A_13 (2)

June 1, 2019

```
In [1]: import matplotlib.pyplot as plt
       from keras.utils import np_utils
       from keras.datasets import mnist
       from keras.models import Sequential
       from keras.layers import Dense, Dropout, Flatten
       from keras.layers import Conv2D, MaxPooling2D
       from keras.layers.normalization import BatchNormalization
       import seaborn as sns
       import numpy as np
       import keras
       %matplotlib inline
Using TensorFlow backend.
In [2]: (X_train, y_train), (X_test, y_test) = mnist.load_data()
       img_rows, img_cols = 28, 28
Downloading data from https://s3.amazonaws.com/img-datasets/mnist.npz
In [3]: print("Training data shape: ", X_train.shape) # (60000, 28, 28) -- 60000 images, each
       print("Test data shape", X_test.shape)
       print("Training label shape: ", y_train.shape) # (60000,) -- 60000 numbers (all 0-9)
       print("First 5 training labels: ", y_train[:5]) # [5, 0, 4, 1, 9]
Training data shape: (60000, 28, 28)
Test data shape (10000, 28, 28)
Training label shape: (60000,)
First 5 training labels: [5 0 4 1 9]
```

```
In [0]: num_classes = 10
        batch_size = 128
        nb_epoch = 10
In [5]: from keras import backend as K
        if K.image_data_format() == 'channels_first':
            X train = X train.reshape(X train.shape[0], 1, img rows, img cols)
            X_test = X_test.reshape(X_test.shape[0], 1, img_rows, img_cols)
            input_shape = (1, img_rows, img_cols)
        else:
            X_train = X_train.reshape(X_train.shape[0], img_rows, img_cols, 1)
            X_test = X_test.reshape(X_test.shape[0], img_rows, img_cols, 1)
            input_shape = (img_rows, img_cols, 1)
        X_train = X_train.astype('float32')
        X_test = X_test.astype('float32')
        X_train /= 255
        X test /= 255
        print('x_train shape:', X_train.shape)
        print(X_train.shape[0], 'train samples')
        print(X_test.shape[0], 'test samples')
x_train shape: (60000, 28, 28, 1)
60000 train samples
10000 test samples
In [0]: # convert class vectors to binary class matrices
        y_train = keras.utils.to_categorical(y_train, num_classes)
        y test = keras.utils.to categorical(y test, num classes)
In [7]: y_train.shape
Out[7]: (60000, 10)
0.0.1 4 layer CNN Model with 3*3 kernel size
In [0]: model1=Sequential() # Initializing the model
        # First ConvNet
        model1.add(Conv2D(32,kernel_size=(3,3),
                            activation='relu',
                            input_shape=input_shape))
        model1.add(Conv2D(64,kernel_size=(3,3),
                            activation='relu'))
```

```
model1.add(Dropout(0.2))
       model1.add(Conv2D(128,kernel_size=(3,3),
                        activation='relu'))
       model1.add(BatchNormalization())
       #maxpooling by (2,2), dropout, flattening
       model1.add(MaxPooling2D(pool_size=(2,2)))
       model1.add(Dropout(0.5))
       model1.add(Flatten())
       #hidden_layer
       model1.add(Dense(256,activation='relu',kernel_initializer='random_uniform'))
       model1.add(Dropout(0.5))
       model1.add(Dense(num_classes,activation='softmax'))
       print(model1.summary())
WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/tensorflow/python/framework/op_
Instructions for updating:
Colocations handled automatically by placer.
WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/keras/backend/tensorflow_backend
Instructions for updating:
Please use `rate` instead of `keep_prob`. Rate should be set to `rate = 1 - keep_prob`.
Layer (type) Output Shape Param #
______
conv2d_1 (Conv2D)
                         (None, 26, 26, 32)
                                                 320
conv2d_2 (Conv2D) (None, 24, 24, 64) 18496
max_pooling2d_1 (MaxPooling2 (None, 12, 12, 64)
dropout_1 (Dropout)
                   (None, 12, 12, 64) 0
conv2d_3 (Conv2D)
                        (None, 10, 10, 128) 73856
batch_normalization_1 (Batch (None, 10, 10, 128)
                                               512
max_pooling2d_2 (MaxPooling2 (None, 5, 5, 128)
```

model1.add(MaxPooling2D(pool_size=(2,2)))

```
dropout_2 (Dropout) (None, 5, 5, 128) 0
._____
flatten_1 (Flatten)
          (None, 3200)
-----
dense 1 (Dense)
         (None, 256)
                   819456
 _____
dropout_3 (Dropout)
         (None, 256)
-----
         (None, 10)
dense 2 (Dense)
                   2570
-----
Total params: 915,210
Trainable params: 914,954
Non-trainable params: 256
------
None
In [0]: model1.compile(optimizer='adam',
        loss='categorical_crossentropy',
        metrics=['accuracy'])
In [0]: # Training the model
  history = model1.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verboater)
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
Epoch 2/10
Epoch 3/10
Epoch 4/10
Epoch 5/10
Epoch 6/10
Epoch 7/10
Epoch 8/10
Epoch 9/10
Epoch 10/10
In [0]: score = model1.evaluate(X_test, y_test, verbose=1)
  print('Test loss:', score[0])
```

print('Test accuracy:', score[1])

```
10000/10000 [===========] - 12s 1ms/step
Test loss: 0.023638954546318383
Test accuracy: 0.9934
In [0]: fig,ax = plt.subplots(1,1)
       ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
        # list of epoch numbers
       list_of_epoch = list(range(1,nb_epoch+1))
       train_loss = history.history['loss']
       val_loss = history.history['val_loss']
       ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
       ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
       plt.legend()
       plt.grid()
       plt.show();
         0.050
                                                           Validation Loss
                                                           Training Loss
         0.045
         0.040
      0.035
         0.030
         0.025
         0.020
                       2
                                   4
                                               6
                                                           8
                                                                      10
```

