

```
In [ ]: from google.colab import drive
drive.mount('/content/drive')
```

Mounted at /content/drive

```
In [ ]: %cd drive/"My Drive"/assignment2/

/content/drive/My Drive/assignment2
```

## Fully-Connected Neural Nets

In the previous homework you implemented a fully-connected two-layer neural network on CIFAR-10. The implementation was simple but not very modular since the loss and gradient were computed in a single monolithic function. This is manageable for a simple two-layer network, but would become impractical as we move to bigger models. Ideally we want to build networks using a more modular design so that we can implement different layer types in isolation and then snap them together into models with different architectures.

In this exercise we will implement fully-connected networks using a more modular approach. For each layer we will implement a `forward` and a `backward` function. The `forward` function will receive inputs, weights, and other parameters and will return both an output and a `cache` object storing data needed for the backward pass, like this:

```
def layer_forward(x, w):
    """ Receive inputs x and weights w """
    # Do some computations ...
    z = # ... some intermediate value
    # Do some more computations ...
    out = # the output

    cache = (x, w, z, out) # Values we need to compute gradients

    return out, cache
```

The backward pass will receive upstream derivatives and the `cache` object, and will return gradients with respect to the inputs and weights, like this:

```
def layer_backward(dout, cache):
    """
    Receive dout (derivative of loss with respect to outputs) and
    cache,
    and compute derivative with respect to inputs.
    """
    # Unpack cache values
    x, w, z, out = cache
```

```

# Use values in cache to compute derivatives
dx = # Derivative of loss with respect to x
dw = # Derivative of loss with respect to w

return dx, dw

```

After implementing a bunch of layers this way, we will be able to easily combine them to build classifiers with different architectures.

In addition to implementing fully-connected networks of arbitrary depth, we will also explore different update rules for optimization, and introduce Dropout as a regularizer and Batch/Layer Normalization as a tool to more efficiently optimize deep networks.

```

In [ ]: # As usual, a bit of setup
from __future__ import print_function
import time
import numpy as np
import matplotlib.pyplot as plt
from cs682.classifiers.fc_net import *
from cs682.data_utils import get_CIFAR10_data
from cs682.gradient_check import eval_numerical_gradient, eval_numerical_grad
from cs682.solver import Solver

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipy
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))

```

```

In [ ]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
for k, v in list(data.items()):
    print((' %s: ' % k, v.shape))

('X_train: ', (49000, 3, 32, 32))
('y_train: ', (49000,))
('X_val: ', (1000, 3, 32, 32))
('y_val: ', (1000,))
('X_test: ', (1000, 3, 32, 32))
('y_test: ', (1000,))

```

# Affine layer: forward

Open the file `cs682/layers.py` and implement the `affine_forward` function.

Once you are done you can test your implementation by running the following:

```
In [ ]: # Test the affine_forward function

num_inputs = 2
input_shape = (4, 5, 6)
output_dim = 3

input_size = num_inputs * np.prod(input_shape)
weight_size = output_dim * np.prod(input_shape)

x = np.linspace(-0.1, 0.5, num=input_size).reshape(num_inputs, *input_shape)
w = np.linspace(-0.2, 0.3, num=weight_size).reshape(np.prod(input_shape), output_dim)
b = np.linspace(-0.3, 0.1, num=output_dim)

out, _ = affine_forward(x, w, b)
correct_out = np.array([[ 1.49834967,  1.70660132,  1.91485297],
                        [ 3.25553199,  3.5141327,  3.77273342]])

# Compare your output with ours. The error should be around e-9 or less.
print('Testing affine_forward function:')
print('difference: ', rel_error(out, correct_out))
```

```
Testing affine_forward function:
difference: 9.769849468192957e-10
```

# Affine layer: backward

Now implement the `affine_backward` function and test your implementation using numeric gradient checking.

```
In [ ]: # Test the affine_backward function
np.random.seed(231)
x = np.random.randn(10, 2, 3)
w = np.random.randn(6, 5)
b = np.random.randn(5)
dout = np.random.randn(10, 5)

dx_num = eval_numerical_gradient_array(lambda x: affine_forward(x, w, b)[0],
dw_num = eval_numerical_gradient_array(lambda w: affine_forward(x, w, b)[0],
db_num = eval_numerical_gradient_array(lambda b: affine_forward(x, w, b)[0],

_, cache = affine_forward(x, w, b)
dx, dw, db = affine_backward(dout, cache)

# The error should be around e-10 or less
print('Testing affine_backward function:')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
```

```
Testing affine_backward function:
dx error:  5.399100368651805e-11
dw error:  9.904211865398145e-11
db error:  2.4122867568119087e-11
```

## ReLU activation: forward

Implement the forward pass for the ReLU activation function in the `relu_forward` function and test your implementation using the following:

```
In [ ]: # Test the relu_forward function

x = np.linspace(-0.5, 0.5, num=12).reshape(3, 4)

out, _ = relu_forward(x)
correct_out = np.array([[ 0.,          0.,          0.,          0.,          ],
                        [ 0.,          0.,          0.04545455,  0.13636364, ],
                        [ 0.22727273,  0.31818182,  0.40909091,  0.5,          ]])

# Compare your output with ours. The error should be on the order of e-8
print('Testing relu_forward function:')
print('difference: ', rel_error(out, correct_out))
```

```
Testing relu_forward function:
difference:  4.999999798022158e-08
```

# ReLU activation: backward

Now implement the backward pass for the ReLU activation function in the `relu_backward` function and test your implementation using numeric gradient checking:

```
In [ ]: np.random.seed(231)
x = np.random.randn(10, 10)
dout = np.random.randn(*x.shape)

dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout)

_, cache = relu_forward(x)
dx = relu_backward(dout, cache)

# The error should be on the order of e-12
print('Testing relu_backward function:')
print('dx error: ', rel_error(dx_num, dx))
```

```
Testing relu_backward function:
dx error:  3.2756349136310288e-12
```

## Inline Question 1:

We've only asked you to implement ReLU, but there are a number of different activation functions that one could use in neural networks, each with its pros and cons. In particular, an issue commonly seen with activation functions is getting zero (or close to zero) gradient flow during backpropagation. Which of the following activation functions have this problem? If you consider these functions in the one dimensional case, what types of input would lead to this behaviour?

1. Sigmoid
2. ReLU
3. Leaky ReLU

## Answer:

1. For large positive and negative positive input values during the forward pass, the sigmoid function has a near zero gradient resulting in zero gradient flow during backpropagation. In one dimension, inputs that are greater than  $1e4$  or smaller than  $1e-4$  would lead to this behavior.
2. When using a ReLu, the negative input values filtered to 0. Therefore, only when the input largely contains negative values, a ReLu gets to a near zero gradient. In one dimension, inputs that are strictly smaller than 0 would lead to this behavior.
3. A Leaky Relu tries to solve the 'dying ReLu' problem. Instead of the function being zero when  $x < 0$ , a leaky ReLU will instead have a small negative slope and therefore, it'll never result in a zero gradient.

## "Sandwich" layers

There are some common patterns of layers that are frequently used in neural nets. For example, affine layers are frequently followed by a ReLU nonlinearity. To make these common patterns easy, we define several convenience layers in the file `cs682/layer_utils.py`.

For now take a look at the `affine_relu_forward` and `affine_relu_backward` functions, and run the following to numerically gradient check the backward pass:

```
In [ ]: from cs682.layer_utils import affine_relu_forward, affine_relu_backward
np.random.seed(231)
x = np.random.randn(2, 3, 4)
w = np.random.randn(12, 10)
b = np.random.randn(10)
dout = np.random.randn(2, 10)

out, cache = affine_relu_forward(x, w, b)
dx, dw, db = affine_relu_backward(dout, cache)

dx_num = eval_numerical_gradient_array(lambda x: affine_relu_forward(x, w, b)
dw_num = eval_numerical_gradient_array(lambda w: affine_relu_forward(x, w, b)
db_num = eval_numerical_gradient_array(lambda b: affine_relu_forward(x, w, b)

# Relative error should be around e-10 or less
print('Testing affine_relu_forward and affine_relu_backward:')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
```

```

Testing affine_relu_forward and affine_relu_backward:
dx error:  2.299579177309368e-11
dw error:  8.162011105764925e-11
db error:  7.826724021458994e-12

```

## Loss layers: Softmax and SVM

You implemented these loss functions in the last assignment, so we'll give them to you for free here. You should still make sure you understand how they work by looking at the implementations in `cs682/layers.py`.

You can make sure that the implementations are correct by running the following:

```

In [ ]: np.random.seed(231)
num_classes, num_inputs = 10, 50
x = 0.001 * np.random.randn(num_inputs, num_classes)
y = np.random.randint(num_classes, size=num_inputs)

dx_num = eval_numerical_gradient(lambda x: svm_loss(x, y)[0], x, verbose=False,
loss, dx = svm_loss(x, y)

# Test svm_loss function. Loss should be around 9 and dx error should be around 1e-9
print('Testing svm_loss:')
print('loss: ', loss)
print('dx error: ', rel_error(dx_num, dx))

dx_num = eval_numerical_gradient(lambda x: softmax_loss(x, y)[0], x, verbose=False,
loss, dx = softmax_loss(x, y)

# Test softmax_loss function. Loss should be close to 2.3 and dx error should be around 1e-9
print('\nTesting softmax_loss:')
print('loss: ', loss)
print('dx error: ', rel_error(dx_num, dx))

```

```

Testing svm_loss:
loss:  8.999602749096233
dx error:  1.4021566006651672e-09

```

```

Testing softmax_loss:
loss:  2.302545844500738
dx error:  9.384673161989355e-09

```

# Two-layer network

In the previous assignment you implemented a two-layer neural network in a single monolithic class. Now that you have implemented modular versions of the necessary layers, you will reimplement the two layer network using these modular implementations.

Open the file `cs682/classifiers/fc_net.py` and complete the implementation of the `TwoLayerNet` class. This class will serve as a model for the other networks you will implement in this assignment, so read through it to make sure you understand the API. You can run the cell below to test your implementation.

```
In [ ]: np.random.seed(231)
N, D, H, C = 3, 5, 50, 7
X = np.random.randn(N, D)
y = np.random.randint(C, size=N)

std = 1e-3
model = TwoLayerNet(input_dim=D, hidden_dim=H, num_classes=C, weight_scale=std)

print('Testing initialization ... ')
W1_std = abs(model.params['W1'].std() - std)
b1 = model.params['b1']
W2_std = abs(model.params['W2'].std() - std)
b2 = model.params['b2']
assert W1_std < std / 10, 'First layer weights do not seem right'
assert np.all(b1 == 0), 'First layer biases do not seem right'
assert W2_std < std / 10, 'Second layer weights do not seem right'
assert np.all(b2 == 0), 'Second layer biases do not seem right'

print('Testing test-time forward pass ... ')
model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).T
scores = model.loss(X)
correct_scores = np.asarray(
    [[11.53165108, 12.2917344, 13.05181771, 13.81190102, 14.57198434, 15.3
      12.05769098, 12.74614105, 13.43459113, 14.1230412, 14.81149128, 15.4
      12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.05099822, 15.6
    scores_diff = np.abs(scores - correct_scores).sum()
    assert scores_diff < 1e-6, 'Problem with test-time forward pass'

print('Testing training loss (no regularization)')
y = np.asarray([0, 5, 1])
loss, grads = model.loss(X, y)
correct_loss = 3.4702243556
assert abs(loss - correct_loss) < 1e-10, 'Problem with training-time loss'
```



```

model.reg = 1.0
loss, grads = model.loss(X, y)
correct_loss = 26.5948426952
assert abs(loss - correct_loss) < 1e-10, 'Problem with regularization loss'

# Errors should be around e-7 or less
for reg in [0.0, 0.7]:
    print('Running numeric gradient check with reg = ', reg)
    model.reg = reg
    loss, grads = model.loss(X, y)

    for name in sorted(grads):
        f = lambda _: model.loss(X, y)[0]
        grad_num = eval_numerical_gradient(f, model.params[name], verbose=False)
        print('%s relative error: %.2e' % (name, rel_error(grad_num, grads[name])))

```

```

Testing initialization ...
Testing test-time forward pass ...
Testing training loss (no regularization)
Running numeric gradient check with reg = 0.0
W1 relative error: 1.83e-08
W2 relative error: 3.12e-10
b1 relative error: 9.83e-09
b2 relative error: 4.33e-10
Running numeric gradient check with reg = 0.7
W1 relative error: 2.53e-07
W2 relative error: 2.85e-08
b1 relative error: 1.56e-08
b2 relative error: 7.76e-10

```

## Solver

In the previous assignment, the logic for training models was coupled to the models themselves. Following a more modular design, for this assignment we have split the logic for training models into a separate class.

Open the file `cs682/solver.py` and read through it to familiarize yourself with the API. After doing so, use a `Solver` instance to train a `TwoLayerNet` that achieves at least 50% accuracy on the validation set.

```

In [ ]: model = TwoLayerNet()
        solver = None
        best_val = 0
        #####
        # TODO: Use a Solver instance to train a TwoLayerNet that achieves at least
        # 50% accuracy on the validation set.
        #####
        model = TwoLayerNet(hidden_dim=185, reg=2.2e-3)
        solver = Solver(model, data, optim_config={'learning_rate':6.4e-4},
                        lr_decay=0.95, batch_size=200, num_epochs=5, print_e

        solver.train()
        #####
        #
        #                               END OF YOUR CODE
        #####

(Iteration 1 / 1225) loss: 2.302839
(Epoch 0 / 5) train acc: 0.132000; val_acc: 0.131000
(Iteration 201 / 1225) loss: 1.591486
(Epoch 1 / 5) train acc: 0.409000; val_acc: 0.407000
(Iteration 401 / 1225) loss: 1.520135
(Epoch 2 / 5) train acc: 0.434000; val_acc: 0.450000
(Iteration 601 / 1225) loss: 1.469207
(Epoch 3 / 5) train acc: 0.464000; val_acc: 0.469000
(Iteration 801 / 1225) loss: 1.403599
(Epoch 4 / 5) train acc: 0.499000; val_acc: 0.479000
(Iteration 1001 / 1225) loss: 1.415417
(Iteration 1201 / 1225) loss: 1.374660
(Epoch 5 / 5) train acc: 0.551000; val_acc: 0.515000

```

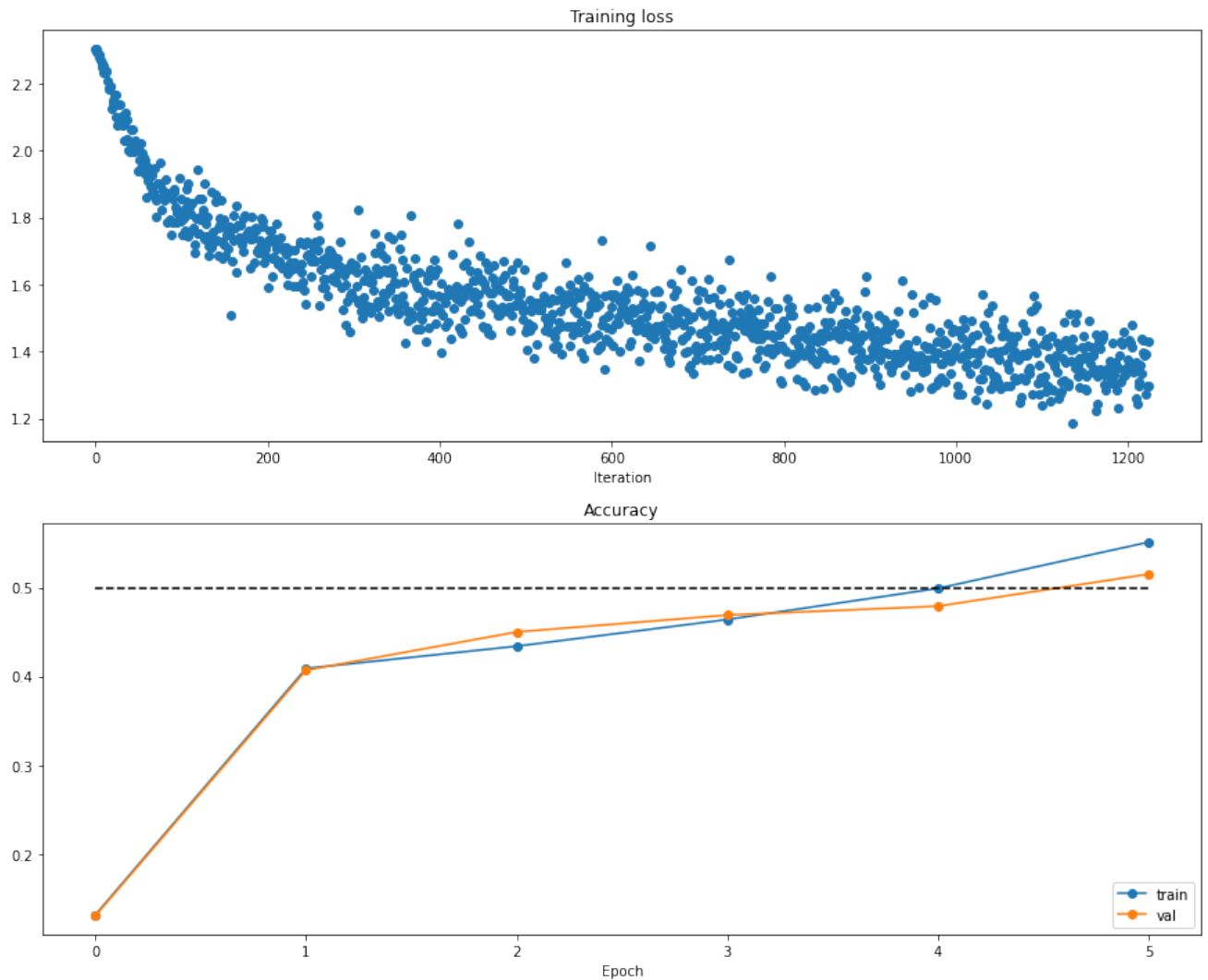
```

In [ ]: # Run this cell to visualize training loss and train / val accuracy

plt.subplot(2, 1, 1)
plt.title('Training loss')
plt.plot(solver.loss_history, 'o')
plt.xlabel('Iteration')

plt.subplot(2, 1, 2)
plt.title('Accuracy')
plt.plot(solver.train_acc_history, '-o', label='train')
plt.plot(solver.val_acc_history, '-o', label='val')
plt.plot([0.5] * len(solver.val_acc_history), 'k--')
plt.xlabel('Epoch')
plt.legend(loc='lower right')
plt.gcf().set_size_inches(15, 12)
plt.show()

```



## Multilayer network

Next you will implement a fully-connected network with an arbitrary number of hidden layers.

Read through the `FullyConnectedNet` class in the file `cs682/classifiers/fc_net.py`.

Implement the initialization, the forward pass, and the backward pass. For the moment don't worry about implementing dropout or batch/layer normalization; we will add those features soon.

## Initial loss and gradient check

As a sanity check, run the following to check the initial loss and to gradient check the network both with and without regularization. Do the initial losses seem reasonable?

For gradient checking, you should expect to see errors around  $1e-7$  or less.

```
In [ ]: np.random.seed(231)
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))

for reg in [0, 3.14]:
    print('Running check with reg = ', reg)
    model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                              reg=reg, weight_scale=5e-2, dtype=np.float64)

    loss, grads = model.loss(X, y)
    print('Initial loss: ', loss)

    # Most of the errors should be on the order of e-7 or smaller.
    # NOTE: It is fine however to see an error for W2 on the order of e-5
    # for the check when reg = 0.0
    for name in sorted(grads):
        f = lambda _: model.loss(X, y)[0]
        grad_num = eval_numerical_gradient(f, model.params[name], verbose=False,
        print('%s relative error: %.2e' % (name, rel_error(grad_num, grads[name]))
```

```
Running check with reg = 0
Initial loss: 2.3004790897684924
W1 relative error: 1.48e-07
W2 relative error: 2.21e-05
W3 relative error: 3.53e-07
b1 relative error: 5.38e-09
b2 relative error: 2.09e-09
b3 relative error: 5.80e-11
Running check with reg = 3.14
Initial loss: 7.052114776533016
W1 relative error: 6.86e-09
W2 relative error: 3.52e-08
W3 relative error: 1.32e-08
b1 relative error: 1.48e-08
b2 relative error: 1.72e-09
b3 relative error: 1.80e-10
```

As another sanity check, make sure you can overfit a small dataset of 50 images. First we will try a three-layer network with 100 units in each hidden layer. In the following cell, tweak the learning rate and initialization scale to overfit and achieve 100% training accuracy within 20 epochs.

```

In [ ]: # TODO: Use a three-layer Net to overfit 50 training examples by
        # tweaking just the learning rate and initialization scale.

num_train = 50
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}

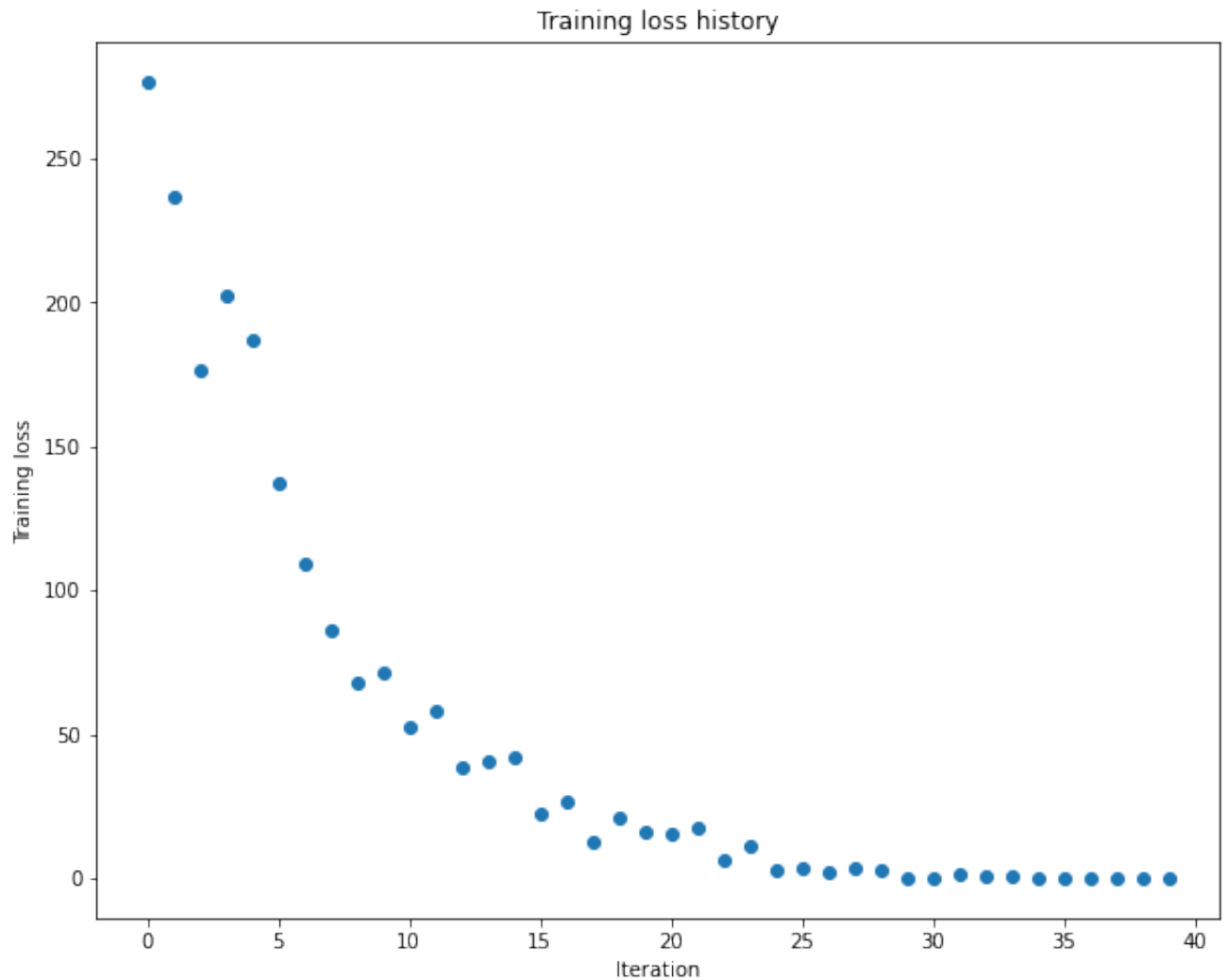
weight_scale = 1e-1
learning_rate = 1e-4
model = FullyConnectedNet([100, 100],
                           weight_scale=weight_scale, dtype=np.float64)
solver = Solver(model, small_data,
                 print_every=10, num_epochs=20, batch_size=25,
                 update_rule='sgd',
                 optim_config={
                     'learning_rate': learning_rate,
                 })
solver.train()

plt.plot(solver.loss_history, 'o')
plt.title('Training loss history')
plt.xlabel('Iteration')
plt.ylabel('Training loss')
plt.show()

(Iteration 1 / 40) loss: 276.679212
(Epoch 0 / 20) train acc: 0.140000; val_acc: 0.113000
(Epoch 1 / 20) train acc: 0.120000; val_acc: 0.119000
(Epoch 2 / 20) train acc: 0.180000; val_acc: 0.110000
(Epoch 3 / 20) train acc: 0.260000; val_acc: 0.133000
(Epoch 4 / 20) train acc: 0.320000; val_acc: 0.145000
(Epoch 5 / 20) train acc: 0.440000; val_acc: 0.142000
(Iteration 11 / 40) loss: 52.396182
(Epoch 6 / 20) train acc: 0.520000; val_acc: 0.135000
(Epoch 7 / 20) train acc: 0.440000; val_acc: 0.127000
(Epoch 8 / 20) train acc: 0.640000; val_acc: 0.134000
(Epoch 9 / 20) train acc: 0.720000; val_acc: 0.140000
(Epoch 10 / 20) train acc: 0.760000; val_acc: 0.137000
(Iteration 21 / 40) loss: 15.661929
(Epoch 11 / 20) train acc: 0.780000; val_acc: 0.135000
(Epoch 12 / 20) train acc: 0.740000; val_acc: 0.136000
(Epoch 13 / 20) train acc: 0.860000; val_acc: 0.139000
(Epoch 14 / 20) train acc: 0.860000; val_acc: 0.144000
(Epoch 15 / 20) train acc: 0.960000; val_acc: 0.147000
(Iteration 31 / 40) loss: 0.001693
(Epoch 16 / 20) train acc: 0.940000; val_acc: 0.147000
(Epoch 17 / 20) train acc: 0.980000; val_acc: 0.143000
(Epoch 18 / 20) train acc: 1.000000; val_acc: 0.144000
(Epoch 19 / 20) train acc: 1.000000; val_acc: 0.144000

