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Experiment No: 3

Aim - Experiment to implement Strassen's matrix multiplication on 2x2 matrix.

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**Objective:** To understand the running time of Strassen's matrix multiplication

**Theory:**

In linear algebra, the **Strassen algorithm**, named after Volker Strassen, is an algorithm for matrix multiplication. It is faster than the standard matrix multiplication algorithm for large matrices, with a better asymptotic complexity, although the naive algorithm is often better for smaller matrices. The Strassen algorithm is slower than the fastest known algorithm for extremely large matrices, but such galactic matrices are not useful in practice, as they are much slower for matrices of practical size. For small matrices even faster algorithms exist.

Strassen's algorithm works for any [ring](#), such as plus/multiply, but not all [semirings](#), such as [min-plus](#) or [boolean algebra](#), where the naive algorithm still works.

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**Algorithm:**

step 1: Start

step 2: Take 2 matrices as input from user say A and B Step2:

Divide A and B into 10 matrices of n/2 size

$$S[0] = B[0][1] - B[1][1];$$

$$S[1] = A[0][0] + A[0][1];$$

$$S[2] = A[1][0] + A[1][1];$$

$$S[3] = B[1][0] - B[0][0];$$

$$S[4] = A[0][0] + A[1][1];$$

$$S[5] = B[0][0] + B[1][1];$$

$$S[6] = A[0][1] - A[1][1];$$

$$S[7] = B[1][0] + B[1][1];$$

$$S[8] = A[0][0] - A[1][0];$$

$$S[9] = B[0][0] + B[0][1];$$

Step 3: Compute p1 to p7

$$P[0] = A[0][0] * S[0];$$

$$P[1] = B[1][1] * S[1];$$

$$P[2] = B[0][0] * S[2];$$

$P[3] = A[1][1] * S[3];$

$P[4] = S[5] * S[4];$

$P[5] = S[6] * S[7];$

$P[6] = S[8] * S[9];$

Step 4: computer the resultant matrix c:  $C[0][0]$   
=  $P[4] + P[3] - P[1] + P[5]$ ;  $C[0][1] = P[0] + P[1]$ ;  
 $C[1][0] = P[2] + P[3]$ ;  
 $C[1][1] = P[4] + P[0] - P[2] - P[6]$ ;

Step5: display c

Step6: End

## Program:

```
//Strassen multiplication
#include<stdio.h>
#include<time.h>
int main()
{
    int i,j;
    int a[2][2],b[2][2],c[2][2];
    int s[10],p[7];
    clock_t start,end;
    printf("\nEnter matrix A in order - a11, a12, a21, a22 : ");
    for(i=0;i<2;i++)
    {
        for(j=0;j<2;j++)
        {
            scanf("%d",&a[i][j]);
        }
    }
    printf("\nEnter matrix B in order - b11, b12, b21, b22 : ");
    for(i=0;i<2;i++)
    {
        for(j=0;j<2;j++)
        {
            scanf("%d",&b[i][j]);
        }
    }
    start=clock();
    s[0]=b[0][1]-b[1][1];
    s[1]=a[0][0]+a[0][1];
    s[2]=a[1][0]+a[1][1];
    s[3]=b[1][0]-b[0][0];
    s[4]=a[0][0]+a[1][1];
    s[5]=b[0][0]+b[1][1];
    s[6]=a[0][1]-a[1][1];
    s[7]=b[1][0]+b[1][1];
    s[8]=a[0][0]-a[1][0];
    s[9]=b[0][0]+b[0][1];
    printf("\n");
    for(i=0;i<10;i++)
    {
        printf("\nS%d = %d", (i+1),s[i]);
    }
    p[0]=s[0]*a[0][0];
    p[1]=s[1]*b[1][1];
    p[2]=s[2]*b[0][0];
    p[3]=s[3]*a[1][1];
    p[4]=s[4]*s[5];
    p[5]=s[6]*s[7];
    p[6]=s[8]*s[9];
    printf("\n");
    for(i=0;i<7;i++)
    {
```

```
    printf("\nP%d = %d", (i+1), p[i]);
}
c[0][0]=p[4]+p[3]-p[1]+p[5];
c[0][1]=p[0]+p[1];
c[1][0]=p[2]+p[3];
c[1][1]=p[4]+p[0]-p[2]-p[6];
printf("\n\nMatrix A =");
for(i=0;i<2;i++)
{
    printf("\n");
    for(j=0;j<2;j++)
    {
        printf("%d\t", a[i][j]);
    }
}
printf("\n\nMatrix B =");
for(i=0;i<2;i++)
{
    printf("\n");
    for(j=0;j<2;j++)
    {
        printf("%d\t", b[i][j]);
    }
}
printf("\n\nMatrix C =");
for(i=0;i<2;i++)
{
    printf("\n");
    for(j=0;j<2;j++)
    {
        printf("%d\t", c[i][j]);
    }
}
printf("\n");
end=clock();
printf("Time taken = %lf\n", (double) (end-start)/CLOCKS_PER_SEC);
}
```

## Result:

```
kunal@Kunals-MacBook-Air DAA CODE % cd "/Users/kunal/Desktop/DAA CODE/" && g++ Exp3.cpp -o Exp3 && "/Users/kunal/Desktop/DAA CODE/"Exp3

Enter matrix A in order - a11, a12, a21, a22 : 5,6,2,4

Enter matrix B in order - b11, b12, b21, b22 :

S1 = 0
S2 = 5
S3 = 0
S4 = 0
S5 = 5
S6 = 0
S7 = 0
S8 = 0
S9 = 5
S10 = 0

P1 = 0
P2 = 0
P3 = 0
P4 = 0
P5 = 0
P6 = 0
P7 = 0

Matrix A =
5      0
0      0

Matrix B =
0      0
0      0

Matrix C =
0      0
0      0
Time taken = 0.000077
kunal@Kunals-MacBook-Air DAA CODE %
```

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## Conclusion:

In this experiment I learnt that Strassen's matrix multiplication improves the run time a lot when multiplying matrices than traditional matrix multiplication. Also it is very simple to implement but storage complexity is larger.