0.0.2 Changing the dropout rate to 0.8

```
In [51]: model1=Sequential() # Initializing the model
# First ConvNet
```

Epochs

```
activation='relu',
                         input_shape=input_shape))
       model1.add(Conv2D(64,kernel_size=(3,3),
                         activation='relu'))
       model1.add(MaxPooling2D(pool_size=(2,2)))
       model1.add(Dropout(0.8))
       model1.add(Conv2D(128,kernel_size=(3,3),
                        activation='relu'))
       model1.add(BatchNormalization())
        #maxpooling by (2,2), dropout, flattening
       model1.add(MaxPooling2D(pool_size=(2,2)))
       model1.add(Dropout(0.8))
       model1.add(Flatten())
       #hidden_layer
       model1.add(Dense(256,activation='relu',kernel_initializer='random_uniform'))
       model1.add(Dropout(0.8))
       model1.add(Dense(num_classes,activation='softmax'))
       print(model1.summary())
                   Output Shape
                                             Param #
Layer (type)
______
conv2d_26 (Conv2D)
                        (None, 26, 26, 32) 320
conv2d_27 (Conv2D) (None, 24, 24, 64)
                                              18496
max_pooling2d_15 (MaxPooling (None, 12, 12, 64) 0
dropout_22 (Dropout) (None, 12, 12, 64)
conv2d_28 (Conv2D) (None, 10, 10, 128) 73856
batch_normalization_8 (Batch (None, 10, 10, 128) 512
```

model1.add(Conv2D(32,kernel_size=(3,3),

```
max_pooling2d_16 (MaxPooling (None, 5, 5, 128)
  ______
dropout_23 (Dropout)
             (None, 5, 5, 128)
flatten 10 (Flatten) (None, 3200)
                         0
-----
dense 21 (Dense)
             (None, 256)
                         819456
-----
             (None, 256)
dropout_24 (Dropout)
-----
         (None, 10)
dense_22 (Dense)
                          2570
______
Total params: 915,210
Trainable params: 914,954
Non-trainable params: 256
None
In [0]: model1.compile(optimizer='adam',
          loss='categorical_crossentropy',
          metrics=['accuracy'])
In [53]: # Training the model
    history = model1.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verb
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
Epoch 2/10
Epoch 3/10
Epoch 4/10
Epoch 5/10
60000/60000 [=============== ] - 6s 98us/step - loss: 0.3079 - acc: 0.9092 - val
Epoch 6/10
60000/60000 [============== ] - 6s 98us/step - loss: 0.2859 - acc: 0.9165 - val
Epoch 7/10
60000/60000 [============== ] - 6s 98us/step - loss: 0.2697 - acc: 0.9222 - val
Epoch 8/10
Epoch 9/10
Epoch 10/10
```

```
In [54]: score = model1.evaluate(X_test, y_test, verbose=1)
        print('Test loss:', score[0])
        print('Test accuracy:', score[1])
10000/10000 [==========] - 1s 70us/step
Test loss: 0.122405351941369
Test accuracy: 0.9697
In [55]: fig,ax = plt.subplots(1,1)
        ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
         # list of epoch numbers
        list_of_epoch = list(range(1,nb_epoch+1))
        train_loss = history.history['loss']
        val_loss = history.history['val_loss']
        ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
        ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
        plt.legend()
        plt.grid()
        plt.show();
                                                          Validation Loss
         1.75
                                                          Training Loss
         1.50
         1.25
         1.00
         0.75
          0.50
         0.25
                       2
                                                                     10
```