```

(Epoch 20 / 20) train acc: 1.000000; val\_acc: 0.144000



Now try to use a five-layer network with 100 units on each layer to overfit 50 training examples. Again you will have to adjust the learning rate and weight initialization, but you should be able to achieve 100% training accuracy within 20 epochs.

```

In [ ]: # TODO: Use a five-layer Net to overfit 50 training examples by
# tweaking just the learning rate and initialization scale.

num_train = 50
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}

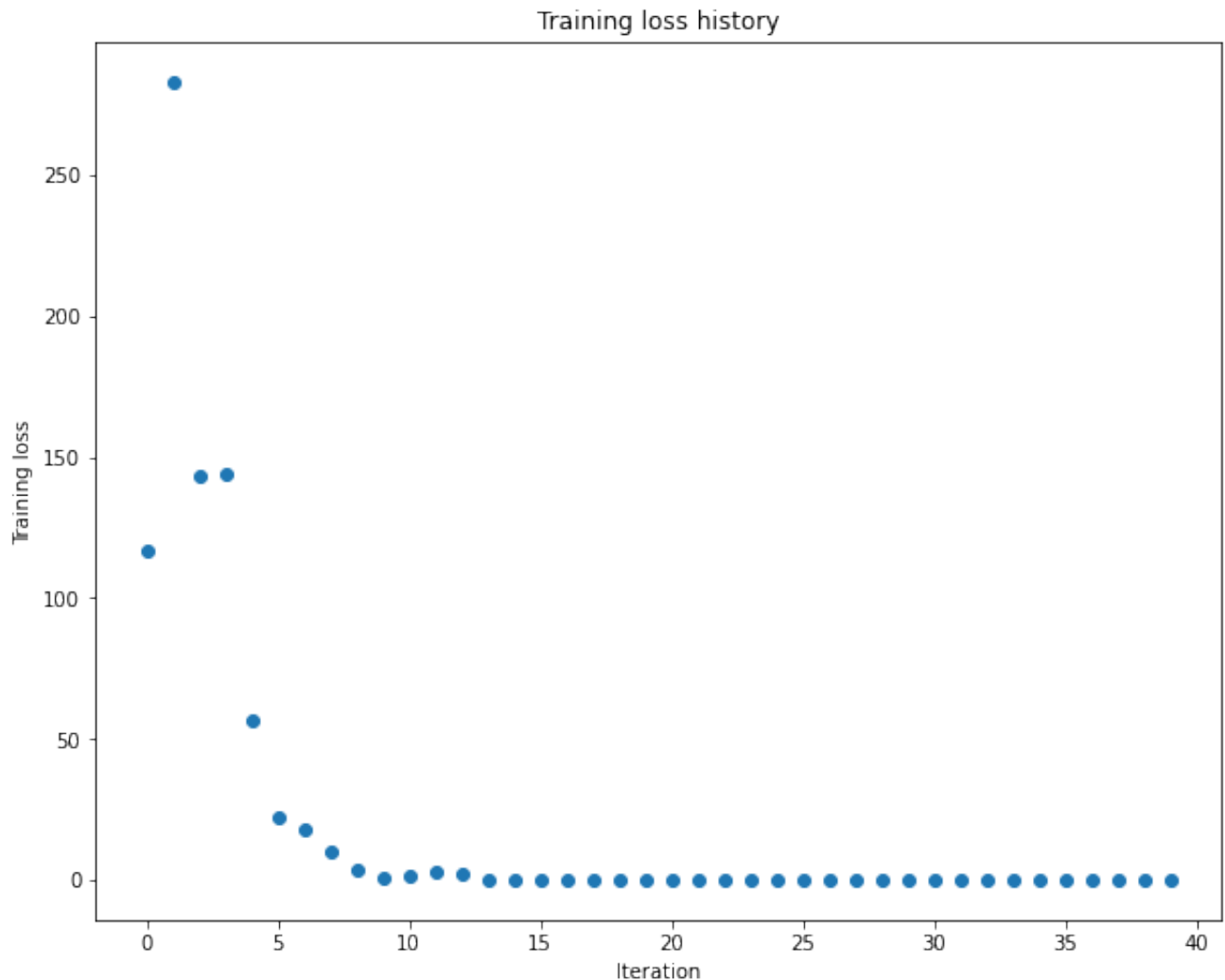
learning_rate = 2e-3
weight_scale = 1e-1
model = FullyConnectedNet([100, 100, 100, 100],
                           weight_scale=weight_scale, dtype=np.float64)
solver = Solver(model, small_data,
                print_every=10, num_epochs=20, batch_size=25,
                update_rule='sgd',
                optim_config={
                    'learning_rate': learning_rate,
                })
solver.train()

plt.plot(solver.loss_history, 'o')
plt.title('Training loss history')
plt.xlabel('Iteration')
plt.ylabel('Training loss')
plt.show()

(Iteration 1 / 40) loss: 116.510392
(Epoch 0 / 20) train acc: 0.180000; val_acc: 0.125000
(Epoch 1 / 20) train acc: 0.160000; val_acc: 0.070000
(Epoch 2 / 20) train acc: 0.180000; val_acc: 0.080000
(Epoch 3 / 20) train acc: 0.360000; val_acc: 0.110000
(Epoch 4 / 20) train acc: 0.740000; val_acc: 0.107000
(Epoch 5 / 20) train acc: 0.820000; val_acc: 0.135000
(Iteration 11 / 40) loss: 1.382389
(Epoch 6 / 20) train acc: 0.900000; val_acc: 0.127000
(Epoch 7 / 20) train acc: 0.960000; val_acc: 0.127000
(Epoch 8 / 20) train acc: 0.980000; val_acc: 0.125000
(Epoch 9 / 20) train acc: 1.000000; val_acc: 0.122000
(Epoch 10 / 20) train acc: 1.000000; val_acc: 0.123000
(Iteration 21 / 40) loss: 0.002014
(Epoch 11 / 20) train acc: 1.000000; val_acc: 0.123000
(Epoch 12 / 20) train acc: 1.000000; val_acc: 0.123000
(Epoch 13 / 20) train acc: 1.000000; val_acc: 0.122000
(Epoch 14 / 20) train acc: 1.000000; val_acc: 0.122000
(Epoch 15 / 20) train acc: 1.000000; val_acc: 0.121000
(Iteration 31 / 40) loss: 0.000831
(Epoch 16 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 17 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 18 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 19 / 20) train acc: 1.000000; val_acc: 0.121000

```

(Epoch 20 / 20) train acc: 1.000000; val\_acc: 0.121000



## Inline Question 2:

Did you notice anything about the comparative difficulty of training the three-layer net vs training the five layer net? In particular, based on your experience, which network seemed more sensitive to the initialization scale? Why do you think that is the case?

## Answer:

Comparatively, training the five layer net is more sensitive than the three layer net to the weight scale. Theoretically, with a deeper network, the probability of resulting in a near zero gradient is higher for a five layer network. A smaller weight scale results in a weight matrix that contains value very close to zero. Therefore, training a five layer net is more difficult.



# Update rules

So far we have used vanilla stochastic gradient descent (SGD) as our update rule. More sophisticated update rules can make it easier to train deep networks. We will implement a few of the most commonly used update rules and compare them to vanilla SGD.

## SGD+Momentum

Stochastic gradient descent with momentum is a widely used update rule that tends to make deep networks converge faster than vanilla stochastic gradient descent. See the Momentum Update section at <https://compsci682-fa19.github.io/notes/neural-networks-3/#sgd> for more information.

Open the file `cs682/optim.py` and read the documentation at the top of the file to make sure you understand the API. Implement the SGD+momentum update rule in the function `sgd_momentum` and run the following to check your implementation. You should see errors less than  $e-8$ .

```
In [ ]: from cs682.optim import sgd_momentum

N, D = 4, 5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)

config = {'learning_rate': 1e-3, 'velocity': v}
next_w, _ = sgd_momentum(w, dw, config=config)

expected_next_w = np.asarray([
    [ 0.1406,      0.20738947,  0.27417895,  0.34096842,  0.40775789],
    [ 0.47454737,  0.54133684,  0.60812632,  0.67491579,  0.74170526],
    [ 0.80849474,  0.87528421,  0.94207368,  1.00886316,  1.07565263],
    [ 1.14244211,  1.20923158,  1.27602105,  1.34281053,  1.4096      ]])
expected_velocity = np.asarray([
    [ 0.5406,      0.55475789,  0.56891579,  0.58307368,  0.59723158],
    [ 0.61138947,  0.62554737,  0.63970526,  0.65386316,  0.66802105],
    [ 0.68217895,  0.69633684,  0.71049474,  0.72465263,  0.73881053],
    [ 0.75296842,  0.76712632,  0.78128421,  0.79544211,  0.8096      ]])

# Should see relative errors around e-8 or less
print('next_w error: ', rel_error(next_w, expected_next_w))
print('velocity error: ', rel_error(expected_velocity, config['velocity']))

next_w error:  8.882347033505819e-09
velocity error:  4.269287743278663e-09
```

Once you have done so, run the following to train a six-layer network with both SGD and SGD+momentum. You should see the SGD+momentum update rule converge faster.

```

In [ ]: num_train = 4000
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}

solvers = {}

for update_rule in ['sgd', 'sgd_momentum']:
    print('running with ', update_rule)
    model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e-2)

    solver = Solver(model, small_data,
                    num_epochs=5, batch_size=100,
                    update_rule=update_rule,
                    optim_config={
                        'learning_rate': 1e-2,
                    },
                    verbose=True)
    solvers[update_rule] = solver
    solver.train()
    print()

plt.subplot(3, 1, 1)
plt.title('Training loss')
plt.xlabel('Iteration')

plt.subplot(3, 1, 2)
plt.title('Training accuracy')
plt.xlabel('Epoch')

plt.subplot(3, 1, 3)
plt.title('Validation accuracy')
plt.xlabel('Epoch')

for update_rule, solver in list(solvers.items()):
    plt.subplot(3, 1, 1)
    plt.plot(solver.loss_history, 'o', label=update_rule)

    plt.subplot(3, 1, 2)
    plt.plot(solver.train_acc_history, '-o', label=update_rule)

    plt.subplot(3, 1, 3)
    plt.plot(solver.val_acc_history, '-o', label=update_rule)

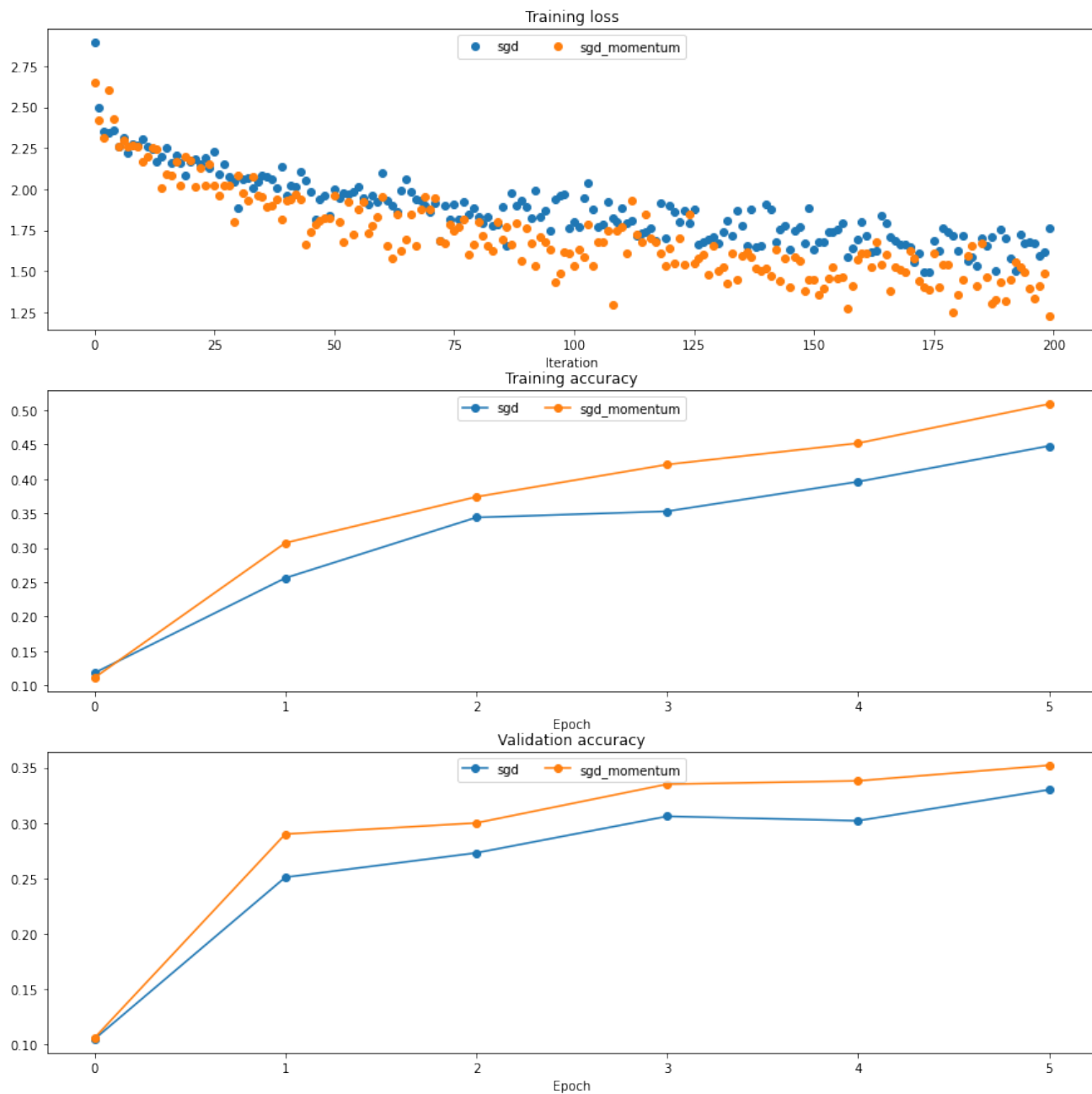
for i in [1, 2, 3]:
    plt.subplot(3, 1, i)
    plt.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()

```

```
running with  sgd
(Iteration 1 / 200) loss: 2.892030
(Epoch 0 / 5) train acc: 0.118000; val_acc: 0.105000
(Iteration 11 / 200) loss: 2.306456
(Iteration 21 / 200) loss: 2.167712
(Iteration 31 / 200) loss: 1.887985
(Epoch 1 / 5) train acc: 0.256000; val_acc: 0.251000
(Iteration 41 / 200) loss: 1.963153
(Iteration 51 / 200) loss: 1.996380
(Iteration 61 / 200) loss: 2.100925
(Iteration 71 / 200) loss: 1.858413
(Epoch 2 / 5) train acc: 0.344000; val_acc: 0.273000
(Iteration 81 / 200) loss: 1.830829
(Iteration 91 / 200) loss: 1.894846
(Iteration 101 / 200) loss: 1.802678
(Iteration 111 / 200) loss: 1.885525
(Epoch 3 / 5) train acc: 0.353000; val_acc: 0.306000
(Iteration 121 / 200) loss: 1.899826
(Iteration 131 / 200) loss: 1.666254
(Iteration 141 / 200) loss: 1.904150
(Iteration 151 / 200) loss: 1.635012
(Epoch 4 / 5) train acc: 0.396000; val_acc: 0.302000
(Iteration 161 / 200) loss: 1.797264
(Iteration 171 / 200) loss: 1.650398
(Iteration 181 / 200) loss: 1.621528
(Iteration 191 / 200) loss: 1.702303
(Epoch 5 / 5) train acc: 0.448000; val_acc: 0.330000
```

```
running with  sgd_momentum
(Iteration 1 / 200) loss: 2.646718
(Epoch 0 / 5) train acc: 0.111000; val_acc: 0.106000
(Iteration 11 / 200) loss: 2.168570
(Iteration 21 / 200) loss: 2.171446
(Iteration 31 / 200) loss: 2.081655
(Epoch 1 / 5) train acc: 0.307000; val_acc: 0.290000
(Iteration 41 / 200) loss: 1.933798
(Iteration 51 / 200) loss: 1.961929
(Iteration 61 / 200) loss: 1.951344
(Iteration 71 / 200) loss: 1.874775
(Epoch 2 / 5) train acc: 0.374000; val_acc: 0.300000
(Iteration 81 / 200) loss: 1.799770
(Iteration 91 / 200) loss: 1.763808
(Iteration 101 / 200) loss: 1.530414
(Iteration 111 / 200) loss: 1.771866
(Epoch 3 / 5) train acc: 0.421000; val_acc: 0.335000
(Iteration 121 / 200) loss: 1.637487
(Iteration 131 / 200) loss: 1.500750
(Iteration 141 / 200) loss: 1.513954
(Iteration 151 / 200) loss: 1.446814
(Epoch 4 / 5) train acc: 0.452000; val_acc: 0.338000
(Iteration 161 / 200) loss: 1.606870
(Iteration 171 / 200) loss: 1.627762
(Iteration 181 / 200) loss: 1.354447
(Iteration 191 / 200) loss: 1.320819
(Epoch 5 / 5) train acc: 0.509000; val_acc: 0.352000
```

```
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:39: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance
.
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:42: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance
.
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:45: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance
.
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:49: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance
.
```



# RMSProp and Adam

RMSProp [1] and Adam [2] are update rules that set per-parameter learning rates by using a running average of the second moments of gradients.

In the file `cs682/optim.py`, implement the RMSProp update rule in the `rmsprop` function and implement the Adam update rule in the `adam` function, and check your implementations using the tests below.

**NOTE:** Please implement the *complete* Adam update rule (with the bias correction mechanism), not the first simplified version mentioned in the course notes.

[1] Tijmen Tieleman and Geoffrey Hinton. "Lecture 6.5-rmsprop: Divide the gradient by a running average of its recent magnitude." COURSERA: Neural Networks for Machine Learning 4 (2012).

[2] Diederik Kingma and Jimmy Ba, "Adam: A Method for Stochastic Optimization", ICLR 2015.

```
In [ ]: # Test RMSProp implementation
from cs682.optim import rmsprop

N, D = 4, 5
w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
cache = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)

config = {'learning_rate': 1e-2, 'cache': cache}
next_w, _ = rmsprop(w, dw, config=config)

expected_next_w = np.asarray([
    [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
    [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
    [ 0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
    [ 0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
expected_cache = np.asarray([
    [ 0.5976, 0.6126277, 0.6277108, 0.64284931, 0.65804321],
    [ 0.67329252, 0.68859723, 0.70395734, 0.71937285, 0.73484377],
    [ 0.75037008, 0.7659518, 0.78158892, 0.79728144, 0.81302936],
    [ 0.82883269, 0.84469141, 0.86060554, 0.87657507, 0.8926 ]])

# You should see relative errors around e-7 or less
print('next_w error: ', rel_error(expected_next_w, next_w))
print('cache error: ', rel_error(expected_cache, config['cache']))

next_w error: 9.524687511038133e-08
cache error: 2.6477955807156126e-09
```

```

In [ ]: # Test Adam implementation
        from cs682.optim import adam

        N, D = 4, 5
        w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
        dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
        m = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
        v = np.linspace(0.7, 0.5, num=N*D).reshape(N, D)

        config = {'learning_rate': 1e-2, 'm': m, 'v': v, 't': 5}
        next_w, _ = adam(w, dw, config=config)

        expected_next_w = np.asarray([
            [-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],
            [-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],
            [ 0.1248705, 0.17744702, 0.23002243, 0.28259667, 0.33516969],
            [ 0.38774145, 0.44031188, 0.49288093, 0.54544852, 0.59801459]])
        expected_v = np.asarray([
            [ 0.69966, 0.68908382, 0.67851319, 0.66794809, 0.65738853,],
            [ 0.64683452, 0.63628604, 0.6257431, 0.61520571, 0.60467385,],
            [ 0.59414753, 0.58362676, 0.57311152, 0.56260183, 0.55209767,],
            [ 0.54159906, 0.53110598, 0.52061845, 0.51013645, 0.49966, ]])
        expected_m = np.asarray([
            [ 0.48, 0.49947368, 0.51894737, 0.53842105, 0.55789474],
            [ 0.57736842, 0.59684211, 0.61631579, 0.63578947, 0.65526316],
            [ 0.67473684, 0.69421053, 0.71368421, 0.73315789, 0.75263158],
            [ 0.77210526, 0.79157895, 0.81105263, 0.83052632, 0.85 ]])

        # You should see relative errors around e-7 or less
        print('next_w error: ', rel_error(expected_next_w, next_w))
        print('v error: ', rel_error(expected_v, config['v']))
        print('m error: ', rel_error(expected_m, config['m']))

        next_w error: 1.1395691798535431e-07
        v error: 4.208314038113071e-09
        m error: 4.214963193114416e-09

```

Once you have debugged your RMSProp and Adam implementations, run the following to train a pair of deep networks using these new update rules:



```

In [ ]: learning_rates = {'rmsprop': 1e-4, 'adam': 1e-3}
for update_rule in ['adam', 'rmsprop']:
    print('running with ', update_rule)
    model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e-2)

    solver = Solver(model, small_data,
                    num_epochs=5, batch_size=100,
                    update_rule=update_rule,
                    optim_config={
                        'learning_rate': learning_rates[update_rule]
                    },
                    verbose=True)
    solvers[update_rule] = solver
    solver.train()
    print()

plt.subplot(3, 1, 1)
plt.title('Training loss')
plt.xlabel('Iteration')

plt.subplot(3, 1, 2)
plt.title('Training accuracy')
plt.xlabel('Epoch')

plt.subplot(3, 1, 3)
plt.title('Validation accuracy')
plt.xlabel('Epoch')

for update_rule, solver in list(solvers.items()):
    plt.subplot(3, 1, 1)
    plt.plot(solver.loss_history, 'o', label=update_rule)

    plt.subplot(3, 1, 2)
    plt.plot(solver.train_acc_history, '-o', label=update_rule)

    plt.subplot(3, 1, 3)
    plt.plot(solver.val_acc_history, '-o', label=update_rule)

for i in [1, 2, 3]:
    plt.subplot(3, 1, i)
    plt.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show()

```

```

running with adam
(Iteration 1 / 200) loss: 2.490469
(Epoch 0 / 5) train acc: 0.134000; val_acc: 0.129000
(Iteration 11 / 200) loss: 1.973660
(Iteration 21 / 200) loss: 1.953040
(Iteration 31 / 200) loss: 1.892135
(Epoch 1 / 5) train acc: 0.350000; val_acc: 0.322000
(Iteration 41 / 200) loss: 1.713873
(Iteration 51 / 200) loss: 1.828796

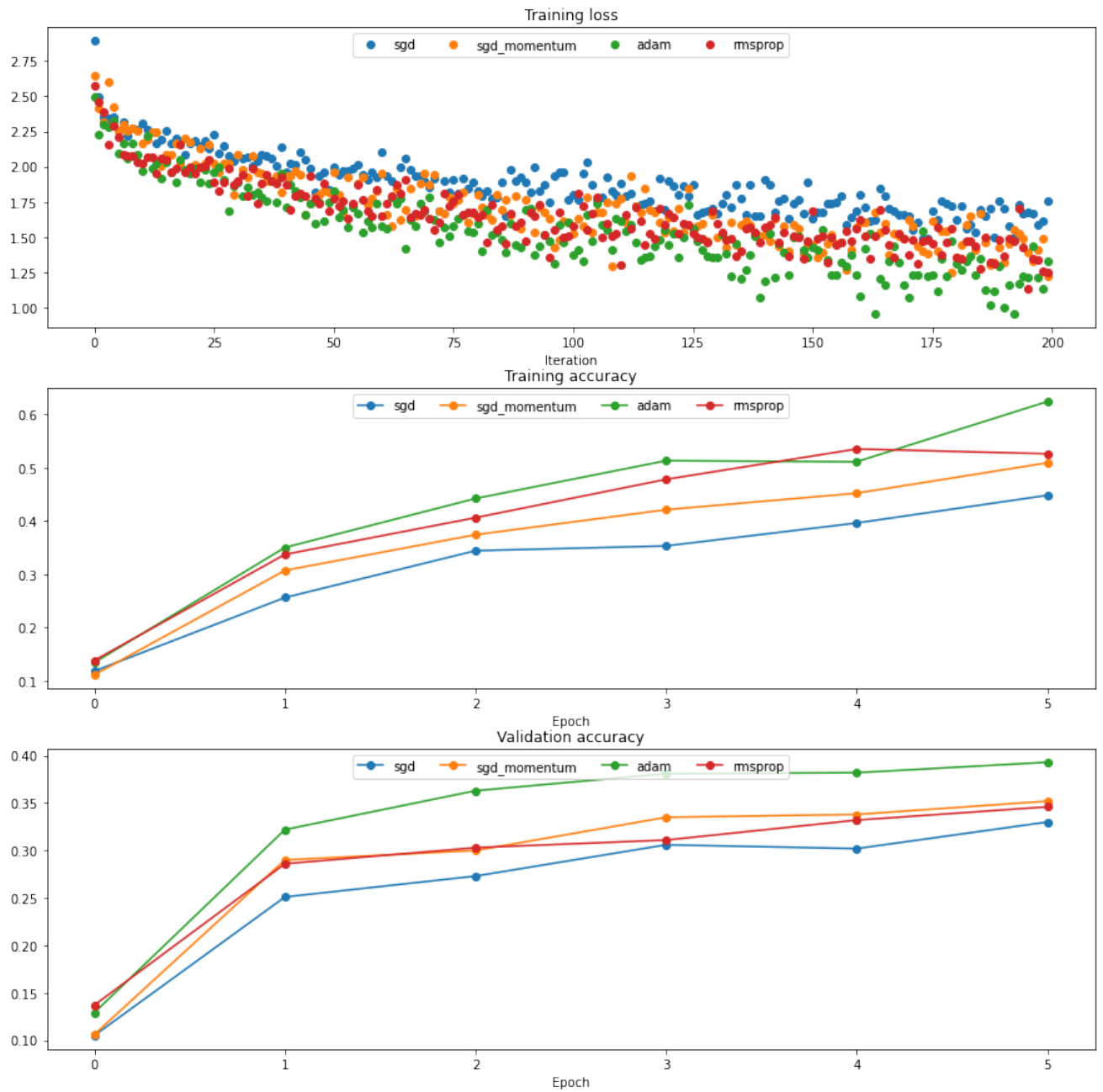
```

```
(Iteration 61 / 200) loss: 1.575631
(Iteration 71 / 200) loss: 1.781359
(Epoch 2 / 5) train acc: 0.442000; val_acc: 0.363000
(Iteration 81 / 200) loss: 1.594522
(Iteration 91 / 200) loss: 1.696074
(Iteration 101 / 200) loss: 1.378397
(Iteration 111 / 200) loss: 1.612359
(Epoch 3 / 5) train acc: 0.513000; val_acc: 0.381000
(Iteration 121 / 200) loss: 1.448592
(Iteration 131 / 200) loss: 1.360336
(Iteration 141 / 200) loss: 1.184235
(Iteration 151 / 200) loss: 1.424340
(Epoch 4 / 5) train acc: 0.511000; val_acc: 0.382000
(Iteration 161 / 200) loss: 1.083490
(Iteration 171 / 200) loss: 1.072450
(Iteration 181 / 200) loss: 1.315783
(Iteration 191 / 200) loss: 0.998149
(Epoch 5 / 5) train acc: 0.624000; val_acc: 0.393000
```

running with rmsprop

```
(Iteration 1 / 200) loss: 2.574417
(Epoch 0 / 5) train acc: 0.138000; val_acc: 0.137000
(Iteration 11 / 200) loss: 2.021802
(Iteration 21 / 200) loss: 1.997881
(Iteration 31 / 200) loss: 1.901340
(Epoch 1 / 5) train acc: 0.337000; val_acc: 0.286000
(Iteration 41 / 200) loss: 1.869426
(Iteration 51 / 200) loss: 1.772157
(Iteration 61 / 200) loss: 1.649632
(Iteration 71 / 200) loss: 1.629210
(Epoch 2 / 5) train acc: 0.406000; val_acc: 0.303000
(Iteration 81 / 200) loss: 1.639434
(Iteration 91 / 200) loss: 1.475039
(Iteration 101 / 200) loss: 1.579245
(Iteration 111 / 200) loss: 1.307083
(Epoch 3 / 5) train acc: 0.478000; val_acc: 0.311000
(Iteration 121 / 200) loss: 1.672531
(Iteration 131 / 200) loss: 1.596700
(Iteration 141 / 200) loss: 1.566642
(Iteration 151 / 200) loss: 1.688949
(Epoch 4 / 5) train acc: 0.535000; val_acc: 0.332000
(Iteration 161 / 200) loss: 1.625567
(Iteration 171 / 200) loss: 1.375148
(Iteration 181 / 200) loss: 1.354166
(Iteration 191 / 200) loss: 1.365568
(Epoch 5 / 5) train acc: 0.526000; val_acc: 0.346000
```

```
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:30: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance
.
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:33: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance
.
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:36: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance
.
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:40: MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance
.
```



## Inline Question 3:

AdaGrad, like Adam, is a per-parameter optimization method that uses the following update rule:

```
cache += dw**2
w += - learning_rate * dw / (np.sqrt(cache) + eps)
```

John notices that when he was training a network with AdaGrad that the updates became very small, and that his network was learning slowly. Using your knowledge of the AdaGrad update rule, why do you think the updates would become very small? Would Adam have the same issue?

