

Convolutional Neural Network

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Most of the materials are from a great blog [1]

How to extract features in images?



vertical edges



horizontal edges

Convolution

3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
4	2	1	6	2	8
2	4	5	2	3	9

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Convolution

3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
4	2	1	6	2	8
2	4	5	2	3	9

*

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Convolution

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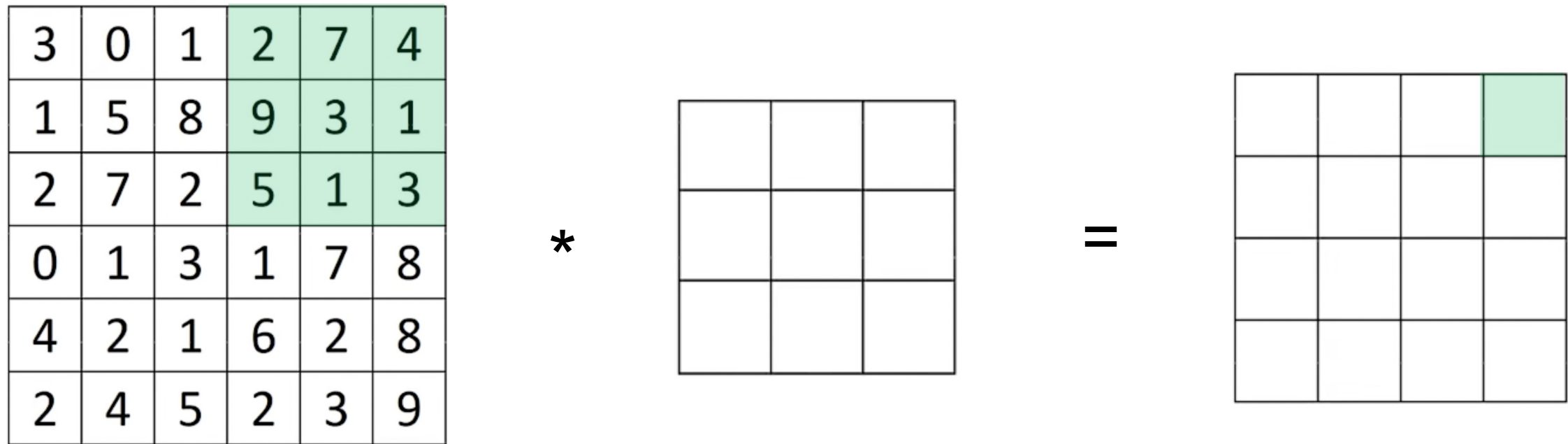
Convolution

3	0	1	2	7	4
1	5	8	9	3	1
2	7	2	5	1	3
0	1	3	1	7	8
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Convolution



Convolution

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Vertical edge detection

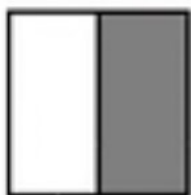
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0
10	10	10	0	0	0

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1	0	-1
1	0	-1
1	0	-1

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0	30	30	0
0	30	30	0
0	30	30	0
0	30	30	0



Vertical edge detection

0	0	0	10	10	10
0	0	0	10	10	10
0	0	0	10	10	10
0	0	0	10	10	10
0	0	0	10	10	10
0	0	0	10	10	10



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1	0	-1
1	0	-1
1	0	-1



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0	-30	-30	0
0	-30	-30	0
0	-30	-30	0
0	-30	-30	0



