## Assignment-6.R

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2020-10-20

#### GitHub Links:

.R File: https://github.com/kunwangRU/Survival-Analysis-of-Patients-with-Heart-Failure/blob/master/Factor%20Analysis%20(Assignment%206).R

```
#Loading Packages
library(mvtnorm)
## Warning: package 'mvtnorm' was built under R version 3.6.3
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
       filter, lag
##
## The following objects are masked from 'package:base':
##
       intersect, setdiff, setequal, union
##
library(psych)
## Warning: package 'psych' was built under R version 3.6.3
#Loading dataset
dataset <-read.csv("C:/Users/wangk/Desktop/Rutgers/Rutgers Courseware/Fall 20</pre>
20/Multivariate Analysis/heart_failure_clinical_records_dataset.csv")
View(dataset)
attach(dataset)
#Identifying different columns names
names(dataset)
## [1] "age"
                                    "anaemia"
## [3] "creatinine_phosphokinase" "diabetes"
## [5] "ejection_fraction"
                                    "high_blood_pressure"
## [7] "platelets"
                                    "serum creatinine"
## [9] "serum_sodium"
                                    "sex"
## [11] "smoking"
                                    "time"
## [13] "DEATH_EVENT"
```

```
#Data Summary
str(dataset)
## 'data.frame':
                   299 obs. of 13 variables:
##
  $ age
                             : num 75 55 65 50 65 90 75 60 65 80 ...
## $ anaemia
                             : int 0001111101...
## $ creatinine_phosphokinase: int 582 7861 146 111 160 47 246 315 157 123
## $ diabetes
                             : int
                                    0000100100...
## $ ejection_fraction
                             : int 20 38 20 20 20 40 15 60 65 35 ...
## $ high blood pressure
                             : int 1000010001...
## $ platelets
                             : num
                                    265000 263358 162000 210000 327000 ...
                                   1.9 1.1 1.3 1.9 2.7 2.1 1.2 1.1 1.5 9.4
## $ serum_creatinine
                             : num
                             : int 130 136 129 137 116 132 137 131 138 133
## $ serum_sodium
. . .
                             : Factor w/ 2 levels "Female", "male": 2 2 2 2 1
## $ sex
2 2 2 1 2 ...
## $ smoking
                             : int 0010010101...
## $ time
                             : int 4 6 7 7 8 8 10 10 10 10 ...
## $ DEATH EVENT
                             : Factor w/ 2 levels "Death", "No Death": 2 2 2
2 2 2 2 2 2 2 ...
summary(dataset)
##
                      anaemia
                                    creatinine phosphokinase
        age
## Min.
                          :0.0000
                                    Min.
                                          : 23.0
          :40.00
                   Min.
                                    1st Qu.: 116.5
##
   1st Qu.:51.00
                   1st Qu.:0.0000
## Median :60.00
                   Median :0.0000
                                    Median : 250.0
                                           : 581.8
##
   Mean
          :60.83
                   Mean
                          :0.4314
                                    Mean
##
                                    3rd Qu.: 582.0
   3rd Qu.:70.00
                   3rd Qu.:1.0000
##
           :95.00
                          :1.0000
                                           :7861.0
   Max.
                   Max.
                                    Max.
##
                    ejection fraction high blood pressure
                                                            platelets
      diabetes
## Min.
          :0.0000
                    Min.
                           :14.00
                                      Min. :0.0000
                                                         Min.
                                                                : 25100
##
   1st Qu.:0.0000
                    1st Qu.:30.00
                                      1st Qu.:0.0000
                                                          1st Qu.:212500
## Median :0.0000
                    Median :38.00
                                      Median :0.0000
                                                          Median :262000
## Mean
                                                                 :263358
          :0.4181
                    Mean
                           :38.08
                                      Mean
                                             :0.3512
                                                          Mean
   3rd Qu.:1.0000
                    3rd Qu.:45.00
                                      3rd Qu.:1.0000
                                                          3rd Qu.:303500
##
   Max.
          :1.0000
                    Max.
                           :80.00
                                      Max. :1.0000
                                                         Max.
                                                                 :850000
##
   serum_creatinine serum_sodium
                                        sex
                                                    smoking
##
   Min.
          :0.500
                    Min.
                           :113.0
                                    Female:105
                                                        :0.0000
                                                 Min.
   1st Qu.:0.900
                    1st Qu.:134.0
                                                 1st Qu.:0.0000
##
                                    male :194
## Median :1.100
                    Median :137.0
                                                 Median :0.0000
##
   Mean
          :1.394
                           :136.6
                    Mean
                                                 Mean
                                                        :0.3211
##
   3rd Qu.:1.400
                    3rd Qu.:140.0
                                                 3rd Qu.:1.0000
##
          :9.400
   Max.
                    Max.
                           :148.0
                                                 Max.
                                                        :1.0000
##
        time
                     DEATH EVENT
## Min. : 4.0
                   Death
                           :203
   1st Qu.: 73.0
                   No Death: 96
## Median :115.0
```

```
## Mean :130.3
## 3rd Qu.:203.0
## Max.
           :285.0
head(dataset)
     age anaemia creatinine_phosphokinase diabetes ejection_fraction
## 1 75
                                      582
## 2 55
               0
                                     7861
                                                                   38
                                                 0
## 3 65
               0
                                      146
                                                 0
                                                                   20
## 4 50
               1
                                      111
                                                 0
                                                                   20
## 5 65
               1
                                      160
                                                 1
                                                                   20
## 6 90
               1
                                       47
                                                 0
                                                                   40
     high_blood_pressure platelets serum_creatinine serum_sodium
                                                                     sex
## 1
                       1
                            265000
                                                1.9
                                                              130
                                                                    male
## 2
                       0
                            263358
                                                1.1
                                                              136
                                                                    male
## 3
                       0
                            162000
                                                1.3
                                                              129
                                                                    male
                       0
## 4
                            210000
                                                1.9
                                                              137
                                                                    male
## 5
                       0
                            327000
                                                2.7
                                                              116 Female
## 6
                       1
                            204000
                                                2.1
                                                              132
                                                                    male
     smoking time DEATH_EVENT
##
## 1
           0
                4
                     No Death
## 2
           0
                6
                     No Death
                7
## 3
           1
                     No Death
                7
## 4
           0
                     No Death
## 5
           0
                8
                     No Death
## 6
           1
                8
                     No Death
dim(dataset)
## [1] 299 13
#Checking for missing values
is.null(dataset)
## [1] FALSE
##The "FALSE" output shows there is no missing data in the dataset.
#Correlation
correlation < -cor(dataset[c(1,3,5,7,8,9,12)])
View(correlation)
#From the table, we can see all the continuous variables are uncorrelated
#Principal components
dataset_pca <- prcomp(dataset[c(1,3,5,7,8,9,12)],scale=TRUE)</pre>
dataset_pca
## Standard deviations (1, .., p=7):
## [1] 1.2143198 1.0842469 1.0146325 0.9829678 0.9421964 0.8587448 0.8537882
```

```
##
## Rotation (n \times k) = (7 \times 7):
                                               PC2
                                                            PC3
                                                                        PC4
##
                                   PC1
## age
                             0.4649617 -0.45213222
                                                     0.00779977
                                                                 0.19809211
## creatinine_phosphokinase -0.1379593   0.19389349 -0.81505355   0.33440577
## ejection fraction
                            -0.1788924 -0.68147830 0.10671326 0.01299509
## platelets
                            -0.1992576 -0.24678636 -0.40331735 -0.82095373
## serum creatinine
                             0.5117770 -0.04569638 -0.10167226 -0.18226520
                            -0.4474108 -0.42971962 -0.11797610 0.36260682
## serum sodium
## time
                            ##
                                   PC5
                                               PC6
                                                            PC7
                             0.1912135 -0.6341378 0.318421659
## age
## creatinine phosphokinase -0.2948224 -0.1008787 0.264832516
## ejection_fraction
                            -0.4694857 0.3913478 0.344177806
## platelets
                             0.1807563 -0.1733047 0.007459381
## serum creatinine
                            -0.6335802 -0.1069130 -0.528757042
## serum sodium
                             0.1513990 -0.1865190 -0.641912443
                            -0.4461860 -0.5985695 0.135357997
## time
#Recreating the summary table manually
(eigen dataset <- dataset pca$sdev^2)</pre>
## [1] 1.4745726 1.1755914 1.0294792 0.9662257 0.8877341 0.7374427 0.7289544
names(eigen_dataset) <- paste("PC",1:7,sep="")</pre>
eigen dataset
##
                   PC2
                             PC3
                                       PC4
                                                  PC5
                                                            PC6
                                                                      PC7
## 1.4745726 1.1755914 1.0294792 0.9662257 0.8877341 0.7374427 0.7289544
sumlambdas <- sum(eigen_dataset)</pre>
sumlambdas
## [1] 7
propvar <- eigen_dataset/sumlambdas</pre>
propvar
##
                   PC2
                             PC3
                                       PC4
                                                  PC5
                                                            PC6
                                                                      PC7
         PC1
## 0.2106532 0.1679416 0.1470685 0.1380322 0.1268192 0.1053490 0.1041363
cumvar_dataset <- cumsum(propvar)</pre>
cumvar_dataset
                             PC3
                                       PC4
                                                  PC5
                                                                      PC7
##
         PC1
                   PC2
                                                            PC6
## 0.2106532 0.3785949 0.5256633 0.6636956 0.7905147 0.8958637 1.0000000
matlambdas <- rbind(eigen_dataset,propvar,cumvar_dataset)</pre>
rownames(matlambdas) <- c("Eigenvalues", "Prop. variance", "Cum. prop. variance</pre>
")
round(matlambdas,6)
```

```
PC3
##
                                    PC2
                                                      PC4
                                                              PC5
                                                                       PC6
## Eigenvalues
                      1.474573 1.175591 1.029479 0.966226 0.887734 0.737443
                      0.210653 0.167942 0.147068 0.138032 0.126819 0.105349
## Prop. variance
## Cum. prop. variance 0.210653 0.378595 0.525663 0.663696 0.790515 0.895864
##
                           PC7
## Eigenvalues
                      0.728954
## Prop. variance
                      0.104136
## Cum. prop. variance 1.000000
#Based on Option 2 rule, which says components whose Eigenvalues are larger t
han 1 should be considered, so we need to keep PC1 through PC3
summary(dataset pca)
## Importance of components:
                                   PC2
                                          PC3
                                                 PC4
                                                        PC5
##
                            PC1
                                                               PC6
                                                                      PC7
                         1.2143 1.0842 1.0146 0.9830 0.9422 0.8587 0.8538
## Standard deviation
## Proportion of Variance 0.2107 0.1679 0.1471 0.1380 0.1268 0.1053 0.1041
## Cumulative Proportion 0.2107 0.3786 0.5257 0.6637 0.7905 0.8959 1.0000
eigvec.heart<-dataset_pca$rotation</pre>
print(eigvec.heart)
##
                                  PC1
                                              PC2
                                                          PC3
                                                                      PC4
## age
                            0.4649617 -0.45213222 0.00779977
                                                               0.19809211
## creatinine_phosphokinase -0.1379593 0.19389349 -0.81505355
                                                              0.33440577
## ejection fraction
                           -0.1788924 -0.68147830 0.10671326 0.01299509
## platelets
                           -0.1992576 -0.24678636 -0.40331735 -0.82095373
## serum_creatinine
                            0.5117770 -0.04569638 -0.10167226 -0.18226520
## serum sodium
                           -0.4474108 -0.42971962 -0.11797610 0.36260682
## time
                           ##
                                  PC5
                                             PC6
                                                          PC7
                            0.1912135 -0.6341378 0.318421659
## age
## creatinine phosphokinase -0.2948224 -0.1008787 0.264832516
## ejection_fraction
                           -0.4694857 0.3913478 0.344177806
## platelets
                            0.1807563 -0.1733047 0.007459381
## serum creatinine
                           -0.6335802 -0.1069130 -0.528757042
## serum_sodium
                            0.1513990 -0.1865190 -0.641912443
## time
                           -0.4461860 -0.5985695 0.135357997
# Taking the first three PCs to generate linear combinations for all the vari
ables with three factors
pcafactors.heart <- eigvec.heart[,1:3]</pre>
pcafactors.heart
##
                                  PC1
                                              PC2
                                                          PC3
                            0.4649617 -0.45213222 0.00779977
## age
## creatinine phosphokinase -0.1379593 0.19389349 -0.81505355
## ejection fraction
                           -0.1788924 -0.68147830
                                                   0.10671326
## platelets
                           -0.1992576 -0.24678636 -0.40331735
                           0.5117770 -0.04569638 -0.10167226
## serum creatinine
```

```
## serum sodium
                            -0.4474108 -0.42971962 -0.11797610
## time
                            -0.4806034 0.21428597 0.37056533
# Multiplying each column of the eigenvector's matrix by the square-root of t
he corresponding eigenvalue in order to get the factor loadings
unrot.fact.heart <- sweep(pcafactors.heart,MARGIN=2,dataset pca$sdev[1:3],`*`
)
unrot.fact.heart
##
                                   PC1
                                                PC2
                                                             PC3
## age
                             0.5646122 -0.49022298 0.007913901
## creatinine_phosphokinase -0.1675268  0.21022842 -0.826979846
## ejection fraction
                            -0.2172326 -0.73889076 0.108274741
## platelets
                            -0.2419625 -0.26757736 -0.409218900
## serum_creatinine
                             0.6214609 -0.04954616 -0.103159985
## serum sodium
                            -0.5432998 -0.46592218 -0.119702387
## time
                            -0.5836063 0.23233891 0.375987635
# Computing communalities
communalities.heart <- rowSums(unrot.fact.heart^2)</pre>
communalities.heart
##
                        age creatinine_phosphokinase
                                                             ejection_fraction
                  0.5591682
##
                                            0.7561569
                                                                     0.6048730
##
                  platelets
                                    serum_creatinine
                                                                  serum sodium
##
                  0.2976036
                                            0.3993105
                                                                     0.5265868
##
                       time
##
                  0.5359443
# Performing the varimax rotation. The default in the varimax function is nor
m=TRUE thus, Kaiser normalization is carried out
rot.fact.heart <- varimax(unrot.fact.heart)</pre>
View(unrot.fact.heart)
rot.fact.heart
## $loadings
##
## Loadings:
##
                            PC1
                                   PC2
                                          PC3
## age
                             0.696 -0.185 0.200
## creatinine phosphokinase
                                           -0.864
## ejection fraction
                                    -0.755 0.157
## platelets
                                    -0.357 -0.412
## serum_creatinine
                             0.586 0.232
## serum sodium
                            -0.240 -0.663 -0.173
## time
                            -0.702
                                            0.201
##
```

```
##
                           PC2
                    PC1
                                 PC3
## SS loadings
                  1.390 1.235 1.054
## Proportion Var 0.199 0.176 0.151
## Cumulative Var 0.199 0.375 0.526
##
## $rotmat
##
              [,1]
                         [,2]
                                    [,3]
## [1,] 0.8660041 0.4477622 0.2225891
## [2,] -0.4270706 0.8938525 -0.1365226
## [3,] -0.2600915 0.0231679 0.9653060
# The print method of varimax omits loadings less than abs(0.1). In order to
display all the loadings, it is necessary to ask explicitly the contents of t
he object $loadings
fact.load.heart <- rot.fact.heart$loadings[1:7,1:3]</pre>
fact.load.heart
##
                                     PC1
                                                 PC2
                                                              PC3
                              0.69625801 -0.18519166
## age
                                                       0.20024241
## creatinine_phosphokinase -0.01977081 0.09374166 -0.86427917
## ejection fraction
                              0.09927290 -0.75521937
                                                       0.15703997
## platelets
                              0.01116830 -0.35699707 -0.41234930
## serum_creatinine
                              0.58617844 0.23158975 0.04551365
## serum sodium
                             -0.24038458 -0.66250806 -0.17287312
## time
                             -0.70242172 -0.04492927 0.20131920
# Computing the rotated factor scores for the 299 Patients
scale.heart <- scale(dataset[c(1,3,5,7,8,9,12)])</pre>
scale.heart
##
                  age creatinine phosphokinase ejection fraction
##
           1.19094867
                                                      -1.527997920
     [1,]
                                    0.000165451
##
     [2,] -0.49045705
                                    7.502062717
                                                      -0.007064906
##
     [3,]
                                                      -1.527997920
          0.35024581
                                   -0.449185725
##
     [4,] -0.91080848
                                   -0.485257493
                                                      -1.527997920
##
                                   -0.434757017
                                                      -1.527997920
     [5,]
          0.35024581
##
     [6,]
          2.45200296
                                   -0.551217299
                                                       0.161927651
##
     [7,]
           1.19094867
                                   -0.346123528
                                                      -1.950479313
##
     [8,] -0.07010562
                                   -0.275010613
                                                       1.851853222
##
     [9,]
          0.35024581
                                   -0.437848883
                                                       2.274334615
##
                                   -0.472890030
                                                      -0.260553742
    [10,]
           1.61130010
##
    [11,]
           1.19094867
                                   -0.516176152
                                                      -0.007064906
##
    [12,]
          0.09803495
                                   -0.361582858
                                                      -1.105516528
##
    [13,] -1.33115991
                                    0.411383614
                                                      -0.683035135
##
    [14,] -0.91080848
                                   -0.426512042
                                                      -0.007064906
##
    [15,] -0.99487877
                                   -0.517206774
                                                      -0.683035135
##
    [16,]
           1.77944067
                                   -0.209050807
                                                       1.006890437
    [17,]
          2.19979210
                                   -0.446093859
                                                      -0.007064906
##
    [18,] -1.33115991
                                    0.000165451
                                                      -2.034975592
    [19,]
##
                                   -0.470828786
          0.77059724
                                                      -1.105516528
  [20,] -1.07894905
                                    0.000165451
                                                       1.429371829
```