## Answer:

The updates to the weight matrix become very small when using AdaGrad as we use the inverse of the square root of the cache. As  $dw$  gets larger, so does the cache. The cache is inversely proportional to the updates and so the network learns slowly. On the other hand, Adam converges much faster and therefore, the updates aren't small.

## Train a good model!

Train the best fully-connected model that you can on CIFAR-10, storing your best model in the `best_model` variable. We require you to get at least 50% accuracy on the validation set using a fully-connected net.

If you are careful it should be possible to get accuracies above 55%, but we don't require it for this part and won't assign extra credit for doing so. Later in the assignment we will ask you to train the best convolutional network that you can on CIFAR-10, and we would prefer that you spend your effort working on convolutional nets rather than fully-connected nets.

You might find it useful to complete the `BatchNormalization.ipynb` and `Dropout.ipynb` notebooks before completing this part, since those techniques can help you train powerful models.

```

In [ ]: best_model = None
#####
# TODO: Train the best FullyConnectedNet that you can on CIFAR-10. You might
# find batch/layer normalization and dropout useful. Store your best model in
# the best_model variable.
#####
best_model = FullyConnectedNet([100, 100, 100, 100], weight_scale=2.2e-2, reg
solver = Solver(best_model, data, optim_config={'learning_rate':7e-4},
                update_rule='adam', lr_decay=0.95, batch_size=200,
                num_epochs=15, print_every=200)

solver.train()
#####
#                                     END OF YOUR CODE
#####

(Iteration 1 / 3675) loss: 2.918921
(Epoch 0 / 15) train acc: 0.118000; val_acc: 0.132000
(Iteration 201 / 3675) loss: 1.773957
(Epoch 1 / 15) train acc: 0.471000; val_acc: 0.433000
(Iteration 401 / 3675) loss: 1.632250
(Epoch 2 / 15) train acc: 0.523000; val_acc: 0.481000
(Iteration 601 / 3675) loss: 1.585608
(Epoch 3 / 15) train acc: 0.493000; val_acc: 0.487000
(Iteration 801 / 3675) loss: 1.524758
(Epoch 4 / 15) train acc: 0.530000; val_acc: 0.506000
(Iteration 1001 / 3675) loss: 1.586086
(Iteration 1201 / 3675) loss: 1.419532
(Epoch 5 / 15) train acc: 0.504000; val_acc: 0.486000
(Iteration 1401 / 3675) loss: 1.483047
(Epoch 6 / 15) train acc: 0.538000; val_acc: 0.513000
(Iteration 1601 / 3675) loss: 1.477452
(Epoch 7 / 15) train acc: 0.537000; val_acc: 0.513000
(Iteration 1801 / 3675) loss: 1.552910
(Epoch 8 / 15) train acc: 0.576000; val_acc: 0.509000
(Iteration 2001 / 3675) loss: 1.541834
(Iteration 2201 / 3675) loss: 1.344541
(Epoch 9 / 15) train acc: 0.605000; val_acc: 0.519000
(Iteration 2401 / 3675) loss: 1.148851
(Epoch 10 / 15) train acc: 0.586000; val_acc: 0.529000
(Iteration 2601 / 3675) loss: 1.312740
(Epoch 11 / 15) train acc: 0.589000; val_acc: 0.536000
(Iteration 2801 / 3675) loss: 1.424538
(Epoch 12 / 15) train acc: 0.599000; val_acc: 0.534000
(Iteration 3001 / 3675) loss: 1.232623
(Epoch 13 / 15) train acc: 0.613000; val_acc: 0.557000
(Iteration 3201 / 3675) loss: 1.279335
(Iteration 3401 / 3675) loss: 1.291203
(Epoch 14 / 15) train acc: 0.594000; val_acc: 0.544000
(Iteration 3601 / 3675) loss: 1.185682
(Epoch 15 / 15) train acc: 0.627000; val_acc: 0.531000

```

# Test your model!

Run your best model on the validation and test sets. You should achieve above 50% accuracy on the validation set.

```
In [ ]: y_test_pred = np.argmax(best_model.loss(data['X_test']), axis=1)
        y_val_pred = np.argmax(best_model.loss(data['X_val']), axis=1)
        print('Validation set accuracy: ', (y_val_pred == data['y_val']).mean())
        print('Test set accuracy: ', (y_test_pred == data['y_test']).mean())
```

```
Validation set accuracy:  0.557
Test set accuracy:  0.537
```

```
In [ ]: from google.colab import drive  
drive.mount('/content/drive')
```

Mounted at /content/drive

```
In [ ]: %cd drive/'My Drive'/assignment2
```

/content/drive/My Drive/assignment2



# Batch Normalization

One way to make deep networks easier to train is to use more sophisticated optimization procedures such as SGD+momentum, RMSProp, or Adam. Another strategy is to change the architecture of the network to make it easier to train. One idea along these lines is batch normalization which was proposed by [3] in 2015.

The idea is relatively straightforward. Machine learning methods tend to work better when their input data consists of uncorrelated features with zero mean and unit variance. When training a neural network, we can preprocess the data before feeding it to the network to explicitly decorrelate its features; this will ensure that the first layer of the network sees data that follows a nice distribution. However, even if we preprocess the input data, the activations at deeper layers of the network will likely no longer be decorrelated and will no longer have zero mean or unit variance since they are output from earlier layers in the network. Even worse, during the training process the distribution of features at each layer of the network will shift as the weights of each layer are updated.

The authors of [3] hypothesize that the shifting distribution of features inside deep neural networks may make training deep networks more difficult. To overcome this problem, [3] proposes to insert batch normalization layers into the network. At training time, a batch normalization layer uses a minibatch of data to estimate the mean and standard deviation of each feature. These estimated means and standard deviations are then used to center and normalize the features of the minibatch. A running average of these means and standard deviations is kept during training, and at test time these running averages are used to center and normalize features.

It is possible that this normalization strategy could reduce the representational power of the network, since it may sometimes be optimal for certain layers to have features that are not zero-mean or unit variance. To this end, the batch normalization layer includes learnable shift and scale parameters for each feature dimension.

[3] [Sergey Ioffe and Christian Szegedy, "Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift", ICML 2015.](#)

```
In [ ]: # As usual, a bit of setup
import time
import numpy as np
import matplotlib.pyplot as plt
from cs682.classifiers.fc_net import *
from cs682.data_utils import get_CIFAR10_data
from cs682.gradient_check import eval_numerical_gradient, eval_numerical_grad
from cs682.solver import Solver

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipy
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))

def print_mean_std(x,axis=0):
    print(' means: ', x.mean(axis=axis))
    print(' stds: ', x.std(axis=axis))
    print()
```

```
In [ ]: # Load the (preprocessed) CIFAR10 data.
data = get_CIFAR10_data()
for k, v in data.items():
    print('%s: ' % k, v.shape)
```

```
X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

## Batch normalization: forward

In the file `cs682/layers.py`, implement the batch normalization forward pass in the function `batchnorm_forward`. Once you have done so, run the following to test your implementation.

Referencing the paper linked to above would be helpful!

```

In [ ]: # Check the training-time forward pass by checking means and variances
        # of features both before and after batch normalization

        # Simulate the forward pass for a two-layer network
        np.random.seed(231)
        N, D1, D2, D3 = 200, 50, 60, 3
        X = np.random.randn(N, D1)
        W1 = np.random.randn(D1, D2)
        W2 = np.random.randn(D2, D3)
        a = np.maximum(0, X.dot(W1)).dot(W2)

        print('Before batch normalization:')
        print_mean_std(a,axis=0)

        gamma = np.ones((D3,))
        beta = np.zeros((D3,))
        # Means should be close to zero and stds close to one
        print('After batch normalization (gamma=1, beta=0)')
        a_norm, _ = batchnorm_forward(a, gamma, beta, {'mode': 'train'})
        print_mean_std(a_norm,axis=0)

        gamma = np.asarray([1.0, 2.0, 3.0])
        beta = np.asarray([11.0, 12.0, 13.0])
        # Now means should be close to beta and stds close to gamma
        print('After batch normalization (gamma=', gamma, ', beta=', beta, ')')
        a_norm, _ = batchnorm_forward(a, gamma, beta, {'mode': 'train'})
        print_mean_std(a_norm,axis=0)

```

Before batch normalization:

```

means:  [ -2.3814598  -13.18038246   1.91780462]
stds:   [27.18502186  34.21455511  37.68611762]

```

After batch normalization (gamma=1, beta=0)

```

means:  [5.32907052e-17  7.04991621e-17  1.85962357e-17]
stds:   [0.99999999  1.          1.          ]

```

After batch normalization (gamma= [1. 2. 3.] , beta= [11. 12. 13.] )

```

means:  [11. 12. 13.]
stds:   [0.99999999  1.99999999  2.99999999]

```

```
In [ ]: # Check the test-time forward pass by running the training-time
# forward pass many times to warm up the running averages, and then
# checking the means and variances of activations after a test-time
# forward pass.

np.random.seed(231)
N, D1, D2, D3 = 200, 50, 60, 3
W1 = np.random.randn(D1, D2)
W2 = np.random.randn(D2, D3)

bn_param = {'mode': 'train'}
gamma = np.ones(D3)
beta = np.zeros(D3)

for t in range(50):
    X = np.random.randn(N, D1)
    a = np.maximum(0, X.dot(W1)).dot(W2)
    batchnorm_forward(a, gamma, beta, bn_param)

bn_param['mode'] = 'test'
X = np.random.randn(N, D1)
a = np.maximum(0, X.dot(W1)).dot(W2)
a_norm, _ = batchnorm_forward(a, gamma, beta, bn_param)

# Means should be close to zero and stds close to one, but will be
# noisier than training-time forward passes.
print('After batch normalization (test-time):')
print_mean_std(a_norm,axis=0)
```

```
After batch normalization (test-time):
means:  [-0.03927354 -0.04349152 -0.10452688]
stds:   [1.01531428 1.01238373 0.97819988]
```

## Batch normalization: backward

Now implement the backward pass for batch normalization in the function `batchnorm_backward`.

To derive the backward pass you should write out the computation graph for batch normalization and backprop through each of the intermediate nodes. Some intermediates may have multiple outgoing branches; make sure to sum gradients across these branches in the backward pass.

Once you have finished, run the following to numerically check your backward pass.

```
In [ ]: # Gradient check batchnorm backward pass
np.random.seed(231)
N, D = 4, 5
x = 5 * np.random.randn(N, D) + 12
gamma = np.random.randn(D)
beta = np.random.randn(D)
dout = np.random.randn(N, D)

bn_param = {'mode': 'train'}
fx = lambda x: batchnorm_forward(x, gamma, beta, bn_param)[0]
fg = lambda a: batchnorm_forward(x, a, beta, bn_param)[0]
fb = lambda b: batchnorm_forward(x, gamma, b, bn_param)[0]

dx_num = eval_numerical_gradient_array(fx, x, dout)
da_num = eval_numerical_gradient_array(fg, gamma.copy(), dout)
db_num = eval_numerical_gradient_array(fb, beta.copy(), dout)

_, cache = batchnorm_forward(x, gamma, beta, bn_param)
dx, dgamma, dbeta = batchnorm_backward(dout, cache)
#You should expect to see relative errors between 1e-13 and 1e-8
print('dx error: ', rel_error(dx_num, dx))
print('dgamma error: ', rel_error(da_num, dgamma))
print('dbeta error: ', rel_error(db_num, dbeta))
```

```
dx error: 1.7029227094228273e-09
dgamma error: 7.420414216247087e-13
dbeta error: 2.8795057655839487e-12
```

## Batch normalization: alternative backward

In class we talked about two different implementations for the sigmoid backward pass. One strategy is to write out a computation graph composed of simple operations and backprop through all intermediate values. Another strategy is to work out the derivatives on paper. For example, you can derive a very simple formula for the sigmoid function's backward pass by simplifying gradients on paper.

Surprisingly, it turns out that you can do a similar simplification for the batch normalization backward pass too.

Given a set of inputs  $X = \begin{bmatrix} x_1 \\ x_2 \\ \dots \\ x_N \end{bmatrix}$ , we first calculate the mean  $\mu = \frac{1}{N} \sum_{k=1}^N x_k$  and

variance  $v = \frac{1}{N} \sum_{k=1}^N (x_k - \mu)^2$ .

With  $\mu$  and  $v$  calculated, we can calculate the standard deviation  $\sigma = \sqrt{v + \epsilon}$  and normalized data  $Y$  with  $y_i = \frac{x_i - \mu}{\sigma}$ .

The meat of our problem is to get  $\frac{\partial L}{\partial X}$  from the upstream gradient  $\frac{\partial L}{\partial Y}$ . It might be challenging to directly reason about the gradients over  $X$  and  $Y$  - try reasoning about it in terms of  $x_i$  and  $y_i$  first.

You will need to come up with the derivations for  $\frac{\partial L}{\partial x_i}$ , by relying on the Chain Rule to first calculate the intermediate  $\frac{\partial \mu}{\partial x_i}$ ,  $\frac{\partial v}{\partial x_i}$ ,  $\frac{\partial \sigma}{\partial x_i}$ , then assemble these pieces to calculate  $\frac{\partial y_i}{\partial x_i}$ . You should make sure each of the intermediary steps are all as simple as possible.

After doing so, implement the simplified batch normalization backward pass in the function `batchnorm_backward_alt` and compare the two implementations by running the following. Your two implementations should compute nearly identical results, but the alternative implementation should be a bit faster.

```
In [ ]: np.random.seed(231)
N, D = 100, 500
x = 5 * np.random.randn(N, D) + 12
gamma = np.random.randn(D)
beta = np.random.randn(D)
dout = np.random.randn(N, D)

bn_param = {'mode': 'train'}
out, cache = batchnorm_forward(x, gamma, beta, bn_param)

t1 = time.time()
dx1, dgamma1, dbeta1 = batchnorm_backward(dout, cache)
t2 = time.time()
dx2, dgamma2, dbeta2 = batchnorm_backward_alt(dout, cache)
t3 = time.time()

print('dx difference: ', rel_error(dx1, dx2))
print('dgamma difference: ', rel_error(dgamma1, dgamma2))
print('dbeta difference: ', rel_error(dbeta1, dbeta2))
print('speedup: %.2fx' % ((t2 - t1) / (t3 - t2)))
```

```
dx difference: 1.5046082106329495e-11
dgamma difference: 0.0
dbeta difference: 0.0
speedup: 1.98x
```

## Fully Connected Nets with Batch Normalization

Now that you have a working implementation for batch normalization, go back to your `FullyConnectedNet` in the file `cs682/classifiers/fc_net.py`. Modify your implementation to add batch normalization.

Concretely, when the `normalization` flag is set to `"batchnorm"` in the constructor, you should insert a batch normalization layer before each ReLU nonlinearity. The outputs from the last layer of the network should not be normalized. Once you are done, run the following to gradient-check your implementation.

HINT: You might find it useful to define an additional helper layer similar to those in the file `cs682/layer_utils.py`. If you decide to do so, do it in the file `cs682/classifiers/fc_net.py`.

```

In [ ]: np.random.seed(231)
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))

# You should expect losses between 1e-4~1e-10 for W,
# losses between 1e-08~1e-10 for b,
# and losses between 1e-08~1e-09 for beta and gammas.
for reg in [0, 3.14]:
    print('Running check with reg = ', reg)
    model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                              reg=reg, weight_scale=5e-2, dtype=np.float64,
                              normalization='batchnorm')

    loss, grads = model.loss(X, y)
    print('Initial loss: ', loss)

    for name in sorted(grads):
        f = lambda _: model.loss(X, y)[0]
        grad_num = eval_numerical_gradient(f, model.params[name], verbose=False,
        print('%s relative error: %.2e' % (name, rel_error(grad_num, grads[name]))
    if reg == 0: print()

```

```

Running check with reg = 0
Initial loss: 2.2611955101340957
W1 relative error: 1.10e-04
W2 relative error: 2.85e-06
W3 relative error: 4.05e-10
b1 relative error: 8.44e-06
b2 relative error: 2.22e-08
b3 relative error: 1.01e-10
beta1 relative error: 7.33e-09
beta2 relative error: 1.89e-09
gamma1 relative error: 6.96e-09
gamma2 relative error: 1.96e-09

```

```

Running check with reg = 3.14
Initial loss: 6.996533220108303
W1 relative error: 1.98e-06
W2 relative error: 2.29e-06
W3 relative error: 2.79e-08
b1 relative error: 3.02e-06
b2 relative error: 1.62e-06
b3 relative error: 2.10e-10
beta1 relative error: 6.65e-09
beta2 relative error: 4.23e-09
gamma1 relative error: 6.27e-09
gamma2 relative error: 5.28e-09

```



# Batchnorm for deep networks

Run the following to train a six-layer network on a subset of 1000 training examples both with and without batch normalization.

```
In [ ]: np.random.seed(231)
# Try training a very deep net with batchnorm
hidden_dims = [100, 100, 100, 100, 100]

num_train = 1000
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}

weight_scale = 2e-2
bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, normalizati
model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, normalizati

bn_solver = Solver(bn_model, small_data,
                    num_epochs=10, batch_size=50,
                    update_rule='adam',
                    optim_config={
                        'learning_rate': 1e-3,
                    },
                    verbose=True, print_every=20)
bn_solver.train()

solver = Solver(model, small_data,
                num_epochs=10, batch_size=50,
                update_rule='adam',
                optim_config={
                    'learning_rate': 1e-3,
                },
                verbose=True, print_every=20)
solver.train()
```

```
(Iteration 1 / 200) loss: 2.340975
(Epoch 0 / 10) train acc: 0.107000; val_acc: 0.115000
(Epoch 1 / 10) train acc: 0.313000; val_acc: 0.263000
(Iteration 21 / 200) loss: 2.039345
(Epoch 2 / 10) train acc: 0.399000; val_acc: 0.284000
(Iteration 41 / 200) loss: 2.047471
(Epoch 3 / 10) train acc: 0.484000; val_acc: 0.316000
(Iteration 61 / 200) loss: 1.739554
(Epoch 4 / 10) train acc: 0.524000; val_acc: 0.318000
(Iteration 81 / 200) loss: 1.246973
(Epoch 5 / 10) train acc: 0.593000; val_acc: 0.335000
(Iteration 101 / 200) loss: 1.353802
(Epoch 6 / 10) train acc: 0.645000; val_acc: 0.326000
(Iteration 121 / 200) loss: 1.004578
(Epoch 7 / 10) train acc: 0.669000; val_acc: 0.342000
(Iteration 141 / 200) loss: 1.198397
(Epoch 8 / 10) train acc: 0.707000; val_acc: 0.293000
(Iteration 161 / 200) loss: 0.824290
(Epoch 9 / 10) train acc: 0.801000; val_acc: 0.339000
(Iteration 181 / 200) loss: 0.767959
(Epoch 10 / 10) train acc: 0.776000; val_acc: 0.319000
(Iteration 1 / 200) loss: 2.302332
(Epoch 0 / 10) train acc: 0.129000; val_acc: 0.131000
(Epoch 1 / 10) train acc: 0.283000; val_acc: 0.250000
(Iteration 21 / 200) loss: 2.041970
(Epoch 2 / 10) train acc: 0.316000; val_acc: 0.277000
(Iteration 41 / 200) loss: 1.900473
(Epoch 3 / 10) train acc: 0.373000; val_acc: 0.282000
(Iteration 61 / 200) loss: 1.713156
(Epoch 4 / 10) train acc: 0.390000; val_acc: 0.310000
(Iteration 81 / 200) loss: 1.662209
(Epoch 5 / 10) train acc: 0.434000; val_acc: 0.300000
(Iteration 101 / 200) loss: 1.696062
(Epoch 6 / 10) train acc: 0.536000; val_acc: 0.346000
(Iteration 121 / 200) loss: 1.550785
(Epoch 7 / 10) train acc: 0.530000; val_acc: 0.310000
(Iteration 141 / 200) loss: 1.436308
(Epoch 8 / 10) train acc: 0.622000; val_acc: 0.342000
(Iteration 161 / 200) loss: 1.000868
(Epoch 9 / 10) train acc: 0.654000; val_acc: 0.328000
(Iteration 181 / 200) loss: 0.925456
(Epoch 10 / 10) train acc: 0.726000; val_acc: 0.335000
```

Run the following to visualize the results from two networks trained above. You should find that using batch normalization helps the network to converge much faster.

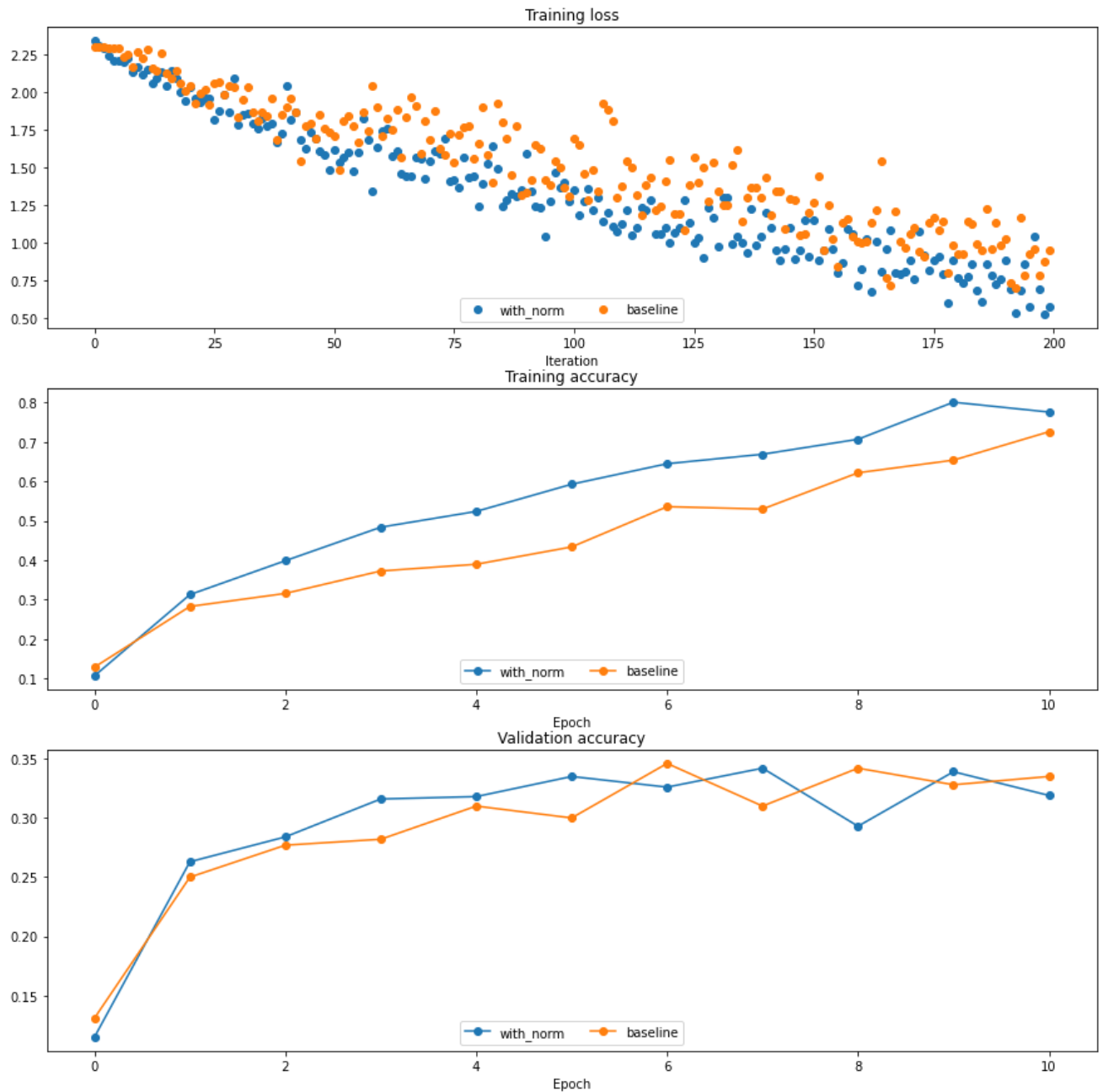
```

In [ ]: def plot_training_history(title, label, baseline, bn_solvers, plot_fn, bl_mar
        """utility function for plotting training history"""
        plt.title(title)
        plt.xlabel(label)
        bn_plots = [plot_fn(bn_solver) for bn_solver in bn_solvers]
        bl_plot = plot_fn(baseline)
        num_bn = len(bn_plots)
        for i in range(num_bn):
            label='with_norm'
            if labels is not None:
                label += str(labels[i])
            plt.plot(bn_plots[i], bn_marker, label=label)
        label='baseline'
        if labels is not None:
            label += str(labels[0])
        plt.plot(bl_plot, bl_marker, label=label)
        plt.legend(loc='lower center', ncol=num_bn+1)

plt.subplot(3, 1, 1)
plot_training_history('Training loss', 'Iteration', solver, [bn_solver], \
                      lambda x: x.loss_history, bl_marker='o', bn_marker='o')
plt.subplot(3, 1, 2)
plot_training_history('Training accuracy', 'Epoch', solver, [bn_solver], \
                      lambda x: x.train_acc_history, bl_marker='-o', bn_marke
plt.subplot(3, 1, 3)
plot_training_history('Validation accuracy', 'Epoch', solver, [bn_solver], \
                      lambda x: x.val_acc_history, bl_marker='-o', bn_marker=

plt.gcf().set_size_inches(15, 15)
plt.show()

```



## Batch normalization and initialization

We will now run a small experiment to study the interaction of batch normalization and weight initialization.

The first cell will train 8-layer networks both with and without batch normalization using different scales for weight initialization. The second layer will plot training accuracy, validation set accuracy, and training loss as a function of the weight initialization scale.

