

Multidimensional Arrays

Introduction to multidimensional arrays

A multidimensional array is an array with more than one dimension. In a multidimensional array, each element is another array with a smaller number of dimensions.

Properties of multidimensional arrays

- Just like single-dimensional arrays, the elements of a 2d array are also stored in contiguous memory locations, where each element of the array occupies a fixed memory size (for integers it is 4).
- An example of a 2D array of size 3 * 5:-

	0	1	2	3	4
0	a[0][0]	a[0][1]	a[0][2]	a[0][3]	a[0][4]
1	a[1][0]	a[1][1]	a[1][2]	a[1][3]	a[1][4]
2	a[2][0]	a[2][1]	a[2][2]	a[2][3]	a[2][4]

Accessing array elements

- The elements of the array are accessed by using their index. The row index of a 2D array of size $N * M$ ranges from 0 to $N - 1$. Similarly, the column index ranges from 0 to $M - 1$. For example: Accessing element at row index 5 and column index 7: `Array[5][7]` -> this is the element at the 6th row and 8th column in the array.
- Every array is identified by its base address i.e the location of the first element of the first row of the array in memory. So, basically, the base address helps in identifying the address of all the elements of the array.
- Since the elements of an array are stored in contiguous memory locations, the address of any element can be accessed from the base address itself. For example, 200 is the base address of the entire array. If the number of columns in the array is equal to 10 then the address of the element stored at the index `Array[5][7]` is equal to $200 + (5 * 10 + 7) * (\text{size of(int)}) = 428$

Applications of Multidimensional arrays

- Multidimensional arrays are used to store the data in a tabular form. For example, storing the roll number and marks of a student can be easily done using multidimensional arrays. Another common usage is to store the images in 3D arrays.
- In dynamic programming questions, multidimensional arrays are used which are used to represent the states of the problem.
- Apart from these, they also have applications in many standard algorithmic problems like:
 - Matrix Multiplication
 - Adjacency matrix representation in graphs
 - Grid search problems

Time Complexity of various operations

- Accessing elements: Since elements in an array are stored at contiguous memory locations, they can be accessed very efficiently (random access) in $O(1)$ time using indices.

- Finding elements: Finding an element in an array takes $O(N * M)$ time in the worst case, where N is the number of rows of the array and M is the number of columns of the array, as you may need to traverse the entire array.