##		0.35024581	-0.546064189	-1.105516528	
##		0.35024581	-0.467736920		
##		0.60245667	-0.372919699		
##		-0.65859762	-0.534727348		
##	[25,]	1.19094867	0.000165451	-0.683035135	
##	[26,]	1.61130010	-0.447124481	-0.007064906	
##	[27,]	2.87235439	-0.484226871	0.161927651	
##	[28,]	0.77059724	-0.473920652	0.584409044	
##	[29,]	-0.23824619	-0.537819214	-0.007064906	
##	[30,]	1.77944067	-0.527512994	-0.683035135	
##	[31,]	2.78828410	0.000165451	-0.007064906	
##	[32,]	2.03165153	-0.575952226	0.584409044	
		-0.91080848	-0.343031663	-0.260553742	
		-0.91080848	-0.435787639	-0.683035135	
##		0.35024581	-0.502778067		
		0.68652695	0.000165451		
##		2.45200296		1.006890437	
		1.77944067	0.281525247		
##		-0.07010562	2.137675402	-0.683035135	
		-0.07010562	-0.357460370		
		0.77059724	0.000165451	-1.527997920	
		-0.91080848	-0.471859408		
		0.77059724		0.584409044	
		0.93873781	-0.468767542		
		-0.07010562	0.006349183		
		-0.91080848	0.000165451		
		-0.82673819	0.822601777		
##		-0.07010562	0.000165451	-0.007064906	
##		1.61130010	-0.029722586		
##		-0.32231648	-0.466706298		
		0.60245667	-0.004987659		
		-0.65859762	-0.505869933		
		-0.07010562	3.485728929	2.020845779	
##		0.77059724	-0.528543616	1.006890437	
##		-0.07010562	-0.331694821	-0.007064906	
##	[56,]		-0.217295783	-0.683035135	
##		0.77059724	-0.522359884	-0.260553742	
##		-0.07010562	0.025931000	0.161927651	
##		-0.99487877	0.213504197	-1.527997920	
##		0.93873781	-0.224510137	-1.527997920	
##		-1.33115991	7.338193825	-1.105516528	
##		-0.91080848	-0.271918747	0.161927651	
##		-0.49045705	-0.487318737	-0.260553742	
##		-1.33115991	0.000165451	-0.260553742	
##		-1.33115991	0.000165451	3.541778793	
##		-0.07010562	-0.529574238	-1.527997920	
##		-1.58337077	-0.342001041	-1.950479313	
##	[68,]		-0.486288115	-1.105516528	
##	[69,]		-0.433726395	-1.105516528	
##	[70,]		-0.483196249	-1.105516528	
ππ	[,0,]	0.33024301	-0.403130243	-1.103310320	