```

In [ ]: np.random.seed(231)
# Try training a very deep net with batchnorm
hidden_dims = [50, 50, 50, 50, 50, 50, 50]
num_train = 1000
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}

bn_solvers_ws = {}
solvers_ws = {}
weight_scales = np.logspace(-4, 0, num=20)
for i, weight_scale in enumerate(weight_scales):
    print('Running weight scale %d / %d' % (i + 1, len(weight_scales)))
    bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, normal
    model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, normaliza

    bn_solver = Solver(bn_model, small_data,
                        num_epochs=10, batch_size=50,
                        update_rule='adam',
                        optim_config={
                            'learning_rate': 1e-3,
                        },
                        verbose=False, print_every=200)
    bn_solver.train()
    bn_solvers_ws[weight_scale] = bn_solver

    solver = Solver(model, small_data,
                    num_epochs=10, batch_size=50,
                    update_rule='adam',
                    optim_config={
                        'learning_rate': 1e-3,
                    },
                    verbose=False, print_every=200)
    solver.train()
    solvers_ws[weight_scale] = solver

```

Running weight scale 1 / 20  
Running weight scale 2 / 20  
Running weight scale 3 / 20  
Running weight scale 4 / 20  
Running weight scale 5 / 20  
Running weight scale 6 / 20  
Running weight scale 7 / 20  
Running weight scale 8 / 20  
Running weight scale 9 / 20  
Running weight scale 10 / 20  
Running weight scale 11 / 20  
Running weight scale 12 / 20  
Running weight scale 13 / 20  
Running weight scale 14 / 20  
Running weight scale 15 / 20  
Running weight scale 16 / 20  
Running weight scale 17 / 20  
Running weight scale 18 / 20  
Running weight scale 19 / 20  
Running weight scale 20 / 20

```

In [ ]: # Plot results of weight scale experiment
best_train_accs, bn_best_train_accs = [], []
best_val_accs, bn_best_val_accs = [], []
final_train_loss, bn_final_train_loss = [], []

for ws in weight_scales:
    best_train_accs.append(max(solvers_ws[ws].train_acc_history))
    bn_best_train_accs.append(max(bn_solvers_ws[ws].train_acc_history))

    best_val_accs.append(max(solvers_ws[ws].val_acc_history))
    bn_best_val_accs.append(max(bn_solvers_ws[ws].val_acc_history))

    final_train_loss.append(np.mean(solvers_ws[ws].loss_history[-100:]))
    bn_final_train_loss.append(np.mean(bn_solvers_ws[ws].loss_history[-100:]))

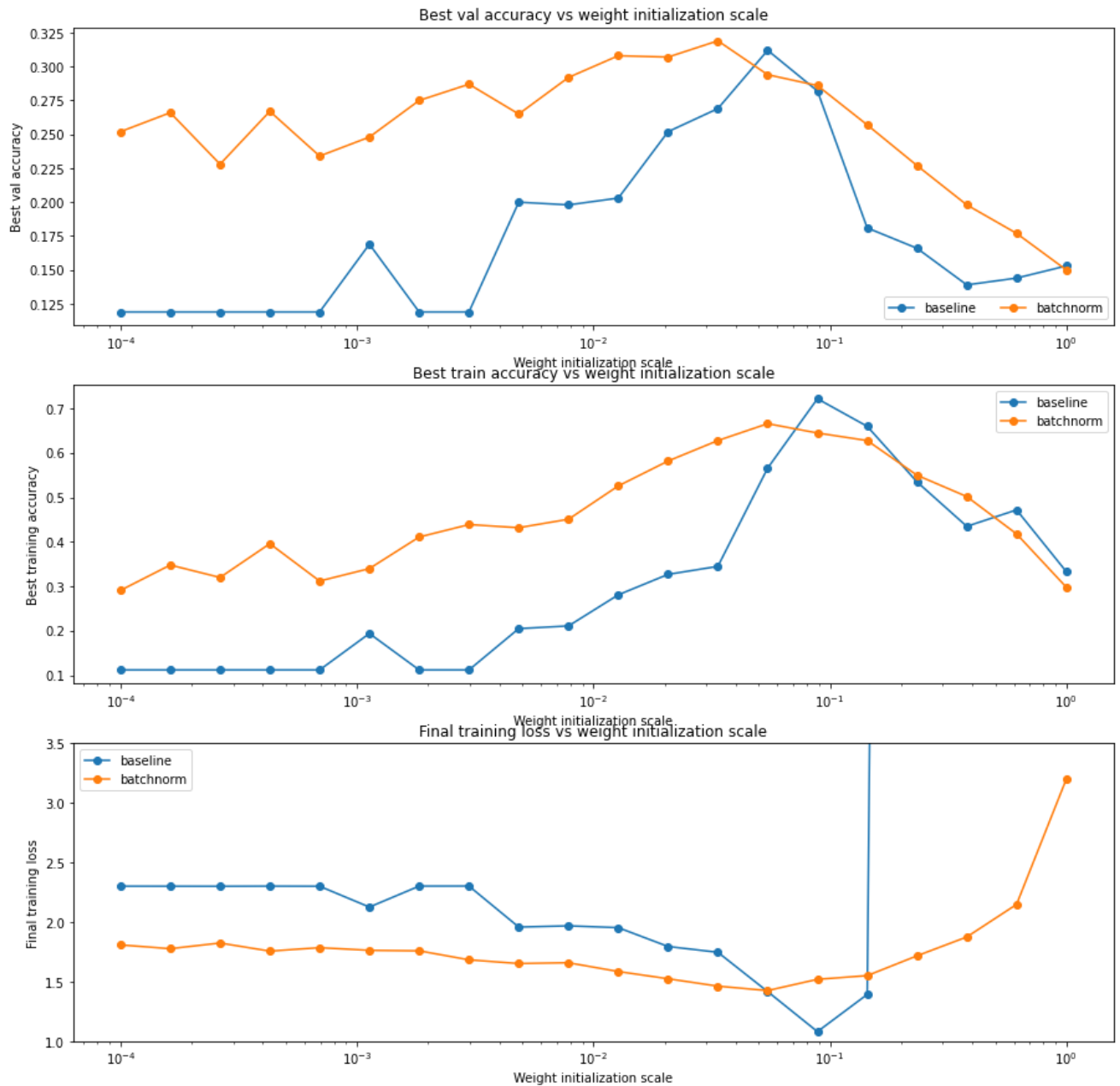
plt.subplot(3, 1, 1)
plt.title('Best val accuracy vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Best val accuracy')
plt.semilogx(weight_scales, best_val_accs, '-o', label='baseline')
plt.semilogx(weight_scales, bn_best_val_accs, '-o', label='batchnorm')
plt.legend(ncol=2, loc='lower right')

plt.subplot(3, 1, 2)
plt.title('Best train accuracy vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Best training accuracy')
plt.semilogx(weight_scales, best_train_accs, '-o', label='baseline')
plt.semilogx(weight_scales, bn_best_train_accs, '-o', label='batchnorm')
plt.legend()

plt.subplot(3, 1, 3)
plt.title('Final training loss vs weight initialization scale')
plt.xlabel('Weight initialization scale')
plt.ylabel('Final training loss')
plt.semilogx(weight_scales, final_train_loss, '-o', label='baseline')
plt.semilogx(weight_scales, bn_final_train_loss, '-o', label='batchnorm')
plt.legend()
plt.gca().set_ylim(1.0, 3.5)

plt.gcf().set_size_inches(15, 15)
plt.show()

```



## Inline Question 1:

Describe the results of this experiment. How does the scale of weight initialization affect models with/without batch normalization differently, and why?



## Answer:

We can say the following using the results of the experiments -

1. Nets using batch normalization are much less sensitive to the weight scale. As you can see in graph 1 and graph 2, the baseline net only performs well when the weight is set to  $1e-1$ . On the other hand, the net using batch normalization, has a very small variance in its validation and training accuracy over varying weight scales.
2. Batch normalization tries to solve the problem of exploding losses. Since batch norm normalizes the values at each layer with zero mean and unit variance, the gradient is never near zero. As seen in the graph 3, the loss explodes for the baseline net. On the contrary, batch norm gets better results.

## Batch normalization and batch size

We will now run a small experiment to study the interaction of batch normalization and batch size.

The first cell will train 6-layer networks both with and without batch normalization using different batch sizes. The second layer will plot training accuracy and validation set accuracy over time.

```

In [ ]: def run_batchsize_experiments(normalization_mode):
    np.random.seed(231)
    # Try training a very deep net with batchnorm
    hidden_dims = [100, 100, 100, 100, 100]
    num_train = 1000
    small_data = {
        'X_train': data['X_train'][:num_train],
        'y_train': data['y_train'][:num_train],
        'X_val': data['X_val'],
        'y_val': data['y_val'],
    }
    n_epochs=10
    weight_scale = 2e-2
    batch_sizes = [5,10,50]
    lr = 10**(-3.5)
    solver_bsize = batch_sizes[0]

    print('No normalization: batch size = ',solver_bsize)
    model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale, normaliz
    solver = Solver(model, small_data,
                    num_epochs=n_epochs, batch_size=solver_bsize,
                    update_rule='adam',
                    optim_config={
                        'learning_rate': lr,
                    },
                    verbose=False)

    solver.train()

    bn_solvers = []
    for i in range(len(batch_sizes)):
        b_size=batch_sizes[i]
        print('Normalization: batch size = ',b_size)
        bn_model = FullyConnectedNet(hidden_dims, weight_scale=weight_scale,
        bn_solver = Solver(bn_model, small_data,
                            num_epochs=n_epochs, batch_size=b_size,
                            update_rule='adam',
                            optim_config={
                                'learning_rate': lr,
                            },
                            verbose=False)

        bn_solver.train()
        bn_solvers.append(bn_solver)

    return bn_solvers, solver, batch_sizes

batch_sizes = [5,10,50]
bn_solvers_bsize, solver_bsize, batch_sizes = run_batchsize_experiments('batch

```

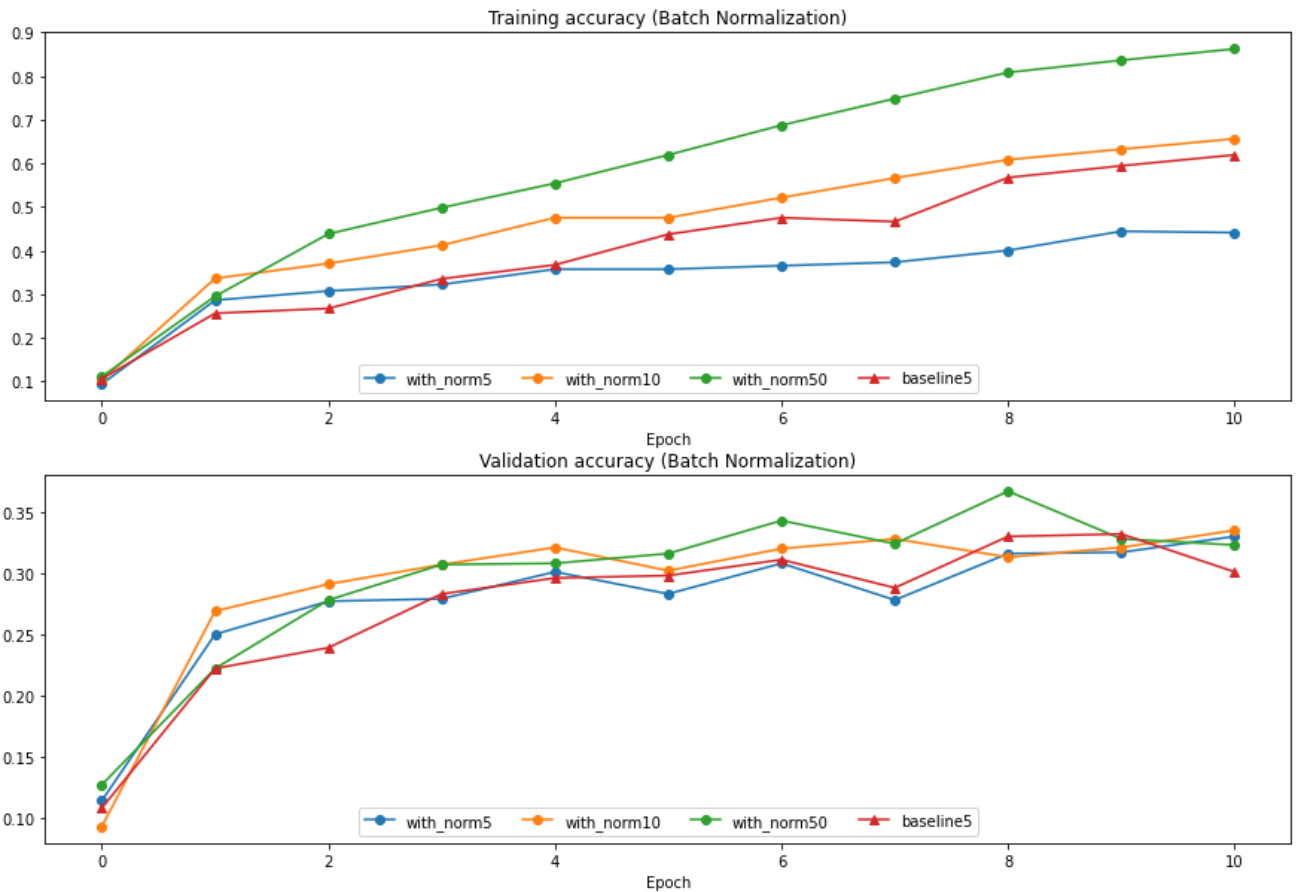
```

No normalization: batch size = 5
Normalization: batch size = 5
Normalization: batch size = 10
Normalization: batch size = 50

```

```
In [ ]: plt.subplot(2, 1, 1)
plot_training_history('Training accuracy (Batch Normalization)', 'Epoch', solve
                    lambda x: x.train_acc_history, bl_marker='--^', bn_marke
plt.subplot(2, 1, 2)
plot_training_history('Validation accuracy (Batch Normalization)', 'Epoch', so
                    lambda x: x.val_acc_history, bl_marker='--^', bn_marker=

plt.gcf().set_size_inches(15, 10)
plt.show()
```



## Inline Question 2:

Describe the results of this experiment. What does this imply about the relationship between batch normalization and batch size? Why is this relationship observed?

### Answer:

From the graphs, we can infer that only nets using batch sizes  $> 10$  actually outperform the baseline net on the training and validating accuracy. This happens because nets using smaller batch sizes aren't capable of normalizing the data accurately. A larger batch size will be much better at representing the data as a whole in comparison to smaller batch sizes. Therefore, we can say that batch normalization with larger batch sizes can approximate the data better and produce better results.

## Layer Normalization

Batch normalization has proved to be effective in making networks easier to train, but the dependency on batch size makes it less useful in complex networks which have a cap on the input batch size due to hardware limitations.

Several alternatives to batch normalization have been proposed to mitigate this problem; one such technique is Layer Normalization [4]. Instead of normalizing over the batch, we normalize over the features. In other words, when using Layer Normalization, each feature vector corresponding to a single datapoint is normalized based on the sum of all terms within that feature vector.

[4] [Ba, Jimmy Lei, Jamie Ryan Kiros, and Geoffrey E. Hinton. "Layer Normalization." stat 1050 \(2016\): 21.](#)

## Inline Question 3:

Which of these data preprocessing steps is analogous to batch normalization, and which is analogous to layer normalization?

1. Scaling each image in the dataset, so that the RGB channels for each row of pixels within an image sums up to 1.
2. Scaling each image in the dataset, so that the RGB channels for all pixels within an image sums up to 1.
3. Subtracting the mean image of the dataset from each image in the dataset.
4. Setting all RGB values to either 0 or 1 depending on a given threshold.

## Answer:

- 2 - Layer Normalization
- 3 - Batch Normalization

# Layer Normalization: Implementation

Now you'll implement layer normalization. This step should be relatively straightforward, as conceptually the implementation is almost identical to that of batch normalization. One significant difference though is that for layer normalization, we do not keep track of the moving moments, and the testing phase is identical to the training phase, where the mean and variance are directly calculated per datapoint.

Here's what you need to do:

- In `cs682/layers.py`, implement the forward pass for layer normalization in the function `layernorm_backward`.

Run the cell below to check your results.

- In `cs682/layers.py`, implement the backward pass for layer normalization in the function `layernorm_backward`.

Run the second cell below to check your results.

- Modify `cs682/classifiers/fc_net.py` to add layer normalization to the `FullyConnectedNet`. When the `normalization` flag is set to `"layernorm"` in the constructor, you should insert a layer normalization layer before each ReLU nonlinearity.

Run the third cell below to run the batch size experiment on layer normalization.

```

In [ ]: # Check the training-time forward pass by checking means and variances
        # of features both before and after layer normalization

        # Simulate the forward pass for a two-layer network
        np.random.seed(231)
        N, D1, D2, D3 = 4, 50, 60, 3
        X = np.random.randn(N, D1)
        W1 = np.random.randn(D1, D2)
        W2 = np.random.randn(D2, D3)
        a = np.maximum(0, X.dot(W1)).dot(W2)

        print('Before layer normalization:')
        print_mean_std(a,axis=1)

        gamma = np.ones(D3)
        beta = np.zeros(D3)
        # Means should be close to zero and stds close to one
        print('After layer normalization (gamma=1, beta=0)')
        a_norm, _ = layernorm_forward(a, gamma, beta, {'mode': 'train'})
        print_mean_std(a_norm,axis=1)

        gamma = np.asarray([3.0,3.0,3.0])
        beta = np.asarray([5.0,5.0,5.0])
        # Now means should be close to beta and stds close to gamma
        print('After layer normalization (gamma=', gamma, ', beta=', beta, ')')
        a_norm, _ = layernorm_forward(a, gamma, beta, {'mode': 'train'})
        print_mean_std(a_norm,axis=1)

```

Before layer normalization:

```

means: [-59.06673243 -47.60782686 -43.31137368 -26.40991744]
stds:  [10.07429373 28.39478981 35.28360729  4.01831507]

```

After layer normalization (gamma=1, beta=0)

```

means: [ 4.81096644e-16 -7.40148683e-17  2.22044605e-16 -5.92118946e-16]
stds:  [0.99999995 0.99999999 1.          0.99999969]

```

After layer normalization (gamma= [3. 3. 3.] , beta= [5. 5. 5.] )

```

means: [5. 5. 5. 5.]
stds:  [2.99999985 2.99999998 2.99999999 2.99999907]

```

```
In [ ]: # Gradient check batchnorm backward pass
np.random.seed(231)
N, D = 4, 5
x = 5 * np.random.randn(N, D) + 12
gamma = np.random.randn(D)
beta = np.random.randn(D)
dout = np.random.randn(N, D)

ln_param = {}
fx = lambda x: layernorm_forward(x, gamma, beta, ln_param)[0]
fg = lambda a: layernorm_forward(x, a, beta, ln_param)[0]
fb = lambda b: layernorm_forward(x, gamma, b, ln_param)[0]

dx_num = eval_numerical_gradient_array(fx, x, dout)
da_num = eval_numerical_gradient_array(fg, gamma.copy(), dout)
db_num = eval_numerical_gradient_array(fb, beta.copy(), dout)

_, cache = layernorm_forward(x, gamma, beta, ln_param)
dx, dgamma, dbeta = layernorm_backward(dout, cache)

#You should expect to see relative errors between 1e-12 and 1e-8
print('dx error: ', rel_error(dx_num, dx))
print('dgamma error: ', rel_error(da_num, dgamma))
print('dbeta error: ', rel_error(db_num, dbeta))

dx error:  1.4336161049967258e-09
dgamma error:  4.519489546032799e-12
dbeta error:  2.276445013433725e-12
```

## Layer Normalization and batch size

We will now run the previous batch size experiment with layer normalization instead of batch normalization. Compared to the previous experiment, you should see a markedly smaller influence of batch size on the training history!

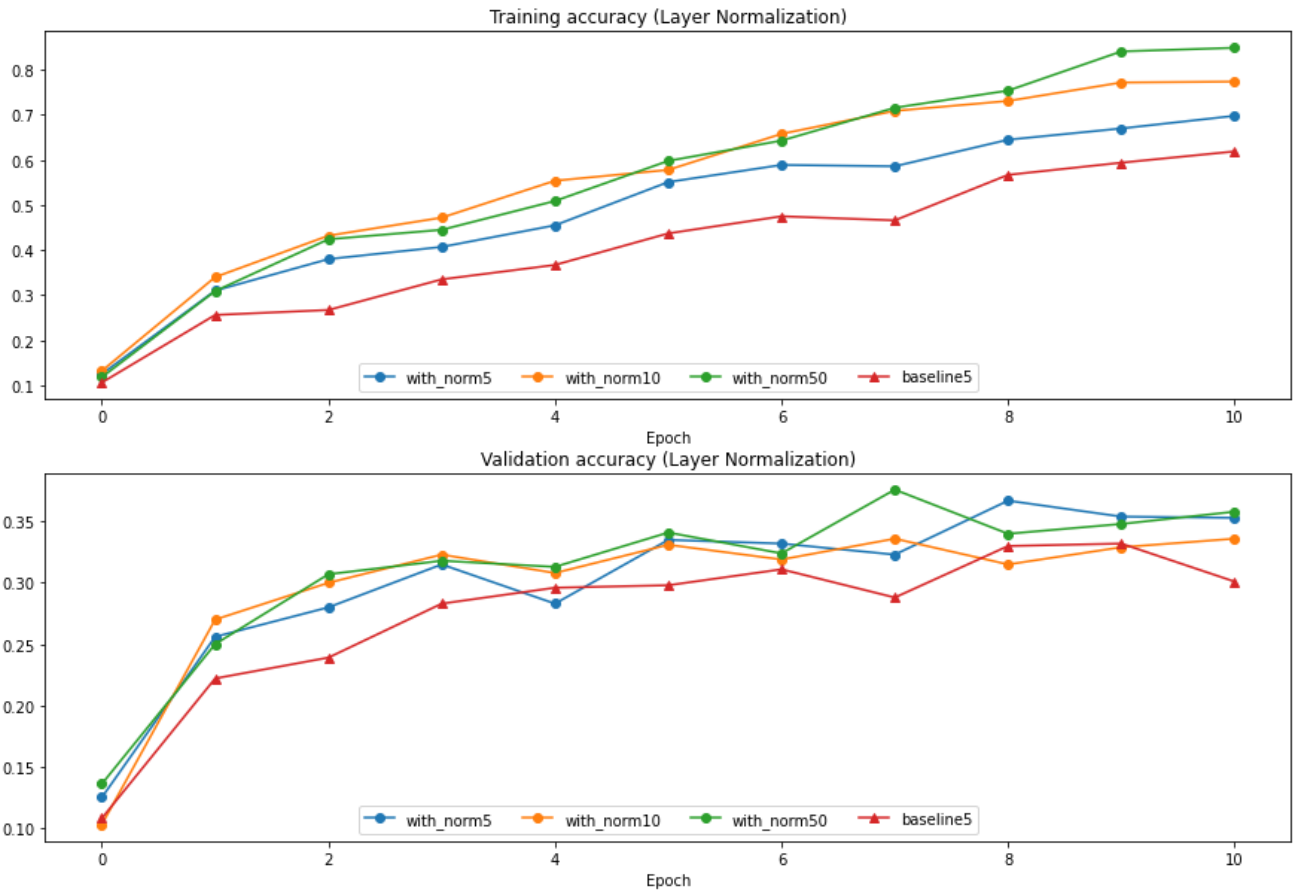
```
In [ ]: ln_solvers_bsize, solver_bsize, batch_sizes = run_batchsize_experiments('layer_norm')

plt.subplot(2, 1, 1)
plot_training_history('Training accuracy (Layer Normalization)', 'Epoch', solver_bsize,
                      lambda x: x.train_acc_history, bl_marker='^-^', bn_marker='x')
plt.subplot(2, 1, 2)
plot_training_history('Validation accuracy (Layer Normalization)', 'Epoch', solver_bsize,
                      lambda x: x.val_acc_history, bl_marker='^-^', bn_marker='x')

plt.gcf().set_size_inches(15, 10)
plt.show()
```



No normalization: batch size = 5  
 Normalization: batch size = 5  
 Normalization: batch size = 10  
 Normalization: batch size = 50



## Inline Question 4:

When is layer normalization likely to not work well, and why?

1. Using it in a very deep network
2. Having a very small dimension of features
3. Having a high regularization term

## Answer:

Layer Normalization will not work well when we have a very small dimension of features. This is because layer normalization normalizes each example over its dimensions. With very small number of dimensions, it won't be able to approximate the data well resulting in poor results

```
In [ ]: from google.colab import drive
drive.mount('/content/drive')
```

Mounted at /content/drive

```
In [ ]: %cd drive/'My Drive'/assignment2

/content/drive/My Drive/assignment2
```

## Dropout

Dropout [1] is a technique for regularizing neural networks by randomly setting some features to zero during the forward pass. In this exercise you will implement a dropout layer and modify your fully-connected network to optionally use dropout.

[1] [Geoffrey E. Hinton et al, "Improving neural networks by preventing co-adaptation of feature detectors", arXiv 2012](#)

```
In [ ]: # As usual, a bit of setup
from __future__ import print_function
import time
import numpy as np
import matplotlib.pyplot as plt
from cs682.classifiers.fc_net import *
from cs682.data_utils import get_CIFAR10_data
from cs682.gradient_check import eval_numerical_gradient, eval_numerical_grad
from cs682.solver import Solver

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipy
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

```
In [ ]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
for k, v in data.items():
    print('%s: ' % k, v.shape)
```

```

X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)

```

## Dropout forward pass

In the file `cs682/layers.py`, implement the forward pass for dropout. Since dropout behaves differently during training and testing, make sure to implement the operation for both modes.

Once you have done so, run the cell below to test your implementation.

```

In [ ]: np.random.seed(231)
x = np.random.randn(500, 500) + 10

for p in [0.25, 0.4, 0.7]:
    out, _ = dropout_forward(x, {'mode': 'train', 'p': p})
    out_test, _ = dropout_forward(x, {'mode': 'test', 'p': p})

    print('Running tests with p = ', p)
    print('Mean of input: ', x.mean())
    print('Mean of train-time output: ', out.mean())
    print('Mean of test-time output: ', out_test.mean())
    print('Fraction of train-time output set to zero: ', (out == 0).mean())
    print('Fraction of test-time output set to zero: ', (out_test == 0).mean())
    print()

```

```

Running tests with p = 0.25
Mean of input: 10.000207878477502
Mean of train-time output: 10.014059116977283
Mean of test-time output: 10.000207878477502
Fraction of train-time output set to zero: 0.749784
Fraction of test-time output set to zero: 0.0

```

```

Running tests with p = 0.4
Mean of input: 10.000207878477502
Mean of train-time output: 9.977917658761159
Mean of test-time output: 10.000207878477502
Fraction of train-time output set to zero: 0.600796
Fraction of test-time output set to zero: 0.0

```

```

Running tests with p = 0.7
Mean of input: 10.000207878477502
Mean of train-time output: 9.987811912159426
Mean of test-time output: 10.000207878477502
Fraction of train-time output set to zero: 0.30074
Fraction of test-time output set to zero: 0.0

```

# Dropout backward pass

In the file `cs682/layers.py`, implement the backward pass for dropout. After doing so, run the following cell to numerically gradient-check your implementation.

```
In [ ]: np.random.seed(231)
x = np.random.randn(10, 10) + 10
dout = np.random.randn(*x.shape)

dropout_param = {'mode': 'train', 'p': 0.2, 'seed': 123}
out, cache = dropout_forward(x, dropout_param)
dx = dropout_backward(dout, cache)
dx_num = eval_numerical_gradient_array(lambda xx: dropout_forward(xx, dropout_param), x, dx)

# Error should be around e-10 or less
print('dx relative error: ', rel_error(dx, dx_num))
```

dx relative error: 5.44560814873387e-11

## Inline Question 1:

What happens if we do not divide the values being passed through inverse dropout by  $p$  in the dropout layer? Why does that happen?

## Answer:

When using dropout, we keep a particular neuron active with some probability  $p$  during training time. Since we do not dropout during test time, we must scale the hidden layer outputs at train time. However, if we do not divide the values, the learned weight matrices will not account for the dropped neurons and be lower than expected. The outputs at test time will not be identical to their expected outputs at training time.