Epochs

0.0.3 Changing the dropout rate to 0.2

```
In [46]: model1=Sequential() # Initializing the model
        # First ConvNet
       model1.add(Conv2D(32,kernel_size=(3,3),
                         activation='relu',
                         input_shape=input_shape))
       model1.add(Conv2D(64,kernel_size=(3,3),
                         activation='relu'))
       model1.add(MaxPooling2D(pool_size=(2,2)))
       model1.add(Dropout(0.2))
       model1.add(Conv2D(128,kernel_size=(3,3),
                        activation='relu'))
       model1.add(BatchNormalization())
        #maxpooling by (2,2), dropout, flattening
       model1.add(MaxPooling2D(pool_size=(2,2)))
       model1.add(Dropout(0.2))
       model1.add(Flatten())
        #hidden_layer
       model1.add(Dense(256,activation='relu',kernel_initializer='random_uniform'))
       model1.add(Dropout(0.2))
       model1.add(Dense(num_classes,activation='softmax'))
       print(model1.summary())
                                       Param #
Layer (type)
             Output Shape
______
conv2d_23 (Conv2D)
                        (None, 26, 26, 32)
                                                320
conv2d_24 (Conv2D) (None, 24, 24, 64) 18496
max_pooling2d_13 (MaxPooling (None, 12, 12, 64)
dropout_19 (Dropout) (None, 12, 12, 64) 0
```

```
conv2d_25 (Conv2D) (None, 10, 10, 128) 73856
batch_normalization_7 (Batch (None, 10, 10, 128)
max_pooling2d_14 (MaxPooling (None, 5, 5, 128) 0
             (None, 5, 5, 128)
dropout_20 (Dropout)
-----
flatten_9 (Flatten)
               (None, 3200)
  -----
           (None, 256)
dense_19 (Dense)
                               819456
dropout_21 (Dropout) (None, 256)
 _____
dense_20 (Dense)
            (None, 10)
______
Total params: 915,210
Trainable params: 914,954
Non-trainable params: 256
-----
None
In [0]: model1.compile(optimizer='adam',
             loss='categorical_crossentropy',
             metrics=['accuracy'])
In [48]: # Training the model
     history = model1.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verb
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
60000/60000 [============== ] - 8s 127us/step - loss: 0.1425 - acc: 0.9573 - va
Epoch 2/10
Epoch 3/10
60000/60000 [============== ] - 6s 98us/step - loss: 0.0343 - acc: 0.9894 - val
Epoch 4/10
60000/60000 [=============== ] - 6s 99us/step - loss: 0.0280 - acc: 0.9912 - val
Epoch 5/10
60000/60000 [============== ] - 6s 99us/step - loss: 0.0266 - acc: 0.9915 - val
Epoch 6/10
Epoch 7/10
Epoch 8/10
Epoch 9/10
```

```
Epoch 10/10
In [49]: score = model1.evaluate(X_test, y_test, verbose=1)
       print('Test loss:', score[0])
       print('Test accuracy:', score[1])
10000/10000 [========= ] - 1s 70us/step
Test loss: 0.07362920074305221
Test accuracy: 0.9802
In [50]: fig,ax = plt.subplots(1,1)
       ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
       # list of epoch numbers
       list_of_epoch = list(range(1,nb_epoch+1))
       train_loss = history.history['loss']
       val_loss = history.history['val_loss']
       ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
       ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
       plt.legend()
       plt.grid()
       plt.show();
        0.14
                                              Validation Loss
                                              Training Loss
        0.12
        0.10
        0.08
        0.06
        0.04
        0.02
                  ż
                           4
                                              8
                                                       10
                                Epochs
```

0.0.4 4 Convolution layers with 5*5 kernel size

```
In [0]: model2=Sequential() # Initializing the model
       # First ConvNet
       model2.add(Conv2D(32,kernel_size=(5,5),
                         activation='relu',
                         input_shape=input_shape))
       model2.add(Conv2D(64,kernel_size=(5,5),
                         activation='relu'))
       model2.add(MaxPooling2D(pool_size=(2,2)))
       model2.add(Dropout(0.2))
       model2.add(Conv2D(128,kernel_size=(5,5),
                        activation='relu'))
       model2.add(BatchNormalization())
       model2.add(MaxPooling2D(pool_size=(2,2)))
       model2.add(Dropout(0.5))
       model2.add(Flatten())
       #hidden layer
       model2.add(Dense(256,activation='relu',kernel_initializer='random_uniform'))
       model2.add(Dropout(0.5))
       model2.add(Dense(num_classes,activation='softmax'))
       print(model2.summary())
Layer (type)
              Output Shape
______
                        (None, 24, 24, 32) 832
conv2d_20 (Conv2D)
conv2d_21 (Conv2D)
                    (None, 20, 20, 64)
                                                51264
max_pooling2d_12 (MaxPooling (None, 10, 10, 64) 0
```

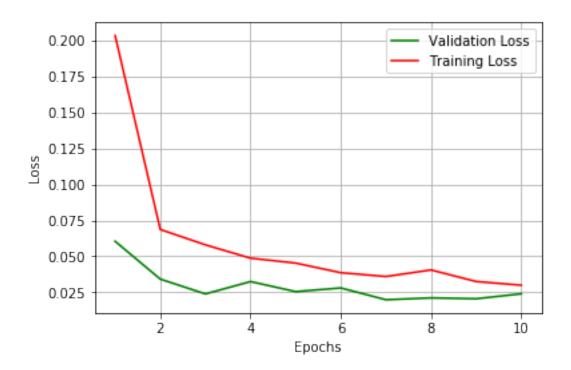
```
(None, 6, 6, 128) 204928
conv2d_22 (Conv2D)
batch_normalization_5 (Batch (None, 6, 6, 128)
max_pooling2d_13 (MaxPooling (None, 3, 3, 128)
dropout_10 (Dropout)
             (None, 3, 3, 128)
flatten_4 (Flatten) (None, 1152)
._____
dense_7 (Dense)
                (None, 256)
                               295168
-----
dropout_11 (Dropout) (None, 256)
                (None, 10)
dense_8 (Dense)
                                2570
______
Total params: 555,274
Trainable params: 555,018
Non-trainable params: 256
-----
None
In [0]: model2.compile(optimizer='adam',
             loss='categorical_crossentropy',
             metrics=['accuracy'])
In [0]: # Training the model
    history = model2.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verboater)
WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/tensorflow/python/ops/math_ops.
Instructions for updating:
Use tf.cast instead.
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
Epoch 2/10
Epoch 3/10
60000/60000 [=============== ] - 5s 91us/step - loss: 0.0580 - acc: 0.9831 - val
Epoch 4/10
Epoch 5/10
Epoch 6/10
```

(None, 10, 10, 64)

dropout_9 (Dropout)

```
Epoch 7/10
60000/60000 [============== ] - 5s 91us/step - loss: 0.0359 - acc: 0.9893 - val
Epoch 8/10
Epoch 9/10
60000/60000 [=============== ] - 5s 91us/step - loss: 0.0325 - acc: 0.9906 - val
Epoch 10/10
In [0]: score = model2.evaluate(X_test, y_test, verbose=1)
     print('Test loss:', score[0])
     print('Test accuracy:', score[1])
10000/10000 [========= ] - 1s 71us/step
Test loss: 0.02391246041604645
Test accuracy: 0.9931
In [0]: fig,ax = plt.subplots(1,1)
     ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
     # list of epoch numbers
     list_of_epoch = list(range(1,nb_epoch+1))
     train_loss = history.history['loss']
     val_loss = history.history['val_loss']
     ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
     ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
     plt.legend()
     plt.grid()
```

plt.show();