##		-1.66744105	-0.447124481	0.161927651	
##		-0.23824619	0.000165451		
##		2.03165153	5.462461853		
##		0.35024581	-0.368797212		
##	[75,]	0.68652695	0.000165451	-1.527997920	
##	[76,]	-0.07010562	-0.551217299	-1.527997920	
##	[77,]	0.77059724	-0.504839311	1.851853222	
##	[78,]	-1.58337077	-0.494533091	0.161927651	
##	[79,]	1.19094867	-0.390440273	-0.007064906	
##	[80,]	-0.49045705	-0.253367552	0.584409044	
##	[81,]	0.77059724	-0.528543616	0.161927651	
##	[82,]	0.51838638	0.000165451	1.006890437	
##	[83,]	-0.07010562	-0.521329262	-1.105516528	
##	[84,]	1.52722981	-0.542972323	1.006890437	
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                                                          0.846998664
##
   [219,]
           7.813538e-02
                             -0.284076114
                                            -0.59499866
                                                          0.859882903
## [220,]
          1.100586e+00
                             -0.670732575
                                             0.76478171
                                                         0.859882903
```

```
## [221,]
           7.523048e-09
                              0.421571927
                                            -0.59499866
                                                          0.872767142
## [222,]
          -7.091516e-01
                             -0.284076114
                                             1.89793202
                                                          0.898535620
  [223,]
           1.039239e+00
                             -0.284076114
                                             0.53815165
                                                          0.911419859
##
                                                          0.911419859
   [224,] -1.363520e+00
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                             -0.574068459
                             -0.380740229
   [225,]
           2.460445e+00
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                                                          0.962956814
   [226,]
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                              0.005916232
                                            -2.63466921
                                                          0.962956814
##
   [227,] -7.602741e-01
                             -0.090747883
                                            -1.04825878
                                                          0.962956814
                                             0.76478171
##
   [228,] -1.251050e+00
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   [229,] -2.694978e-01
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                                            -1.50151891
                                                          0.988725292
   [230,]
##
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                             -0.187411999
                                            -0.59499866
                                                          0.988725292
   [231,] -2.058786e+00
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                                            -2.18140909
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   [232,] -8.011721e-01
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                                            -0.59499866
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   [233,] -8.545672e-02
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                                             0.08489153
                                                          1.014493770
  [234,]
           6.813812e-01
                              0.005916232
                                             0.08489153
                                                          1.014493770
##
##
   [235,]
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                                             0.08489153
                                                          1.014493770
   [236,]
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                                             0.08489153
                                                          1.014493770
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   [238,] -9.238662e-01
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                                            -1.04825878
                                                          1.027378009
   [239,] -6.500771e-02
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                                                          1.027378009
##
                             -0.380740229
   [240,]
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                             -0.206744822
                                             0.08489153
                                                          1.040262248
  [241,]
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                                             0.53815165
                                                          1.053146487
   [242,] -1.468038e-01
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                                            -0.14173853
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##
  [243,] -8.545672e-02
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                                            -0.14173853
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   [244,] -4.433144e-01
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  [245,]
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                              0.392572693
                                            -0.59499866
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##
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                                             0.08489153
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   [247,]
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                                            -0.36836860
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   [249,]
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  [252,] -3.308449e-01
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                                             1.44467190
                                                          1.091799204
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                                                          1.285062788
##
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                                            -0.36836860
                                                          1.297947027
   [261,] -6.171310e-01
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                                            -0.82162872
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   [263,] -6.682536e-01
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                                            -1.72814897
                                                          1.349483982
   [264,] -5.660085e-01
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                                             0.76478171
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   [265,] -1.189703e+00
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                                                          1.375252460
                             -0.187411999
  [266,]
                                                          1.413905177
##
           1.008565e+00
                             -0.477404344
                                             0.76478171
   [267,]
           7.523048e-09
                                            -0.59499866
                                                          1.426789416
##
                              0.421571927
## [268,] -1.332846e+00
                              0.295908577
                                             0.76478171
                                                          1.465442133
##
   [269,]
           3.950951e-01
                             -0.477404344
                                             0.76478171
                                                          1.465442133
## [270,] -4.228654e-01
                             -0.380740229
                                            -1.04825878
                                                         1.465442133
```

```
## [271,] 7.523048e-09
                           0.199244462
                                          -1.50151891 1.465442133
## [272,] -4.330899e-01
                            -0.477404344
                                          -0.59499866 1.465442133
## [273,] -4.944370e-01
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                                          -0.82162872 1.478326372
## [274,] -7.602741e-01
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                                           0.76478171 1.478326372
## [275,] -1.159030e+00
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                                          0.08489153 1.478326372
## [276,] 1.622036e+00
                            -0.574068459
                                           0.08489153 1.478326372
## [277,]
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                                          1.21804184 1.478326372
## [278,] -2.436071e+00
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                                           0.76478171 1.491210611
## [279,] -3.206204e-01
                            -0.670732575
                                          -0.14173853 1.491210611
## [280,]
         1.918546e+00
                                          -0.14173853 1.491210611
                            -0.090747883
## [281,] -2.285998e-01
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                                           0.08489153 1.504094850
## [282,] -2.171256e+00
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                                          -0.14173853
                                                      1.542747566
## [283,] -4.944370e-01
                                          -1.95477903 1.542747566
                             2.325854996
## [284,] 7.523048e-09
                            -0.284076114
                                          0.31152159 1.542747566
## [285,]
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                            -0.574068459
                                                       1.542747566
## [286,] 7.427283e-01
                            -0.187411999
                                          -0.36836860 1.542747566
## [287,]
          1.599314e-01
                             0.295908577
                                           0.76478171
                                                       1.542747566
## [288,]
          2.859201e+00
                            -0.380740229
                                          -1.04825878
                                                      1.542747566
## [289,]
         7.523048e-09
                            -0.284076114
                                           1.21804184 1.620053000
## [290,]
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                            -0.477404344
                                           1.67130196 1.620053000
## [291,] -4.228654e-01
                                           0.99141178 1.632937239
                            -0.574068459
## [292,] -1.332846e+00
                             0.005916232
                                           0.53815165 1.645821478
## [293,] 1.213056e+00
                            -0.380740229
                                           0.76478171 1.645821478
## [294,] -8.625192e-01
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                                          -0.14173853
                                                       1.800432345
## [295,] -1.107907e+00
                            -0.284076114
                                          1.44467190
                                                      1.800432345
## [296,]
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                                           0.53815165
                                                       1.813316584
## [297,] 4.893878e+00
                            -0.574068459
                                           0.31152159
                                                      1.903506257
## [298,] -1.261275e+00
                            0.005916232
                                           0.76478171 1.929274734
## [299,] 1.345974e+00
                             0.199244462
                                        -0.14173853 1.993695929
## attr(,"scaled:center")
                        age creatinine_phosphokinase
                                                            ejection_fraction
##
##
                   60.83389
                                                                     38.08361
                                           581.83946
##
                  platelets
                                    serum creatinine
                                                                serum sodium
                                             1.39388
                                                                    136.62542
##
              263358.02926
##
                       time
                  130.26087
## attr(,"scaled:scale")
                        age creatinine phosphokinase
                                                            ejection fraction
##
##
                  11.894809
                                          970.287881
                                                                    11.834841
##
                                                                serum_sodium
                  platelets
                                    serum_creatinine
##
              97804.236869
                                            1.034510
                                                                     4.412477
```