# Fully-connected nets with Dropout

In the file `cs682/classifiers/fc_net.py`, modify your implementation to use dropout. Specifically, if the constructor of the net receives a value that is not 1 for the `dropout` parameter, then the net should add dropout immediately after every ReLU nonlinearity. After doing so, run the following to numerically gradient-check your implementation.

```
In [ ]: np.random.seed(231)
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))

for dropout in [1, 0.75, 0.5]:
    print('Running check with dropout = ', dropout)
    model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                              weight_scale=5e-2, dtype=np.float64,
                              dropout=dropout, seed=123)

    loss, grads = model.loss(X, y)
    print('Initial loss: ', loss)

    # Relative errors should be around e-6 or less; Note that it's fine
    # if for dropout=1 you have W2 error be on the order of e-5.
    for name in sorted(grads):
        f = lambda _: model.loss(X, y)[0]
        grad_num = eval_numerical_gradient(f, model.params[name], verbose=False,
        print('%s relative error: %.2e' % (name, rel_error(grad_num, grads[name]))
    print()
```

```
Running check with dropout = 1
Initial loss: 2.3004790897684924
W1 relative error: 1.48e-07
W2 relative error: 2.21e-05
W3 relative error: 3.53e-07
b1 relative error: 5.38e-09
b2 relative error: 2.09e-09
b3 relative error: 5.80e-11
```

```
Running check with dropout = 0.75
Initial loss: 2.302371489704412
W1 relative error: 1.90e-07
W2 relative error: 4.76e-06
W3 relative error: 2.60e-08
b1 relative error: 4.73e-09
b2 relative error: 1.82e-09
b3 relative error: 1.70e-10
```

```
Running check with dropout = 0.5
Initial loss: 2.3042759220785896
W1 relative error: 3.11e-07
W2 relative error: 1.84e-08
W3 relative error: 5.35e-08
b1 relative error: 5.37e-09
b2 relative error: 2.99e-09
b3 relative error: 1.13e-10
```

# Regularization experiment

As an experiment, we will train a pair of two-layer networks on 500 training examples: one will use no dropout, and one will use a keep probability of 0.25. We will then visualize the training and validation accuracies of the two networks over time.

```
In [ ]: # Train two identical nets, one with dropout and one without
np.random.seed(231)
num_train = 500
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}

solvers = {}
dropout_choices = [1, 0.25]
for dropout in dropout_choices:
    model = FullyConnectedNet([500], dropout=dropout)
    print(dropout)

    solver = Solver(model, small_data,
                    num_epochs=25, batch_size=100,
                    update_rule='adam',
                    optim_config={
                        'learning_rate': 5e-4,
                    },
                    verbose=True, print_every=100)

    solver.train()
    solvers[dropout] = solver
```

```
1
(Iteration 1 / 125) loss: 7.856643
(Epoch 0 / 25) train acc: 0.260000; val_acc: 0.184000
(Epoch 1 / 25) train acc: 0.416000; val_acc: 0.258000
(Epoch 2 / 25) train acc: 0.482000; val_acc: 0.276000
(Epoch 3 / 25) train acc: 0.532000; val_acc: 0.277000
(Epoch 4 / 25) train acc: 0.600000; val_acc: 0.271000
(Epoch 5 / 25) train acc: 0.708000; val_acc: 0.299000
(Epoch 6 / 25) train acc: 0.722000; val_acc: 0.282000
(Epoch 7 / 25) train acc: 0.832000; val_acc: 0.255000
(Epoch 8 / 25) train acc: 0.878000; val_acc: 0.269000
(Epoch 9 / 25) train acc: 0.902000; val_acc: 0.275000
(Epoch 10 / 25) train acc: 0.888000; val_acc: 0.261000
(Epoch 11 / 25) train acc: 0.926000; val_acc: 0.278000
(Epoch 12 / 25) train acc: 0.960000; val_acc: 0.302000
(Epoch 13 / 25) train acc: 0.964000; val_acc: 0.306000
(Epoch 14 / 25) train acc: 0.966000; val_acc: 0.309000
(Epoch 15 / 25) train acc: 0.976000; val_acc: 0.288000
(Epoch 16 / 25) train acc: 0.988000; val_acc: 0.301000
```

```
(Epoch 17 / 25) train acc: 0.988000; val_acc: 0.310000
(Epoch 18 / 25) train acc: 0.990000; val_acc: 0.311000
(Epoch 19 / 25) train acc: 0.990000; val_acc: 0.310000
(Epoch 20 / 25) train acc: 0.988000; val_acc: 0.312000
(Iteration 101 / 125) loss: 0.084611
(Epoch 21 / 25) train acc: 0.990000; val_acc: 0.302000
(Epoch 22 / 25) train acc: 0.978000; val_acc: 0.299000
(Epoch 23 / 25) train acc: 0.986000; val_acc: 0.291000
(Epoch 24 / 25) train acc: 0.994000; val_acc: 0.302000
(Epoch 25 / 25) train acc: 0.994000; val_acc: 0.293000
0.25
(Iteration 1 / 125) loss: 17.318478
(Epoch 0 / 25) train acc: 0.230000; val_acc: 0.177000
(Epoch 1 / 25) train acc: 0.378000; val_acc: 0.243000
(Epoch 2 / 25) train acc: 0.402000; val_acc: 0.254000
(Epoch 3 / 25) train acc: 0.502000; val_acc: 0.276000
(Epoch 4 / 25) train acc: 0.528000; val_acc: 0.298000
(Epoch 5 / 25) train acc: 0.562000; val_acc: 0.297000
(Epoch 6 / 25) train acc: 0.626000; val_acc: 0.290000
(Epoch 7 / 25) train acc: 0.628000; val_acc: 0.298000
(Epoch 8 / 25) train acc: 0.686000; val_acc: 0.310000
(Epoch 9 / 25) train acc: 0.722000; val_acc: 0.289000
(Epoch 10 / 25) train acc: 0.724000; val_acc: 0.300000
(Epoch 11 / 25) train acc: 0.760000; val_acc: 0.305000
(Epoch 12 / 25) train acc: 0.772000; val_acc: 0.278000
(Epoch 13 / 25) train acc: 0.818000; val_acc: 0.306000
(Epoch 14 / 25) train acc: 0.816000; val_acc: 0.339000
(Epoch 15 / 25) train acc: 0.854000; val_acc: 0.351000
(Epoch 16 / 25) train acc: 0.832000; val_acc: 0.296000
(Epoch 17 / 25) train acc: 0.854000; val_acc: 0.288000
(Epoch 18 / 25) train acc: 0.846000; val_acc: 0.320000
(Epoch 19 / 25) train acc: 0.872000; val_acc: 0.344000
(Epoch 20 / 25) train acc: 0.868000; val_acc: 0.305000
(Iteration 101 / 125) loss: 5.472347
(Epoch 21 / 25) train acc: 0.866000; val_acc: 0.329000
(Epoch 22 / 25) train acc: 0.902000; val_acc: 0.308000
(Epoch 23 / 25) train acc: 0.898000; val_acc: 0.313000
(Epoch 24 / 25) train acc: 0.912000; val_acc: 0.334000
(Epoch 25 / 25) train acc: 0.914000; val_acc: 0.322000
```

```
In [ ]: # Plot train and validation accuracies of the two models

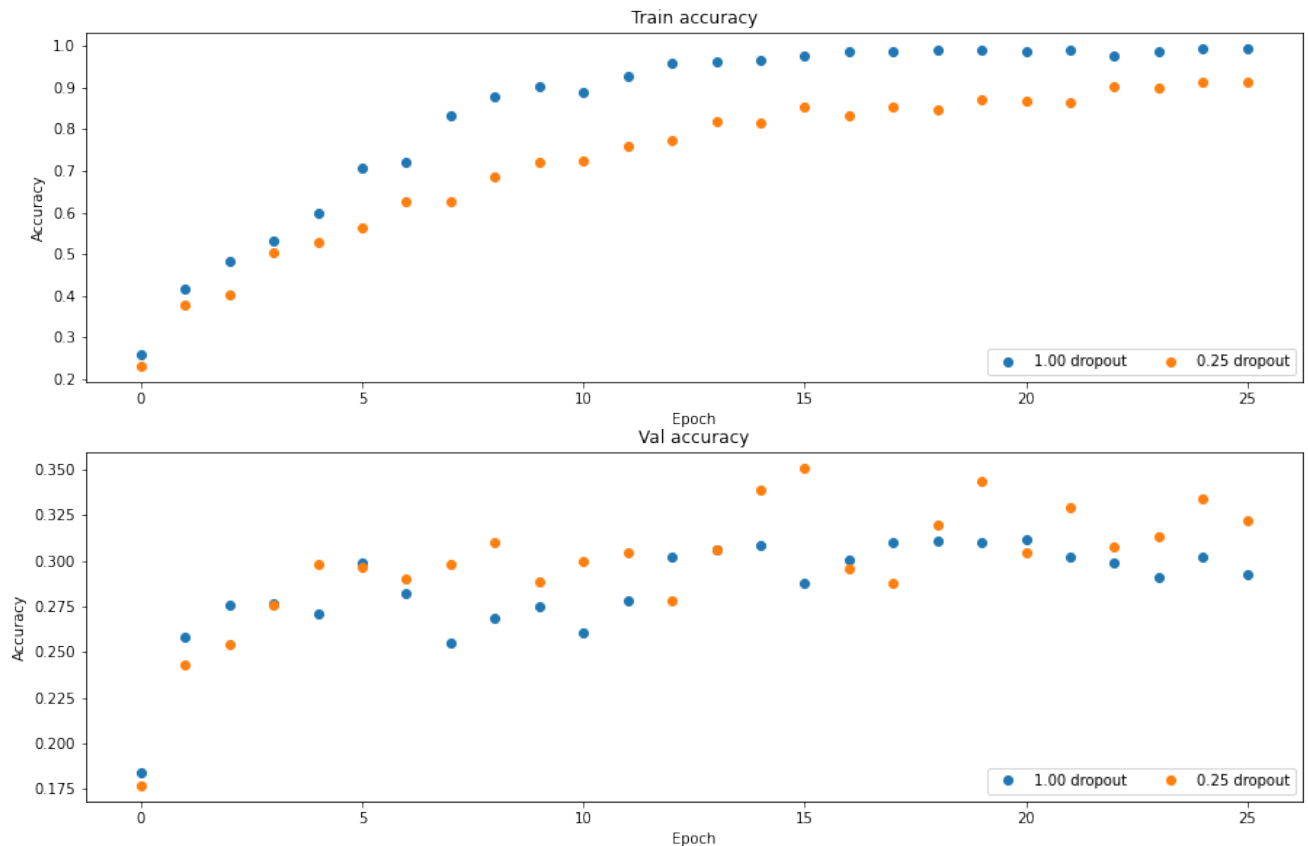
train_accs = []
val_accs = []
for dropout in dropout_choices:
    solver = solvers[dropout]
    train_accs.append(solver.train_acc_history[-1])
    val_accs.append(solver.val_acc_history[-1])

plt.subplot(3, 1, 1)
for dropout in dropout_choices:
    plt.plot(solvers[dropout].train_acc_history, 'o', label='%.2f dropout' % dropout)
plt.title('Train accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend(ncol=2, loc='lower right')

plt.subplot(3, 1, 2)
for dropout in dropout_choices:
    plt.plot(solvers[dropout].val_acc_history, 'o', label='%.2f dropout' % dropout)
plt.title('Val accuracy')
plt.xlabel('Epoch')
plt.ylabel('Accuracy')
plt.legend(ncol=2, loc='lower right')

plt.gcf().set_size_inches(15, 15)
plt.show()
```





## Inline Question 2:

Compare the validation and training accuracies with and without dropout -- what do your results suggest about dropout as a regularizer?

## Answer:

The graphs show that the net without dropout overfits the data. At epoch = 25, the net without dropout has a training accuracy of nearly 1.0 and a validation accuracy of 0.3. On the other hand, the net with dropout avoids overfitting the data and has a higher validation accuracy. This suggests that dropout is an effective regularizer and promotes a generalized network.

## Inline Question 3:

Suppose we are training a deep fully-connected network for image classification, with dropout after hidden layers (parameterized by keep probability  $p$ ). How should we modify  $p$ , if at all, if we decide to decrease the size of the hidden layers (that is, the number of nodes in each layer)?

## Answer:

Even if we decide to decrease the size of the hidden layers, we are not required to change the value of  $p$ . The value of  $p$  represents the probability of keeping a particular neuron alive, which work using percentages and not using an absolute value. The number of neurons to be kept alive is directly proportional to the size of the hidden layers by a factor of  $p$ .

Mounted at /content/drive

```
/content/drive/My Drive/assignment2
```

```
Collecting scipy==1.2
  Downloading https://files.pythonhosted.org/packages/67/e6/6d4edaceee6a110ecf6f318482f5229792f143e468b34a631f5a0899f56d/scipy-1.2.0-cp36-cp36m-manylinux1_x86_64.whl (26.6MB)
    |████████████████████████████████████████| 26.6MB 168kB/s
Requirement already satisfied: numpy>=1.8.2 in /usr/local/lib/python3.6/dist-packages (from scipy==1.2) (1.18.5)
ERROR: umap-learn 0.4.6 has requirement scipy>=1.3.1, but you'll have scipy 1.2.0 which is incompatible.
ERROR: tensorflow 2.3.0 has requirement scipy==1.4.1, but you'll have scipy 1.2.0 which is incompatible.
ERROR: alumentations 0.1.12 has requirement imgaug<0.2.7,>=0.2.5, but you'll have imgaug 0.2.9 which is incompatible.
Installing collected packages: scipy
  Found existing installation: scipy 1.4.1
    Uninstalling scipy-1.4.1:
      Successfully uninstalled scipy-1.4.1
Successfully installed scipy-1.2.0
```

So far we have worked with deep fully-connected networks, using them to explore different optimization strategies and network architectures. Fully-connected networks are a good testbed for experimentation because they are very computationally efficient, but in practice all state-of-the-art results use convolutional networks instead.

file:///Users/kunidedhia/Downloads/assignment2/ConvolutionalNetworks.html

```
In [ ]: # As usual, a bit of setup
import numpy as np
import matplotlib.pyplot as plt
from cs682.classifiers.cnn import *
from cs682.data_utils import get_CIFAR10_data
from cs682.gradient_check import eval_numerical_gradient_array, eval_numerica
from cs682.layers import *
from cs682.fast_layers import *
from cs682.solver import Solver

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipy
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

```
In [41]: # Load the (preprocessed) CIFAR10 data.
```

```
data = get_CIFAR10_data()
for k, v in data.items():
    print('%s: ' % k, v.shape)
```

```
X_train: (49000, 3, 32, 32)
y_train: (49000,)
X_val: (1000, 3, 32, 32)
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

## Convolution: Naive forward pass

The core of a convolutional network is the convolution operation. In the file `cs682/layers.py`, implement the forward pass for the convolution layer in the function `conv_forward_naive`.

You don't have to worry too much about efficiency at this point; just write the code in whatever way you find most clear.

You can test your implementation by running the following:

```
In [42]: x_shape = (2, 3, 4, 4)
w_shape = (3, 3, 4, 4)
x = np.linspace(-0.1, 0.5, num=np.prod(x_shape)).reshape(x_shape)
w = np.linspace(-0.2, 0.3, num=np.prod(w_shape)).reshape(w_shape)
b = np.linspace(-0.1, 0.2, num=3)

conv_param = {'stride': 2, 'pad': 1}
out, _ = conv_forward_naive(x, w, b, conv_param)
correct_out = np.array([[[[-0.08759809, -0.10987781],
                           [-0.18387192, -0.2109216 ]],
                          [[ 0.21027089,  0.21661097],
                           [ 0.22847626,  0.23004637]],
                          [[ 0.50813986,  0.54309974],
                           [ 0.64082444,  0.67101435]]],
                        [[[-0.98053589, -1.03143541],
                           [-1.19128892, -1.24695841]],
                          [[ 0.69108355,  0.66880383],
                           [ 0.59480972,  0.56776003]],
                          [[ 2.36270298,  2.36904306],
                           [ 2.38090835,  2.38247847]]]])

# Compare your output to ours; difference should be around e-8
print('Testing conv_forward_naive')
print('difference: ', rel_error(out, correct_out))
```

```
Testing conv_forward_naive
difference: 2.2121476417505994e-08
```

## Aside: Image processing via convolutions

As fun way to both check your implementation and gain a better understanding of the type of operation that convolutional layers can perform, we will set up an input containing two images and manually set up filters that perform common image processing operations (grayscale conversion and edge detection). The convolution forward pass will apply these operations to each of the input images. We can then visualize the results as a sanity check.

```
In [43]: from scipy.misc import imread, imresize

kitten, puppy = imread('kitten.jpg'), imread('puppy.jpg')
# kitten is wide, and puppy is already square
d = kitten.shape[1] - kitten.shape[0]
kitten_cropped = kitten[:, d//2:-d//2, :]

img_size = 200 # Make this smaller if it runs too slow
x = np.zeros((2, 3, img_size, img_size))
x[0, :, :, :] = imresize(puppy, (img_size, img_size)).transpose((2, 0, 1))
x[1, :, :, :] = imresize(kitten_cropped, (img_size, img_size)).transpose((2,

# Set up a convolutional weights holding 2 filters, each 3x3
```

```

w = np.zeros((2, 3, 3, 3))

# The first filter converts the image to grayscale.
# Set up the red, green, and blue channels of the filter.
w[0, 0, :, :] = [[0, 0, 0], [0, 0.3, 0], [0, 0, 0]]
w[0, 1, :, :] = [[0, 0, 0], [0, 0.6, 0], [0, 0, 0]]
w[0, 2, :, :] = [[0, 0, 0], [0, 0.1, 0], [0, 0, 0]]

# Second filter detects horizontal edges in the blue channel.
w[1, 2, :, :] = [[1, 2, 1], [0, 0, 0], [-1, -2, -1]]

# Vector of biases. We don't need any bias for the grayscale
# filter, but for the edge detection filter we want to add 128
# to each output so that nothing is negative.
b = np.array([0, 128])

# Compute the result of convolving each input in x with each filter in w,
# offsetting by b, and storing the results in out.
out, _ = conv_forward_naive(x, w, b, {'stride': 1, 'pad': 1})

def imshow_noax(img, normalize=True):
    """ Tiny helper to show images as uint8 and remove axis labels """
    if normalize:
        img_max, img_min = np.max(img), np.min(img)
        img = 255.0 * (img - img_min) / (img_max - img_min)
    plt.imshow(img.astype('uint8'))
    plt.gca().axis('off')

# Show the original images and the results of the conv operation
plt.subplot(2, 3, 1)
imshow_noax(puppy, normalize=False)
plt.title('Original image')
plt.subplot(2, 3, 2)
imshow_noax(out[0, 0])
plt.title('Grayscale')
plt.subplot(2, 3, 3)
imshow_noax(out[0, 1])
plt.title('Edges')
plt.subplot(2, 3, 4)
imshow_noax(kitten_cropped, normalize=False)
plt.subplot(2, 3, 5)
imshow_noax(out[1, 0])
plt.subplot(2, 3, 6)
imshow_noax(out[1, 1])
plt.show()

```

```
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:3: DeprecationWarning: `imread` is deprecated!
`imread` is deprecated in SciPy 1.0.0, and will be removed in 1.2.0.
Use ``imageio.imread`` instead.
```

This is separate from the ipykernel package so we can avoid doing imports until

```
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:10: DeprecationWarning: `imresize` is deprecated!
```

```
`imresize` is deprecated in SciPy 1.0.0, and will be removed in 1.3.0.
Use Pillow instead: ``numpy.array(Image.fromarray(arr).resize())``.
```

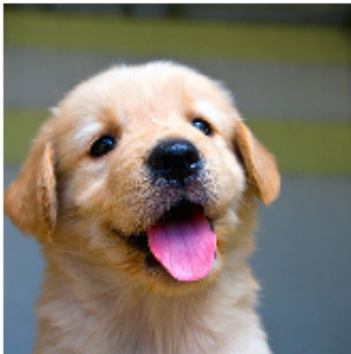
```
# Remove the CWD from sys.path while we load stuff.
```

```
/usr/local/lib/python3.6/dist-packages/ipykernel_launcher.py:11: DeprecationWarning: `imresize` is deprecated!
```

```
`imresize` is deprecated in SciPy 1.0.0, and will be removed in 1.3.0.
Use Pillow instead: ``numpy.array(Image.fromarray(arr).resize())``.
```

```
# This is added back by InteractiveShellApp.init_path()
```

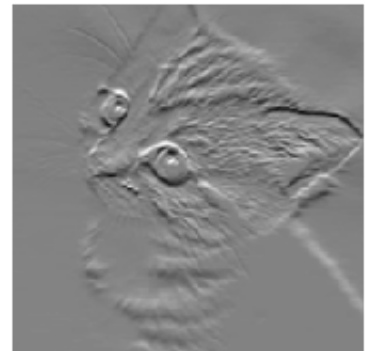
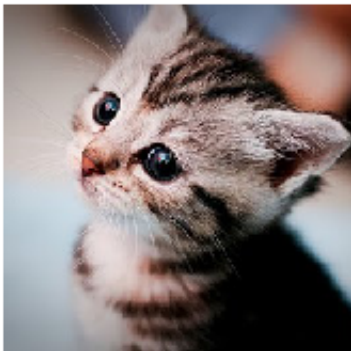
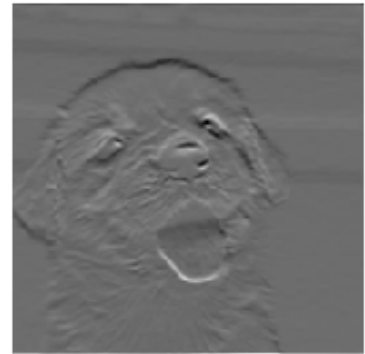
Original image



Grayscale



Edges



# Convolution: Naive backward pass

Implement the backward pass for the convolution operation in the function

`conv_backward_naive` in the file `cs682/layers.py`. Again, you don't need to worry too much about computational efficiency.

When you are done, run the following to check your backward pass with a numeric gradient check.

```
In [44]: np.random.seed(231)
x = np.random.randn(4, 3, 5, 5)
w = np.random.randn(2, 3, 3, 3)
b = np.random.randn(2,)
dout = np.random.randn(4, 2, 5, 5)
conv_param = {'stride': 1, 'pad': 1}

dx_num = eval_numerical_gradient_array(lambda x: conv_forward_naive(x, w, b, conv_param), x, dout)
dw_num = eval_numerical_gradient_array(lambda w: conv_forward_naive(x, w, b, conv_param), w, dout)
db_num = eval_numerical_gradient_array(lambda b: conv_forward_naive(x, w, b, conv_param), b, dout)

out, cache = conv_forward_naive(x, w, b, conv_param)
dx, dw, db = conv_backward_naive(dout, cache)

# Your errors should be around e-8 or less.
print('Testing conv_backward_naive function')
print('dx error: ', rel_error(dx, dx_num))
print('dw error: ', rel_error(dw, dw_num))
print('db error: ', rel_error(db, db_num))
```

```
Testing conv_backward_naive function
dx error:  1.159803161159293e-08
dw error:  2.2471264748452487e-10
db error:  3.37264006649648e-11
```

# Max-Pooling: Naive forward

Implement the forward pass for the max-pooling operation in the function

`max_pool_forward_naive` in the file `cs682/layers.py`. Again, don't worry too much about computational efficiency.

Check your implementation by running the following:



```
In [45]: x_shape = (2, 3, 4, 4)
x = np.linspace(-0.3, 0.4, num=np.prod(x_shape)).reshape(x_shape)
pool_param = {'pool_width': 2, 'pool_height': 2, 'stride': 2}

out, _ = max_pool_forward_naive(x, pool_param)

correct_out = np.array([[[[-0.26315789, -0.24842105],
                           [-0.20421053, -0.18947368]],
                          [[-0.14526316, -0.13052632],
                           [-0.08631579, -0.07157895]],
                          [[-0.02736842, -0.01263158],
                           [ 0.03157895,  0.04631579]]],
                        [[[ 0.09052632,  0.10526316],
                           [ 0.14947368,  0.16421053]],
                          [[ 0.20842105,  0.22315789],
                           [ 0.26736842,  0.28210526]],
                          [[ 0.32631579,  0.34105263],
                           [ 0.38526316,  0.4          ]]]]])

# Compare your output with ours. Difference should be on the order of e-8.
print('Testing max_pool_forward_naive function:')
print('difference: ', rel_error(out, correct_out))
```

```
Testing max_pool_forward_naive function:
difference: 4.1666665157267834e-08
```

## Max-Pooling: Naive backward

Implement the backward pass for the max-pooling operation in the function

`max_pool_backward_naive` in the file `cs682/layers.py`. You don't need to worry about computational efficiency.

Check your implementation with numeric gradient checking by running the following:

```
In [46]: np.random.seed(231)
x = np.random.randn(3, 2, 8, 8)
dout = np.random.randn(3, 2, 4, 4)
pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}

dx_num = eval_numerical_gradient_array(lambda x: max_pool_forward_naive(x, pool_param),
                                       x, dout)

out, cache = max_pool_forward_naive(x, pool_param)
dx = max_pool_backward_naive(dout, cache)

# Your error should be on the order of e-12
print('Testing max_pool_backward_naive function:')
print('dx error: ', rel_error(dx, dx_num))
```

```
Testing max_pool_backward_naive function:
dx error: 3.27562514223145e-12
```

# Fast layers

Making convolution and pooling layers fast can be challenging. To spare you the pain, we've provided fast implementations of the forward and backward passes for convolution and pooling layers in the file `cs682/fast_layers.py`.

The fast convolution implementation depends on a Cython extension; to compile it you need to run the following from the `cs682` directory:

```
python setup.py build_ext --inplace
```

The API for the fast versions of the convolution and pooling layers is exactly the same as the naive versions that you implemented above: the forward pass receives data, weights, and parameters and produces outputs and a cache object; the backward pass receives upstream derivatives and the cache object and produces gradients with respect to the data and weights.

**NOTE:** The fast implementation for pooling will only perform optimally if the pooling regions are non-overlapping and tile the input. If these conditions are not met then the fast pooling implementation will not be much faster than the naive implementation.

