Code:

```
import numpy as np
import random
import itertools
import math
import cv2
def apply_filter(filter, arr):
  try:
     000
     This method convolves an image with a given kernel.
     Parameters
     filter:array, Required
     arr: array, Required
     return tuple
     canvas = updated_arr(arr)
     img = updated_arr(arr)
     for i in range(1, len(arr) - 1):
        for j in range(1, len(arr[i]) - 1):
           pos = 0
           for rows in range(len(filter)):
              for columns in range(len(filter[rows])):
                 x = rows - (len(filter) // 2)
                 y = columns - (len(filter[rows]) // 2)
                 pos += filter[rows][columns] * arr[i + x][j + y]
           canvas[i][j] = pos
           img[i][j] = 0 if pos < 0 else 255 if pos > 255 else pos
     return (canvas, img)
   except:
     print("error in Apply_filter fn")
def overlay_image(item1, item2, bg = False):
  try:
     0.00
     This method used to overlays images based on gradient value.
```

```
Parameters
     _____
     item1:array, Required
     item2:array, Required
     bg:boolean, Optional
     return tuple of item1 and image
     img = item1.copy()
     for i in range(len(item1)):
        for j in range(len(item1[i])):
           if not bg:
              val = math.sqrt(item1[i][j] ** 2 + item2[i][j] ** 2)
              item1[i][j] = val
              img[i][j] = 0 if val < 0 else 255 if val > 255 else val
           else:
              if item2[i][j] > item1[i][j]:
                 item1[i][j] = item2[i][j]
              img[i][j] = 0 if item1[i][j] < 0 else 255 if item1[i][j] > 255 else item1[i][j]
     return (item1, img)
   except:
     print("Error in overlay_image function")
def non_max_supresn(arr, horizontal, vertical, mode):
  try:
     0.000
     This method supresses pixel intensities based on the neighborhood pixel,
     Parameters
     _____
     arr: array, Required
     horizontal:array, Required
     vertical:array, Required
     mode: str, Required
     return list
```

```
canvas = arr.copy()
     img = arr.copy()
     for i in range(len(arr)):
        for j in range(len(arr[i])):
            if mode == "edges":
              angle = math.atan2(vertical[i][j], horizontal[i][j])
              canvas[i][j] = arr[i][j]
              if i == 0 or j == 0 or i == len(arr) - 1 or j == len(arr[i]) - 1:
                 canvas[i][j] = 0
              elif (angle >= -1*math.pi/8 and angle <= math.pi / 8) or (angle > 7*math.pi/8 and
angle \leq -7*math.pi/8):
                 if arr[i][j] \le arr[i][j+1] or arr[i][j] \le arr[i][j-1]:
                    canvas[i][j] = 0
              elif (angle < -1*math.pi/8 and angle >= -3*math.pi/8) or (angle > math.pi/8 and angle
<= 3*math.pi/8):
                 if arr[i][j] <= arr[i+1][j+1] or arr[i][j] <= arr[i-1][j-1]:
                    canvas[i][j] = 0
              elif (angle < -3*math.pi/8 and angle >= -5*math.pi/8) or (angle > 3*math.pi/8 and
angle \leq 5*math.pi/8):
                 if arr[i][j] \le arr[i+1][j] or arr[i][j] \le arr[i-1][j]:
                    canvas[i][j] = 0
              elif (angle < -5*math.pi/8 and angle >= -7*math.pi/8) or (angle > 5*math.pi/8 and
angle \leq 7*math.pi/8):
                 if arr[i][j] \le arr[i+1][j-1] or arr[i][j] \le arr[i-1][j+1]:
                    canvas[i][j] = 0
              else:
                 canvas[i][j] = 0
              img[i][j] = 0 if canvas[i][j] < 0 else 255 if canvas[i][j] > 255 else canvas[i][j]
           elif mode == "corners":
              canvas[i][j] = arr[i][j]
              if (i == 0 \text{ or } j == 0 \text{ or } i == \text{len}(arr) - 1 \text{ or } j == \text{len}(arr[i]) - 1):
                 canvas[i][j] = 0
              elif not (arr[i][j] > arr[i+1][j+1] and arr[i][j] > arr[i-1][j-1] and arr[i][j] >
arr[i+1][j-1] and arr[i][j] > arr[i-1][j+1] and arr[i][j] > arr[i][j+1] and arr[i][j] > arr[i][j-1] and
arr[i][j] > arr[i+1][j] and arr[i][j] > arr[i-1][j]:
                 canvas[i][j] = 0
              img[i][j] = 0 if canvas[i][j] < 0 else 255 if canvas[i][j] > 255 else canvas[i][j]
```

```
except:
     print("Error in non_max_supresn fn")
def threshold(canvas,min_value,max_value):
  try:
     This method used to set pixel value to zero when it
less than min_value,
     and if it is greater than min_value and less than
max value then set to 125 else 255.
     Parameters
     _____
     canvas: , Required
     min_value:int, Required
     max_value:int, Required
     return canvas
     canvas_len=len(canvas)
     for i in range(canvas_len):
        canvas_item_len=len(canvas[i])
        for j in range(canvas_item_len):
          canvas[i][j] = 0 if canvas[i][j] < min_value else 125 if canvas[i][j] < max_value else 255
     return canvas
  except:
     print("Error in threshold function")
def hes_matrix(xxcord, yycord, xycord, yxcord, threshold):
  try:
     This method used to hessian matrix to detect corners
     Parameters
     xxcord:array, Required
     yycord:array, Required
     xycord:array, Required
```

```
yxcord:array, Required
     threshold:float, Required
     return list of list item
     arr = xxcord.copy()
     img = xxcord.copy()
     for i in range(len(xxcord)):
        for j in range(len(xxcord[i])):
           det = xxcord[i][j]*yycord[i][j]-xycord[i][j]*yxcord[i][j]
           trace = xxcord[i][j] + yycord[i][j]
           r = det - .06*(trace**2)
           arr[i][j] = r
           if r > threshold:
              img[i][j] = 255
           else:
              arr[i][j] = 0
              img[i][j] = 0
     return [arr, img]
  except:
     print("Error in hes_matrix fn")
def updated_arr(img):
  try:
     This method create a array of a image
     Parameters
     -----
     img:array, Required
     return list
     arr_item = []
     for i in range(len(img)):
        arr_item += [[]]
        for j in range(len(img[i])):
           arr_item[i] += [img[i][j]]
     arr_item = np.array(arr_item, dtype="float32")
     return arr_item
  except:
     print("Error updated_arr in Function")
```