```
##
                        time
##
                   77.614208
as.matrix(scale.heart)%*%fact.load.heart%*%solve(t(fact.load.heart)%*%fact.lo
ad.heart)
##
                                 PC2
                    PC1
                                                PC3
##
     [1,]
           1.661261807
                         1.554800886 -0.2391648108
##
     [2,]
           0.743266680
                         0.800052166 -6.6257827317
##
           0.927179080
     [3,]
                         2.016941671
                                      0.4549872007
##
     [4,]
           0.334885605
                         1.266839858 -0.1473115437
##
     [5,]
           1.925456863
                         3.274592726
                                      0.2063397138
##
     [6,]
           2.435918328
                         0.165636681
                                      0.8575735122
##
     [7,]
           1.012119703
                         1.263416904
                                      0.3244895181
##
     [8,]
           1.124477246 -1.115611048 -0.4460294461
##
     [9,]
           1.234722890
                       -1.691814397
                                       0.3538296415
##
           4.919709448
                         0.999011928 -0.1358685604
    [10,]
##
           2.640695114
                         0.439924198
                                      0.0044503303
    [11,]
##
           0.428072549
                         0.186827135 -0.2931060423
    [12,]
##
    [13,]
          -0.139463181
                         1.005910129 -0.5149623433
##
    [14,]
                         0.013367351 -0.2133024344
           0.205750073
##
    [15,]
           0.100190044 -0.129530927 -0.8853088186
##
           1.649820322 -0.324891744
                                      1.1159824597
    [16,]
##
    [17,]
           1.595345623 -0.956323503
                                      0.2371917548
##
    [18,]
          -0.156822106
                         2.866432703 -0.1779870700
    [19,]
                         0.103388790 -0.0231261139
##
           0.762120879
##
    [20,]
           0.907950332
                         1.748387342 0.9061044026
##
    [21,]
           0.762655848
                         0.465114447 -0.0799383657
##
    [22,]
           0.944646930
                         0.308381123 -0.1180144130
##
    [23,]
           0.733921935 -0.548331547 -0.1903647967
##
           0.457662548 -1.284173827 -0.0687137964
    [24,]
##
    [25,]
           1.492282733
                         0.549949036 -0.1711517403
##
    [26,]
           1.455420414 -0.835943301
                                       0.5028730340
##
           1.941662073 -0.755655310
    [27,]
                                       0.7523795208
##
    [28,]
                                      0.2150997676
           1.134926967 -0.573778900
##
    [29,]
           2.308580309
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                                      0.6226136569
##
           1.520043263
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##
    [31,]
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##
    [32,]
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##
    [33,]
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##
    [34,]
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##
           0.663877522 -0.991149461
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##
    [36,]
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##
    [37,]
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##
           1.353571970 -2.188128649 -0.6137036191
    [38,]
##
    [39,]
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                         0.588312865 -2.3617777846
##
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##
                        1.163688178 -0.3401328031
    [41,]
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##
    [42,] -0.020711589
                         0.926623118
                                      0.3053509355
    [43,]
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```

```
##
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##
    [45,]
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##
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##
    [47,]
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##
    [48,]
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##
    [49,]
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##
    [50,]
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##
    [51,]
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                        0.626436159 -0.0009576655
##
    [52,]
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           2.783428934 -1.275225506 -3.1242865473
##
    [53,]
##
    [54,]
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##
    [55,]
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##
           2.396441039 -0.122309343 -0.3800272497
    [56,]
##
    [57,]
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                        0.096229075 0.3931885056
           0.117242708 -0.230750573 -0.0975868884
##
    [58,]
##
    [59,] -0.230865053
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                        0.906990443 -7.2203194356
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    [62,]
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    [64,] -0.549357130 -0.979474617 -1.2025062067
##
##
          0.083935800 -2.028983076
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##
    [66,]
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##
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    [70,]
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##
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    [72,] -0.096008591
##
    [73,]
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##
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##
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    [76,] -0.216828225
##
    [77,]
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##
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##
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##
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##
    [81,]
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                                      0.3100879741
##
    [82,]
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                                      0.0545080160
##
    [83,]
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##
    [85,] -0.113963882
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    [86,] -0.258837308 -1.431743479 -0.3730824376
##
    [87,] -0.132936474
                        0.384334804
                                      0.5311877910
##
    [88,]
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                                      0.3481862241
##
    [89,] -0.728453310 -0.165887725
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##
    [90,] -0.325982563 0.033839181
                                      0.1137702233
##
    [91,]
          0.551045835 -0.542978350 0.5658370679
##
    [92,]
           0.342583850 -0.0533331595 -0.3617566227
  [93,] -0.363720014 -0.919551965 -0.1109323635
```

```
##
    [94,]
          0.281720144 1.053032127 0.2996120563
##
    [95,] -0.201173206 -0.914928165 -0.2348252272
##
    [96,]
          0.090540886 -1.601030602 0.5241222915
##
                      0.967996687 -0.1101564113
    [97,]
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           0.783213325 -1.310128264 0.7599096037
##
    [98,]
##
    [99,]
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                        0.429114466 -0.1875312235
## [100,]
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##
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## [102,]
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## [103,]
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## [104,] -0.696897702 0.825599986 -4.3693073628
## [105,]
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## [106,]
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          0.060003135 -0.312400494 -0.2643827297
## [107,]
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                        0.264159990 -0.4517056571
## [109,]
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## [110,] -0.263211207 -1.966140938 -2.6273981587
## [111,]
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                                    0.8286984171
## [112,] -0.079851430 0.476705134 0.3987411216
## [113,] -0.232857424
                        0.987410715 -0.1836507253
## [114,]
          0.861926056 -1.672184717
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## [115,]
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## [116,] -0.124361588 -0.121099491
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## [117,]
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                                     0.5654697557
## [118,]
          2.291232248 -2.230747174 -0.1209613524
## [119,]
          0.292592223 -1.569407098
                                     0.7579634732
## [120,]
           1.554116575 -0.051411596
                                     0.2919360483
## [121,]
           0.471353622 -0.769453621
                                     0.3000942339
## [122,]
                        0.179511841
                                     0.8150414891
          0.239404523
## [123,] -0.183468621 -0.418602246
                                     0.3254376420
## [124,] -0.379654647 -0.225010617
                                     0.0511604751
## [125,]
          1.168530259
                        0.687054723
                                     0.1837383744
## [126,] -0.439853331 -0.096473505
                                     0.1761735895
## [127,] -0.020406232
                       2.895762575
                                     0.1700108754
## [128,]
          0.029381207 -1.385234054
                                     0.3355970649
## [129,] -0.160749776
                        0.354127757
                                     0.1035501859
## [130,]
          0.339556664 -0.332058477 -0.0667005248
## [131,] -0.237984674 -1.134193809 -0.9177089771
          2.210066656 1.073871848 -0.1719603923
## [132,]
## [133,] -0.548148785 0.084896488 -0.3618093076
## [134,]
          0.200275116 -2.329893544 0.1807820612
## [135,]
           1.012954927 0.207848181 -3.1075914230
## [136,]
          0.684773385 -0.418180700 0.1193766853
## [137,]
          0.265991270 -1.127564425
                                     1.0622916315
## [138,]
                       1.337238996 -0.1567333112
          0.816047289
## [139,] -0.004758957
                        0.254210240 0.3494468499
## [140,] -0.659513150
                        0.603226065 -0.9684829433
## [141,]
         0.923062231 -0.032713985 0.0676803357
## [142,] -0.766013551 -0.333299547 -0.4898487459
## [143,] -0.431084079 0.882918765 -0.3375768085
```

```
## [144,] -0.190133535 -0.640424682 0.3848998983
## [145,]
           0.594737173
                        0.078962400 -0.7680732406
## [146,] -0.822369651 -0.053442218 -0.1115508170
## [147,] -0.632086337
                        0.639659696
                                      0.3084664918
## [148,]
           0.318971640 -1.156013079 -0.5291490901
## [149,]
                        0.671332644
                                      0.2568422316
           0.863876747
## [150,] -0.102833245
                        0.438284149 -1.3662033639
## [151,]
           1.097728686 -0.154049087
                                      0.6481837510
## [152,]
           0.058513888
                       -1.525735600
                                      0.7298158827
## [153,] -0.501623706
                        0.244712801
                                      0.7113591605
## [154,] -0.466410671
                        0.387641116 -1.2984836637
## [155,] -0.026249918
                        0.140029667
                                      0.3217130039
## [156,] -0.116271543
                        0.519456212
                                      0.2552566197
## [157,] -0.328502961
                        0.297409376
                                      0.2283230337
## [158,] -0.670127696
                        0.863873950 -0.0320977323
                                      0.3480628341
          1.236631450 -0.628600664
## [159,]
## [160,] -0.087149306
                       -0.989271375 -0.0447048996
## [161,]
          0.264931050
                        0.108130352
                                      0.6630592328
## [162,] -1.011591855
                        0.282794292
                                      0.3950346566
          0.064674548 -0.794095498 -0.7180245971
## [163,]
## [164,] -0.855164135
                        0.353179379 -1.1021613126
## [165,] -0.817630171
                        0.338158269 -2.2477161022
## [166,]
          0.790071410
                        0.085952387
                                      0.4093134146
## [167,] -0.364973805 -0.605203649
                                      0.8129999106
          0.051590540
                        1.959827996
                                      1.0494779489
## [168,]
## [169,] -0.058338220 -0.409337783
                                      0.0359104234
## [170,]
          0.159737156
                        0.254669123 -0.1473645979
## [171,] -0.489533321
                        0.419949638 -0.0988150804
## [172,] -0.595220420 -0.285623727 -3.2696000954
## [173,]
          0.085653123 -2.126932185
                                      0.8797935760
## [174,] -1.101774379
                        0.948102234
                                      0.2916000702
## [175,] -0.166037172 -0.108567577
                                      0.3032487590
## [176,] -0.097398428 -1.622331214
                                      0.4001096589
## [177,]
          0.077392575
                        0.439270324
                                      0.1476584803
## [178,] -0.847221750 -0.547109788
                                      0.9085380018
                                      0.4746835928
## [179,] -0.127606139 -2.264892371
## [180,] -0.690762926 -0.522014464 -0.3837300635
## [181,] -1.244346835
                        0.658517059 -0.3641916993
## [182,] -0.514946965
                        0.827817681
                                      0.3989361780
## [183,] -0.172665628
                        0.647201739
                                      0.1258618235
## [184,]
          0.858257113
                        0.307871855
                                      0.9277885573
## [185,] -0.642483481
                        0.760191790
                                      0.4506613356
## [186,] -0.241494042
                        0.111254457 -0.0564260901
## [187,] -0.937666219
                        0.077076546
                                      0.6672609206
## [188,] -0.255431065
                                    -1.8079088692
                       -0.236095185
## [189,] -0.460797704
                        0.065475798
                                      0.7839240452
## [190,] -1.408796077 -0.544433129
                                      0.0945931696
                        0.001930967
## [191,]
          0.896368333
                                      0.0750159818
## [192,]
           0.146044715 -1.181534430
                                      0.7722082772
## [193,] -0.858056614 0.737315437
                                      0.6394594140
```

```
## [194,] -0.197251951 -0.170279072
                                     0.7379426061
## [195,] -1.140428526
                        1.852050166
                                      0.3155272212
## [196,]
                                      0.4808327148
          0.325426969 -1.463111748
## [197,] -1.139571685
                                    -0.0453437056
                        0.202664970
## [198,] -0.563968269
                        0.088513773
                                     0.4422084068
## [199,] -1.086028156
                        1.352543347 -0.1819051765
## [200,]
          0.382812764
                        3.094221200
                                     0.3362310993
## [201,] -0.572810886
                        0.126824436
                                      0.0238687266
## [202,] -0.921088541 -1.225260712
                                      0.0570952712
## [203,] -0.049124158 -1.459231030
                                      1.1118129779
## [204,]
          0.257805972
                        1.189500127
                                      0.6668767422
## [205,]
          0.074748808 -0.617912310
                                      0.7867845639
## [206,] -0.872191759 -0.486364167
                                      0.1067486746
## [207,] -1.645178492 -0.281541525
                                      0.3536193491
## [208,]
          0.411305453 -0.203541128
                                     1.1172313308
## [209,] -0.601616408 -0.554671402 -1.4750001020
## [210,] -0.955119693
                       1.089864345 -0.1569386064
## [211,] -0.276077959
                        0.580271097 -0.1500176716
## [212,] -1.044240318 -1.218357423
                                     0.7190084888
## [213,]
          0.514319443 -1.745361381 -0.0449525080
## [214,] -0.813768250
                       1.478470608
                                     0.5964264070
## [215,] -0.444032668
                        0.204602604
                                     0.5628851690
## [216,]
          0.052099177
                        0.437476293
                                      0.6339590882
## [217,] -0.172145649 -1.585499295 -0.5722453206
          2.496763775 -0.200777416
                                     1.1196635080
## [218,]
## [219,] -0.197712351
                        0.335412570 -0.0672413174
## [220,] -1.028972799 -0.545444230 -0.4469534152
## [221,]
          0.133728397
                        1.129970941
                                     0.2085540954
## [222,] -0.578029718 -1.566105155
                                      0.8250059417
## [223,] -1.446534248 -0.178091687 -0.1196636579
## [224,] -1.435219779
                       1.547758563
                                     0.4838741521
## [225,] -0.798291149 -0.176369046 -0.9801923146
          0.633708473 -0.010070080
                                     0.9765007437
## [226,]
## [227,] -0.723949834
                        1.449128438
                                      0.9110323577
## [228,] -1.030544496
                        0.377486823
                                    -1.3845133459
                        1.958924376
## [229,]
                                     0.8886990582
          1.107193215
## [230,] -0.177352212
                        0.727349896
                                     0.5602343511
## [231,] -0.382554098
                        2.181949995
                                     1.5801305215
## [232,] -0.270465487
                        0.467890423
                                      1.1229275581
## [233,] -1.674866120
                        0.390174384
                                     0.3437570553
## [234,] -0.828338660 -0.081849356 -0.2421741564
## [235,] -0.899183143 -0.433349049
                                      0.0541855242
## [236,] 0.216850133 -1.442856753
                                      0.4216441943
## [237,] -0.260734248 -2.247006891
                                      0.6672969538
## [238,] -0.240412393
                       1.031285447
                                      1.0570939845
## [239,] -0.477973585 -0.114754991
                                      0.2479793462
## [240,] -0.834705507 -0.371072459
                                      0.5932273199
## [241,] -0.146097282 -1.113592351 -0.3975691472
## [242,] -0.478350273
                        0.467514588
                                     0.2735254772
## [243,] -1.590244047 0.533883949 0.4184106249
```

```
## [244,] -0.337491933 -0.703958612 -0.0495325011
## [245,] -0.616985393
                        0.495454082
                                     0.2479309897
## [246,] -0.564588356 -0.134668438
                                     0.5948572768
                        0.579147470 -1.4544247652
## [247,] -1.010428348
## [248,] -0.137655299
                        0.993127257
                                     0.6218160308
## [249,] -1.759514498 -0.274842579 -0.4034560489
## [250,] -0.813783277
                        0.878697260
                                     0.8719692563
## [251,] -1.368612816 -0.021316492 -2.2729743066
## [252,] -1.275899254 -0.475442827
                                     0.0786717985
## [253,] -1.029142756
                        0.136056729
                                     0.5715204228
## [254,] -0.193496871
                        0.569879346
                                     1.0094653812
## [255,] -0.919133283 -1.367103676
                                     0.4859672953
## [256,] -1.304260771 -0.350205504 -0.0748085330
## [257,] -0.360695064 -0.407225800
                                     0.3469299128
## [258,] -1.034864271 -0.286602875
                                     0.6156970433
## [259,] -1.699350741
                       1.116851998
                                     0.5446641225
## [260,] -1.119929739 -0.573998136
                                     0.6845877600
## [261,] -1.169037355 -0.082835319
                                     0.9001028427
## [262,] -0.784809716
                        0.167920028
                                     0.3269090559
## [263,] -0.493708629
                        1.695450884
                                     0.9796642972
## [264,] -0.497304930 -1.601722724
                                     1.1761804108
## [265,] -0.976574569 -0.192412282
                                     0.6509580136
## [266,] -1.467961242 -0.427896169 -0.1003924068
                       1.496147172 -0.4109312622
## [267,] -0.902077101
## [268,] -1.036389744
                        0.082329109
                                     1.0784647253
## [269,] -1.705386507 -0.299483803 -0.1146301416
## [270,] -1.739073319
                        1.138271940
                                     0.3559990233
## [271,] -1.300129495
                        1.536663050
                                     0.2416124330
## [272,] -1.315969968
                                     0.4998004636
                        0.440075513
## [273,] -0.529848105
                        0.419933966
                                     1.0482014072
## [274,] -1.985877359 -0.100740767
                                     0.7664031671
## [275,] -1.130127906
                        0.653364324
                                     0.9493329437
## [276,] -1.598593607 -0.309970406 -0.4940385513
## [277,] -0.632759027 -0.841159617 -0.0294273529
## [278,] -0.738333683
                        0.116872897
                                     1.3081957816
## [279,] -1.578182522
                        0.731749724 -0.1439136175
## [280,] -0.953911115 -0.420001999 -0.0239870270
## [281,] -0.480593516 -0.083066046 -1.2235734344
## [282,]
                        0.638979802
                                     1.3749238633
          0.010452664
## [283,] -0.548950968
                       2.217153856
                                     0.9372928135
## [284,] -0.743013091 -0.155648639 -0.5674839806
## [285,] -1.612155439 -0.603633903
                                     0.5012124553
## [286,] -1.039827166 -0.076912746
                                     0.4303027182
## [287,] -0.843330937 -0.242317466
                                     0.4266714040
## [288,] -1.182272798 -0.941536117 -0.5788535918
## [289,] -0.948575182 -0.543794864 -0.0384268999
## [290,] 0.070130052 -1.812508190
                                     0.2191244979
## [291,] -1.743137930 -1.091959585
                                     0.4053547510
## [292,] -1.073623081 0.267028528
                                     1.0060410433
## [293,] -1.427227293 -0.672588422 0.0315439986
```

```
## [294,] -1.122843832 0.345719829 1.1758990412
## [295,] -1.263199681 -0.528831385 1.1119318115
## [296,] -1.290036191 -0.095482767 -0.7991514192
## [297,] -1.393302226 -2.385879900 -2.6677123780
## [298,] -1.782271248  0.420525876 -0.9155996847
## [299,] -1.273483991 -0.483974683 0.2522706621
fit.pc <- principal(dataset[c(1,3,5,7,8,9,12)], nfactors=3, rotate="varimax")</pre>
fit.pc
## Principal Components Analysis
## Call: principal(r = dataset[c(1, 3, 5, 7, 8, 9, 12)], nfactors = 3,
       rotate = "varimax")
## Standardized loadings (pattern matrix) based upon correlation matrix
##
                              RC1
                                    RC2
                                          RC3
                                                h2
                                                     u2 com
## age
                             0.70 0.19 -0.20 0.56 0.44 1.3
## creatinine phosphokinase -0.02 -0.09 0.86 0.76 0.24 1.0
## ejection_fraction
                             0.10 0.76 -0.16 0.60 0.40 1.1
                             0.01 0.36 0.41 0.30 0.70 2.0
## platelets
## serum_creatinine
                             0.59 -0.23 -0.05 0.40 0.60 1.3
## serum sodium
                            -0.24 0.66 0.17 0.53 0.47 1.4
## time
                            -0.70 0.04 -0.20 0.54 0.46 1.2
##
##
                         RC1 RC2 RC3
## SS loadings
                         1.39 1.24 1.05
## Proportion Var
                         0.20 0.18 0.15
## Cumulative Var
                         0.20 0.38 0.53
## Proportion Explained 0.38 0.34 0.29
## Cumulative Proportion 0.38 0.71 1.00
##
## Mean item complexity = 1.3
## Test of the hypothesis that 3 components are sufficient.
## The root mean square of the residuals (RMSR) is 0.16
## with the empirical chi square 326.89 with prob < 1.5e-70
## Fit based upon off diagonal values = -1.65
round(fit.pc$values, 3)
## [1] 1.475 1.176 1.029 0.966 0.888 0.737 0.729
fit.pc$loadings
##
## Loadings:
##
                            RC1
                                   RC2
                                          RC3
## age
                             0.696 0.185 -0.200
## creatinine phosphokinase
                                           0.864
## ejection_fraction
                                    0.755 -0.157
## platelets
                                    0.357 0.412
```

```
## serum creatinine
                            0.586 -0.232
## serum sodium
                            -0.240 0.663 0.173
                            -0.702
## time
                                          -0.201
##
##
                    RC1
                         RC2
                                RC3
## SS loadings
                 1.390 1.235 1.054
## Proportion Var 0.199 0.176 0.151
## Cumulative Var 0.199 0.375 0.526
# Loadings with more digits
pc.load.heart <- fit.pc$loadings[1:7,1:3]</pre>
print(pc.load.heart)
##
                                   RC1
                                               RC2
                                                            RC3
## age
                             0.69625801 0.18519166 -0.20024241
## creatinine phosphokinase -0.01977081 -0.09374166 0.86427917
## ejection fraction
                            0.09927290 0.75521937 -0.15703997
## platelets
                            0.01116830 0.35699707 0.41234930
## serum creatinine
                            0.58617844 -0.23158975 -0.04551365
## serum_sodium
                           -0.24038458   0.66250806   0.17287312
## time
                           # Communalities
fit.pc$communality
##
                       age creatinine_phosphokinase
                                                           ejection_fraction
                 0.5591682
                                                                   0.6048730
##
                                          0.7561569
##
                 platelets
                                   serum_creatinine
                                                                serum sodium
##
                 0.2976036
                                          0.3993105
                                                                   0.5265868
##
                      time
##
                 0.5359443
# Rotated factor scores
fit.pc$scores
##
                  RC1
                                RC2
                                              RC3
##
     [1,]
          1.661261807 -1.554800886 0.2391648108
##
          0.743266680 -0.800052166 6.6257827317
     [2,]
##
     [3,]
          0.927179080 -2.016941671 -0.4549872007
##
     [4,]
          0.334885605 -1.266839858 0.1473115437
##
     [5,]
          1.925456863 -3.274592726 -0.2063397138
##
          2.435918328 -0.165636681 -0.8575735122
     [6,]
##
     [7,]
          1.012119703 -1.263416904 -0.3244895181
##
          1.124477246 1.115611048 0.4460294461
     [8,]
##
     [9,]
          1.234722890 1.691814397 -0.3538296415
##
    [10,]
          4.919709448 -0.999011928 0.1358685604
   [11,] 2.640695114 -0.439924198 -0.0044503303
```

```
##
    [12,]
           0.428072549 -0.186827135
                                       0.2931060423
##
    [13,] -0.139463181 -1.005910129
                                       0.5149623433
##
    [14,]
           0.205750073 -0.013367351
                                       0.2133024344
##
                         0.129530927
                                       0.8853088186
    [15,]
           0.100190044
                         0.324891744 -1.1159824597
##
    [16,]
           1.649820322
##
    [17,]
           1.595345623
                         0.956323503 -0.2371917548
##
    [18,]
          -0.156822106 -2.866432703
                                       0.1779870700
##
    [19,]
           0.762120879 -0.103388790
                                       0.0231261139
    [20,]
##
           0.907950332 -1.748387342 -0.9061044026
    [21,]
##
           0.762655848 -0.465114447
                                       0.0799383657
##
           0.944646930 -0.308381123
                                       0.1180144130
    [22,]
##
    [23,]
           0.733921935
                         0.548331547
                                       0.1903647967
##
    [24,]
           0.457662548
                         1.284173827
                                       0.0687137964
##
    [25,]
           1.492282733 -0.549949036
                                       0.1711517403
##
    [26,]
           1.455420414
                         0.835943301 -0.5028730340
##
                         0.755655310 -0.7523795208
    [27,]
           1.941662073
##
    [28,]
           1.134926967
                         0.573778900 -0.2150997676
##
    [29,]
           2.308580309 -1.259927295 -0.6226136569
           1.520043263 -0.715581081 -0.6753536792
##
    [30,]
##
                         0.193596104 -0.1844817096
    [31,]
           2.353027773
##
    [32,]
           2.584217212
                         0.341226598 -0.3233372990
##
           0.295532144 -1.105549289
                                       0.1548664887
    [33,]
##
    [34,]
           0.035612527 -0.257097226
                                       0.3899811986
                         0.991149461 -0.5046204217
##
    [35,]
           0.663877522
##
           1.876218740 -0.731427455
                                       0.0146293253
    [36,]
##
    [37,]
           1.908293478
                         0.818363037 -0.8903389408
##
    [38,]
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                                       0.6137036191
    [39,]
##
           1.007463177 -0.588312865
                                       2.3617777846
##
                         0.620878762
                                       0.4508776138
    [40,]
           1.154552043
##
           1.129162665 -1.163688178
    [41,]
                                       0.3401328031
##
    [42,]
          -0.020711589 -0.926623118 -0.3053509355
##
    [43,]
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                         0.610849610 -0.1530495710
##
    [44,]
           1.117429820
                         0.484077775 -0.6480190259
##
    [45,]
           0.525787658
                         1.628332541 -0.0773460918
##
    [46,]
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                        -0.306472980
                                       0.5615070471
##
    [47,]
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                        -1.612860316
                                       1.0768836850
##
    [48,]
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                         0.816335765
                                       1.0803374958
##
    [49,]
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##
    [50,]
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                         0.400124857
                                       0.6707819730
##
    [51,]
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                                       0.0009576655
##
    [52,]
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                                       0.8749494801
##
    [53,]
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                         1.275225506
                                       3.1242865473
##
    [54,]
           1.035561944
                         0.843644912 -0.1766442263
##
    [55,]
           0.964937677 -0.667315954 -0.1836188315
##
           2.396441039
                         0.122309343
                                       0.3800272497
    [56,]
##
    [57,]
           1.311884637 -0.096229075 -0.3931885056
##
                         0.230750573
                                       0.0975868884
    [58,]
           0.117242708
##
    [59,] -0.230865053 -1.036172140
                                       0.9937338718
##
    [60,]
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                                       0.0716641805
    [61,] -0.222187227 -0.906990443
                                      7.2203194356
```