Vertical and horizontal edge detection

1	0	-1
1	0	-1
1	0	-1

Vertical

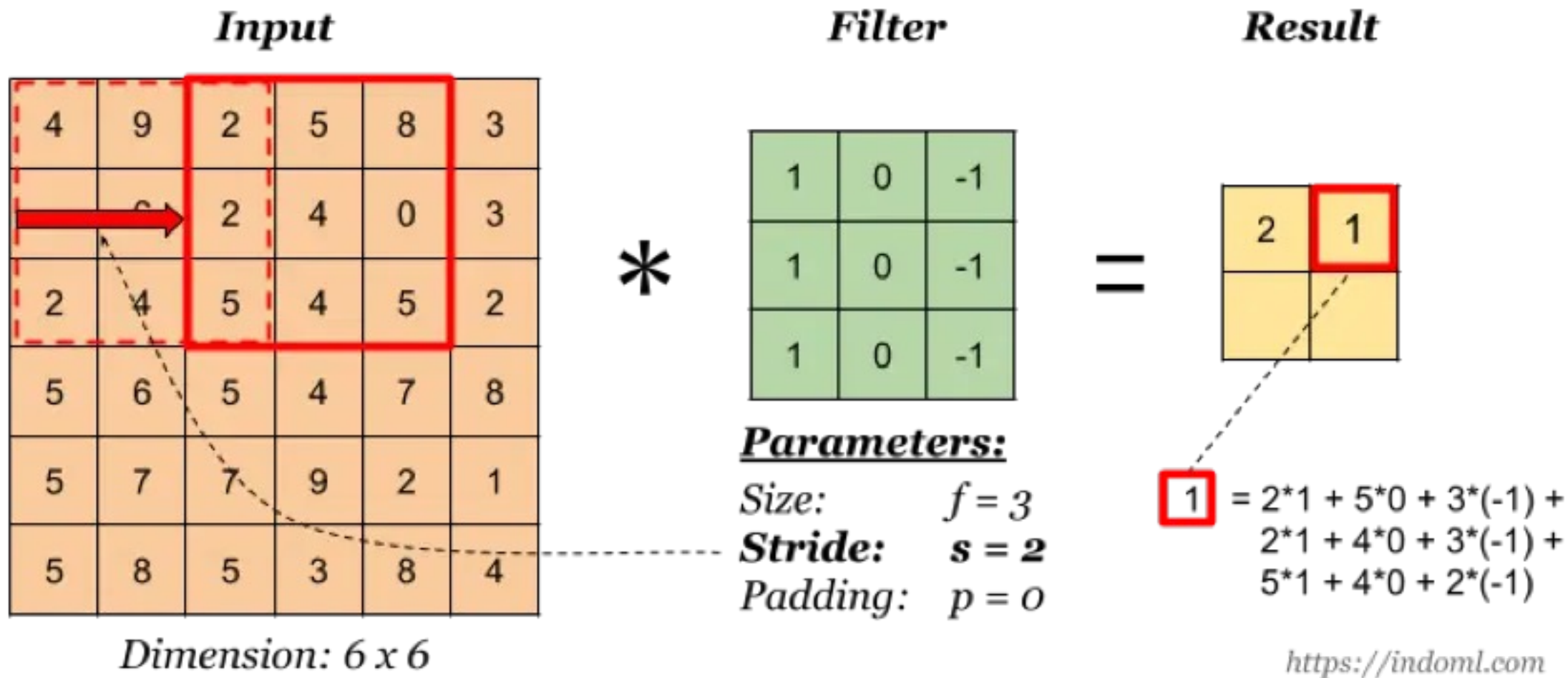
1	1	1
0	0	0
-1	-1	-1

Horizontal

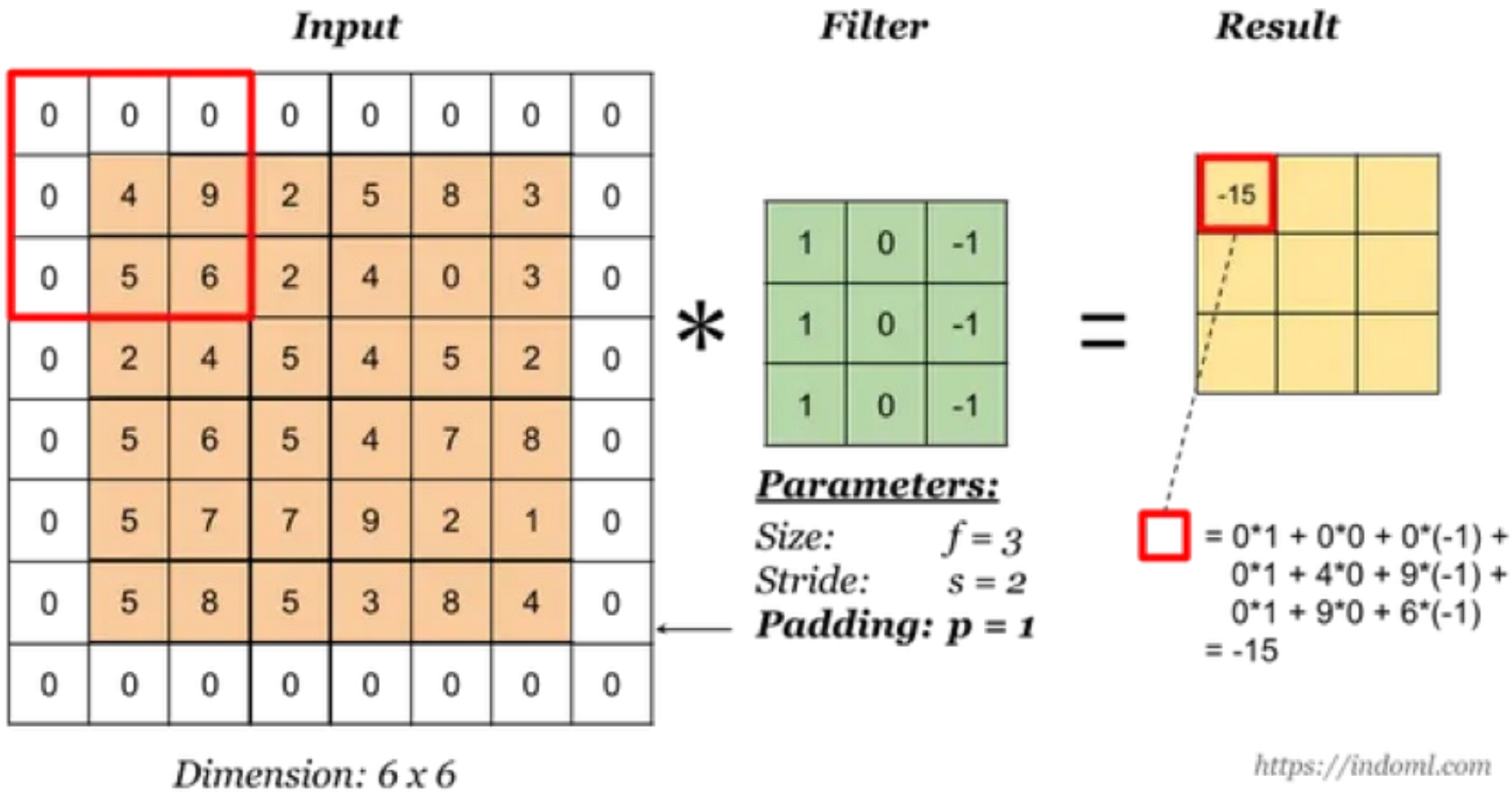
We can also develop other filters to extract curves, circles, etc.

In CNNs, we will let neural network to learn filters by itself; no need to design!