def corners_to_list(corners):

```
try:
     This methods change the list of corners into a list
     Parameters
     _____
     corners: array, Required
     Return list of corners
     corners_list = []
     for i in range(len(corners)):
        for j in range(len(corners[i])):
           if corners[i][j] > 0:
              corners_list += [(i, j)]
     return corners_list
  except:
     print("Error in Corner_to_list function")
def ransac_algo(corners, threshold, inliers, it):
  try:
     This methods uses the RANSAC algorithm on set of
points of image.
     Parameters
     _____
     corners: array, Required
     threshold: float, Required
     inliers: Required
     it: int, Required
     Return list of list
     maxpts = []
     passes = []
     success = []
     used = []
     endpoints = []
     for i in range(it):
        maxpts += [[0, 0]]
```

```
passes +=[[(0,0)]]
        success += [0]
        used += [[]]
        endpoints += [[]]
     for j in range(17):
        items = random.sample(range(len(corners)), 2)
        endpoints[j] = [corners[items[0]], corners[items[1]]]
        passes[j] = [corners[items[0]], corners[items[1]]]
        line_dim = (corners[items[0]][0] -
corners[items[1]][0])**2 + (corners[items[0]][1] -
corners[items[1]][1])**2
        try:
           m = (corners[items[0]][0] - corners[items[1]][0]) / (corners[items[0]][1] -
corners[items[1]][1])
        except:
           continue
        if m == 0:
           continue
        b = -m*corners[items[0]][1] + corners[items[0]][0]
        for k in range(len(corners)):
           cornerx = (corners[k][1] / m + corners[k][0] - b)/(m + 1/m)
           cornery = cornerx * m + b
           d = (corners[k][1] - cornerx) ** 2 + (corners[k][0] - cornery) ** 2
           if d <= threshold ** 2:
             success[j] += 1
              used[j] += [corners[k]]
             first\_dim = (corners[k][0] - endpoints[j][0][0])**2 + (corners[k][1] -
endpoints[j][0][1])**2
             second\_dim = (corners[k][0] - endpoints[j][1][0])**2 + (corners[k][1] -
endpoints[j][1][1])**2
             if first_dim > line_dim or second_dim > line_dim:
                if first_dim <= second_dim:</pre>
                   if first_dim > maxpts[j][0]:
                      maxpts[j][0] = first_dim
                      passes[j][0] = corners[k]
                else:
                   if second_dim > maxpts[j][1]:
                      maxpts[j][1] = second_dim
                      passes[j][1] = corners[k]
           if success[j] >= inliers:
              return [passes[j], used[j], endpoints[j]]
     winner = success.index(max(success))
     return [passes[winner], used[winner], endpoints[winner]]
  except:
     print("Error in ransac_algo function")
```

```
def apply_ransac(img, corners, threshold =
math.sqrt(3.84), inliers = 1000, features = 4, it = 17):
  try:
     This methods apply the RANSAC algorithm on an
image as per iteration value(it parameter),
     and creates an image.
     Parameters
     _____
     img: array, Required
     corners: array, Required
     threshold: float, Optional
     inliers: int, Optional
     features: int, Optional
     it: int, Optional
     Return array
     colors = list(itertools.product([0, 255], repeat = 3))
     color = random.sample(colors[1:-1], features + 1)
     for i in range(features):
        winner = ransac_algo(corners, threshold, inliers, it)
        img = cv2.line(img, (winner[0][0])[::-1], (winner[0][1])[::-1], color[i], 1)
        for j in range(len(winner[1])):
           pt = winner[1][j]
           for row in range(3):
              for column in range(3):
                x = row - 1
                y = column - 1
                 img[pt[0] + x][pt[1] + y] = color[i] if pt != winner[2][0] and pt != winner[2][1]
else color[-1]
           corners.remove(pt)
     return img
  except:
     print("Error in apply_ransac function")
```

