



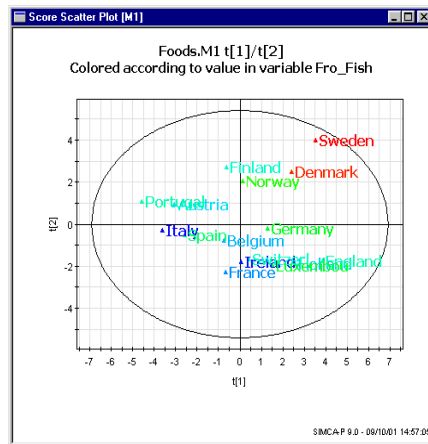
# The OPLS method and recent extensions: -unlocking interpretation in two block modeling and multivariate calibration

**Johan Trygg**

Computational Life Science cluster (CLiC), Umeå University, Sweden  
Group leader, Chemometrics & Bioinformatics Umeå Plant Science Centre  
Co-director WCN Metabolomics platform

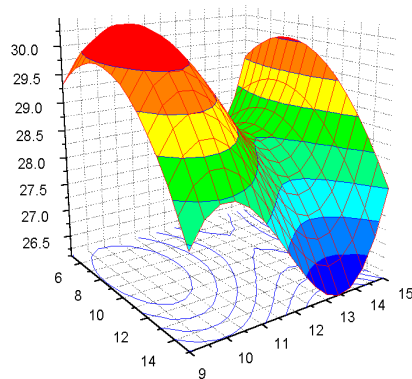
Research group for Chemometrics  
Department of Chemistry, Umeå University, Sweden

# MVA and DoE



- **Multivariate Analysis**

- Extract information from multivariate data sets
- Graphical overview & quantitative modelling
- Large datasets and databases
- Reduces complexity



- **Design of Experiments (DoE)**

- For new experiments and already collected data
- Maximise the information, minimize experiments
- Get causality no correlation
  - What are the important factors?
  - What to Optimise
  - Improve Robustness and Quality



# Umeå University/Chemometrics - Bio-applications

## Disease diagnosis, theranostics

- Autoimmune diseases
- Neurodegenerative diseases.
- Cancer

## Post surgery:

- Kidney transplant

## Nutrition:

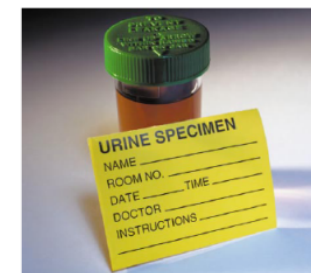
- Functional foods

## Rehabilitation

- Medical imaging of muscle tissue function

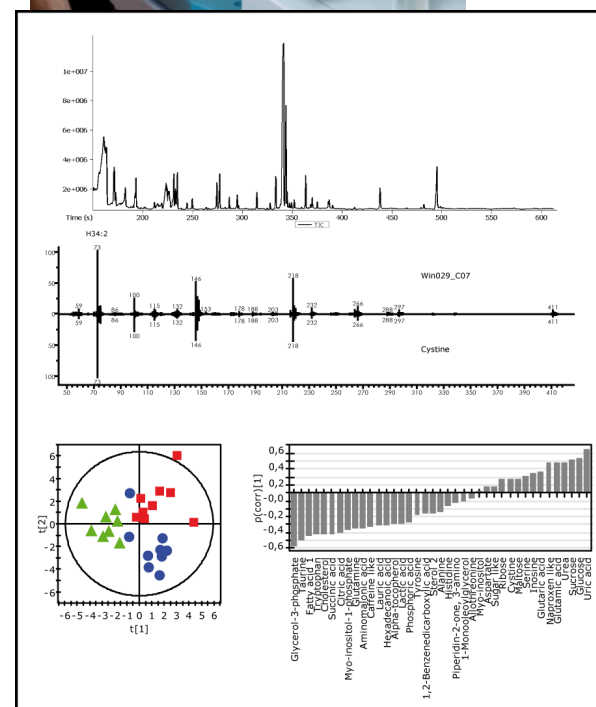


Urine test to monitor kidney-transplant rejection



A urine test that diagnoses acute rejection without the need for an invasive biopsy

Multi-disciplinary collaborations  
Biotech companies, patient  
organizations, leading research  
groups, clinicians, and diagnostics  
companies





# Umeå University/Chemometrics

## - PAT/QbD initiative for process understanding

### Food and Drug Administration (FDA)

Instead go from product testing to *quality by design*!

***Risk minimisation – process understanding***

The FDA's initiative is built on the premise that  
**if manufacturers can demonstrate understanding  
of their processes, less risk** of making bad product.

