ users.}$$

- (e) If each cell covers 5 sq. km, then how many subscribers could be supported in an urban market that is 50 km x 50 km for the case of omnidirectional base station antenna.

$$\text{total area} = 50 \times 50 = 2500 \text{ sq. km}$$

$$\text{cell area} = 5 \text{ sq. km}$$

$$\text{no. of cells} = \frac{2500}{5} = 500 \text{ cells.}$$

$$\text{no. of users} = \frac{500 \times 750 \text{ users/cell}}{\text{cell}}$$

$$U = 4,50,000 \text{ users}$$

- (f) same scenario as (e) with  $120^\circ$  sectored antenna.

500 cells ; 750 users/cell

$$\text{no. of users } U = 500 \times 750 = 3,75,000 \text{ users.}$$