def hough_transform(img, corners, angle, radius,

```
features):
  try:
     000
     This method apply Hough Transform on a set of points.
     Parameters
     img:array, Required
     corners: array, Required
     angle: int, Optional
     radius: Optional
     features: int, Optional
     return cordinates, list
     cordinates = []
     for i in range(features):
        coordinates +=[[(0, 0), 0]]
     hough = []
     for i in range(radius):
        hough += [[]]
        for j in range(angle):
           hough[i] += [0]
     for i in range(len(corners)):
        for j in range(0, angle):
           r = corners[i][1]*math.cos(j * math.pi / angle) + corners[i][0]*math.sin(j * math.pi /
angle)
           rbin = math.floor(radius/2 \ / \ math.sqrt(len(img)**2 \ + \ len(img[1])**2) \ * \ r \ + \ radius/2)
           r = math.floor(r)
           hough[rbin][j] += 1
           for k in range(features):
              if hough[rbin][j] > cordinates[k][1]:
                 if [(r, j * math.pi / angle), hough[rbin][j]-1] in cordinates:
                    index = cordinates.index([(r, j * math.pi / angle), hough[rbin][j]-1])
                    cordinates = cordinates[:k] + [[(r, j * math.pi / angle), hough[rbin][j]]] +
cordinates[k:index] + cordinates[index+1:]
                 else:
                    cordinates = cordinates[:k] + [[(r, j * math.pi / angle), hough[rbin][j]]] +
cordinates[k:-1]
                 break
      return cordinates
```

```
except:
     print("Error in hough_transform function")
def apply_hough(img, corners, angle = 180, radius =
None, features = 4):
  try:
     000
     This method apply Hough Transofrm a specifed
amount of times, and creates an image depicting the
result.
     Parameters
     _____
     img:array, Required
     corners: array, Required
     angle: int, Optional
     radius: Optional
     features: int, Optional
     return array
     if radius == None:
        radius = math.ceil(2*math.sqrt(len(img)**2 +
len(img[1])**2))
     hough = hough_transform(img, corners, angle,
radius, features)
     for i in range(features):
        pt1 = int(hough[i][0][0]/math.sin(hough[i][0][1]))
        pt2 = int((hough[i][0][0] -
len(img[1])*math.cos(hough[i][0][1]))/math.sin(hough[i][0][1]))
        img = cv2.line(img, (0, pt1), (len(img[1]), pt2), (0, 0, 255), 1)
     return img
  except:
     print("Error in apply_hough function")
if ___name___ == "___main___":
  try:
     """Filtering variable and corrosponding values.
     g: gaussian
```

```
h_sobel: Horizontal Sobel Filter values
v_sobel: Verticle Sobel Filter values
g = [[0.077847, 0.123317, 0.077847],
        [0.123317, 0.195346, 0.123317],
        [0.077847, 0.123317, 0.077847]]
h_{sobel} = [[1, 2, 1],
     [0, 0, 0],
     [-1, -2, -1]
v_{sobel} = [[1, 0, -1],
     [2, 0, -2],
     [1, 0, -1]]
img = cv2.imread("road.png", 0)
arr = updated_arr(img)
gfilImg = apply_filter(g, arr)
h = apply_filter(h_sobel, gfilImg[0])
v = apply_filter(v_sobel, gfilImg[0])
"""Apply fiter for Horizontal and Vertical sobel
cord1 xx: for XX cordinates
cord1_yy: for YY cordinates
cord1 xy: for XY cordinates
cord1 yx: for YX cordinates
cord1_xx = apply_filter(h_sobel, h[0])
cord1_yy = apply_filter(v_sobel, v[0])
cord1 xy = apply filter(v sobel, h[0])
cord1_yx = apply_filter(h_sobel, v[0])
edges = overlay_image(h[0], v[0])
suppress_edges = non_max_supresn(edges[0], h[0], v[0], "edges")
threshold edges = threshold(suppress edges[0], 175, 60)
hess_matrix = hes_matrix(cord1_xx[0], cord1_yy[0], cord1_xy[0], cord1_yx[0], 175000)
hess_threshold = non_max_supresn(hess_matrix[0], h[0], v[0], "corners")
updated_hess_matrix = overlay_image(hess_threshold[0], threshold_edges / 4, bg=True)
colored = (updated_hess_matrix[1]).copy()
colored = cv2.cvtColor(updated hess matrix[1], cv2.COLOR GRAY2RGB)
```

```
0.00
     ransac_image = colored.copy()
     ransac image = apply ransac(ransac image,
corners_to_list(hess_threshold[1]), it = 25)
     000
     Hough Transformation with the hess threshold values
     Hough_transform = colored.copy()
     Hough_transform = apply_hough(Hough_transform,
corners_to_list(hess_threshold[1]), angle=45)
     0.00
     Saving all output images
     cv2.imwrite("gaussian_filter.png", gfilImg[1])
     cv2.imwrite("h_sobel_filter.png", h[1])
     cv2.imwrite("v_sobel_filter.png", v[1])
     cv2.imwrite("cord1.png", cord1_xx[1])
     cv2.imwrite("cord2.png", cord1_yy[1])
     cv2.imwrite("cord3.png", cord1_xy[1])
     cv2.imwrite("cord4.png", cord1_yx[1])
     cv2.imwrite("edges_with_no_supress.png", edges[1])
     cv2.imwrite("edges_with_supress.png", suppress_edges[1])
     cv2.imwrite("edges_threshold.png", threshold_edges)
     cv2.imwrite("corners.png", hess_matrix[1])
     cv2.imwrite("corners_threshold.png", hess_threshold[1])
     cv2.imwrite("updated_corners.png", updated_hess_matrix[1])
     cv2.imwrite("ransac.png", ransac_image)
     cv2.imwrite("hough_image.png", Hough_transform)
  except:
     print("Error n main Fn")
```