0.0.5 Changing the dropout rate to 0.8

```
#hidden layer
      model2.add(Dense(256,activation='relu',kernel_initializer='random_uniform'))
      model2.add(Dropout(0.8))
      model2.add(Dense(num_classes,activation='softmax'))
      print(model2.summary())
             Output Shape
                                Param #
Layer (type)
______
conv2d_7 (Conv2D)
                   (None, 24, 24, 32)
                                     832
conv2d_8 (Conv2D) (None, 20, 20, 64) 51264
max_pooling2d_5 (MaxPooling2 (None, 10, 10, 64)
 -----
dropout_7 (Dropout)
               (None, 10, 10, 64)
conv2d 9 (Conv2D) (None, 6, 6, 128)
_____
batch_normalization_3 (Batch (None, 6, 6, 128)
                                     512
max_pooling2d_6 (MaxPooling2 (None, 3, 3, 128)
               (None, 3, 3, 128)
dropout_8 (Dropout)
flatten_3 (Flatten) (None, 1152)
dense_5 (Dense)
                  (None, 256)
                                      295168
_____
dropout_9 (Dropout)
               (None, 256)
dense_6 (Dense) (None, 10) 2570
Total params: 555,274
Trainable params: 555,018
Non-trainable params: 256
None
```

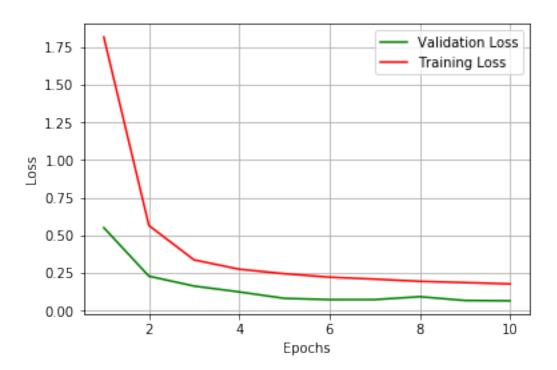
In [0]: model2.compile(optimizer='adam',

model2.add(Flatten())

```
metrics=['accuracy'])
In [18]: # Training the model
    history = model2.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verb
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
Epoch 2/10
Epoch 3/10
Epoch 4/10
Epoch 5/10
Epoch 6/10
Epoch 7/10
Epoch 8/10
Epoch 9/10
Epoch 10/10
In [19]: score = model2.evaluate(X_test, y_test, verbose=1)
    print('Test loss:', score[0])
    print('Test accuracy:', score[1])
10000/10000 [=========== ] - 1s 78us/step
Test loss: 0.06442127133197209
Test accuracy: 0.9845
In [20]: fig,ax = plt.subplots(1,1)
    ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
    # list of epoch numbers
    list_of_epoch = list(range(1,nb_epoch+1))
    train_loss = history.history['loss']
    val_loss = history.history['val_loss']
    ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
    ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
```

loss='categorical_crossentropy',

```
plt.legend()
plt.grid()
plt.show()
```



0.0.6 Changing the dropout to 0.2

```
model2.add(MaxPooling2D(pool_size=(2,2)))
model2.add(Dropout(0.2))

model2.add(Flatten())

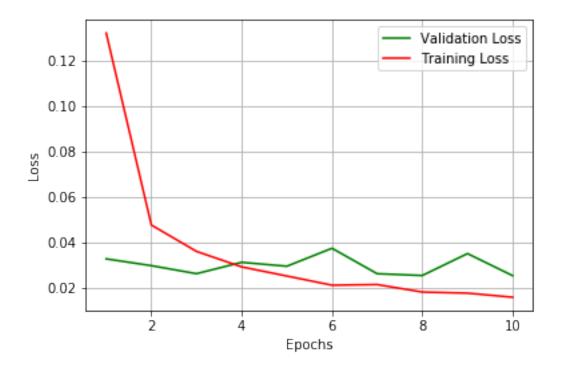
#hidden layer
model2.add(Dense(256,activation='relu',kernel_initializer='random_uniform'))
model2.add(Dropout(0.2))
model2.add(Dense(num_classes,activation='softmax'))
print(model2.summary())
```

Layer (type)	-	Shape	Param #
conv2d_20 (Conv2D)		24, 24, 32)	832
conv2d_21 (Conv2D)	(None,	20, 20, 64)	51264
max_pooling2d_11 (MaxPooling	(None,	10, 10, 64)	0
dropout_16 (Dropout)	(None,	10, 10, 64)	0
conv2d_22 (Conv2D)	(None,	6, 6, 128)	204928
batch_normalization_6 (Batch	(None,	6, 6, 128)	512
max_pooling2d_12 (MaxPooling	(None,	3, 3, 128)	0
dropout_17 (Dropout)	(None,	3, 3, 128)	0
flatten_8 (Flatten)	(None,	1152)	0
dense_17 (Dense)	(None,	256)	295168
dropout_18 (Dropout)	(None,	256)	0
dense_18 (Dense)	(None,	10)	2570
Total params: 555 974			

