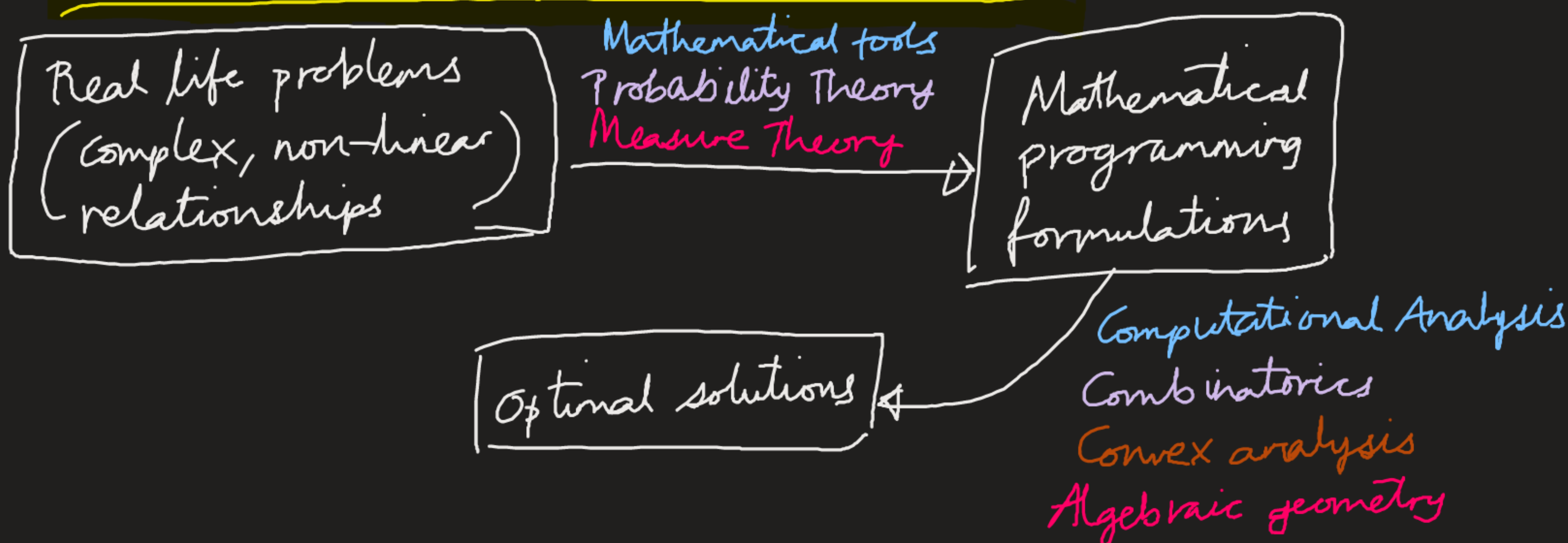


Mathematical Programming Formulations



Parameters of the problem: The data describing the physical system/process.

Decision Variables: Decisions that we need to take (optimization problem variables).

Objective function: (measurable real valued function) $f: \mathbb{R}^n \rightarrow \mathbb{R}$.
(function of the decision variables)

Constraints: Restrictions on the functions of decision variables that help us represent a physical system/phenomenon/process.
(algebraic/semi-algebraic)

Knapsack Problem

n items: $\{1, 2, \dots, n\}$. Each item i has utility/unit u_i and volume/unit c_i .

Items can be divided into three categories:

I - divisible items (water, wood etc.)

J - indivisible items (bags of chips, cookie boxes etc.)

K - unique items (tent, stove etc.)

The volume of the knapsack: B

Parameters of the problem:
Utility/unit - u_i
Volume/unit - c_i
Volume of knapsack - B

Decision Variables:

→ For each item $i \in I$, amount of i to be added to the knapsack,
 $x_i \in \mathbb{R}_+$ continuous variables

→ For each item $j \in J$, the number of units of j to be added to the knapsack, $x_j \in \mathbb{Z}_+$ discrete variables

→ For each item $k \in K$, whether k is added to the knapsack or not.
 $x_k \in \{0, 1\}$ binary variables

Objective function:

Total utility of the knapsack: $\sum_{i \in I} u_i x_i + \sum_{j \in J} u_j x_j + \sum_{k \in K} u_k x_k$

Constraints:

objective sense: maximization

Volume of the knapsack:

$$\sum_{i \in I} c_i x_i + \sum_{j \in J} c_j x_j + \sum_{k \in K} c_k x_k \leq B$$

Variable constraints:

$$x_i \geq 0 \quad \forall i \in I$$

$$x_j \geq 0, x_j \in \mathbb{Z}_+ \quad \forall j \in J$$

$$x_k \in \{0, 1\} \quad \forall k \in K$$