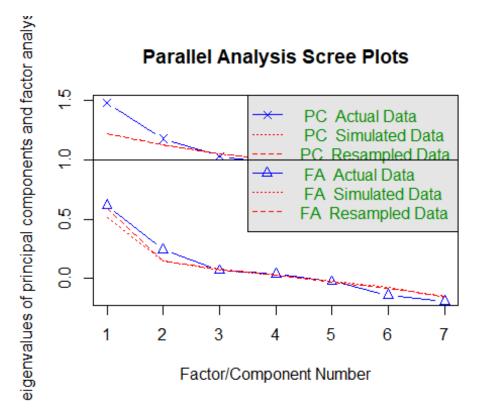
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##
    [62,]
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##
    [63,] -0.008689059
                         0.085367104 -0.0345107941
##
    [64,] -0.549357130
                         0.979474617
                                     1.2025062067
##
                        2.028983076 -0.1298242971
    [65,]
           0.083935800
##
    [66,]
           0.988680110 -2.692397650 -0.8718446516
    [67,] -0.648148747 -1.708399982 0.2357704108
##
##
    [68,]
           0.532711245
                         0.034977861 -0.0205406501
##
    [69,]
           0.449358882
                        0.116363372 -0.0114748486
##
    [70,]
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    [71,] -0.684673449
##
                         0.620888501
                                     0.5949996183
##
    [72,] -0.096008591 -0.266505695 -0.2283303489
##
    [73,]
           1.537899958 -0.792079545
                                     4.1950500318
##
    [74,]
           0.555768980
                         0.462584538 -0.7769184732
##
    [75,]
           0.556411378 -1.086577298 0.2364415509
##
    [76,] -0.216828225 -0.707001512 -0.1918664146
                        2.005827437 -0.3236278154
##
    [77,]
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##
    [78,] -0.607749063
                         0.183163996 -0.0212675426
##
    [79,]
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                       -0.217708128 -0.4254147686
                         0.943013569 0.2959498846
##
    [80,] -0.063297651
##
    [81,]
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                         0.278359780 -0.3100879741
##
    [82,]
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                         0.814464099 -0.0545080160
##
           0.701850273 -1.556076413 -0.5038258391
    [83,]
##
    [84,]
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                         0.236687990 -1.1519445673
##
    [85,] -0.113963882 -0.001775022
                                     0.3909018947
##
    [86,] -0.258837308
                         1.431743479 0.3730824376
##
    [87,] -0.132936474 -0.384334804 -0.5311877910
##
    [88,]
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                        1.884983446 -0.3481862241
    [89,] -0.728453310
##
                         0.165887725 -0.1153721621
##
    [90,] -0.325982563 -0.033839181 -0.1137702233
##
    [91,]
                         0.542978350 -0.5658370679
          0.551045835
##
    [92,]
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                        0.053331595
                                      0.3617566227
##
    [93,] -0.363720014
                         0.919551965
                                      0.1109323635
##
           0.281720144 -1.053032127 -0.2996120563
    [94,]
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    [95,] -0.201173206
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                                      0.2348252272
##
    [96,]
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                       -0.967996687
##
                                      0.1101564113
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##
    [98,]
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                         1.310128264 -0.7599096037
##
    [99,]
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## [100,]
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                         0.508384870 -0.4203188124
## [101,]
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## [102,]
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## [103,]
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                                      0.1110579911
## [104,] -0.696897702
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## [105,]
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## [106,]
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           0.972097738
## [107,]
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                                      0.2643827297
## [108,] -0.630359888 -0.422572840
                                      1.3656024435
## [109,]
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                                      0.4517056571
## [110,] -0.263211207
                        1.966140938
                                      2.6273981587
## [111,] 1.570689585 1.218400716 -0.8286984171
```