Stride(移动步长)



Padding (填充)



Padding can maintain the influence of the corner elements in input matrix

Padding can help maintain the matrix size

Input size: $n \times n$

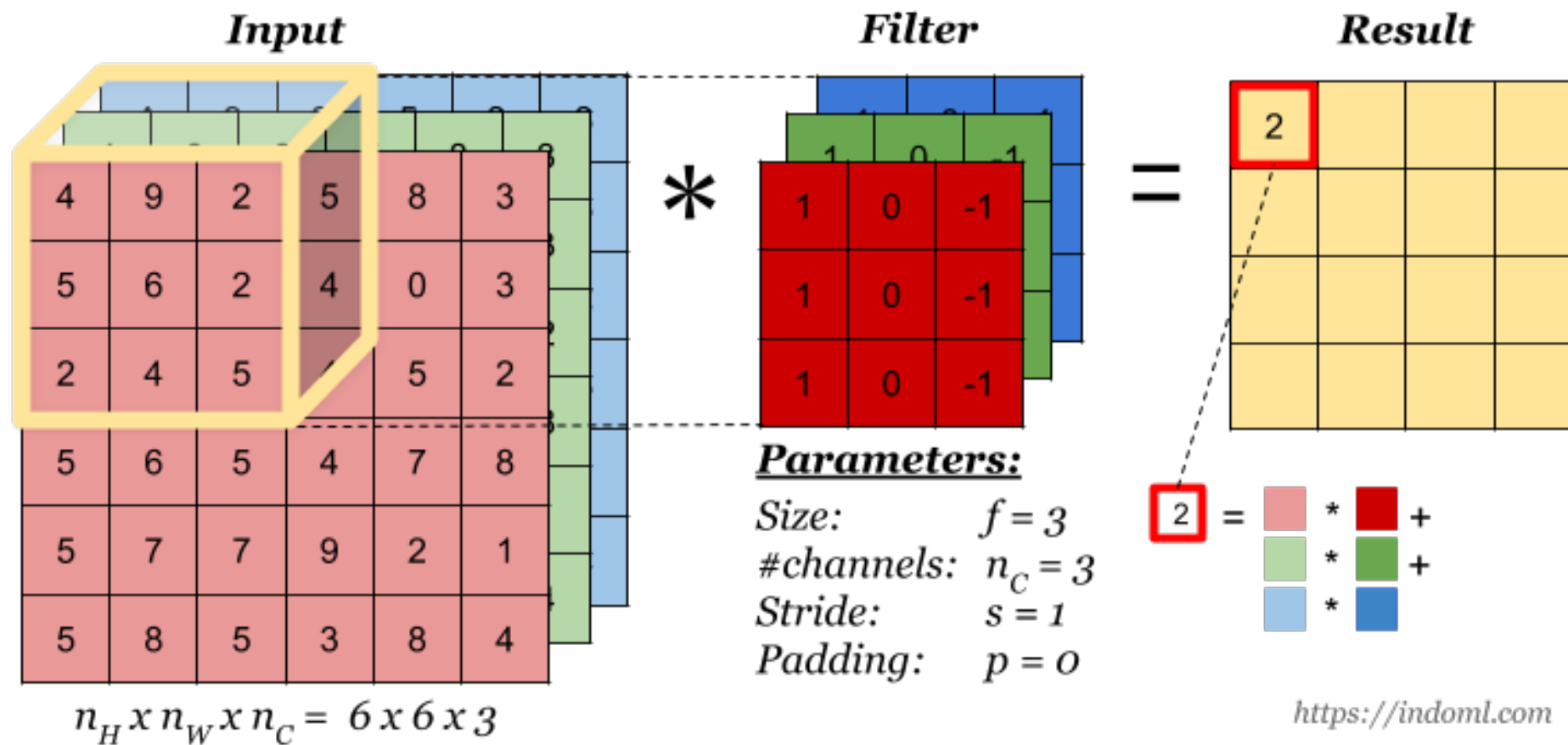
Filter size: $f \times f$

Padding: p

Stride: s

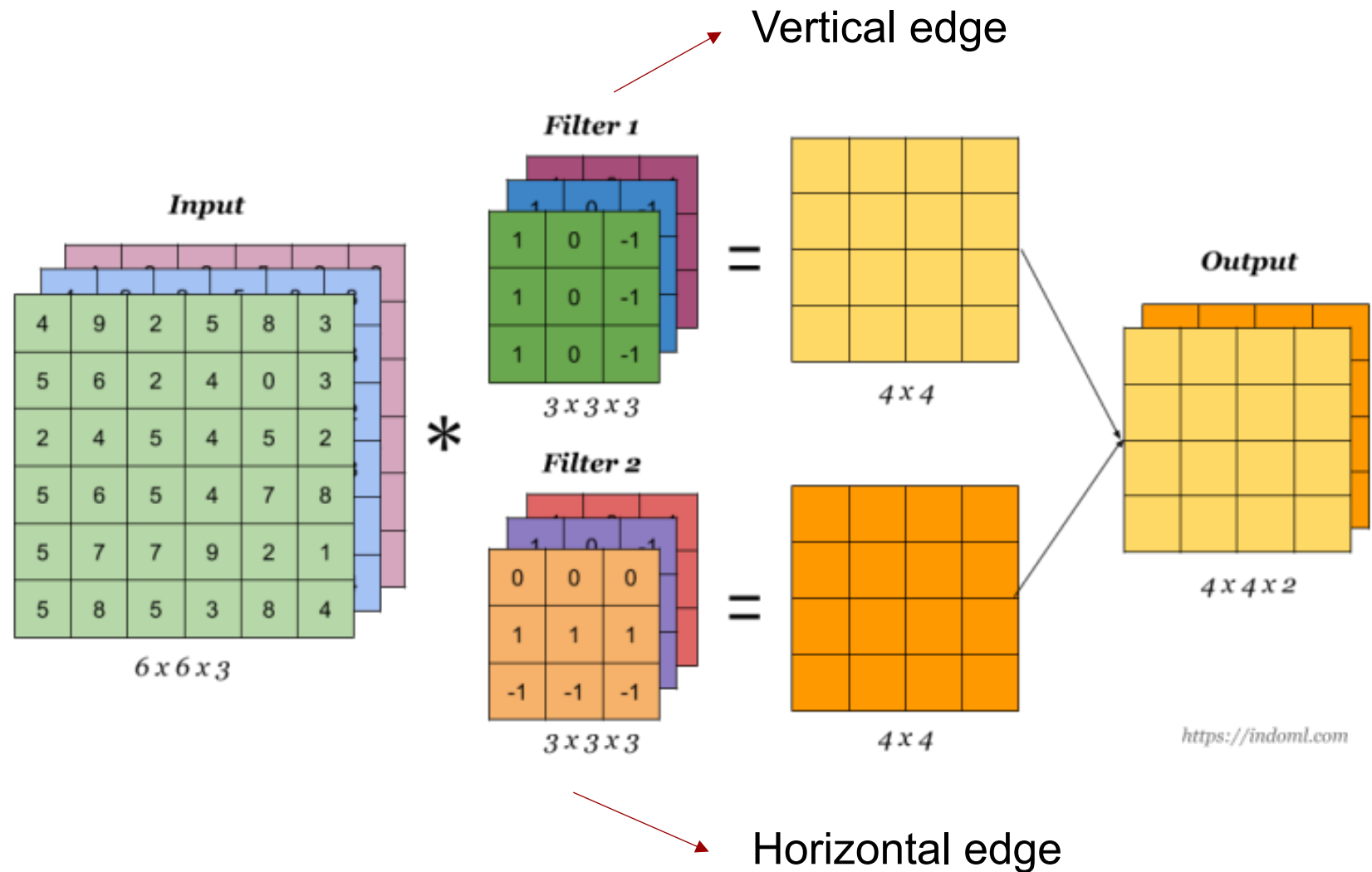
Output size: $\left\lfloor \frac{n + 2p - f}{s} + 1 \right\rfloor$