Total params: 555,274 Trainable params: 555,018 Non-trainable params: 256

```
In [0]: model2.compile(optimizer='adam',
           loss='categorical_crossentropy',
           metrics=['accuracy'])
In [43]: # Training the model
    history = model2.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verb
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
Epoch 2/10
Epoch 3/10
Epoch 4/10
Epoch 5/10
Epoch 6/10
Epoch 7/10
Epoch 8/10
Epoch 9/10
60000/60000 [=============== ] - 6s 94us/step - loss: 0.0176 - acc: 0.9947 - val
Epoch 10/10
In [44]: score = model2.evaluate(X_test, y_test, verbose=1)
    print('Test loss:', score[0])
    print('Test accuracy:', score[1])
10000/10000 [============ ] - 1s 69us/step
Test loss: 0.025309462502247287
Test accuracy: 0.9937
In [45]: fig,ax = plt.subplots(1,1)
    ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
    # list of epoch numbers
    list_of_epoch = list(range(1,nb_epoch+1))
    train_loss = history.history['loss']
```

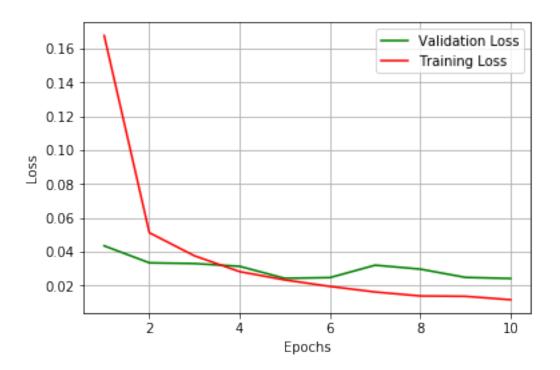
```
val_loss = history.history['val_loss']
ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
plt.legend()
plt.grid()
plt.show()
```



0.0.7 3 layer convolution layer with 3*3 kernel size

```
#hidden_layer
     model3.add(Flatten())
     model3.add(Dense(256,activation='relu',kernel_initializer='random_uniform'))
     model3.add(Dense(num_classes,activation='softmax'))
     print(model3.summary())
-----
Layer (type)
          Output Shape Param #
______
conv2d 23 (Conv2D)
                  (None, 26, 26, 32)
_____
max_pooling2d_14 (MaxPooling (None, 13, 13, 32) 0
conv2d_24 (Conv2D)
               (None, 11, 11, 64) 18496
-----
               (None, 11, 11, 64)
dropout_12 (Dropout)
flatten_5 (Flatten) (None, 7744)
dense_9 (Dense)
                  (None, 256)
                                   1982720
dense_10 (Dense)
            (None, 10)
                             2570
______
Total params: 2,004,106
Trainable params: 2,004,106
Non-trainable params: 0
______
None
In [0]: model3.compile(optimizer='adam',
               loss='categorical_crossentropy',
               metrics=['accuracy'])
In [0]: # Training the model
     history = model3.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verboater)
WARNING:tensorflow:From /usr/local/lib/python3.6/dist-packages/tensorflow/python/ops/math_ops.
Instructions for updating:
Use tf.cast instead.
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
Epoch 2/10
```

```
Epoch 3/10
60000/60000 [============== ] - 3s 57us/step - loss: 0.0375 - acc: 0.9883 - val
Epoch 4/10
Epoch 5/10
60000/60000 [=============== ] - 3s 57us/step - loss: 0.0232 - acc: 0.9927 - val
Epoch 6/10
60000/60000 [=============== ] - 3s 58us/step - loss: 0.0194 - acc: 0.9937 - val
Epoch 7/10
60000/60000 [============== ] - 3s 58us/step - loss: 0.0161 - acc: 0.9946 - val
Epoch 8/10
Epoch 9/10
Epoch 10/10
In [0]: score = model3.evaluate(X_test, y_test, verbose=1)
     print('Test loss:', score[0])
     print('Test accuracy:', score[1])
10000/10000 [============ ] - 1s 52us/step
Test loss: 0.024075999808483902
Test accuracy: 0.9931
In [0]: fig,ax = plt.subplots(1,1)
     ax.set_xlabel('Epochs'); ax.set_ylabel('Loss')
     # list of epoch numbers
     list_of_epoch = list(range(1,nb_epoch+1))
     train_loss = history.history['loss']
     val_loss = history.history['val_loss']
     ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
     ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
     plt.legend()
     plt.grid()
     plt.show();
```