```
## [112,] -0.079851430 -0.476705134 -0.3987411216
## [113,] -0.232857424 -0.987410715 0.1836507253
## [114,]
                       1.672184717 -0.2905798137
          0.861926056
          0.502907066 -0.964718479 0.1722577393
## [115,]
## [116,] -0.124361588
                        0.121099491 -0.3427441451
## [117,]
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                        1.241001991 -0.5654697557
## [118,]
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                       2.230747174 0.1209613524
## [119,]
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                       1.569407098 -0.7579634732
## [120,]
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                        0.051411596 -0.2919360483
## [121,]
                        0.769453621 -0.3000942339
           0.471353622
## [122,]
          0.239404523 -0.179511841 -0.8150414891
## [123,] -0.183468621
                        0.418602246 -0.3254376420
## [124,] -0.379654647
                        0.225010617 -0.0511604751
## [125,]
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## [126,] -0.439853331
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## [127,] -0.020406232 -2.895762575 -0.1700108754
## [128,]
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## [129,] -0.160749776 -0.354127757 -0.1035501859
## [130,]
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          0.339556664
                        1.134193809
## [131,] -0.237984674
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## [132,]
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                                     0.1719603923
## [133,] -0.548148785 -0.084896488
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## [134,]
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## [135,]
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                                     3.1075914230
## [136,]
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## [137,]
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## [138,]
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                                    0.1567333112
## [139,] -0.004758957 -0.254210240 -0.3494468499
## [140,] -0.659513150 -0.603226065
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## [141,]
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## [142,] -0.766013551
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                                     0.4898487459
## [143,] -0.431084079 -0.882918765
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## [144,] -0.190133535
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## [145,] 0.594737173 -0.078962400
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## [146,] -0.822369651
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## [147,] -0.632086337 -0.639659696 -0.3084664918
## [148,]
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## [149,]
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## [150,] -0.102833245 -0.438284149 1.3662033639
## [151,]
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## [152,]
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## [153,] -0.501623706 -0.244712801 -0.7113591605
## [154,] -0.466410671 -0.387641116 1.2984836637
## [155,] -0.026249918 -0.140029667 -0.3217130039
## [156,] -0.116271543 -0.519456212 -0.2552566197
## [157,] -0.328502961 -0.297409376 -0.2283230337
## [158,] -0.670127696 -0.863873950 0.0320977323
## [159,] 1.236631450
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## [160,] -0.087149306
                        0.989271375 0.0447048996
## [161,] 0.264931050 -0.108130352 -0.6630592328
```