3D convolution

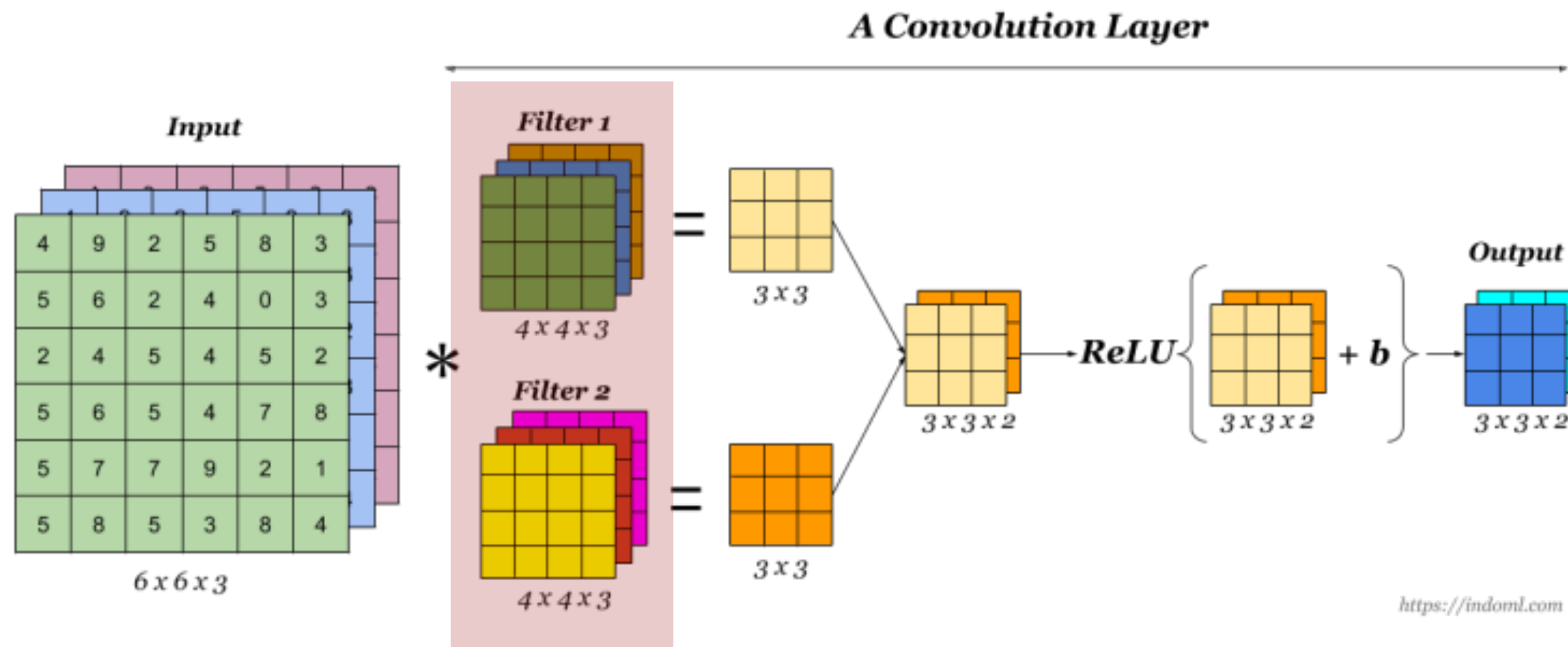


Filters in different channels can be different

Use multiple filters to extract different features

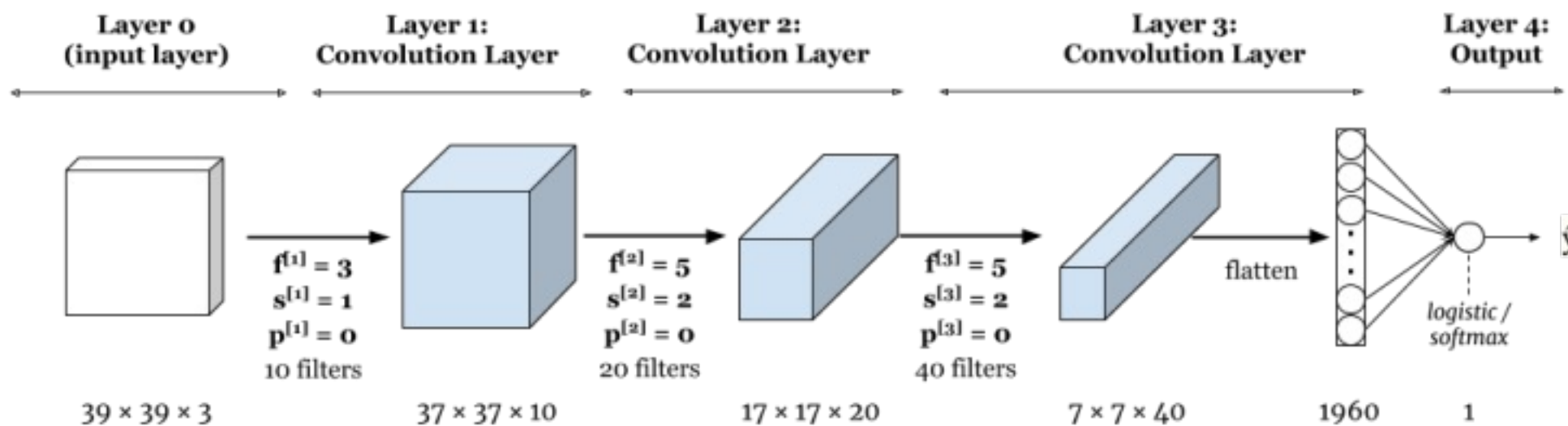


One convolutional layer



Parameters to learn

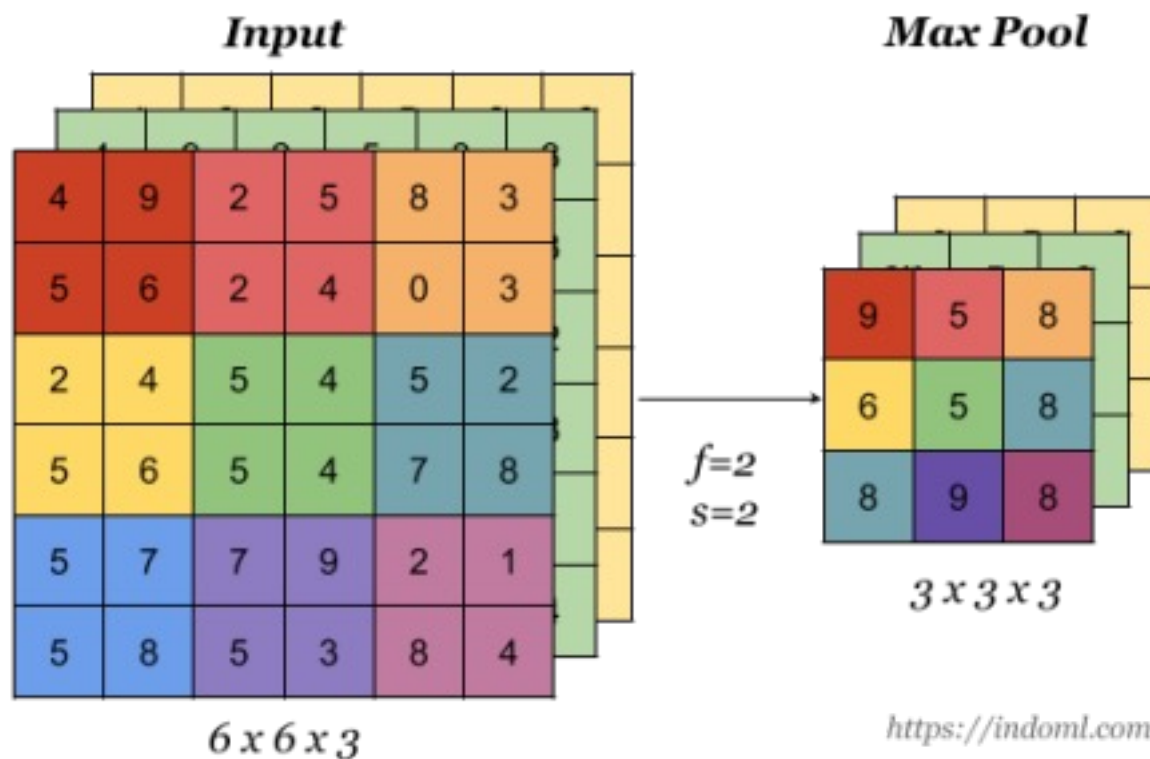
Sample complete network



<https://indoml.com>

Pooling

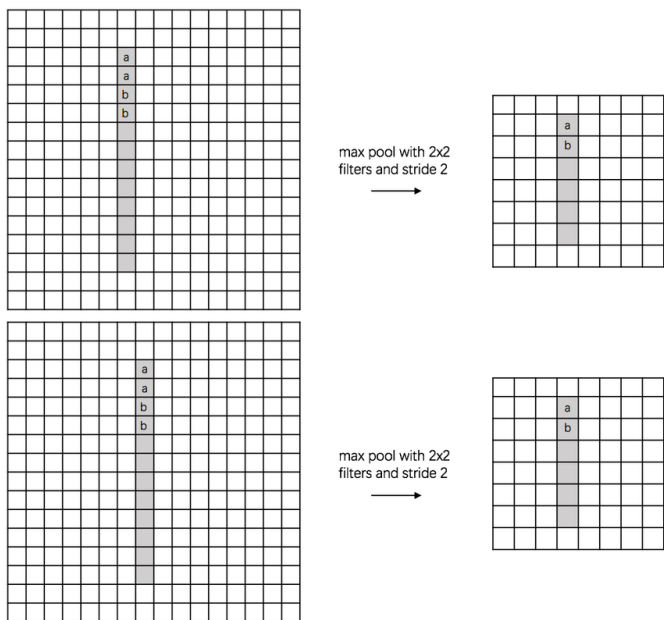
Pooling can reduce the size of representations, speedup calculations, and make feature extraction more robust