You can compare the performance of the naive and fast versions of these layers by running the following:

```
In [47]: # Rel errors should be around e-9 or less
from cs682.fast_layers import conv_forward_fast, conv_backward_fast
from time import time
np.random.seed(231)
x = np.random.randn(100, 3, 31, 31)
w = np.random.randn(25, 3, 3, 3)
b = np.random.randn(25,)
dout = np.random.randn(100, 25, 16, 16)
conv_param = {'stride': 2, 'pad': 1}

t0 = time()
out_naive, cache_naive = conv_forward_naive(x, w, b, conv_param)
t1 = time()
out_fast, cache_fast = conv_forward_fast(x, w, b, conv_param)
t2 = time()

print('Testing conv_forward_fast:')
print('Naive: %fs' % (t1 - t0))
print('Fast: %fs' % (t2 - t1))
print('Speedup: %fx' % ((t1 - t0) / (t2 - t1)))
print('Difference: ', rel_error(out_naive, out_fast))

t0 = time()
dx_naive, dw_naive, db_naive = conv_backward_naive(dout, cache_naive)
t1 = time()
dx_fast, dw_fast, db_fast = conv_backward_fast(dout, cache_fast)
t2 = time()

print('\nTesting conv_backward_fast:')
print('Naive: %fs' % (t1 - t0))
print('Fast: %fs' % (t2 - t1))
print('Speedup: %fx' % ((t1 - t0) / (t2 - t1)))
print('dx difference: ', rel_error(dx_naive, dx_fast))
print('dw difference: ', rel_error(dw_naive, dw_fast))
print('db difference: ', rel_error(db_naive, db_fast))
```

```
Testing conv_forward_fast:
Naive: 0.200158s
Fast: 0.010576s
Speedup: 18.924776x
Difference: 4.926407851494105e-11
```

```
Testing conv_backward_fast:
Naive: 7.807969s
Fast: 0.011293s
Speedup: 691.417608x
dx difference: 1.949764775345631e-11
dw difference: 3.681156828004736e-13
db difference: 0.0
```

```
In [48]: # Relative errors should be close to 0.0
from cs682.fast_layers import max_pool_forward_fast, max_pool_backward_fast
np.random.seed(231)
x = np.random.randn(100, 3, 32, 32)
dout = np.random.randn(100, 3, 16, 16)
pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}

t0 = time()
out_naive, cache_naive = max_pool_forward_naive(x, pool_param)
t1 = time()
out_fast, cache_fast = max_pool_forward_fast(x, pool_param)
t2 = time()

print('Testing pool_forward_fast:')
print('Naive: %fs' % (t1 - t0))
print('fast: %fs' % (t2 - t1))
print('speedup: %fx' % ((t1 - t0) / (t2 - t1)))
print('difference: ', rel_error(out_naive, out_fast))

t0 = time()
dx_naive = max_pool_backward_naive(dout, cache_naive)
t1 = time()
dx_fast = max_pool_backward_fast(dout, cache_fast)
t2 = time()

print('\nTesting pool_backward_fast:')
print('Naive: %fs' % (t1 - t0))
print('fast: %fs' % (t2 - t1))
print('speedup: %fx' % ((t1 - t0) / (t2 - t1)))
print('dx difference: ', rel_error(dx_naive, dx_fast))
```

```
Testing pool_forward_fast:
Naive: 0.014004s
fast: 0.004253s
speedup: 3.292617x
difference: 0.0
```

```
Testing pool_backward_fast:
Naive: 0.575547s
fast: 0.013104s
speedup: 43.919984x
dx difference: 0.0
```

## Convolutional "sandwich" layers

Previously we introduced the concept of "sandwich" layers that combine multiple operations into commonly used patterns. In the file `cs682/layer_utils.py` you will find sandwich layers that implement a few commonly used patterns for convolutional networks.

```
In [49]: from cs682.layer_utils import conv_relu_pool_forward, conv_relu_pool_backward
np.random.seed(231)
x = np.random.randn(2, 3, 16, 16)
w = np.random.randn(3, 3, 3, 3)
b = np.random.randn(3,)
dout = np.random.randn(2, 3, 8, 8)
conv_param = {'stride': 1, 'pad': 1}
pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}

out, cache = conv_relu_pool_forward(x, w, b, conv_param, pool_param)
dx, dw, db = conv_relu_pool_backward(dout, cache)

dx_num = eval_numerical_gradient_array(lambda x: conv_relu_pool_forward(x, w,
dw_num = eval_numerical_gradient_array(lambda w: conv_relu_pool_forward(x, w,
db_num = eval_numerical_gradient_array(lambda b: conv_relu_pool_forward(x, w,

# Relative errors should be around e-8 or less
print('Testing conv_relu_pool')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
```

```
Testing conv_relu_pool
dx error: 9.591132621921372e-09
dw error: 5.802391137330214e-09
db error: 1.0146343411762047e-09
```

```
In [50]: from cs682.layer_utils import conv_relu_forward, conv_relu_backward
np.random.seed(231)
x = np.random.randn(2, 3, 8, 8)
w = np.random.randn(3, 3, 3, 3)
b = np.random.randn(3,)
dout = np.random.randn(2, 3, 8, 8)
conv_param = {'stride': 1, 'pad': 1}

out, cache = conv_relu_forward(x, w, b, conv_param)
dx, dw, db = conv_relu_backward(dout, cache)

dx_num = eval_numerical_gradient_array(lambda x: conv_relu_forward(x, w, b, c
dw_num = eval_numerical_gradient_array(lambda w: conv_relu_forward(x, w, b, c
db_num = eval_numerical_gradient_array(lambda b: conv_relu_forward(x, w, b, c

# Relative errors should be around e-8 or less
print('Testing conv_relu:')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
```

```
Testing conv_relu:
dx error: 1.5218619980349303e-09
dw error: 2.702022646099404e-10
db error: 1.451272393591721e-10
```

# Three-layer ConvNet

Now that you have implemented all the necessary layers, we can put them together into a simple convolutional network.

Open the file `cs682/classifiers/cnn.py` and complete the implementation of the `ThreeLayerConvNet` class. Remember you can use the `fast/sandwich` layers (already imported for you) in your implementation. Run the following cells to help you debug:

## Sanity check loss

After you build a new network, one of the first things you should do is sanity check the loss. When we use the softmax loss, we expect the loss for random weights (and no regularization) to be about  $\log(C)$  for  $C$  classes. When we add regularization this should go up.

```
In [51]: model = ThreeLayerConvNet()

N = 50
X = np.random.randn(N, 3, 32, 32)
y = np.random.randint(10, size=N)

loss, grads = model.loss(X, y)
print('Initial loss (no regularization): ', loss)

model.reg = 0.5
loss, grads = model.loss(X, y)
print('Initial loss (with regularization): ', loss)
```

```
Initial loss (no regularization):  2.302586071243987
Initial loss (with regularization): 2.508255638232932
```

## Gradient check

After the loss looks reasonable, use numeric gradient checking to make sure that your backward pass is correct. When you use numeric gradient checking you should use a small amount of artificial data and a small number of neurons at each layer. Note: correct implementations may still have relative errors up to the order of  $e^{-2}$ .

```
In [52]: num_inputs = 2
input_dim = (3, 16, 16)
reg = 0.0
num_classes = 10
np.random.seed(231)
X = np.random.randn(num_inputs, *input_dim)
y = np.random.randint(num_classes, size=num_inputs)

model = ThreeLayerConvNet(num_filters=3, filter_size=3,
                           input_dim=input_dim, hidden_dim=7,
                           dtype=np.float64)

loss, grads = model.loss(X, y)
# Errors should be small, but correct implementations may have
# relative errors up to the order of e-2
for param_name in sorted(grads):
    f = lambda _: model.loss(X, y)[0]
    param_grad_num = eval_numerical_gradient(f, model.params[param_name], verbose=0)
    e = rel_error(param_grad_num, grads[param_name])
    print('%s max relative error: %e' % (param_name, rel_error(param_grad_num, grads[param_name])))

W1 max relative error: 1.380104e-04
W2 max relative error: 1.822723e-02
W3 max relative error: 3.064049e-04
b1 max relative error: 3.477652e-05
b2 max relative error: 2.516375e-03
b3 max relative error: 7.945660e-10
```

## Overfit small data

A nice trick is to train your model with just a few training samples. You should be able to overfit small datasets, which will result in very high training accuracy and comparatively low validation accuracy.

```
In [53]: np.random.seed(231)

num_train = 100
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}

model = ThreeLayerConvNet(weight_scale=1e-2)

solver = Solver(model, small_data,
                 num_epochs=15, batch_size=50,
                 update_rule='adam',
                 optim_config={
                     'learning_rate': 1e-3,
                 },
                 verbose=True, print_every=1)
solver.train()
```

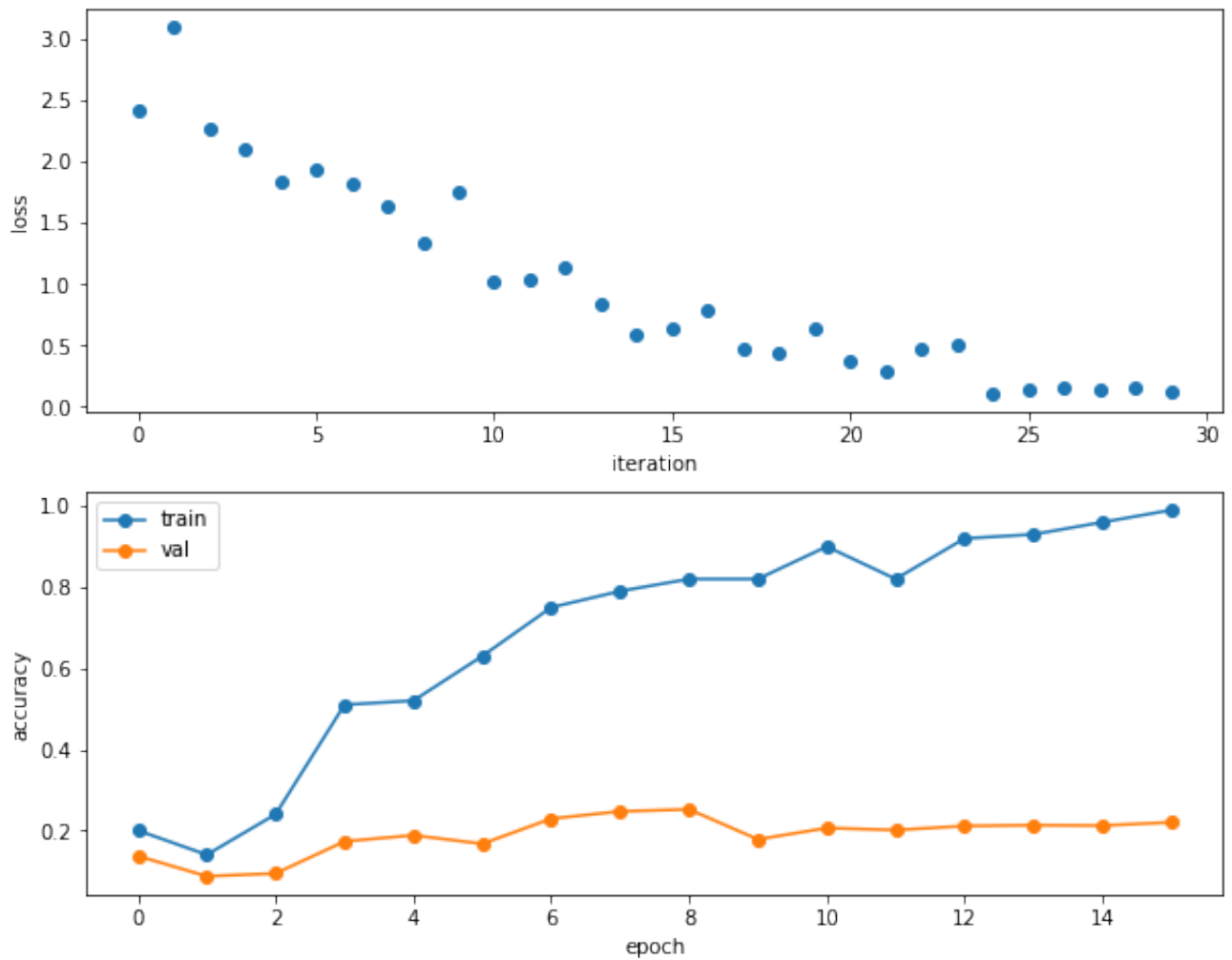


```
(Iteration 1 / 30) loss: 2.414060
(Epoch 0 / 15) train acc: 0.200000; val_acc: 0.137000
(Iteration 2 / 30) loss: 3.102925
(Epoch 1 / 15) train acc: 0.140000; val_acc: 0.087000
(Iteration 3 / 30) loss: 2.270330
(Iteration 4 / 30) loss: 2.096705
(Epoch 2 / 15) train acc: 0.240000; val_acc: 0.094000
(Iteration 5 / 30) loss: 1.838880
(Iteration 6 / 30) loss: 1.934188
(Epoch 3 / 15) train acc: 0.510000; val_acc: 0.173000
(Iteration 7 / 30) loss: 1.827912
(Iteration 8 / 30) loss: 1.639574
(Epoch 4 / 15) train acc: 0.520000; val_acc: 0.188000
(Iteration 9 / 30) loss: 1.330082
(Iteration 10 / 30) loss: 1.756115
(Epoch 5 / 15) train acc: 0.630000; val_acc: 0.167000
(Iteration 11 / 30) loss: 1.024162
(Iteration 12 / 30) loss: 1.041826
(Epoch 6 / 15) train acc: 0.750000; val_acc: 0.229000
(Iteration 13 / 30) loss: 1.142777
(Iteration 14 / 30) loss: 0.835706
(Epoch 7 / 15) train acc: 0.790000; val_acc: 0.247000
(Iteration 15 / 30) loss: 0.587786
(Iteration 16 / 30) loss: 0.645509
(Epoch 8 / 15) train acc: 0.820000; val_acc: 0.252000
(Iteration 17 / 30) loss: 0.786844
(Iteration 18 / 30) loss: 0.467054
(Epoch 9 / 15) train acc: 0.820000; val_acc: 0.178000
(Iteration 19 / 30) loss: 0.429880
(Iteration 20 / 30) loss: 0.635498
(Epoch 10 / 15) train acc: 0.900000; val_acc: 0.206000
(Iteration 21 / 30) loss: 0.365807
(Iteration 22 / 30) loss: 0.284220
(Epoch 11 / 15) train acc: 0.820000; val_acc: 0.201000
(Iteration 23 / 30) loss: 0.469343
(Iteration 24 / 30) loss: 0.509369
(Epoch 12 / 15) train acc: 0.920000; val_acc: 0.211000
(Iteration 25 / 30) loss: 0.111638
(Iteration 26 / 30) loss: 0.145388
(Epoch 13 / 15) train acc: 0.930000; val_acc: 0.213000
(Iteration 27 / 30) loss: 0.155575
(Iteration 28 / 30) loss: 0.143398
(Epoch 14 / 15) train acc: 0.960000; val_acc: 0.212000
(Iteration 29 / 30) loss: 0.158160
(Iteration 30 / 30) loss: 0.118934
(Epoch 15 / 15) train acc: 0.990000; val_acc: 0.220000
```

Plotting the loss, training accuracy, and validation accuracy should show clear overfitting:

```
In [54]: plt.subplot(2, 1, 1)
plt.plot(solver.loss_history, 'o')
plt.xlabel('iteration')
plt.ylabel('loss')

plt.subplot(2, 1, 2)
plt.plot(solver.train_acc_history, '-o')
plt.plot(solver.val_acc_history, '-o')
plt.legend(['train', 'val'], loc='upper left')
plt.xlabel('epoch')
plt.ylabel('accuracy')
plt.show()
```



## Train the net

By training the three-layer convolutional network for one epoch, you should achieve greater than 40% accuracy on the training set:

```
In [55]: model = ThreeLayerConvNet(weight_scale=0.001, hidden_dim=500, reg=0.001)

solver = Solver(model, data,
                 num_epochs=1, batch_size=50,
                 update_rule='adam',
                 optim_config={
                     'learning_rate': 1e-3,
                 },
                 verbose=True, print_every=20)

solver.train()
```

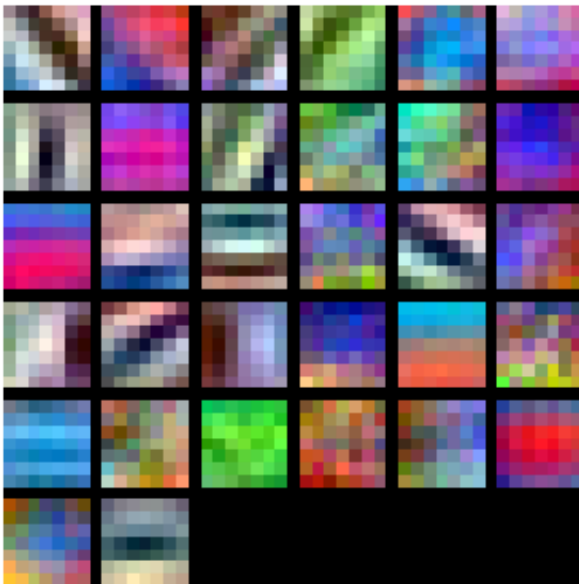
```
(Iteration 1 / 980) loss: 2.304740
(Epoch 0 / 1) train acc: 0.103000; val_acc: 0.107000
(Iteration 21 / 980) loss: 2.098229
(Iteration 41 / 980) loss: 1.949788
(Iteration 61 / 980) loss: 1.888398
(Iteration 81 / 980) loss: 1.877093
(Iteration 101 / 980) loss: 1.851877
(Iteration 121 / 980) loss: 1.859353
(Iteration 141 / 980) loss: 1.800181
(Iteration 161 / 980) loss: 2.143292
(Iteration 181 / 980) loss: 1.830573
(Iteration 201 / 980) loss: 2.037280
(Iteration 221 / 980) loss: 2.020304
(Iteration 241 / 980) loss: 1.823728
(Iteration 261 / 980) loss: 1.692679
(Iteration 281 / 980) loss: 1.882594
(Iteration 301 / 980) loss: 1.798261
(Iteration 321 / 980) loss: 1.851960
(Iteration 341 / 980) loss: 1.716323
(Iteration 361 / 980) loss: 1.897655
(Iteration 381 / 980) loss: 1.319744
(Iteration 401 / 980) loss: 1.738790
(Iteration 421 / 980) loss: 1.488866
(Iteration 441 / 980) loss: 1.718409
(Iteration 461 / 980) loss: 1.744440
(Iteration 481 / 980) loss: 1.605460
(Iteration 501 / 980) loss: 1.494847
(Iteration 521 / 980) loss: 1.835179
(Iteration 541 / 980) loss: 1.483923
(Iteration 561 / 980) loss: 1.676871
(Iteration 581 / 980) loss: 1.438325
(Iteration 601 / 980) loss: 1.443469
(Iteration 621 / 980) loss: 1.529369
(Iteration 641 / 980) loss: 1.763475
(Iteration 661 / 980) loss: 1.790329
(Iteration 681 / 980) loss: 1.693343
(Iteration 701 / 980) loss: 1.637078
(Iteration 721 / 980) loss: 1.644564
(Iteration 741 / 980) loss: 1.708919
(Iteration 761 / 980) loss: 1.494252
(Iteration 781 / 980) loss: 1.901751
(Iteration 801 / 980) loss: 1.898991
(Iteration 821 / 980) loss: 1.489988
(Iteration 841 / 980) loss: 1.377615
(Iteration 861 / 980) loss: 1.763751
(Iteration 881 / 980) loss: 1.540284
(Iteration 901 / 980) loss: 1.525582
(Iteration 921 / 980) loss: 1.674166
(Iteration 941 / 980) loss: 1.714316
(Iteration 961 / 980) loss: 1.534668
(Epoch 1 / 1) train acc: 0.504000; val_acc: 0.499000
```

# Visualize Filters

You can visualize the first-layer convolutional filters from the trained network by running the following:

```
In [56]: from cs682.vis_utils import visualize_grid

grid = visualize_grid(model.params['W1'].transpose(0, 2, 3, 1))
plt.imshow(grid.astype('uint8'))
plt.axis('off')
plt.gcf().set_size_inches(5, 5)
plt.show()
```



# Spatial Batch Normalization

We already saw that batch normalization is a very useful technique for training deep fully-connected networks. As proposed in the original paper [3], batch normalization can also be used for convolutional networks, but we need to tweak it a bit; the modification will be called "spatial batch normalization."

Normally batch-normalization accepts inputs of shape  $(N, D)$  and produces outputs of shape  $(N, D)$ , where we normalize across the minibatch dimension  $N$ . For data coming from convolutional layers, batch normalization needs to accept inputs of shape  $(N, C, H, W)$  and produce outputs of shape  $(N, C, H, W)$  where the  $N$  dimension gives the minibatch size and the  $(H, W)$  dimensions give the spatial size of the feature map.

If the feature map was produced using convolutions, then we expect the statistics of each feature channel to be relatively consistent both between different images and different locations within the same image. Therefore spatial batch normalization computes a mean and variance for each of the  $C$  feature channels by computing statistics over both the minibatch dimension  $N$  and the spatial dimensions  $H$  and  $W$ .

[3] [Sergey Ioffe and Christian Szegedy, "Batch Normalization: Accelerating Deep Network Training by Reducing Internal Covariate Shift", ICML 2015.](#)

## Spatial batch normalization: forward

In the file `cs682/layers.py`, implement the forward pass for spatial batch normalization in the function `spatial_batchnorm_forward`. Check your implementation by running the following:

```

In [57]: np.random.seed(231)
# Check the training-time forward pass by checking means and variances
# of features both before and after spatial batch normalization

N, C, H, W = 2, 3, 4, 5
x = 4 * np.random.randn(N, C, H, W) + 10

print('Before spatial batch normalization:')
print('  Shape: ', x.shape)
print('  Means: ', x.mean(axis=(0, 2, 3)))
print('  Stds: ', x.std(axis=(0, 2, 3)))

# Means should be close to zero and stds close to one
gamma, beta = np.ones(C), np.zeros(C)
bn_param = {'mode': 'train'}
out, _ = spatial_batchnorm_forward(x, gamma, beta, bn_param)
print('After spatial batch normalization:')
print('  Shape: ', out.shape)
print('  Means: ', out.mean(axis=(0, 2, 3)))
print('  Stds: ', out.std(axis=(0, 2, 3)))

# Means should be close to beta and stds close to gamma
gamma, beta = np.asarray([3, 4, 5]), np.asarray([6, 7, 8])
out, _ = spatial_batchnorm_forward(x, gamma, beta, bn_param)
print('After spatial batch normalization (nontrivial gamma, beta):')
print('  Shape: ', out.shape)
print('  Means: ', out.mean(axis=(0, 2, 3)))
print('  Stds: ', out.std(axis=(0, 2, 3)))

```

Before spatial batch normalization:

```

Shape: (2, 3, 4, 5)
Means: [9.33463814 8.90909116 9.11056338]
Stds: [3.61447857 3.19347686 3.5168142 ]

```

After spatial batch normalization:

```

Shape: (2, 3, 4, 5)
Means: [ 6.18949336e-16  5.99520433e-16 -1.22124533e-16]
Stds: [0.99999962 0.99999951 0.9999996 ]

```

After spatial batch normalization (nontrivial gamma, beta):

```

Shape: (2, 3, 4, 5)
Means: [6. 7. 8.]
Stds: [2.99999885 3.99999804 4.99999798]

```

```
In [ ]: np.random.seed(231)
# Check the test-time forward pass by running the training-time
# forward pass many times to warm up the running averages, and then
# checking the means and variances of activations after a test-time
# forward pass.
N, C, H, W = 10, 4, 11, 12

bn_param = {'mode': 'train'}
gamma = np.ones(C)
beta = np.zeros(C)
for t in range(50):
    x = 2.3 * np.random.randn(N, C, H, W) + 13
    spatial_batchnorm_forward(x, gamma, beta, bn_param)
bn_param['mode'] = 'test'
x = 2.3 * np.random.randn(N, C, H, W) + 13
a_norm, _ = spatial_batchnorm_forward(x, gamma, beta, bn_param)

# Means should be close to zero and stds close to one, but will be
# noisier than training-time forward passes.
print('After spatial batch normalization (test-time):')
print('  means: ', a_norm.mean(axis=(0, 2, 3)))
print('  stds: ', a_norm.std(axis=(0, 2, 3)))
```

## Spatial batch normalization: backward

In the file `cs682/layers.py`, implement the backward pass for spatial batch normalization in the function `spatial_batchnorm_backward`. Run the following to check your implementation using a numeric gradient check:



```
In [58]: np.random.seed(231)
N, C, H, W = 2, 3, 4, 5
x = 5 * np.random.randn(N, C, H, W) + 12
gamma = np.random.randn(C)
beta = np.random.randn(C)
dout = np.random.randn(N, C, H, W)

bn_param = {'mode': 'train'}
fx = lambda x: spatial_batchnorm_forward(x, gamma, beta, bn_param)[0]
fg = lambda a: spatial_batchnorm_forward(x, gamma, beta, bn_param)[0]
fb = lambda b: spatial_batchnorm_forward(x, gamma, beta, bn_param)[0]

dx_num = eval_numerical_gradient_array(fx, x, dout)
da_num = eval_numerical_gradient_array(fg, gamma, dout)
db_num = eval_numerical_gradient_array(fb, beta, dout)

#You should expect errors of magnitudes between 1e-12~1e-06
_, cache = spatial_batchnorm_forward(x, gamma, beta, bn_param)
dx, dgamma, dbeta = spatial_batchnorm_backward(dout, cache)
print('dx error: ', rel_error(dx_num, dx))
print('dgamma error: ', rel_error(da_num, dgamma))
print('dbeta error: ', rel_error(db_num, dbeta))

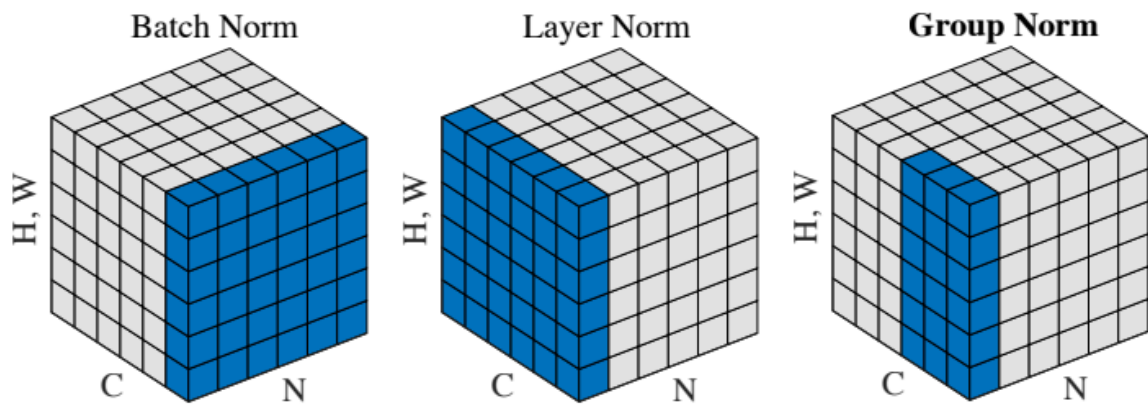
dx error:  2.7866481890178303e-07
dgamma error:  7.0974817113608705e-12
dbeta error:  3.275608725278405e-12
```

## Group Normalization

In the previous notebook, we mentioned that Layer Normalization is an alternative normalization technique that mitigates the batch size limitations of Batch Normalization. However, as the authors of [4] observed, Layer Normalization does not perform as well as Batch Normalization when used with Convolutional Layers:

With fully connected layers, all the hidden units in a layer tend to make similar contributions to the final prediction, and re-centering and rescaling the summed inputs to a layer works well. However, the assumption of similar contributions is no longer true for convolutional neural networks. The large number of the hidden units whose receptive fields lie near the boundary of the image are rarely turned on and thus have very different statistics from the rest of the hidden units within the same layer.

The authors of [5] propose an intermediary technique. In contrast to Layer Normalization, where you normalize over the entire feature per-datapoint, they suggest a consistent splitting of each per-datapoint feature into  $G$  groups, and a per-group per-datapoint normalization instead.



**\*\*Visual comparison of the normalization techniques discussed so far (image edited from [5])\*\***

Even though an assumption of equal contribution is still being made within each group, the authors hypothesize that this is not as problematic, as innate grouping arises within features for visual recognition. One example they use to illustrate this is that many high-performance handcrafted features in traditional Computer Vision have terms that are explicitly grouped together. Take for example Histogram of Oriented Gradients [6]-- after computing histograms per spatially local block, each per-block histogram is normalized before being concatenated together to form the final feature vector.

You will now implement Group Normalization. Note that this normalization technique that you are to implement in the following cells was introduced and published to arXiv *less than a month ago* -- this truly is still an ongoing and excitingly active field of research!