Explanation and Images:

Pre-Processing Step

The code reads in the image from the provided file, road.png, converts it to grayscale and then begins the pre-processing part of the code.

The pre-processing starts by first creating a Gaussian filter using the Guassian value equation provided in the slidesThe result of applying the filter to the image can be seen below in Figure 1.

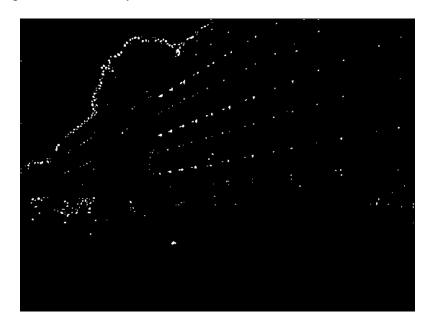


Figure 1: Guassian Filtered Image



Figure 2: Horizontal Sobel Filtered Image (Left) and Verticle Sobel Filtered Image (Right)

The image is then subjected to Sobel filters as derivatives operators in order to determine the image's second x, second y, and x of y derivatives. The determinant of the Hessian matrix is then calculated using these derivative matrices. The Hessian matrix's determinant was then threshold, with all pixels with values less than 150 set to 0 and all pixels with values more than 150 set to 255. All of the places on the image where the Hessian detector responds significantly were shown as a result. The black tree and the extremely light sky have a significant intensity difference.