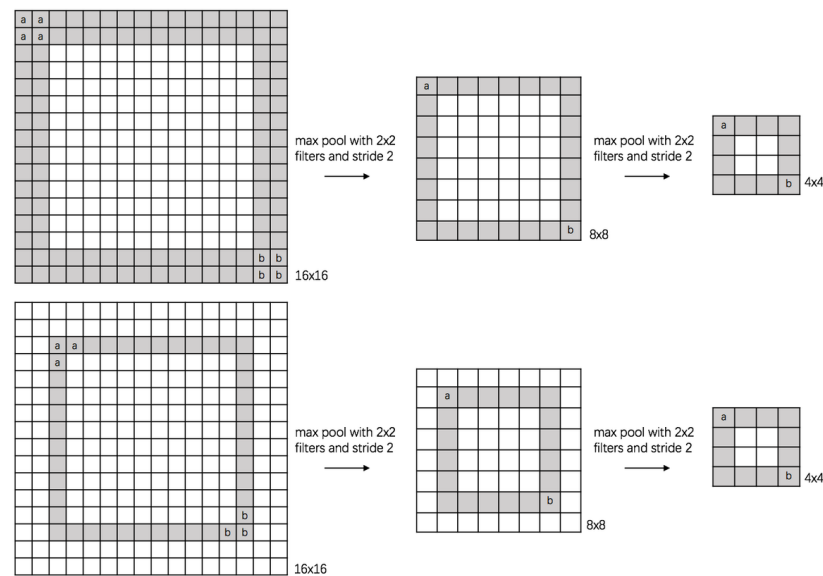
Pooling

Pooling can reduce variance (from 知乎-谢志宁)