[4] [Ba, Jimmy Lei, Jamie Ryan Kiros, and Geoffrey E. Hinton. "Layer Normalization." stat 1050 \(2016\): 21.](#)

[5] [Wu, Yuxin, and Kaiming He. "Group Normalization." arXiv preprint arXiv:1803.08494 \(2018\).](#)

[6] [N. Dalal and B. Triggs. Histograms of oriented gradients for human detection. In Computer Vision and Pattern Recognition \(CVPR\), 2005.](#)

## Group normalization: forward

In the file `cs682/layers.py`, implement the forward pass for group normalization in the function `spatial_groupnorm_forward`. Check your implementation by running the following:

```
In [66]: np.random.seed(231)
# Check the training-time forward pass by checking means and variances
# of features both before and after spatial batch normalization

N, C, H, W = 2, 6, 4, 5
G = 2
x = 4 * np.random.randn(N, C, H, W) + 10
x_g = x.reshape((N*G,-1))
print('Before spatial group normalization:')
print('  Shape: ', x.shape)
print('  Means: ', x_g.mean(axis=1))
print('  Stds: ', x_g.std(axis=1))

# Means should be close to zero and stds close to one
gamma, beta = np.ones((1,C,1,1)), np.zeros((1,C,1,1))
bn_param = {'mode': 'train'}

out, _ = spatial_groupnorm_forward(x, gamma, beta, G, bn_param)
out_g = out.reshape((N*G,-1))
print('After spatial group normalization:')
print('  Shape: ', out.shape)
print('  Means: ', out_g.mean(axis=1))
print('  Stds: ', out_g.std(axis=1))
```

Before spatial group normalization:

Shape: (2, 6, 4, 5)

Means: [9.72505327 8.51114185 8.9147544 9.43448077]

Stds: [3.67070958 3.09892597 4.27043622 3.97521327]

After spatial group normalization:

Shape: (2, 6, 4, 5)

Means: [-2.14643118e-16 5.25505565e-16 2.65528340e-16 -3.38618023e-16]

Stds: [0.99999963 0.99999948 0.99999973 0.99999968]

## Spatial group normalization: backward

In the file `cs682/layers.py`, implement the backward pass for spatial batch normalization in the function `spatial_groupnorm_backward`. Run the following to check your implementation using a numeric gradient check:

```

In [83]: np.random.seed(231)
N, C, H, W = 2, 6, 4, 5
G = 2
x = 5 * np.random.randn(N, C, H, W) + 12
gamma = np.random.randn(1, C, 1, 1)
beta = np.random.randn(1, C, 1, 1)
dout = np.random.randn(N, C, H, W)

gn_param = {}
fx = lambda x: spatial_groupnorm_forward(x, gamma, beta, G, gn_param)[0]
fg = lambda a: spatial_groupnorm_forward(x, gamma, beta, G, gn_param)[0]
fb = lambda b: spatial_groupnorm_forward(x, gamma, beta, G, gn_param)[0]

dx_num = eval_numerical_gradient_array(fx, x, dout)
da_num = eval_numerical_gradient_array(fg, gamma, dout)
db_num = eval_numerical_gradient_array(fb, beta, dout)

_, cache = spatial_groupnorm_forward(x, gamma, beta, G, gn_param)
dx, dgamma, dbeta = spatial_groupnorm_backward(dout, cache)
#You should expect errors of magnitudes between 1e-12~1e-07
print('dx error: ', rel_error(dx_num, dx))
print('dgamma error: ', rel_error(da_num, dgamma))
print('dbeta error: ', rel_error(db_num, dbeta))

```

```

dx error: 7.413109404620405e-08
dgamma error: 9.468195772749234e-12
dbeta error: 3.354494437653335e-12

```

```
In [ ]: from google.colab import drive  
drive.mount('/content/drive')
```

Mounted at /content/drive

```
In [ ]: %cd drive/'My Drive'/assignment2
```

/content/drive/My Drive/assignment2

## What's this PyTorch business?

You've written a lot of code in this assignment to provide a whole host of neural network functionality. Dropout, Batch Norm, and 2D convolutions are some of the workhorses of deep learning in computer vision. You've also worked hard to make your code efficient and vectorized.

For the last part of this assignment, though, we're going to leave behind your beautiful codebase and instead migrate to one of two popular deep learning frameworks: in this instance, PyTorch (or TensorFlow, if you switch over to that notebook).

## What is PyTorch?

PyTorch is a system for executing dynamic computational graphs over Tensor objects that behave similarly as numpy ndarray. It comes with a powerful automatic differentiation engine that removes the need for manual back-propagation.

## Why?

- Our code will now run on GPUs! Much faster training. When using a framework like PyTorch or TensorFlow you can harness the power of the GPU for your own custom neural network architectures without having to write CUDA code directly (which is beyond the scope of this class).
- We want you to be ready to use one of these frameworks for your project so you can experiment more efficiently than if you were writing every feature you want to use by hand.
- We want you to stand on the shoulders of giants! TensorFlow and PyTorch are both excellent frameworks that will make your lives a lot easier, and now that you understand their guts, you are free to use them :)
- We want you to be exposed to the sort of deep learning code you might run into in academia or industry.

## PyTorch versions

This notebook assumes that you are using **PyTorch version 0.4**. Prior to this version, Tensors had to be wrapped in Variable objects to be used in autograd; however Variables have now been deprecated. In addition 0.4 also separates a Tensor's datatype from its device, and uses numpy-style factories for constructing Tensors rather than directly invoking Tensor constructors.

## How will I learn PyTorch?

Justin Johnson has made an excellent [tutorial](#) for PyTorch.

You can also find the detailed [API doc](#) here. If you have other questions that are not addressed by the API docs, the [PyTorch forum](#) is a much better place to ask than StackOverflow.

## Table of Contents

This assignment has 5 parts. You will learn PyTorch on different levels of abstractions, which will help you understand it better and prepare you for the final project.

1. Preparation: we will use CIFAR-10 dataset.
2. Barebones PyTorch: we will work directly with the lowest-level PyTorch Tensors.
3. PyTorch Module API: we will use `nn.Module` to define arbitrary neural network architecture.
4. PyTorch Sequential API: we will use `nn.Sequential` to define a linear feed-forward network very conveniently.
5. CIFAR-10 open-ended challenge: please implement your own network to get as high accuracy as possible on CIFAR-10. You can experiment with any layer, optimizer, hyperparameters or other advanced features.

Here is a table of comparison:

API	Flexibility	Convenience
Barebone	High	Low
<code>nn.Module</code>	High	Medium
<code>nn.Sequential</code>	Low	High

# Part I. Preparation

First, we load the CIFAR-10 dataset. This might take a couple minutes the first time you do it, but the files should stay cached after that.

In previous parts of the assignment we had to write our own code to download the CIFAR-10 dataset, preprocess it, and iterate through it in minibatches; PyTorch provides convenient tools to automate this process for us.

```
In [ ]: import torch
import torch.nn as nn
import torch.optim as optim
from torch.utils.data import DataLoader
from torch.utils.data import sampler

import torchvision.datasets as dset
import torchvision.transforms as T

import numpy as np
```

```
In [ ]: NUM_TRAIN = 49000

# The torchvision.transforms package provides tools for preprocessing data
# and for performing data augmentation; here we set up a transform to
# preprocess the data by subtracting the mean RGB value and dividing by the
# standard deviation of each RGB value; we've hardcoded the mean and std.
transform = T.Compose([
    T.ToTensor(),
    T.Normalize((0.4914, 0.4822, 0.4465), (0.2023, 0.1994, 0.2010))
])

# We set up a Dataset object for each split (train / val / test); Datasets load
# training examples one at a time, so we wrap each Dataset in a DataLoader which
# iterates through the Dataset and forms minibatches. We divide the CIFAR-10
# training set into train and val sets by passing a Sampler object to the
# DataLoader telling how it should sample from the underlying Dataset.
cifar10_train = dset.CIFAR10('./cs682/datasets', train=True, download=True,
                             transform=transform)
loader_train = DataLoader(cifar10_train, batch_size=64,
                          sampler=sampler.SubsetRandomSampler(range(NUM_TRAIN)))

cifar10_val = dset.CIFAR10('./cs682/datasets', train=True, download=True,
                           transform=transform)
loader_val = DataLoader(cifar10_val, batch_size=64,
                        sampler=sampler.SubsetRandomSampler(range(NUM_TRAIN,
                                                                    NUM_TRAIN +
                                                                    NUM_VAL)))

cifar10_test = dset.CIFAR10('./cs682/datasets', train=False, download=True,
                             transform=transform)
loader_test = DataLoader(cifar10_test, batch_size=64)
```

```
Files already downloaded and verified
Files already downloaded and verified
Files already downloaded and verified
```

You have an option to **use GPU by setting the flag to True below**. It is not necessary to use GPU for this assignment. Note that if your computer does not have CUDA enabled, `torch.cuda.is_available()` will return False and this notebook will fallback to CPU mode.

The global variables `dtype` and `device` will control the data types throughout this assignment.



```
In [ ]: USE_GPU = True

dtype = torch.float32 # we will be using float throughout this tutorial

if USE_GPU and torch.cuda.is_available():
    device = torch.device('cuda')
else:
    device = torch.device('cpu')

# Constant to control how frequently we print train loss
print_every = 100

print('using device:', device)

using device: cuda
```

## Part II. Barebones PyTorch

PyTorch ships with high-level APIs to help us define model architectures conveniently, which we will cover in Part II of this tutorial. In this section, we will start with the barebone PyTorch elements to understand the autograd engine better. After this exercise, you will come to appreciate the high-level model API more.

We will start with a simple fully-connected ReLU network with two hidden layers and no biases for CIFAR classification. This implementation computes the forward pass using operations on PyTorch Tensors, and uses PyTorch autograd to compute gradients. It is important that you understand every line, because you will write a harder version after the example.

When we create a PyTorch Tensor with `requires_grad=True`, then operations involving that Tensor will not just compute values; they will also build up a computational graph in the background, allowing us to easily backpropagate through the graph to compute gradients of some Tensors with respect to a downstream loss. Concretely if `x` is a Tensor with `x.requires_grad == True` then after backpropagation `x.grad` will be another Tensor holding the gradient of `x` with respect to the scalar loss at the end.

## PyTorch Tensors: Flatten Function

A PyTorch Tensor is conceptionally similar to a numpy array: it is an n-dimensional grid of numbers, and like numpy PyTorch provides many functions to efficiently operate on Tensors. As a simple example, we provide a `flatten` function below which reshapes image data for use in a fully-connected neural network.

Recall that image data is typically stored in a Tensor of shape  $N \times C \times H \times W$ , where:

- $N$  is the number of datapoints
- $C$  is the number of channels
- $H$  is the height of the intermediate feature map in pixels
- $W$  is the width of the intermediate feature map in pixels

This is the right way to represent the data when we are doing something like a 2D convolution, that needs spatial understanding of where the intermediate features are relative to each other. When we use fully connected affine layers to process the image, however, we want each datapoint to be represented by a single vector -- it's no longer useful to segregate the different channels, rows, and columns of the data. So, we use a "flatten" operation to collapse the  $C \times H \times W$  values per representation into a single long vector. The `flatten` function below first reads in the  $N$ ,  $C$ ,  $H$ , and  $W$  values from a given batch of data, and then returns a "view" of that data. "View" is analogous to numpy's "reshape" method: it reshapes  $x$ 's dimensions to be  $N \times ??$ , where  $??$  is allowed to be anything (in this case, it will be  $C \times H \times W$ , but we don't need to specify that explicitly).

```
In [ ]: def flatten(x):
        N = x.shape[0] # read in N, C, H, W
        return x.view(N, -1) # "flatten" the C * H * W values into a single vector

def test_flatten():
    x = torch.arange(12).view(2, 1, 3, 2)
    print('Before flattening: ', x)
    print('After flattening: ', flatten(x))

test_flatten()
```

```
Before flattening:  tensor([[[[ 0,  1],
        [ 2,  3],
        [ 4,  5]]],
        [[[ 6,  7],
        [ 8,  9],
        [10, 11]]]])
After flattening:  tensor([[ 0,  1,  2,  3,  4,  5],
        [ 6,  7,  8,  9, 10, 11]])
```

## Barebones PyTorch: Two-Layer Network

Here we define a function `two_layer_fc` which performs the forward pass of a two-layer fully-connected ReLU network on a batch of image data. After defining the forward pass we check that it doesn't crash and that it produces outputs of the right shape by running zeros through the network.

You don't have to write any code here, but it's important that you read and understand the implementation.

```
In [ ]: import torch.nn.functional as F # useful stateless functions

def two_layer_fc(x, params):
    """
    A fully-connected neural networks; the architecture is:
    NN is fully connected -> ReLU -> fully connected layer.
    Note that this function only defines the forward pass;
    PyTorch will take care of the backward pass for us.

    The input to the network will be a minibatch of data, of shape
    (N, d1, ..., dM) where d1 * ... * dM = D. The hidden layer will have H un
    and the output layer will produce scores for C classes.

    Inputs:
    - x: A PyTorch Tensor of shape (N, d1, ..., dM) giving a minibatch of
      input data.
    - params: A list [w1, w2] of PyTorch Tensors giving weights for the netwo
      w1 has shape (D, H) and w2 has shape (H, C).

    Returns:
    - scores: A PyTorch Tensor of shape (N, C) giving classification scores f
      the input data x.
    """
    # first we flatten the image
    x = flatten(x) # shape: [batch_size, C x H x W]

    w1, w2 = params

    # Forward pass: compute predicted y using operations on Tensors. Since w1
    # w2 have requires_grad=True, operations involving these Tensors will cau
    # PyTorch to build a computational graph, allowing automatic computation
    # gradients. Since we are no longer implementing the backward pass by han
    # don't need to keep references to intermediate values.
    # you can also use `.clamp(min=0)`, equivalent to F.relu()
    x = F.relu(x.mm(w1))
    x = x.mm(w2)
    return x

def two_layer_fc_test():
    hidden_layer_size = 42
    x = torch.zeros((64, 50), dtype=dtype) # minibatch size 64, feature dime
    w1 = torch.zeros((50, hidden_layer_size), dtype=dtype)
    w2 = torch.zeros((hidden_layer_size, 10), dtype=dtype)
    scores = two_layer_fc(x, [w1, w2])
    print(scores.size()) # you should see [64, 10]

two_layer_fc_test()

torch.Size([64, 10])
```

## Barebones PyTorch: Three-Layer ConvNet

Here you will complete the implementation of the function `three_layer_convnet`, which will perform the forward pass of a three-layer convolutional network. Like above, we can immediately test our implementation by passing zeros through the network. The network should have the following architecture:

1. A convolutional layer (with bias) with `channel_1` filters, each with shape `KW1 x KH1`, and zero-padding of two
2. ReLU nonlinearity
3. A convolutional layer (with bias) with `channel_2` filters, each with shape `KW2 x KH2`, and zero-padding of one
4. ReLU nonlinearity
5. Fully-connected layer with bias, producing scores for `C` classes.

**HINT:** For convolutions: <http://pytorch.org/docs/stable/nn.html#torch.nn.functional.conv2d>; pay attention to the shapes of convolutional filters!

```

In [ ]: def three_layer_convnet(x, params):
        """
        Performs the forward pass of a three-layer convolutional network with the
        architecture defined above.

        Inputs:
        - x: A PyTorch Tensor of shape (N, 3, H, W) giving a minibatch of images
        - params: A list of PyTorch Tensors giving the weights and biases for the
          network; should contain the following:
          - conv_w1: PyTorch Tensor of shape (channel_1, 3, KH1, KW1) giving weights
            for the first convolutional layer
          - conv_b1: PyTorch Tensor of shape (channel_1,) giving biases for the first
            convolutional layer
          - conv_w2: PyTorch Tensor of shape (channel_2, channel_1, KH2, KW2) giving
            weights for the second convolutional layer
          - conv_b2: PyTorch Tensor of shape (channel_2,) giving biases for the second
            convolutional layer
          - fc_w: PyTorch Tensor giving weights for the fully-connected layer. Can
            figure out what the shape should be?
          - fc_b: PyTorch Tensor giving biases for the fully-connected layer. Can
            figure out what the shape should be?

        Returns:
        - scores: PyTorch Tensor of shape (N, C) giving classification scores for
          """

        conv_w1, conv_b1, conv_w2, conv_b2, fc_w, fc_b = params
        scores = None
        #####
        # TODO: Implement the forward pass for the three-layer ConvNet.
        #####
        l1 = F.relu(F.conv2d(x, conv_w1, conv_b1, padding=2))
        l2 = F.relu(F.conv2d(l1, conv_w2, conv_b2, padding=1))

        l2 = flatten(l2)
        scores = l2.mm(fc_w) + fc_b
        #####
        #                                     END OF YOUR CODE
        #####
        return scores

```

After defining the forward pass of the ConvNet above, run the following cell to test your implementation.

When you run this function, scores should have shape (64, 10).

```
In [ ]: def three_layer_convnet_test():
    x = torch.zeros((64, 3, 32, 32), dtype=dtype) # minibatch size 64, image

    conv_w1 = torch.zeros((6, 3, 5, 5), dtype=dtype) # [out_channel, in_chan
    conv_b1 = torch.zeros((6,)) # out_channel
    conv_w2 = torch.zeros((9, 6, 3, 3), dtype=dtype) # [out_channel, in_chan
    conv_b2 = torch.zeros((9,)) # out_channel

    # you must calculate the shape of the tensor after two conv layers, befor
    fc_w = torch.zeros((9 * 32 * 32, 10))
    fc_b = torch.zeros(10)

    scores = three_layer_convnet(x, [conv_w1, conv_b1, conv_w2, conv_b2, fc_w
    print(scores.size()) # you should see [64, 10]
    three_layer_convnet_test()

torch.Size([64, 10])
```

## Barebones PyTorch: Initialization

Let's write a couple utility methods to initialize the weight matrices for our models.

- `random_weight(shape)` initializes a weight tensor with the Kaiming normalization method.
- `zero_weight(shape)` initializes a weight tensor with all zeros. Useful for instantiating bias parameters.

The `random_weight` function uses the Kaiming normal initialization method, described in:

He et al, *Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification*, ICCV 2015, <https://arxiv.org/abs/1502.01852>

```
In [ ]: def random_weight(shape):
        """
        Create random Tensors for weights; setting requires_grad=True means that
        we want to compute gradients for these Tensors during the backward pass.
        We use Kaiming normalization: sqrt(2 / fan_in)
        """
        if len(shape) == 2: # FC weight
            fan_in = shape[0]
        else:
            fan_in = np.prod(shape[1:]) # conv weight [out_channel, in_channel, k
            # randn is standard normal distribution generator.
        w = torch.randn(shape, device=device, dtype=dtype) * np.sqrt(2. / fan_in)
        w.requires_grad = True
        return w

def zero_weight(shape):
    return torch.zeros(shape, device=device, dtype=dtype, requires_grad=True)

# create a weight of shape [3 x 5]
# you should see the type `torch.cuda.FloatTensor` if you use GPU.
# Otherwise it should be `torch.FloatTensor`
random_weight((3, 5))
```

```
Out[ ]: tensor([[ 0.2881, -1.1215, -0.4992,  1.6163,  0.0931],
                [ 0.2477, -0.2718,  0.3513, -0.0390,  0.5250],
                [ 0.9507,  0.9545, -0.6882, -0.4800,  0.0175]], device='cuda:0',
        requires_grad=True)
```

## Barebones PyTorch: Check Accuracy

When training the model we will use the following function to check the accuracy of our model on the training or validation sets.

When checking accuracy we don't need to compute any gradients; as a result we don't need PyTorch to build a computational graph for us when we compute scores. To prevent a graph from being built we scope our computation under a `torch.no_grad()` context manager.



```
In [ ]: def check_accuracy_part2(loader, model_fn, params):
        """
        Check the accuracy of a classification model.

        Inputs:
        - loader: A DataLoader for the data split we want to check
        - model_fn: A function that performs the forward pass of the model,
          with the signature scores = model_fn(x, params)
        - params: List of PyTorch Tensors giving parameters of the model

        Returns: Nothing, but prints the accuracy of the model
        """
        split = 'val' if loader.dataset.train else 'test'
        print('Checking accuracy on the %s set' % split)
        num_correct, num_samples = 0, 0
        with torch.no_grad():
            for x, y in loader:
                x = x.to(device=device, dtype=dtype) # move to device, e.g. GPU
                y = y.to(device=device, dtype=torch.int64)
                scores = model_fn(x, params)
                _, preds = scores.max(1)
                num_correct += (preds == y).sum()
                num_samples += preds.size(0)
        acc = float(num_correct) / num_samples
        print('Got %d / %d correct (%.2f%%)' % (num_correct, num_samples, 100
```

## BareBones PyTorch: Training Loop

We can now set up a basic training loop to train our network. We will train the model using stochastic gradient descent without momentum. We will use

`torch.functional.cross_entropy` to compute the loss; you can [read about it here](#).

The training loop takes as input the neural network function, a list of initialized parameters ( `[w1, w2]` in our example), and learning rate.

```
In [ ]: def train_part2(model_fn, params, learning_rate):
        """
        Train a model on CIFAR-10.

        Inputs:
        - model_fn: A Python function that performs the forward pass of the model
          It should have the signature scores = model_fn(x, params) where x is a
          PyTorch Tensor of image data, params is a list of PyTorch Tensors giving
          model weights, and scores is a PyTorch Tensor of shape (N, C) giving
          scores for the elements in x.
        - params: List of PyTorch Tensors giving weights for the model
        - learning_rate: Python scalar giving the learning rate to use for SGD

        Returns: Nothing
        """
        for t, (x, y) in enumerate(loader_train):
            # Move the data to the proper device (GPU or CPU)
            x = x.to(device=device, dtype=dtype)
            y = y.to(device=device, dtype=torch.long)

            # Forward pass: compute scores and loss
            scores = model_fn(x, params)
            loss = F.cross_entropy(scores, y)

            # Backward pass: PyTorch figures out which Tensors in the computation
            # graph has requires_grad=True and uses backpropagation to compute the
            # gradient of the loss with respect to these Tensors, and stores the
            # gradients in the .grad attribute of each Tensor.
            loss.backward()

            # Update parameters. We don't want to backpropagate through the
            # parameter updates, so we scope the updates under a torch.no_grad()
            # context manager to prevent a computational graph from being built.
            with torch.no_grad():
                for w in params:
                    w -= learning_rate * w.grad

                    # Manually zero the gradients after running the backward pass
                    w.grad.zero_()

            if t % print_every == 0:
                print('Iteration %d, loss = %.4f' % (t, loss.item()))
                check_accuracy_part2(loader_val, model_fn, params)
                print()
```

## BareBones PyTorch: Train a Two-Layer Network

Now we are ready to run the training loop. We need to explicitly allocate tensors for the fully connected weights,  $w_1$  and  $w_2$ .

Each minibatch of CIFAR has 64 examples, so the tensor shape is  $[64, 3, 32, 32]$ .

After flattening,  $x$  shape should be  $[64, 3 * 32 * 32]$ . This will be the size of the first dimension of  $w_1$ . The second dimension of  $w_1$  is the hidden layer size, which will also be the first dimension of  $w_2$ .

Finally, the output of the network is a 10-dimensional vector that represents the probability distribution over 10 classes.

You don't need to tune any hyperparameters but you should see accuracies above 40% after training for one epoch.

```
In [ ]: hidden_layer_size = 4000
        learning_rate = 1e-2

        w1 = random_weight((3 * 32 * 32, hidden_layer_size))
        w2 = random_weight((hidden_layer_size, 10))

        train_part2(two_layer_fc, [w1, w2], learning_rate)
```

```
Iteration 0, loss = 3.5717
Checking accuracy on the val set
Got 148 / 1000 correct (14.80%)

Iteration 100, loss = 2.7121
Checking accuracy on the val set
Got 342 / 1000 correct (34.20%)

Iteration 200, loss = 2.5636
Checking accuracy on the val set
Got 363 / 1000 correct (36.30%)

Iteration 300, loss = 2.0811
Checking accuracy on the val set
Got 393 / 1000 correct (39.30%)

Iteration 400, loss = 1.8740
Checking accuracy on the val set
Got 418 / 1000 correct (41.80%)

Iteration 500, loss = 1.8955
Checking accuracy on the val set
Got 438 / 1000 correct (43.80%)

Iteration 600, loss = 1.8256
Checking accuracy on the val set
Got 429 / 1000 correct (42.90%)

Iteration 700, loss = 1.6103
Checking accuracy on the val set
Got 447 / 1000 correct (44.70%)
```

## BareBones PyTorch: Training a ConvNet

In the below you should use the functions defined above to train a three-layer convolutional network on CIFAR. The network should have the following architecture:

1. Convolutional layer (with bias) with 32 5x5 filters, with zero-padding of 2
2. ReLU
3. Convolutional layer (with bias) with 16 3x3 filters, with zero-padding of 1
4. ReLU
5. Fully-connected layer (with bias) to compute scores for 10 classes

You should initialize your weight matrices using the `random_weight` function defined above, and you should initialize your bias vectors using the `zero_weight` function above.

You don't need to tune any hyperparameters, but if everything works correctly you should achieve an accuracy above 42% after one epoch.

```

In [ ]: learning_rate = 3e-3

channel_1 = 32
channel_2 = 16

conv_w1 = None
conv_b1 = None
conv_w2 = None
conv_b2 = None
fc_w = None
fc_b = None

#####
# TODO: Initialize the parameters of a three-layer ConvNet.
#####
conv_w1 = random_weight((channel_1, 3, 5, 5))
conv_b1 = random_weight((channel_1,))

conv_w2 = random_weight((channel_2, channel_1, 3, 3))
conv_b2 = random_weight((channel_2,))

fc_w = random_weight((channel_2 * 32 * 32, 10))
fc_b = random_weight((10,))
#####
#                               END OF YOUR CODE
#####

params = [conv_w1, conv_b1, conv_w2, conv_b2, fc_w, fc_b]
train_part2(three_layer_convnet, params, learning_rate)

```

Iteration 0, loss = 4.4105  
Checking accuracy on the val set  
Got 88 / 1000 correct (8.80%)

Iteration 100, loss = 1.7848  
Checking accuracy on the val set  
Got 335 / 1000 correct (33.50%)

Iteration 200, loss = 1.9400  
Checking accuracy on the val set  
Got 370 / 1000 correct (37.00%)

Iteration 300, loss = 1.5869  
Checking accuracy on the val set  
Got 424 / 1000 correct (42.40%)

Iteration 400, loss = 1.5864  
Checking accuracy on the val set  
Got 398 / 1000 correct (39.80%)

Iteration 500, loss = 1.6674  
Checking accuracy on the val set  
Got 455 / 1000 correct (45.50%)

Iteration 600, loss = 1.4378  
Checking accuracy on the val set  
Got 464 / 1000 correct (46.40%)

Iteration 700, loss = 1.4332  
Checking accuracy on the val set  
Got 474 / 1000 correct (47.40%)

## Part III. PyTorch Module API

Barebone PyTorch requires that we track all the parameter tensors by hand. This is fine for small networks with a few tensors, but it would be extremely inconvenient and error-prone to track tens or hundreds of tensors in larger networks.

PyTorch provides the `nn.Module` API for you to define arbitrary network architectures, while tracking every learnable parameters for you. In Part II, we implemented SGD ourselves. PyTorch also provides the `torch.optim` package that implements all the common optimizers, such as RMSProp, Adagrad, and Adam. It even supports approximate second-order methods like L-BFGS! You can refer to the [doc](#) for the exact specifications of each optimizer.

To use the Module API, follow the steps below:

1. Subclass `nn.Module` . Give your network class an intuitive name like `TwoLayerFC` .
2. In the constructor `__init__()` , define all the layers you need as class attributes. Layer objects like `nn.Linear` and `nn.Conv2d` are themselves `nn.Module` subclasses and contain learnable parameters, so that you don't have to instantiate the raw tensors yourself. `nn.Module` will track these internal parameters for you. Refer to the [doc](#) to learn more about the dozens of builtin layers. **Warning:** don't forget to call the `super().__init__()` first!
3. In the `forward()` method, define the *connectivity* of your network. You should use the attributes defined in `__init__` as function calls that take tensor as input and output the "transformed" tensor. Do *not* create any new layers with learnable parameters in `forward()` ! All of them must be declared upfront in `__init__` .

After you define your Module subclass, you can instantiate it as an object and call it just like the NN forward function in part II.