Thresholded Hessian Response



Non Maximum Suppressed Response



Edges with No supress



Edges with supress

The result was then subjected to non-maximum suppression in order to extract examples of the best Hessian detector responses. Figure 2 shows the thresholded Hessian detector response as well as the non-maximum suppressed version. The Hessian detector responds strongly to many of the angles and straight lines that make up the building's characteristics, which is good, but it also responds strongly to the tree in the image's upper left corner, which is not ideal.

RANSAC:

The RANSAC portion of the code takes within the yield of pre-processing step which ought to be an array of all the zones on the picture where the Hessian detector reacted exceptionally unequivocally after non-maximum suppression was connected. The algorithm first gathers all the points in the image where the locator reacted strongly and stores them as tuples in a list that may be easily accessed later. Two points are then picked at random from the list, and the parameters for the condition of a line, slant m, and y caught c, are discovered using some basic variable-based algebra. The rest of the focuses are at that point circled through in order to decide the focuses that are near sufficient to the line to be inliers for the line. This is often done by calculating the opposite separate between the point and the line and checking in the event that it is underneath a certain threshold.

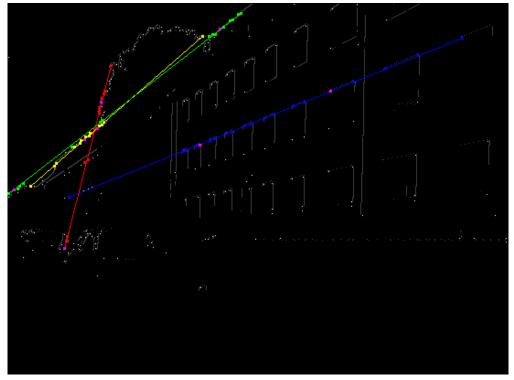
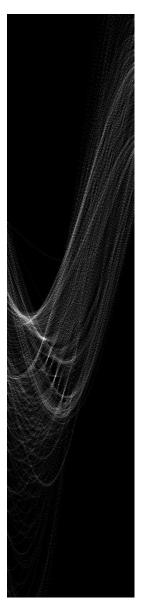


Figure 5: Four Best Lines Produced by RANSAC Plotted

Hough:

The Hough transform section of the code, like RANSAC, takes in the pre-processing step's output, which should be an array of all the locations on the image where the Hessian detector responded extremely strongly when non-maximum suppression was applied. The algorithm begins by calculating the size that the accumulator will require. To do this, the highest and lowest values for the function ρ = x cos θ . The algorithm begins by calculating the size that the accumulator will require. To do this, the highest and lowest values for the function ρ = x cos θ Because we can't directly express the negative values that rho will take in the accumulator, the range of values is used for the first dimension. To compensate for this, we apply an offset, which is simply the negative of the low value multiplied by the rho given by the equation to produce a correct index to utilise.



Visualized Hough Space



Suppressed Hough Space



Areas Removed From Hough Space

The algorithm extracts all of the points in the picture where the detector responded strongly and saves them as tuples in a list that may be retrieved later. The line in the image space with the most support based on the number of image space points that voted for it should correspond to the point in the Hough space with the highest value. Non maximum suppression is performed to the Hough space before identifying the points with the highest support in order to prevent near identical lines from being proposed. The model is transformed back into two linear form and two points are created in order to draw a line between them on the picture after the strongest point in suppressed Hough space is discovered.

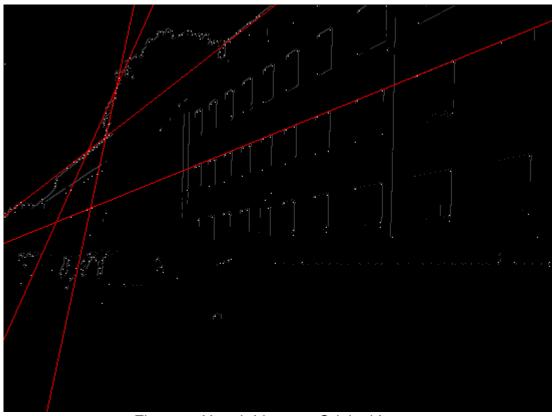


Figure 7: Hough Lines on Original Image