<https://www.zhihu.com/question/36686900/answer/130890492>

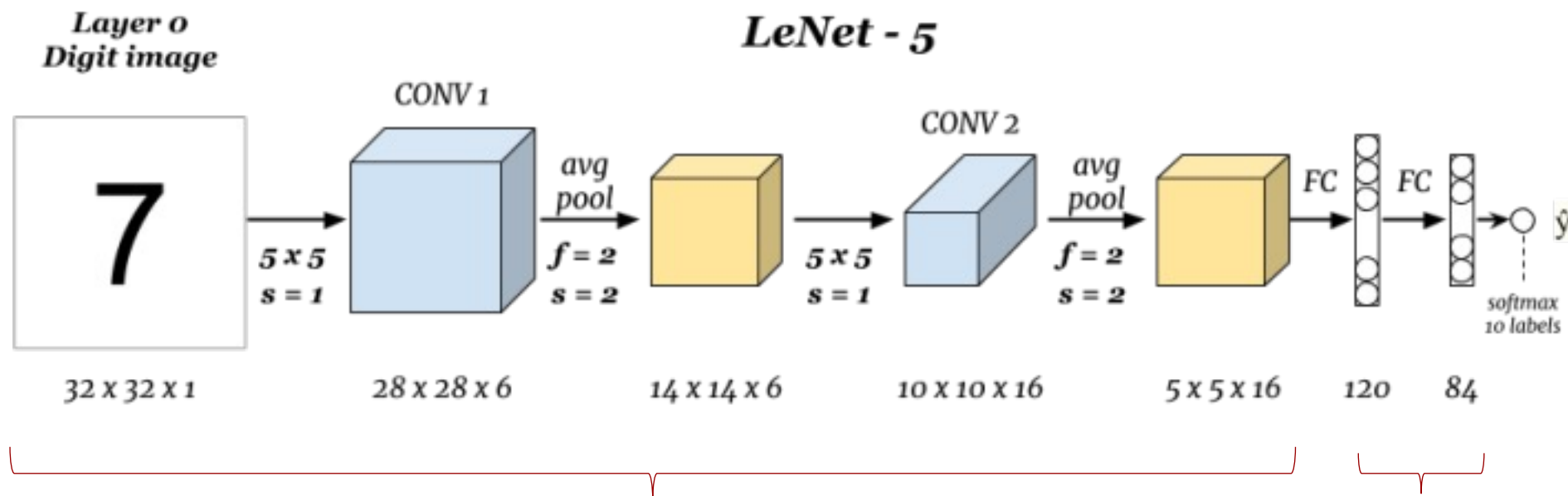


Shift invariance



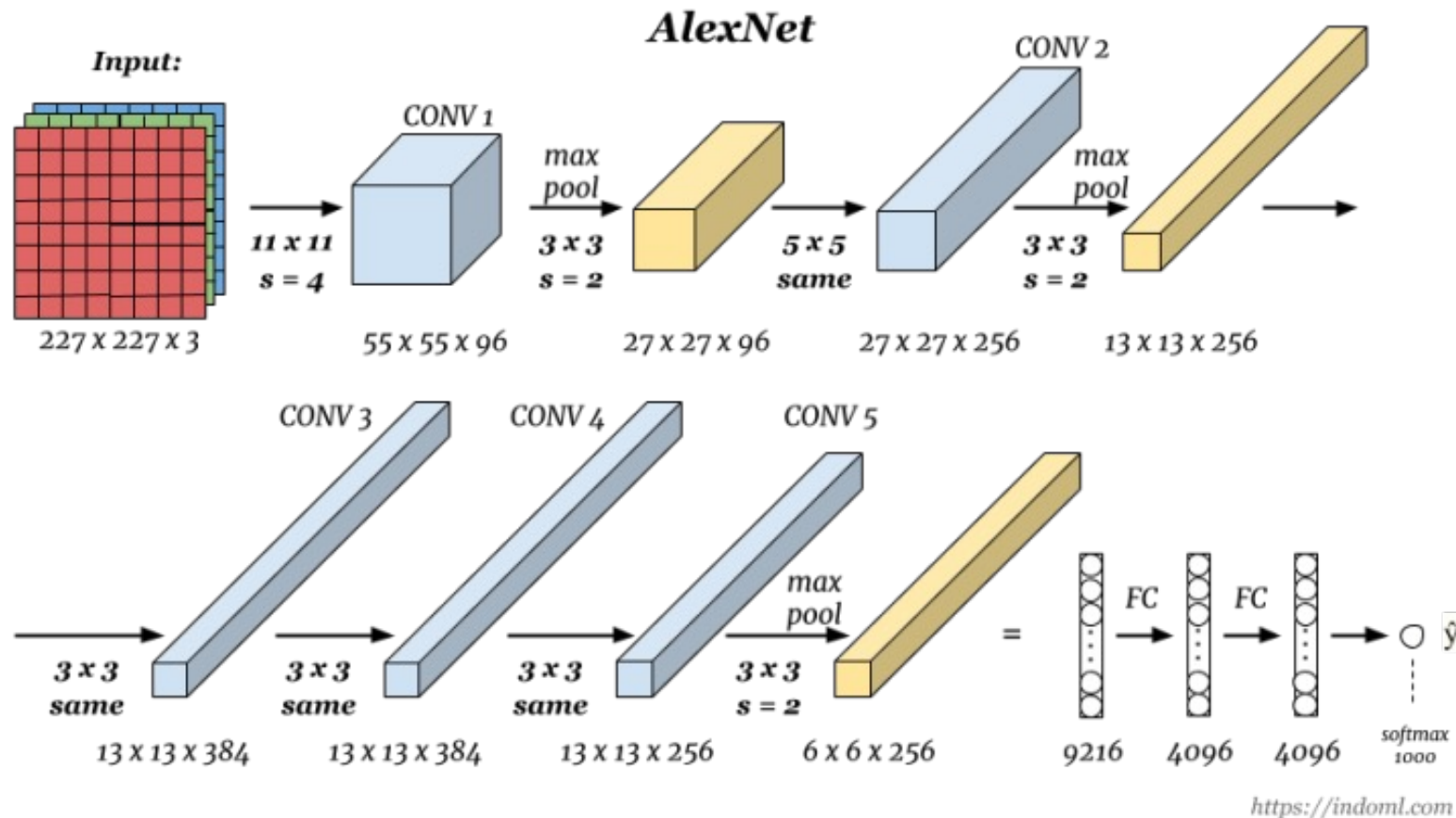
Scale invariance

Well-known architectures: LeNet

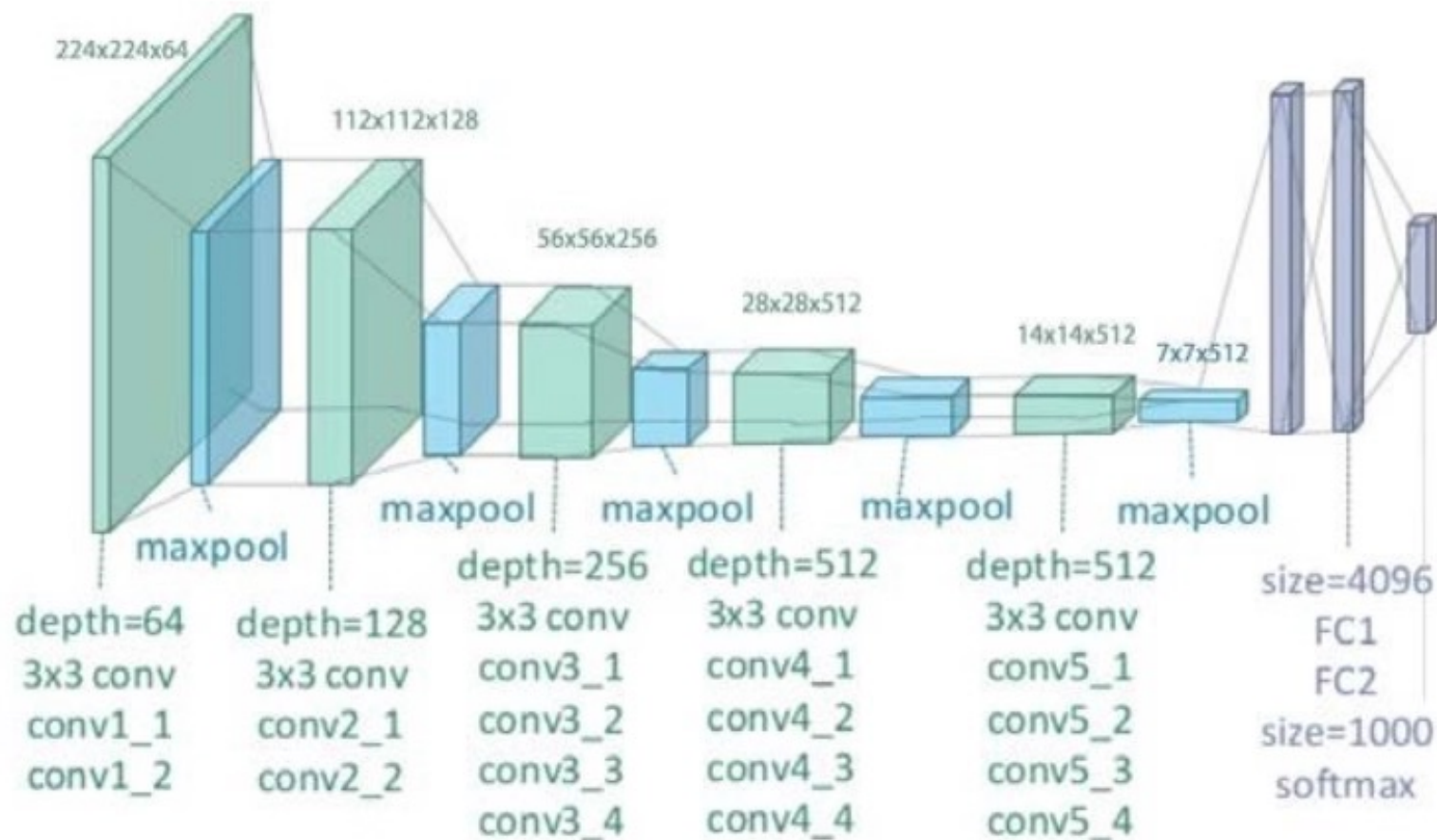


Conv layers only have a few parameters to learn; lightweight **99% weights**

Well-known architectures: AlexNet