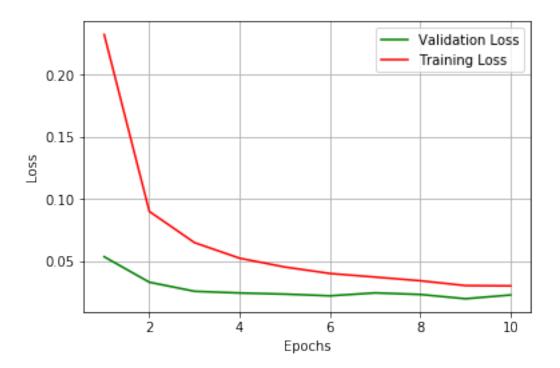
0.0.8 Changing the dropout rate to 0.8

print(model3.summary())

```
Layer (type)
        Output Shape
                     Param #
______
conv2d_10 (Conv2D)
            (None, 26, 26, 32)
                         320
max_pooling2d_7 (MaxPooling2 (None, 13, 13, 32) 0
    -----
conv2d_11 (Conv2D)
            (None, 11, 11, 64) 18496
_____
dropout_10 (Dropout) (None, 11, 11, 64)
_____
            (None, 7744)
flatten 4 (Flatten)
._____
dense 7 (Dense)
            (None, 256)
                        1982720
dense_8 (Dense)
        (None, 10)
                         2570
______
Total params: 2,004,106
Trainable params: 2,004,106
Non-trainable params: 0
None
In [0]: model3.compile(optimizer='adam',
          loss='categorical_crossentropy',
          metrics=['accuracy'])
In [23]: # Training the model
    history = model3.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verb
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
Epoch 2/10
Epoch 3/10
Epoch 4/10
Epoch 5/10
60000/60000 [============== ] - 4s 62us/step - loss: 0.0453 - acc: 0.9854 - val
Epoch 6/10
Epoch 7/10
```

```
Epoch 8/10
Epoch 9/10
Epoch 10/10
60000/60000 [=============== ] - 4s 61us/step - loss: 0.0302 - acc: 0.9899 - val
In [24]: score = model3.evaluate(X_test, y_test, verbose=1)
      print('Test loss:', score[0])
      print('Test accuracy:', score[1])
10000/10000 [========= ] - 1s 56us/step
Test loss: 0.02286809604455375
Test accuracy: 0.9922
In [25]: fig,ax = plt.subplots(1,1)
      ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
      # list of epoch numbers
      list_of_epoch = list(range(1,nb_epoch+1))
      train_loss = history.history['loss']
      val_loss = history.history['val_loss']
      ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
      ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
      plt.legend()
      plt.grid()
```

plt.show();

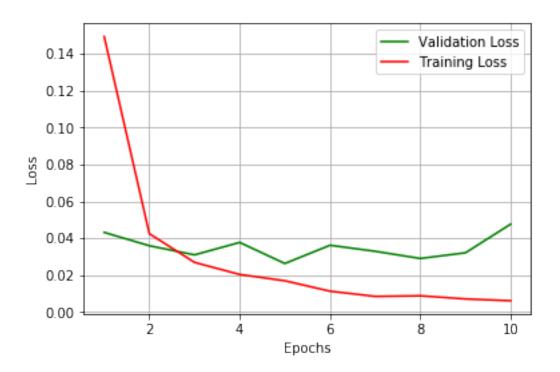


0.0.9 Changing dropout rate to 0.2

print(model3.summary())

```
Layer (type)
          Output Shape
                         Param #
______
conv2d_18 (Conv2D)
               (None, 26, 26, 32)
                              320
max_pooling2d_10 (MaxPooling (None, 13, 13, 32) 0
     -----
conv2d_19 (Conv2D)
               (None, 11, 11, 64) 18496
_____
dropout_15 (Dropout) (None, 11, 11, 64)
-----
               (None, 7744)
flatten 7 (Flatten)
._____
dense 15 (Dense)
              (None, 256)
                             1982720
dense 16 (Dense)
          (None, 10)
                              2570
_____
Total params: 2,004,106
Trainable params: 2,004,106
Non-trainable params: 0
None
In [0]: model3.compile(optimizer='adam',
            loss='categorical_crossentropy',
            metrics=['accuracy'])
In [38]: # Training the model
    history = model3.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verb
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
Epoch 2/10
Epoch 3/10
60000/60000 [=============== ] - 4s 61us/step - loss: 0.0269 - acc: 0.9915 - val
Epoch 4/10
60000/60000 [=============== ] - 4s 61us/step - loss: 0.0204 - acc: 0.9933 - val
Epoch 5/10
60000/60000 [=============== ] - 4s 61us/step - loss: 0.0169 - acc: 0.9946 - val
Epoch 6/10
Epoch 7/10
```

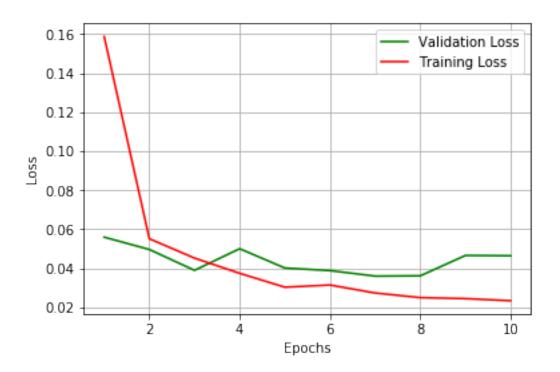
```
Epoch 8/10
Epoch 9/10
Epoch 10/10
In [39]: score = model3.evaluate(X_test, y_test, verbose=1)
      print('Test loss:', score[0])
      print('Test accuracy:', score[1])
10000/10000 [========= ] - 1s 51us/step
Test loss: 0.04763601563378916
Test accuracy: 0.9866
In [40]: fig,ax = plt.subplots(1,1)
      ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
      # list of epoch numbers
      list_of_epoch = list(range(1,nb_epoch+1))
      train_loss = history.history['loss']
      val_loss = history.history['val_loss']
      ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
      ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
      plt.legend()
      plt.grid()
      plt.show();
```