```
## [162,] -1.011591855 -0.282794292 -0.3950346566
## [163,] 0.064674548 0.794095498 0.7180245971
## [164,] -0.855164135 -0.353179379
                                   1.1021613126
## [165,] -0.817630171 -0.338158269 2.2477161022
## [166,] 0.790071410 -0.085952387 -0.4093134146
## [167,] -0.364973805  0.605203649 -0.8129999106
## [168,] 0.051590540 -1.959827996 -1.0494779489
## [169,] -0.058338220 0.409337783 -0.0359104234
## [170,] 0.159737156 -0.254669123 0.1473645979
## [171,] -0.489533321 -0.419949638 0.0988150804
## [172,] -0.595220420 0.285623727 3.2696000954
## [173,] 0.085653123 2.126932185 -0.8797935760
## [174,] -1.101774379 -0.948102234 -0.2916000702
## [175,] -0.166037172  0.108567577 -0.3032487590
## [176,] -0.097398428 1.622331214 -0.4001096589
## [177,] 0.077392575 -0.439270324 -0.1476584803
## [178,] -0.847221750 0.547109788 -0.9085380018
## [179,] -0.127606139 2.264892371 -0.4746835928
## [180,] -0.690762926 0.522014464 0.3837300635
## [181,] -1.244346835 -0.658517059 0.3641916993
## [182,] -0.514946965 -0.827817681 -0.3989361780
## [183,] -0.172665628 -0.647201739 -0.1258618235
## [184,] 0.858257113 -0.307871855 -0.9277885573
## [185,] -0.642483481 -0.760191790 -0.4506613356
## [186,] -0.241494042 -0.111254457 0.0564260901
## [187,] -0.937666219 -0.077076546 -0.6672609206
## [189,] -0.460797704 -0.065475798 -0.7839240452
## [190,] -1.408796077 0.544433129 -0.0945931696
## [191,] 0.896368333 -0.001930967 -0.0750159818
## [192,] 0.146044715 1.181534430 -0.7722082772
## [193,] -0.858056614 -0.737315437 -0.6394594140
## [194,] -0.197251951 0.170279072 -0.7379426061
## [195,] -1.140428526 -1.852050166 -0.3155272212
## [196,]
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## [197,] -1.139571685 -0.202664970 0.0453437056
## [198,] -0.563968269 -0.088513773 -0.4422084068
## [199,] -1.086028156 -1.352543347 0.1819051765
## [200,] 0.382812764 -3.094221200 -0.3362310993
## [201,] -0.572810886 -0.126824436 -0.0238687266
## [202,] -0.921088541 1.225260712 -0.0570952712
## [203,] -0.049124158 1.459231030 -1.1118129779
## [204,] 0.257805972 -1.189500127 -0.6668767422
## [205,]
         ## [206,] -0.872191759 0.486364167 -0.1067486746
## [207,] -1.645178492 0.281541525 -0.3536193491
## [208,] 0.411305453 0.203541128 -1.1172313308
## [209,] -0.601616408 0.554671402 1.4750001020
## [210,] -0.955119693 -1.089864345 0.1569386064
## [211,] -0.276077959 -0.580271097 0.1500176716
```

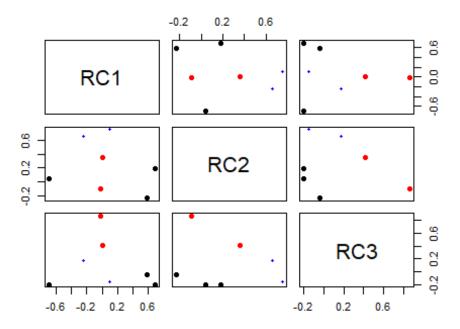
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## [212,] -1.044240318 1.218357423 -0.7190084888
## [213,] 0.514319443 1.745361381 0.0449525080
## [214,] -0.813768250 -1.478470608 -0.5964264070
## [215,] -0.444032668 -0.204602604 -0.5628851690
## [216,] 0.052099177 -0.437476293 -0.6339590882
## [217,] -0.172145649 1.585499295 0.5722453206
## [218,] 2.496763775
                       0.200777416 -1.1196635080
## [219,] -0.197712351 -0.335412570 0.0672413174
## [220,] -1.028972799 0.545444230 0.4469534152
## [221,]
          0.133728397 -1.129970941 -0.2085540954
## [222,] -0.578029718 1.566105155 -0.8250059417
## [223,] -1.446534248
                       0.178091687 0.1196636579
## [224,] -1.435219779 -1.547758563 -0.4838741521
## [225,] -0.798291149
                       0.176369046 0.9801923146
## [226,] 0.633708473
                       0.010070080 -0.9765007437
## [227,] -0.723949834 -1.449128438 -0.9110323577
## [228,] -1.030544496 -0.377486823 1.3845133459
## [229,] 1.107193215 -1.958924376 -0.8886990582
## [230,] -0.177352212 -0.727349896 -0.5602343511
## [231,] -0.382554098 -2.181949995 -1.5801305215
## [232,] -0.270465487 -0.467890423 -1.1229275581
## [233,] -1.674866120 -0.390174384 -0.3437570553
## [234,] -0.828338660 0.081849356 0.2421741564
## [235,] -0.899183143  0.433349049 -0.0541855242
## [236,] 0.216850133 1.442856753 -0.4216441943
## [237,] -0.260734248 2.247006891 -0.6672969538
## [238,] -0.240412393 -1.031285447 -1.0570939845
## [239,] -0.477973585   0.114754991 -0.2479793462
## [240,] -0.834705507
                       0.371072459 -0.5932273199
## [241,] -0.146097282 1.113592351 0.3975691472
## [242,] -0.478350273 -0.467514588 -0.2735254772
## [243,] -1.590244047 -0.533883949 -0.4184106249
## [244,] -0.337491933
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## [245,] -0.616985393 -0.495454082 -0.2479309897
## [246,] -0.564588356  0.134668438 -0.5948572768
## [247,] -1.010428348 -0.579147470 1.4544247652
## [248,] -0.137655299 -0.993127257 -0.6218160308
## [249,] -1.759514498
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## [250,] -0.813783277 -0.878697260 -0.8719692563
## [251,] -1.368612816
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                       0.475442827 -0.0786717985
## [252,] -1.275899254
## [253,] -1.029142756 -0.136056729 -0.5715204228
## [254,] -0.193496871 -0.569879346 -1.0094653812
## [255,] -0.919133283
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## [256,] -1.304260771
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## [257,] -0.360695064
                       0.407225800 -0.3469299128
## [258,] -1.034864271
                      0.286602875 -0.6156970433
## [259,] -1.699350741 -1.116851998 -0.5446641225
## [260,] -1.119929739
                       0.573998136 -0.6845877600
## [261,] -1.169037355 0.082835319 -0.9001028427
```

```
## [262,] -0.784809716 -0.167920028 -0.3269090559
## [263,] -0.493708629 -1.695450884 -0.9796642972
## [264,] -0.497304930 1.601722724 -1.1761804108
## [265,] -0.976574569
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## [266,] -1.467961242
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## [267,] -0.902077101 -1.496147172 0.4109312622
## [268,] -1.036389744 -0.082329109 -1.0784647253
## [269,] -1.705386507 0.299483803 0.1146301416
## [270,] -1.739073319 -1.138271940 -0.3559990233
## [271,] -1.300129495 -1.536663050 -0.2416124330
## [272,] -1.315969968 -0.440075513 -0.4998004636
## [273,] -0.529848105 -0.419933966 -1.0482014072
## [274,] -1.985877359
                       0.100740767 -0.7664031671
## [275,] -1.130127906 -0.653364324 -0.9493329437
## [276,] -1.598593607
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                       0.841159617 0.0294273529
## [277,] -0.632759027
## [278,] -0.738333683 -0.116872897 -1.3081957816
## [279,] -1.578182522 -0.731749724 0.1439136175
## [280,] -0.953911115
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                       0.083066046
## [281,] -0.480593516
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## [282,]
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## [283,] -0.548950968 -2.217153856 -0.9372928135
## [284,] -0.743013091
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## [285,] -1.612155439
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## [286,] -1.039827166
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## [287,] -0.843330937
                       0.242317466 -0.4266714040
## [288,] -1.182272798
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## [289,] -0.948575182
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## [290,] 0.070130052
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## [291,] -1.743137930
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## [292,] -1.073623081 -0.267028528 -1.0060410433
## [293,] -1.427227293
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## [294,] -1.122843832 -0.345719829 -1.1758990412
## [295,] -1.263199681
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## [296,] -1.290036191
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                                    0.7991514192
## [297,] -1.393302226
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                                    2.6677123780
## [298,] -1.782271248 -0.420525876 0.9155996847
## [299,] -1.273483991
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# Factor Analysis utilities
fa.parallel(dataset[c(1,3,5,7,8,9,12)])
```