### Module API: Two-Layer Network

Here is a concrete example of a 2-layer fully connected network:

```
In [ ]: class TwoLayerFC(nn.Module):
    def __init__(self, input_size, hidden_size, num_classes):
        super().__init__()
        # assign layer objects to class attributes
        self.fc1 = nn.Linear(input_size, hidden_size)
        # nn.init package contains convenient initialization methods
        # http://pytorch.org/docs/master/nn.html#torch-nn-init
        nn.init.kaiming_normal_(self.fc1.weight)
        self.fc2 = nn.Linear(hidden_size, num_classes)
        nn.init.kaiming_normal_(self.fc2.weight)

    def forward(self, x):
        # forward always defines connectivity
        x = flatten(x)
        scores = self.fc2(F.relu(self.fc1(x)))
        return scores

def test_TwoLayerFC():
    input_size = 50
    x = torch.zeros((64, input_size), dtype=dtype) # minibatch size 64, feat
    model = TwoLayerFC(input_size, 42, 10)
    scores = model(x)
    print(scores.size()) # you should see [64, 10]
test_TwoLayerFC()
```

```
torch.Size([64, 10])
```

## Module API: Three-Layer ConvNet

It's your turn to implement a 3-layer ConvNet followed by a fully connected layer. The network architecture should be the same as in Part II:

1. Convolutional layer with `channel_1` 5x5 filters with zero-padding of 2
2. ReLU
3. Convolutional layer with `channel_2` 3x3 filters with zero-padding of 1
4. ReLU
5. Fully-connected layer to `num_classes` classes

You should initialize the weight matrices of the model using the Kaiming normal initialization method.

**HINT:** <http://pytorch.org/docs/stable/nn.html#conv2d>

After you implement the three-layer ConvNet, the `test_ThreeLayerConvNet` function will run your implementation; it should print `(64, 10)` for the shape of the output scores.



```

In [ ]: class ThreeLayerConvNet(nn.Module):
    def __init__(self, in_channel, channel_1, channel_2, num_classes):
        super().__init__()
        #####
        # TODO: Set up the layers you need for a three-layer ConvNet with the
        # architecture defined above.
        #####
        self.l1 = nn.Conv2d(3, channel_1, 5, padding = 2)
        nn.init.kaiming_normal_(self.l1.weight)

        self.l2 = nn.Conv2d(channel_1, channel_2, 3, padding = 1)
        nn.init.kaiming_normal_(self.l2.weight)

        self.fc = nn.Linear(channel_2*32*32, 10)
        nn.init.kaiming_normal_(self.fc.weight)
        #####
        #                               END OF YOUR CODE
        #####

    def forward(self, x):
        scores = None
        #####
        # TODO: Implement the forward function for a 3-layer ConvNet. you
        # should use the layers you defined in __init__ and specify the
        # connectivity of those layers in forward()
        #####
        l1_scores = F.relu(self.l1(x))
        l2_scores = F.relu(self.l2(l1_scores))

        l2_scores = flatten(l2_scores)
        scores = self.fc(l2_scores)
        #####
        #                               END OF YOUR CODE
        #####
        return scores

def test_ThreeLayerConvNet():
    x = torch.zeros((64, 3, 32, 32), dtype=dtype) # minibatch size 64, image
    model = ThreeLayerConvNet(in_channel=3, channel_1=12, channel_2=8, num_cl
    scores = model(x)
    print(scores.size()) # you should see [64, 10]
    test_ThreeLayerConvNet()

torch.Size([64, 10])

```

## Module API: Check Accuracy

Given the validation or test set, we can check the classification accuracy of a neural network.

This version is slightly different from the one in part II. You don't manually pass in the parameters anymore.

```
In [ ]: def check_accuracy_part34(loader, model):
    if loader.dataset.train:
        print('Checking accuracy on validation set')
    else:
        print('Checking accuracy on test set')
    num_correct = 0
    num_samples = 0
    model.eval() # set model to evaluation mode
    with torch.no_grad():
        for x, y in loader:
            x = x.to(device=device, dtype=dtype) # move to device, e.g. GPU
            y = y.to(device=device, dtype=torch.long)
            scores = model(x)
            _, preds = scores.max(1)
            num_correct += (preds == y).sum()
            num_samples += preds.size(0)
    acc = float(num_correct) / num_samples
    print('Got %d / %d correct (%.2f)' % (num_correct, num_samples, 100 *
```

## Module API: Training Loop

We also use a slightly different training loop. Rather than updating the values of the weights ourselves, we use an Optimizer object from the `torch.optim` package, which abstract the notion of an optimization algorithm and provides implementations of most of the algorithms commonly used to optimize neural networks.

```
In [ ]: def train_part34(model, optimizer, epochs=1):
        """
        Train a model on CIFAR-10 using the PyTorch Module API.

        Inputs:
        - model: A PyTorch Module giving the model to train.
        - optimizer: An Optimizer object we will use to train the model
        - epochs: (Optional) A Python integer giving the number of epochs to train

        Returns: Nothing, but prints model accuracies during training.
        """
        model = model.to(device=device) # move the model parameters to CPU/GPU
        for e in range(epochs):
            for t, (x, y) in enumerate(loader_train):
                model.train() # put model to training mode
                x = x.to(device=device, dtype=dtype) # move to device, e.g. GPU
                y = y.to(device=device, dtype=torch.long)

                scores = model(x)
                loss = F.cross_entropy(scores, y)

                # Zero out all of the gradients for the variables which the optimizer
                # will update.
                optimizer.zero_grad()

                # This is the backwards pass: compute the gradient of the loss with
                # respect to each parameter of the model.
                loss.backward()

                # Actually update the parameters of the model using the gradients
                # computed by the backwards pass.
                optimizer.step()

            if t % print_every == 0:
                print('Iteration %d, loss = %.4f' % (t, loss.item()))
                check_accuracy_part34(loader_val, model)
                print()
```

## Module API: Train a Two-Layer Network

Now we are ready to run the training loop. In contrast to part II, we don't explicitly allocate parameter tensors anymore.

Simply pass the input size, hidden layer size, and number of classes (i.e. output size) to the constructor of `TwoLayerFC`.

You also need to define an optimizer that tracks all the learnable parameters inside `TwoLayerFC`.

You don't need to tune any hyperparameters, but you should see model accuracies above 40% after training for one epoch.

```
In [ ]: hidden_layer_size = 4000
        learning_rate = 1e-2
        model = TwoLayerFC(3 * 32 * 32, hidden_layer_size, 10)
        optimizer = optim.SGD(model.parameters(), lr=learning_rate)

        train_part34(model, optimizer)
```

```
Iteration 0, loss = 3.5576
Checking accuracy on validation set
Got 147 / 1000 correct (14.70)

Iteration 100, loss = 2.3058
Checking accuracy on validation set
Got 316 / 1000 correct (31.60)

Iteration 200, loss = 1.5816
Checking accuracy on validation set
Got 389 / 1000 correct (38.90)

Iteration 300, loss = 2.4165
Checking accuracy on validation set
Got 375 / 1000 correct (37.50)

Iteration 400, loss = 1.9937
Checking accuracy on validation set
Got 394 / 1000 correct (39.40)

Iteration 500, loss = 1.3074
Checking accuracy on validation set
Got 434 / 1000 correct (43.40)

Iteration 600, loss = 1.5334
Checking accuracy on validation set
Got 407 / 1000 correct (40.70)

Iteration 700, loss = 2.0902
Checking accuracy on validation set
Got 433 / 1000 correct (43.30)
```

## Module API: Train a Three-Layer ConvNet

You should now use the Module API to train a three-layer ConvNet on CIFAR. This should look very similar to training the two-layer network! You don't need to tune any hyperparameters, but you should achieve above 45% after training for one epoch.

You should train the model using stochastic gradient descent without momentum.

```
In [ ]: learning_rate = 3e-3
channel_1 = 32
channel_2 = 16

model = None
optimizer = None
#####
# TODO: Instantiate your ThreeLayerConvNet model and a corresponding optimizer
#####
model = ThreeLayerConvNet(3, channel_1, channel_2, 10)
optimizer = optim.SGD(model.parameters(), lr=learning_rate)
#####
#                                     END OF YOUR CODE
#####

train_part34(model, optimizer)
```

```
Iteration 0, loss = 4.0372
Checking accuracy on validation set
Got 118 / 1000 correct (11.80)
```

```
Iteration 100, loss = 1.8218
Checking accuracy on validation set
Got 347 / 1000 correct (34.70)
```

```
Iteration 200, loss = 1.8026
Checking accuracy on validation set
Got 394 / 1000 correct (39.40)
```

```
Iteration 300, loss = 1.8290
Checking accuracy on validation set
Got 409 / 1000 correct (40.90)
```

```
Iteration 400, loss = 1.6821
Checking accuracy on validation set
Got 447 / 1000 correct (44.70)
```

```
Iteration 500, loss = 1.7684
Checking accuracy on validation set
Got 461 / 1000 correct (46.10)
```

```
Iteration 600, loss = 1.7884
Checking accuracy on validation set
Got 461 / 1000 correct (46.10)
```

```
Iteration 700, loss = 1.5378
Checking accuracy on validation set
Got 458 / 1000 correct (45.80)
```

## Part IV. PyTorch Sequential API

Part III introduced the PyTorch Module API, which allows you to define arbitrary learnable layers and their connectivity.

For simple models like a stack of feed forward layers, you still need to go through 3 steps: subclass `nn.Module`, assign layers to class attributes in `__init__`, and call each layer one by one in `forward()`. Is there a more convenient way?

Fortunately, PyTorch provides a container Module called `nn.Sequential`, which merges the above steps into one. It is not as flexible as `nn.Module`, because you cannot specify more complex topology than a feed-forward stack, but it's good enough for many use cases.

### Sequential API: Two-Layer Network

Let's see how to rewrite our two-layer fully connected network example with `nn.Sequential`, and train it using the training loop defined above.

Again, you don't need to tune any hyperparameters here, but you should achieve above 40% accuracy after one epoch of training.

```
In [ ]: # We need to wrap `flatten` function in a module in order to stack it
# in nn.Sequential
class Flatten(nn.Module):
    def forward(self, x):
        return flatten(x)

hidden_layer_size = 4000
learning_rate = 1e-2

model = nn.Sequential(
    Flatten(),
    nn.Linear(3 * 32 * 32, hidden_layer_size),
    nn.ReLU(),
    nn.Linear(hidden_layer_size, 10),
)

# you can use Nesterov momentum in optim.SGD
optimizer = optim.SGD(model.parameters(), lr=learning_rate,
                       momentum=0.9, nesterov=True)

train_part34(model, optimizer)
```

```
Iteration 0, loss = 2.2513
Checking accuracy on validation set
Got 189 / 1000 correct (18.90)

Iteration 100, loss = 2.0988
Checking accuracy on validation set
Got 404 / 1000 correct (40.40)

Iteration 200, loss = 1.7705
Checking accuracy on validation set
Got 409 / 1000 correct (40.90)

Iteration 300, loss = 1.7138
Checking accuracy on validation set
Got 411 / 1000 correct (41.10)

Iteration 400, loss = 1.8047
Checking accuracy on validation set
Got 406 / 1000 correct (40.60)

Iteration 500, loss = 1.6942
Checking accuracy on validation set
Got 409 / 1000 correct (40.90)

Iteration 600, loss = 1.9711
Checking accuracy on validation set
Got 463 / 1000 correct (46.30)

Iteration 700, loss = 1.8276
Checking accuracy on validation set
Got 460 / 1000 correct (46.00)
```



## Sequential API: Three-Layer ConvNet

Here you should use `nn.Sequential` to define and train a three-layer ConvNet with the same architecture we used in Part III:

1. Convolutional layer (with bias) with 32 5x5 filters, with zero-padding of 2
2. ReLU
3. Convolutional layer (with bias) with 16 3x3 filters, with zero-padding of 1
4. ReLU
5. Fully-connected layer (with bias) to compute scores for 10 classes

You should initialize your weight matrices using the `random_weight` function defined above, and you should initialize your bias vectors using the `zero_weight` function above.

You should optimize your model using stochastic gradient descent with Nesterov momentum 0.9.

Again, you don't need to tune any hyperparameters but you should see accuracy above 55% after one epoch of training.

```
In [ ]: channel_1 = 32
channel_2 = 16
learning_rate = 1e-2

model = None
optimizer = None

#####
# TODO: Rewrite the 2-layer ConvNet with bias from Part III with the
# Sequential API.
#####
model = nn.Sequential (
    nn.Conv2d(3, channel_1, 5, padding = 2),
    nn.ReLU(),
    nn.Conv2d(channel_1, channel_2, 3, padding = 1),
    nn.ReLU(),
    Flatten(),
    nn.Linear(channel_2*32*32, 10)
)
optimizer = optim.SGD(model.parameters(), lr=learning_rate,
                        momentum=0.9, nesterov=True)
#####
#                               END OF YOUR CODE
#####

train_part34(model, optimizer)
```

```
Iteration 0, loss = 2.3125
Checking accuracy on validation set
Got 134 / 1000 correct (13.40)

Iteration 100, loss = 1.6648
Checking accuracy on validation set
Got 476 / 1000 correct (47.60)

Iteration 200, loss = 1.5706
Checking accuracy on validation set
Got 496 / 1000 correct (49.60)

Iteration 300, loss = 1.3650
Checking accuracy on validation set
Got 505 / 1000 correct (50.50)

Iteration 400, loss = 1.2987
Checking accuracy on validation set
Got 501 / 1000 correct (50.10)

Iteration 500, loss = 1.2815
Checking accuracy on validation set
Got 584 / 1000 correct (58.40)

Iteration 600, loss = 1.4267
Checking accuracy on validation set
Got 544 / 1000 correct (54.40)

Iteration 700, loss = 1.0460
Checking accuracy on validation set
Got 574 / 1000 correct (57.40)
```

## Part V. CIFAR-10 open-ended challenge

In this section, you can experiment with whatever ConvNet architecture you'd like on CIFAR-10.

Now it's your job to experiment with architectures, hyperparameters, loss functions, and optimizers to train a model that achieves **at least 70%** accuracy on the CIFAR-10 **validation** set within 10 epochs. You can use the `check_accuracy` and `train` functions from above. You can use either `nn.Module` or `nn.Sequential` API.

Describe what you did at the end of this notebook.

Here are the official API documentation for each component. One note: what we call in the class "spatial batch norm" is called "BatchNorm2D" in PyTorch.

- Layers in torch.nn package: <http://pytorch.org/docs/stable/nn.html>
- Activations: <http://pytorch.org/docs/stable/nn.html#non-linear-activations>

- Loss functions: <http://pytorch.org/docs/stable/nn.html#loss-functions>
- Optimizers: <http://pytorch.org/docs/stable/optim.html>

## Things you might try:

- **Filter size:** Above we used 5x5; would smaller filters be more efficient?
- **Number of filters:** Above we used 32 filters. Do more or fewer do better?
- **Pooling vs Strided Convolution:** Do you use max pooling or just stride convolutions?
- **Batch normalization:** Try adding spatial batch normalization after convolution layers and vanilla batch normalization after affine layers. Do your networks train faster?
- **Network architecture:** The network above has two layers of trainable parameters. Can you do better with a deep network? Good architectures to try include:
  - [conv-relu-pool]xN -> [affine]xM -> [softmax or SVM]
  - [conv-relu-conv-relu-pool]xN -> [affine]xM -> [softmax or SVM]
  - [batchnorm-relu-conv]xN -> [affine]xM -> [softmax or SVM]
- **Global Average Pooling:** Instead of flattening and then having multiple affine layers, perform convolutions until your image gets small (7x7 or so) and then perform an average pooling operation to get to a 1x1 image picture (1, 1, Filter#), which is then reshaped into a (Filter#) vector. This is used in [Google's Inception Network](#) (See Table 1 for their architecture).
- **Regularization:** Add l2 weight regularization, or perhaps use Dropout.

## Tips for training

For each network architecture that you try, you should tune the learning rate and other hyperparameters. When doing this there are a couple important things to keep in mind:

- If the parameters are working well, you should see improvement within a few hundred iterations
- Remember the coarse-to-fine approach for hyperparameter tuning: start by testing a large range of hyperparameters for just a few training iterations to find the combinations of parameters that are working at all.
- Once you have found some sets of parameters that seem to work, search more finely around these parameters. You may need to train for more epochs.
- You should use the validation set for hyperparameter search, and save your test set for evaluating your architecture on the best parameters as selected by the validation set.

## Going above and beyond

If you are feeling adventurous there are many other features you can implement to try and

improve your performance. You are **not required** to implement any of these, but don't miss the fun if you have time!

- Alternative optimizers: you can try Adam, Adagrad, RMSprop, etc.
- Alternative activation functions such as leaky ReLU, parametric ReLU, ELU, or MaxOut.
- Model ensembles
- Data augmentation
- New Architectures
  - [ResNets](#) where the input from the previous layer is added to the output.
  - [DenseNets](#) where inputs into previous layers are concatenated together.
  - [This blog has an in-depth overview](#)

**Have fun and happy training!**

```

In [ ]: #####
# TODO:
# Experiment with any architectures, optimizers, and hyperparameters.
# Achieve AT LEAST 70% accuracy on the *validation set* within 10 epochs.
#
# Note that you can use the check_accuracy function to evaluate on either
# the test set or the validation set, by passing either loader_test or
# loader_val as the second argument to check_accuracy. You should not touch
# the test set until you have finished your architecture and hyperparameter
# tuning, and only run the test set once at the end to report a final value.
#####
learning_rate = 1e-3
channel_1 = 128
channel_2 = 64

model = nn.Sequential (
    nn.Conv2d(3, channel_1, 5, padding = 2),
    nn.ReLU(),
    nn.Conv2d(channel_1, channel_1, 5, padding = 2),
    nn.ReLU(),
    nn.GroupNorm(4, channel_1),
    nn.MaxPool2d(kernel_size=2, stride=2),
    nn.Conv2d(channel_1, channel_2, 3, padding = 1),
    nn.ReLU(),
    nn.Conv2d(channel_2, channel_2, 3, padding = 1),
    nn.ReLU(),
    nn.Conv2d(channel_2, channel_2, 3, padding = 1),
    nn.ReLU(),
    nn.GroupNorm(8, channel_2),
    nn.MaxPool2d(kernel_size=2, stride=2),
    Flatten(),
    nn.Linear(channel_2*8*8, 10)
)
optimizer = optim.Adam(model.parameters(),lr=learning_rate)
#####
#                                     END OF YOUR CODE
#####

# You should get at least 70% accuracy
train_part34(model, optimizer, epochs=10)

```

```

Iteration 0, loss = 2.2672
Checking accuracy on validation set
Got 127 / 1000 correct (12.70)

```

```

Iteration 100, loss = 1.8396
Checking accuracy on validation set
Got 355 / 1000 correct (35.50)

```

```

Iteration 200, loss = 1.7827
Checking accuracy on validation set
Got 365 / 1000 correct (36.50)

```

```
Iteration 300, loss = 1.8297
Checking accuracy on validation set
Got 448 / 1000 correct (44.80)

Iteration 400, loss = 1.3110
Checking accuracy on validation set
Got 491 / 1000 correct (49.10)

Iteration 500, loss = 1.4501
Checking accuracy on validation set
Got 525 / 1000 correct (52.50)

Iteration 600, loss = 1.5110
Checking accuracy on validation set
Got 580 / 1000 correct (58.00)

Iteration 700, loss = 1.1932
Checking accuracy on validation set
Got 570 / 1000 correct (57.00)

Iteration 0, loss = 1.1149
Checking accuracy on validation set
Got 592 / 1000 correct (59.20)

Iteration 100, loss = 1.2798
Checking accuracy on validation set
Got 579 / 1000 correct (57.90)

Iteration 200, loss = 1.0623
Checking accuracy on validation set
Got 607 / 1000 correct (60.70)

Iteration 300, loss = 1.1708
Checking accuracy on validation set
Got 656 / 1000 correct (65.60)

Iteration 400, loss = 1.2187
Checking accuracy on validation set
Got 667 / 1000 correct (66.70)

Iteration 500, loss = 1.1944
Checking accuracy on validation set
Got 651 / 1000 correct (65.10)

Iteration 600, loss = 0.8212
Checking accuracy on validation set
Got 654 / 1000 correct (65.40)

Iteration 700, loss = 0.8129
Checking accuracy on validation set
Got 697 / 1000 correct (69.70)

Iteration 0, loss = 0.8998
Checking accuracy on validation set
Got 683 / 1000 correct (68.30)

Iteration 100, loss = 0.5712
```

Checking accuracy on validation set  
Got 688 / 1000 correct (68.80)

Iteration 200, loss = 0.6639  
Checking accuracy on validation set  
Got 708 / 1000 correct (70.80)

Iteration 300, loss = 0.8540  
Checking accuracy on validation set  
Got 718 / 1000 correct (71.80)

Iteration 400, loss = 0.7994  
Checking accuracy on validation set  
Got 710 / 1000 correct (71.00)

Iteration 500, loss = 0.8769  
Checking accuracy on validation set  
Got 723 / 1000 correct (72.30)

Iteration 600, loss = 0.7592  
Checking accuracy on validation set  
Got 727 / 1000 correct (72.70)

Iteration 700, loss = 1.0531  
Checking accuracy on validation set  
Got 706 / 1000 correct (70.60)

Iteration 0, loss = 0.6203  
Checking accuracy on validation set  
Got 728 / 1000 correct (72.80)

Iteration 100, loss = 0.7227  
Checking accuracy on validation set  
Got 718 / 1000 correct (71.80)

Iteration 200, loss = 0.7008  
Checking accuracy on validation set  
Got 739 / 1000 correct (73.90)

Iteration 300, loss = 0.6505  
Checking accuracy on validation set  
Got 733 / 1000 correct (73.30)

Iteration 400, loss = 0.6771  
Checking accuracy on validation set  
Got 732 / 1000 correct (73.20)

Iteration 500, loss = 0.8567  
Checking accuracy on validation set  
Got 733 / 1000 correct (73.30)

Iteration 600, loss = 0.6549  
Checking accuracy on validation set  
Got 741 / 1000 correct (74.10)

Iteration 700, loss = 0.5803  
Checking accuracy on validation set

```
Got 755 / 1000 correct (75.50)

Iteration 0, loss = 0.5068
Checking accuracy on validation set
Got 737 / 1000 correct (73.70)

Iteration 100, loss = 0.6055
Checking accuracy on validation set
Got 730 / 1000 correct (73.00)

Iteration 200, loss = 0.6572
Checking accuracy on validation set
Got 744 / 1000 correct (74.40)

Iteration 300, loss = 0.6555
Checking accuracy on validation set
Got 767 / 1000 correct (76.70)

Iteration 400, loss = 0.5379
Checking accuracy on validation set
Got 774 / 1000 correct (77.40)

Iteration 500, loss = 0.5272
Checking accuracy on validation set
Got 766 / 1000 correct (76.60)

Iteration 600, loss = 0.6865
Checking accuracy on validation set
Got 772 / 1000 correct (77.20)

Iteration 700, loss = 0.6040
Checking accuracy on validation set
Got 769 / 1000 correct (76.90)

Iteration 0, loss = 0.3881
Checking accuracy on validation set
Got 776 / 1000 correct (77.60)

Iteration 100, loss = 0.3172
Checking accuracy on validation set
Got 772 / 1000 correct (77.20)

Iteration 200, loss = 0.5385
Checking accuracy on validation set
Got 769 / 1000 correct (76.90)

Iteration 300, loss = 0.4428
Checking accuracy on validation set
Got 774 / 1000 correct (77.40)

Iteration 400, loss = 0.5054
Checking accuracy on validation set
Got 748 / 1000 correct (74.80)

Iteration 500, loss = 0.3880
Checking accuracy on validation set
Got 772 / 1000 correct (77.20)
```



Iteration 600, loss = 0.3945  
Checking accuracy on validation set  
Got 771 / 1000 correct (77.10)

Iteration 700, loss = 0.6015  
Checking accuracy on validation set  
Got 774 / 1000 correct (77.40)

Iteration 0, loss = 0.4369  
Checking accuracy on validation set  
Got 770 / 1000 correct (77.00)

Iteration 100, loss = 0.2985  
Checking accuracy on validation set  
Got 771 / 1000 correct (77.10)

Iteration 200, loss = 0.7158  
Checking accuracy on validation set  
Got 761 / 1000 correct (76.10)

Iteration 300, loss = 0.4502  
Checking accuracy on validation set  
Got 777 / 1000 correct (77.70)

Iteration 400, loss = 0.3488  
Checking accuracy on validation set  
Got 762 / 1000 correct (76.20)

Iteration 500, loss = 0.3505  
Checking accuracy on validation set  
Got 779 / 1000 correct (77.90)

Iteration 600, loss = 0.5062  
Checking accuracy on validation set  
Got 784 / 1000 correct (78.40)

Iteration 700, loss = 0.4028  
Checking accuracy on validation set  
Got 795 / 1000 correct (79.50)

Iteration 0, loss = 0.4364  
Checking accuracy on validation set  
Got 775 / 1000 correct (77.50)

Iteration 100, loss = 0.2360  
Checking accuracy on validation set  
Got 774 / 1000 correct (77.40)

Iteration 200, loss = 0.3642  
Checking accuracy on validation set  
Got 774 / 1000 correct (77.40)

Iteration 300, loss = 0.5848  
Checking accuracy on validation set  
Got 764 / 1000 correct (76.40)

```
Iteration 400, loss = 0.3765
Checking accuracy on validation set
Got 775 / 1000 correct (77.50)

Iteration 500, loss = 0.4578
Checking accuracy on validation set
Got 783 / 1000 correct (78.30)

Iteration 600, loss = 0.5754
Checking accuracy on validation set
Got 789 / 1000 correct (78.90)

Iteration 700, loss = 0.4053
Checking accuracy on validation set
Got 768 / 1000 correct (76.80)

Iteration 0, loss = 0.4127
Checking accuracy on validation set
Got 779 / 1000 correct (77.90)

Iteration 100, loss = 0.1507
Checking accuracy on validation set
Got 768 / 1000 correct (76.80)

Iteration 200, loss = 0.3494
Checking accuracy on validation set
Got 773 / 1000 correct (77.30)

Iteration 300, loss = 0.2991
Checking accuracy on validation set
Got 772 / 1000 correct (77.20)

Iteration 400, loss = 0.4558
Checking accuracy on validation set
Got 760 / 1000 correct (76.00)

Iteration 500, loss = 0.3771
Checking accuracy on validation set
Got 788 / 1000 correct (78.80)

Iteration 600, loss = 0.6274
Checking accuracy on validation set
Got 777 / 1000 correct (77.70)

Iteration 700, loss = 0.3949
Checking accuracy on validation set
Got 782 / 1000 correct (78.20)

Iteration 0, loss = 0.2978
Checking accuracy on validation set
Got 782 / 1000 correct (78.20)

Iteration 100, loss = 0.2790
Checking accuracy on validation set
Got 776 / 1000 correct (77.60)

Iteration 200, loss = 0.2982
```

```
Checking accuracy on validation set  
Got 765 / 1000 correct (76.50)
```

```
Iteration 300, loss = 0.1901  
Checking accuracy on validation set  
Got 766 / 1000 correct (76.60)
```

```
Iteration 400, loss = 0.5353  
Checking accuracy on validation set  
Got 778 / 1000 correct (77.80)
```

```
Iteration 500, loss = 0.3622  
Checking accuracy on validation set  
Got 780 / 1000 correct (78.00)
```

```
Iteration 600, loss = 0.2383  
Checking accuracy on validation set  
Got 766 / 1000 correct (76.60)
```

```
Iteration 700, loss = 0.4090  
Checking accuracy on validation set  
Got 768 / 1000 correct (76.80)
```

## Describe what you did

In the cell below you should write an explanation of what you did, any additional features that you implemented, and/or any graphs that you made in the process of training and evaluating your network.

I used some techniques that have been used in AlexNet - start with a small number of large sized filters and then build a deeper network with a large number of small sized filters. I used a ReLu as the activation function and applied a Spatial Group Normalization and MaxPooling after each change in filter size. I ended the network with a fully connected layer to output scores for the 10 classes.

Optimizer - Adam

## Test set -- run this only once

Now that we've gotten a result we're happy with, we test our final model on the test set (which you should store in `best_model`). Think about how this compares to your validation set accuracy.

```
In [ ]: best_model = model  
        check_accuracy_part34(loader_test, best_model)
```

```
Checking accuracy on test set  
Got 7644 / 10000 correct (76.44)
```