0.0.10 5 layer convolution layer with 5*5 kernel size

```
#hidden_layer
      model4.add(Dense(256,activation='relu',kernel_initializer='random_uniform'))
      model4.add(Dense(512,activation='relu',kernel_initializer='random_uniform'))
      model4.add(Dropout(0.5))
      model4.add(Dense(num_classes,activation='softmax'))
      print(model4.summary())
 ayer (type) Output Shape Param #
Layer (type)
______
conv2d_48 (Conv2D)
                     (None, 24, 24, 32)
                                         832
   ._____
max_pooling2d_21 (MaxPooling (None, 12, 12, 32) 0
conv2d_49 (Conv2D)
                  (None, 8, 8, 64) 51264
batch_normalization_12 (Batc (None, 8, 8, 64)
                                         256
conv2d_50 (Conv2D) (None, 4, 4, 128) 204928
dropout_20 (Dropout) (None, 4, 4, 128)
flatten_7 (Flatten) (None, 2048)
                     (None, 256)
dense_13 (Dense)
                                         524544
dense_14 (Dense)
              (None, 512)
                                         131584
dropout_21 (Dropout) (None, 512)
dense 15 (Dense) (None, 10)
                                         5130
______
Total params: 918,538
Trainable params: 918,410
Non-trainable params: 128
None
In [0]: model4.compile(optimizer='adam',
                 loss='categorical_crossentropy',
                 metrics=['accuracy'])
In [0]: # Training the model
      history = model4.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verboater)
```

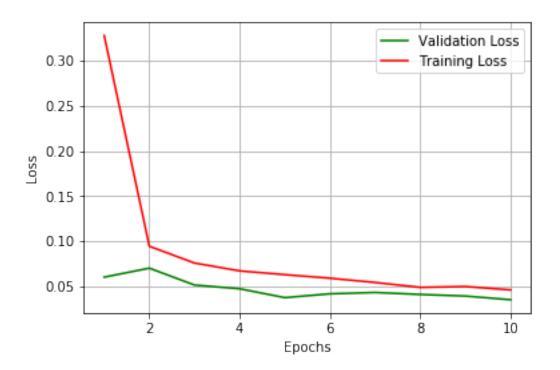
```
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
Epoch 2/10
60000/60000 [=============== ] - 4s 64us/step - loss: 0.0551 - acc: 0.9844 - val
Epoch 3/10
Epoch 4/10
60000/60000 [=============== ] - 4s 65us/step - loss: 0.0374 - acc: 0.9897 - val
Epoch 5/10
60000/60000 [=============== ] - 4s 63us/step - loss: 0.0303 - acc: 0.9913 - val
Epoch 6/10
Epoch 7/10
Epoch 8/10
Epoch 9/10
Epoch 10/10
In [0]: score = model4.evaluate(X_test, y_test, verbose=1)
    print('Test loss:', score[0])
    print('Test accuracy:', score[1])
10000/10000 [============ ] - 1s 66us/step
Test loss: 0.046396231524863836
Test accuracy: 0.9905
In [0]: fig,ax = plt.subplots(1,1)
    ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
    # list of epoch numbers
    list_of_epoch = list(range(1,nb_epoch+1))
    train_loss = history.history['loss']
    val_loss = history.history['val_loss']
    ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
    ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
    plt.legend()
    plt.grid()
    plt.show();
```



0.0.11 Changing the dropout rate to 0.8

```
#hidden_layer
       model4.add(Dense(256,activation='relu',kernel_initializer='random_uniform'))
       model4.add(Dense(512,activation='relu',kernel_initializer='random_uniform'))
       model4.add(Dropout(0.8))
       model4.add(Dense(num_classes,activation='softmax'))
       print(model4.summary())
            Output Shape Param #
Layer (type)
______
conv2d_12 (Conv2D)
                      (None, 24, 24, 32)
                                            832
max_pooling2d_8 (MaxPooling2 (None, 12, 12, 32) 0
                  (None, 8, 8, 64) 51264
conv2d_13 (Conv2D)
batch_normalization_4 (Batch (None, 8, 8, 64)
                                           256
conv2d_14 (Conv2D) (None, 4, 4, 128) 204928
dropout_11 (Dropout) (None, 4, 4, 128)
flatten_5 (Flatten) (None, 2048)
                      (None, 256)
dense_9 (Dense)
                                           524544
dense_10 (Dense)
               (None, 512)
                                           131584
dropout_12 (Dropout) (None, 512)
dense 11 (Dense) (None, 10)
                                           5130
______
Total params: 918,538
Trainable params: 918,410
Non-trainable params: 128
None
In [0]: model4.compile(optimizer='adam',
                  loss='categorical_crossentropy',
                  metrics=['accuracy'])
In [28]: # Training the model
       history = model4.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verb
```

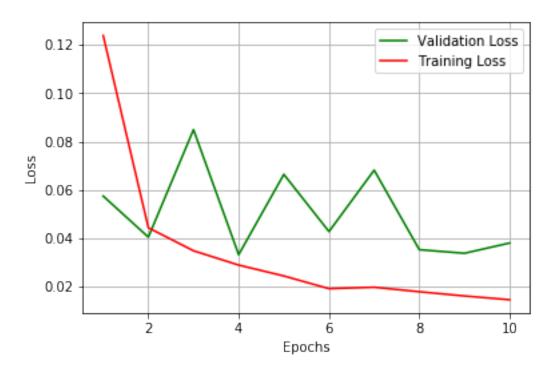
```
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
60000/60000 [============== ] - 5s 88us/step - loss: 0.3279 - acc: 0.8987 - val
Epoch 2/10
60000/60000 [============== ] - 4s 67us/step - loss: 0.0944 - acc: 0.9759 - val
Epoch 3/10
Epoch 4/10
Epoch 5/10
60000/60000 [=============== ] - 4s 67us/step - loss: 0.0630 - acc: 0.9849 - val
Epoch 6/10
Epoch 7/10
Epoch 8/10
Epoch 9/10
Epoch 10/10
In [29]: score = model4.evaluate(X_test, y_test, verbose=1)
     print('Test loss:', score[0])
     print('Test accuracy:', score[1])
10000/10000 [============ ] - 1s 61us/step
Test loss: 0.035173485061816334
Test accuracy: 0.9926
In [30]: fig,ax = plt.subplots(1,1)
     ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
     # list of epoch numbers
     list_of_epoch = list(range(1,nb_epoch+1))
     train_loss = history.history['loss']
     val_loss = history.history['val_loss']
     ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
     ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
     plt.legend()
     plt.grid()
     plt.show();
```