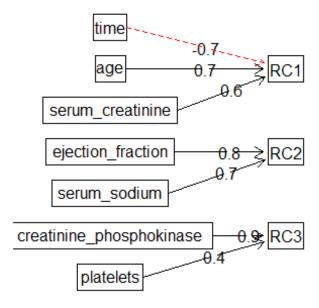
## Parallel analysis suggests that the number of factors = 0 and the number
of components = 1
#Based on the plot, we should retain two factors(based on the first elbow)
fa.plot(fit.pc)

## **Principal Component Analysis**



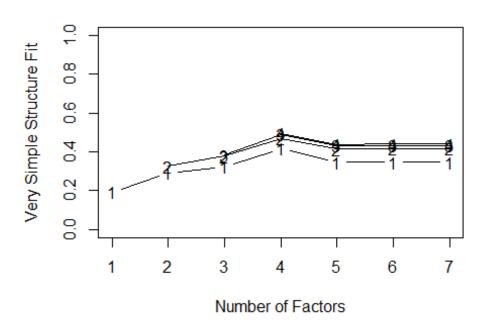
#Based on the plot, we can confirm that there is no correlation between RCs fa.diagram(fit.pc)

# **Components Analysis**



```
vss(dataset[c(1,3,5,7,8,9,12)])
```

#### Very Simple Structure



```
##
## Very Simple Structure
## Call: vss(x = dataset[c(1, 3, 5, 7, 8, 9, 12)])
## VSS complexity 1 achieves a maximimum of 0.42 with
## VSS complexity 2 achieves a maximimum of 0.47
                                                  with
                                                            factors
##
## The Velicer MAP achieves a minimum of NA with
## BIC achieves a minimum of NA with 1 factors
## Sample Size adjusted BIC achieves a minimum of NA with 2 factors
##
## Statistics by number of factors
##
     vss1 vss2
                 map dof
                           chisq prob sqresid fit RMSEA BIC SABIC complex
## 1 0.19 0.00 0.035 14 2.1e+01 0.095
                                           6.0 0.19 0.042 -59 -14.1
## 2 0.29 0.33 0.075
                       8 5.0e+00 0.760
                                            5.0 0.33 0.000 -41 -15.3
                                                                         1.3
## 3 0.33 0.38 0.134
                       3 1.9e+00 0.589
                                           4.6 0.38 0.000
                                                           -15
                                                                -5.7
                                                                         1.5
## 4 0.42 0.47 0.251
                                            3.7 0.49
                                                                  NA
                                                                         1.5
                      -1 3.0e-02
                                    NA
                                                        NA
                                                            NA
## 5 0.35 0.42 0.417
                                           4.1 0.44
                                                                  NA
                                                                         1.4
                      -4 2.0e-08
                                    NA
                                                        NA
                                                            NA
## 6 0.35 0.42 1.000
                      -6 2.6e-13
                                    NA
                                           4.1 0.45
                                                        NA
                                                            NA
                                                                  NA
                                                                         1.4
## 7 0.35 0.42
                  NA
                      -7 2.6e-13
                                           4.1 0.45
                                                                  NA
                                                                         1.4
                                    NA
                                                        NA
                                                            NA
      eChisa
                SRMR eCRMS eBIC
## 1 3.7e+01 5.4e-02 0.066
                            -43
## 2 7.8e+00 2.5e-02 0.040
                            -38
## 3 3.0e+00 1.6e-02 0.041
                            -14
```

```
## 4 4.7e-02 1.9e-03 NA NA
## 5 2.6e-08 1.4e-06 NA NA
## 6 5.0e-13 6.3e-09 NA NA
## 7 5.0e-13 6.3e-09 NA NA
#The Very Simple Structure recommends to retain 4 factors to achieve the maximum fit

detach(dataset)
```