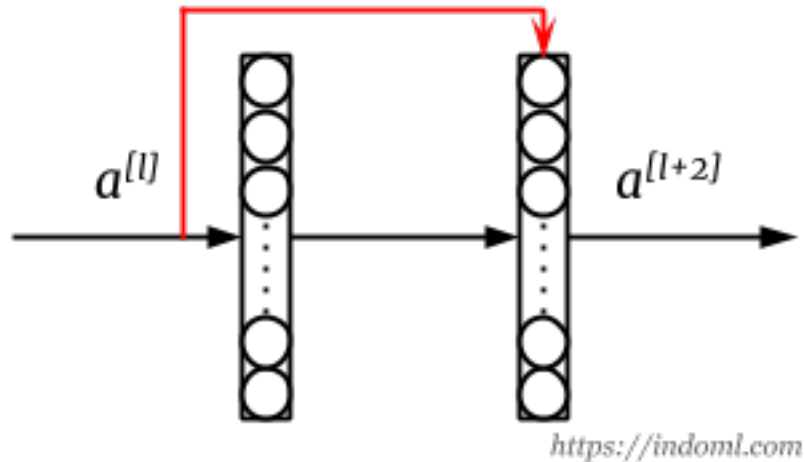
Well-known architectures: VGG



The strength is in the simplicity: the dimension is halved and the depth is increased on every step

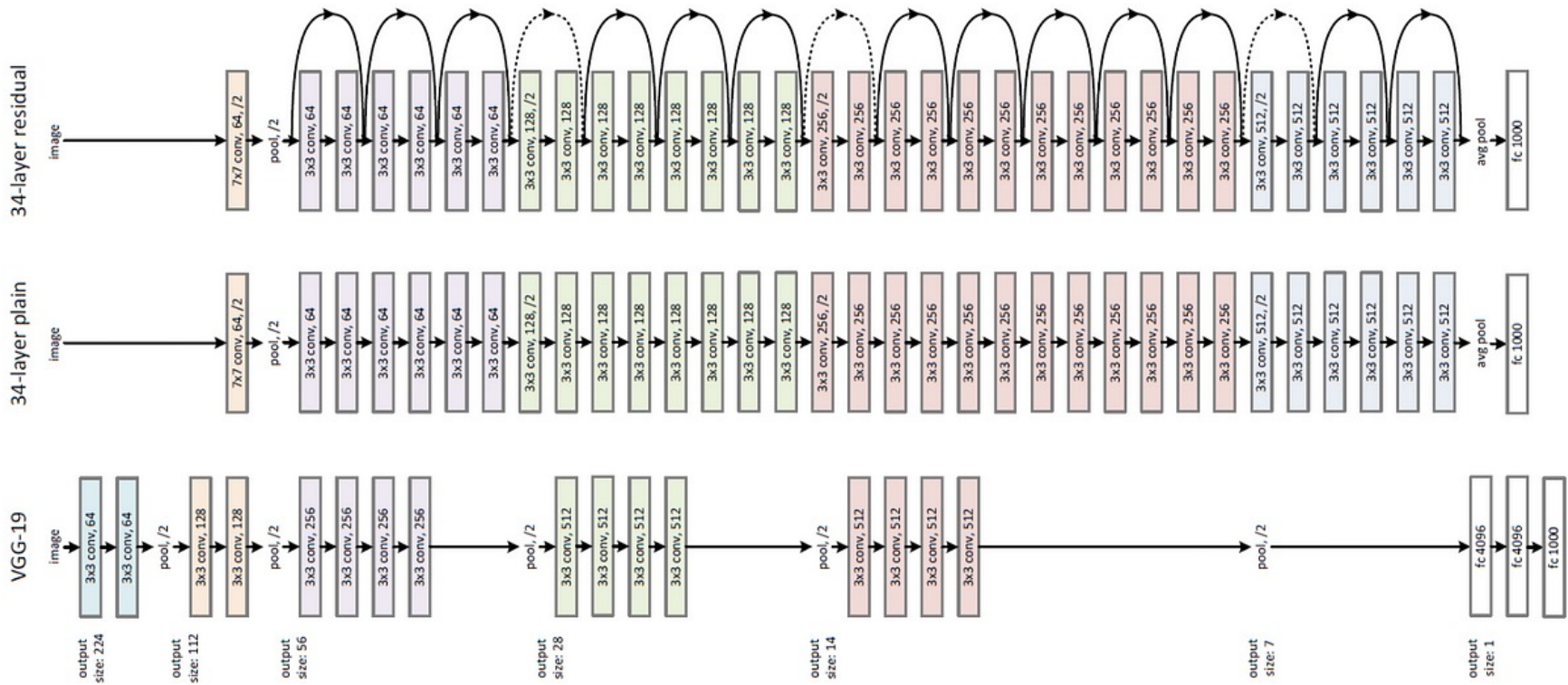
Deeper neural networks are harder to train; gradient vanishing or exploding

Skip connection helps the gradient to back-propagate



$$z^{[l+2]} = W^{[l+2]} a^{[l+1]} + b^{[l+2]}$$

$$a^{[l+2]} = g^{[l+2]}(z^{[l+2]} + a^{[l]})$$



ResNet can train very deep neural networks

[1] Student Notes: Convolutional Neural Networks (CNN) Introduction

<https://indoml.com/2018/03/07/student-notes-convolutional-neural-networks-cnn-introduction/>

[2] Andrew Ng, Convolutional Neural Networks

https://www.bilibili.com/video/BV1BF411w7xQ/?spm_id_from=333.337.search-card.all.click