

RC5 ECE3110J Analog Circuits

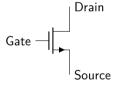
Kezhi Li 2024 Summer



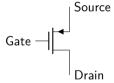
MOSFET Basics



NMOS



PMOS



I-V Characteristics (NMOS)



When $V_{DS} < V_{GS} - V_{TH}$, the NMOS is in triode region.

$$I_{D} = \mu_{n} C_{ox} \frac{W}{L_{eff}} \left[(V_{GS} - V_{TH}) V_{DS} - \frac{1}{2} V_{DS}^{2} \right] \tag{1}$$

When $V_{DS} \ge V_{GS} - V_{TH}$, the NMOS is in saturation region.

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L'} \left(V_{GS} - V_{TH} \right)^2 \tag{2}$$

I-V Characteristics (PMOS)



When $V_{SD} < V_{SC} - |V_{TH}|$, the PMOS is in triode region.

$$I_{D} = \mu_{p} C_{ox} \frac{W}{L_{eff}} \left[(V_{SG} - |V_{TH}|) V_{SD} - \frac{1}{2} V_{SD}^{2} \right]$$
 (3)

When $V_{SD} \ge V_{SG} - |V_{TH}|$, the NMOS is in saturation region.

$$I_{D} = \frac{1}{2} \mu_{p} C_{ox} \frac{W}{L'} \left(V_{SG} - |V_{TH}| \right)^{2} \tag{4}$$

MOSFET Basics

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Second Effects



Channel-Length Modulation

$$L' = L_{\text{eff}} - \Delta L \tag{5}$$

$$\begin{split} I_{D} &= \frac{1}{2} \mu_{n} C_{ox} \frac{W}{L_{\text{eff}}} \left(V_{GS} - V_{TH} \right)^{2} \left(1 + \frac{\Delta L}{L_{\text{eff}}} \right) \\ &= \frac{1}{2} \mu_{n} C_{ox} \frac{W}{L_{\text{eff}}} \left(V_{GS} - V_{TH} \right)^{2} \left(1 + \lambda V_{DS} \right) \end{split} \tag{6}$$

Body Effect

$$V_{TH} = V_{TH0} + \gamma(\sqrt{|2\Phi_F + V_{SB}|} - \sqrt{|2\Phi_F|})$$
 (7)

$$g_{mb} = g_m \cdot \eta, \eta = \frac{\gamma}{2\sqrt{2\Phi_F + V_{SB}}} \tag{8}$$

Transconductance



$$g_{m} = \frac{\partial I_{D}}{\partial V_{GS}} = \mu_{n} C_{ox} \frac{W}{L'} (V_{GS} - V_{TH}) = \sqrt{2\mu_{n} C_{ox} \frac{W}{L'} I_{D}} = \frac{2I_{D}}{V_{GS} - V_{TH}}$$
(9)

With channel-length modulation:

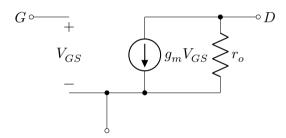
$$g_{m} = \mu_{n} C_{ox} \frac{W}{L} (V_{GS} - V_{TH}) (1 + \lambda V_{DS})$$

$$= \sqrt{2\mu_{n} C_{ox} (W/L) I_{D} (1 + \lambda V_{DS})}$$
(10)

Small-Signal Model for NMOS



$$\lambda \neq 0, \ \gamma = 0$$



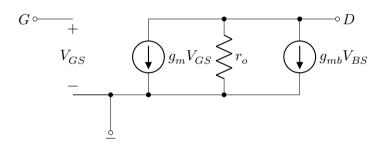
Where,

$$r_o = \frac{1}{\partial I_D/\partial V_{DS}} = \frac{1}{\frac{1}{2}\mu_n C_{ox} \frac{W}{L} \left(V_{GS} - V_{TH}\right)^2 \cdot \lambda}$$

Small-Signal Model for NMOS



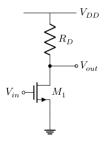
$$\lambda \neq 0, \ \gamma \neq 0$$



$$V_{BS}$$
 V_{B} \longrightarrow

Common-Source with Resistive Load

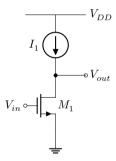




- Draw the curves of V_{out} vs V_{in} and write the corresponding relationship.
- Calculate the voltage gain $A_v = \frac{\partial V_{out}}{\partial V_{in}}.$
- What if $\lambda \neq 0$, $\gamma \neq 0$?

Common-Source with Resistive Load

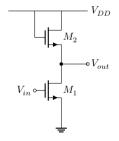




• Calculate the voltage gain $A_v = \frac{\partial V_{out}}{\partial V_{in}}$ if $\lambda \neq 0, \ \gamma \neq 0$.

Common-Source with Diode-Connected Load





- Draw the curves of V_{out} vs V_{in} and write the corresponding relationship.
- How to compare it to resistive load?
- Calculate the voltage gain $A_v = \frac{\partial V_{out}}{\partial V_{in}}.$
- What if $\lambda \neq 0$, $\gamma \neq 0$?

Something to Talk about Midterm