0.0.12 Changing the dropout rate to 0.2

```
#hidden_layer
       model4.add(Dense(256,activation='relu',kernel_initializer='random_uniform'))
       model4.add(Dense(512,activation='relu',kernel_initializer='random_uniform'))
       model4.add(Dropout(0.2))
       model4.add(Dense(num_classes,activation='softmax'))
       print(model4.summary())
            Output Shape Param #
Layer (type)
______
conv2d_15 (Conv2D)
                      (None, 24, 24, 32)
                                            832
max_pooling2d_9 (MaxPooling2 (None, 12, 12, 32) 0
                  (None, 8, 8, 64) 51264
conv2d_16 (Conv2D)
batch_normalization_5 (Batch (None, 8, 8, 64)
                                           256
conv2d_17 (Conv2D) (None, 4, 4, 128) 204928
dropout_13 (Dropout) (None, 4, 4, 128)
flatten_6 (Flatten) (None, 2048)
                      (None, 256)
dense_12 (Dense)
                                           524544
dense_13 (Dense)
               (None, 512)
                                           131584
dropout_14 (Dropout) (None, 512)
dense 14 (Dense) (None, 10)
                                           5130
______
Total params: 918,538
Trainable params: 918,410
Non-trainable params: 128
None
In [0]: model4.compile(optimizer='adam',
                  loss='categorical_crossentropy',
                  metrics=['accuracy'])
In [33]: # Training the model
       history = model4.fit(X_train, y_train, batch_size = batch_size, epochs=nb_epoch, verb
```

```
Train on 60000 samples, validate on 10000 samples
Epoch 1/10
60000/60000 [=============== ] - 5s 87us/step - loss: 0.1238 - acc: 0.9626 - val
Epoch 2/10
60000/60000 [=============== ] - 4s 66us/step - loss: 0.0444 - acc: 0.9868 - val
Epoch 3/10
Epoch 4/10
Epoch 5/10
60000/60000 [=============== ] - 4s 67us/step - loss: 0.0244 - acc: 0.9929 - val
Epoch 6/10
Epoch 7/10
Epoch 8/10
Epoch 9/10
Epoch 10/10
In [34]: score = model4.evaluate(X_test, y_test, verbose=1)
     print('Test loss:', score[0])
     print('Test accuracy:', score[1])
10000/10000 [============ ] - 1s 58us/step
Test loss: 0.03803959398596803
Test accuracy: 0.9914
In [35]: fig,ax = plt.subplots(1,1)
     ax.set_xlabel('Epochs') ; ax.set_ylabel('Loss')
     # list of epoch numbers
     list_of_epoch = list(range(1,nb_epoch+1))
     train_loss = history.history['loss']
     val_loss = history.history['val_loss']
     ax.plot(list_of_epoch, val_loss, 'g', label="Validation Loss")
     ax.plot(list_of_epoch, train_loss, 'r', label="Training Loss")
     plt.legend()
     plt.grid()
     plt.show();
```



1 Conclusions

```
In [57]: # Please compare all your models using Prettytable library
    from prettytable import PrettyTable

x = PrettyTable()

x.field_names = ["Numer of Layers", "Kernel Size", "BN", "Dropout", "Accuracy"]

x.add_row(["3",'3*3', 'NO','0.5', 0.9931])
x.add_row(["3",'3*3', 'NO','0.8', 0.9922])
x.add_row(["3",'3*3', 'NO','0.2', 0.9866])

x.add_row(["4",'3*3', 'YES','0.5', 0.9934])
x.add_row(["4",'3*3', 'YES','0.8', 0.9697])
x.add_row(["4",'3*3', 'YES','0.2', 0.9802])

x.add_row(["4",'5*5', 'YES','0.5', 0.9931])
x.add_row(["4",'5*5', 'YES','0.8', 0.9845])
x.add_row(["4",'5*5', 'YES','0.2', 0.9937])
```

```
x.add_row(["5",'5*5', 'YES','0.5', 0.9905])
x.add_row(["5",'5*5', 'YES','0.8', 0.9926])
x.add_row(["5",'5*5', 'YES','0.2', 0.9914])
```

print(x)

+	+		+		-+-		+		-+
Numer of L	ayers Ke	rnel Siz	e	BN		Dropout	.	Accuracy	
3	 	 3*3		NO		0.5	 	0.9931	-+
3	1	3*3	- 1	NO	1	0.8	I	0.9922	-
3	1	3*3	- 1	NO		0.2		0.9866	-
4	1	3*3	- 1	YES	1	0.5		0.9934	-
4	1	3*3	- 1	YES		0.8		0.9697	-
4	1	3*3		YES		0.2		0.9802	-
4	1	5*5	- 1	YES		0.5		0.9931	-
4	1	5*5	- 1	YES		0.8		0.9845	-
4	1	5*5	- 1	YES		0.2		0.9937	-
J 5	1	5*5	- 1	YES		0.5		0.9905	-
J 5		5*5	- 1	YES		0.8		0.9926	-
1 5	1	5*5	1	YES		0.2	I	0.9914	
+	+		+		-+-		+		-+