To control the manufacturing process

**Control = to ensure**

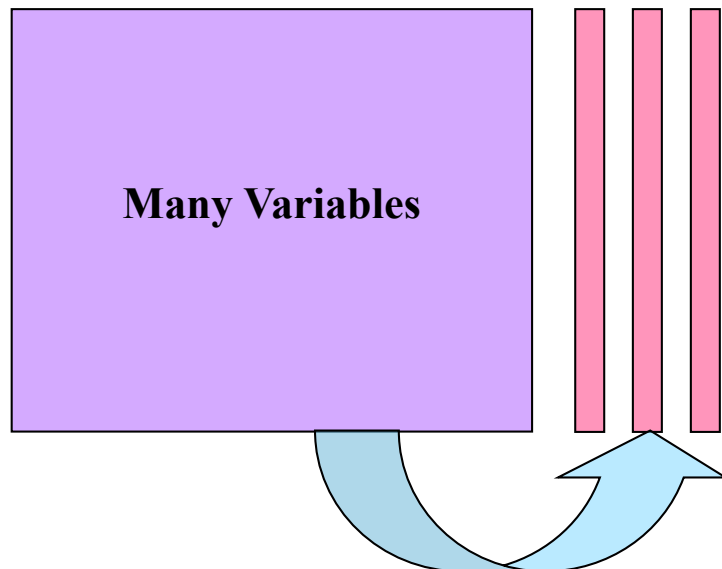
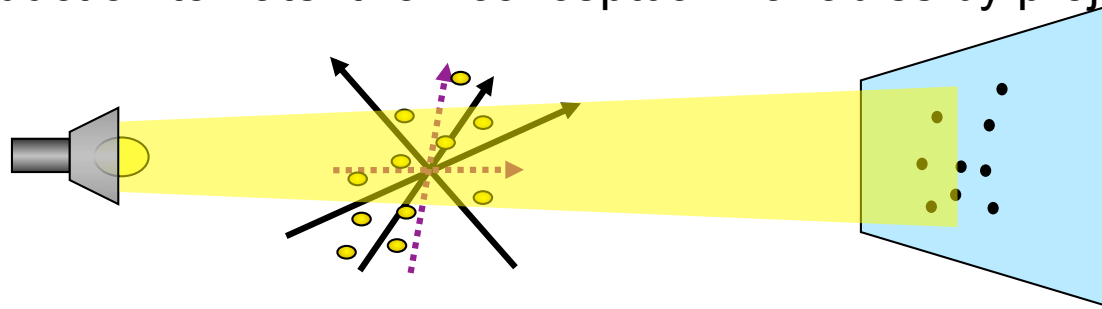
Control  $\neq$  to check



# Multivariate data analysis by means of projection methods

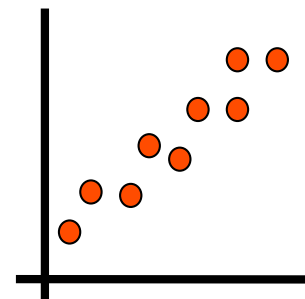
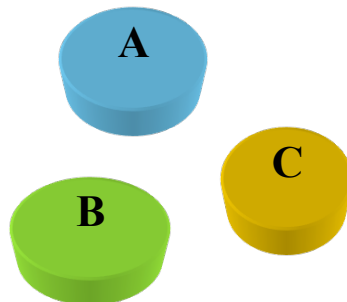
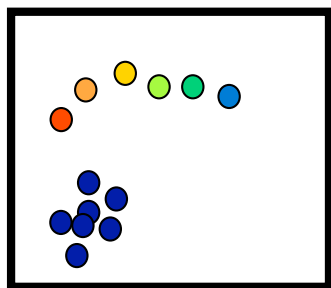
## PRINCIPAL COMPONENT ANALYSIS

- Data reduction to “latent” or “conceptual” variables by projection



- Fewer ‘Latent’ Variables
- Concise summary of the old
  - Finds correlations (=systematic variation)
  - Leaves noise behind (=unsystematic variation)

# 3 Basic Data Analysis Questions



Overview	Classification	Relationship
Process monitoring Chemical Property Maps Selection of drug candidates Encoding proteins and DNA sequences Assessing biological variation Trends in quality Sensory profiling Competitor Analysis Silicon chip manufacture	Classification of raw materials / foodstuffs Wine authenticity Drug Transport & Toxicity Mechanisms Genomics / Proteomics / Metabonomics i.e. Control / Treated Genetic Modification detection	Drug Activity (QSAR) Detergent design New material properties Calibration models Online NIR – moisture/ particle size / actives Sensory information Wheat Quality Process Quality prediction Batch Modelling
<b>PCA</b>	<b>SIMCA / PLS-DA / OPLS-DA</b>	<b>PLS / OPLS / O2PLS</b>



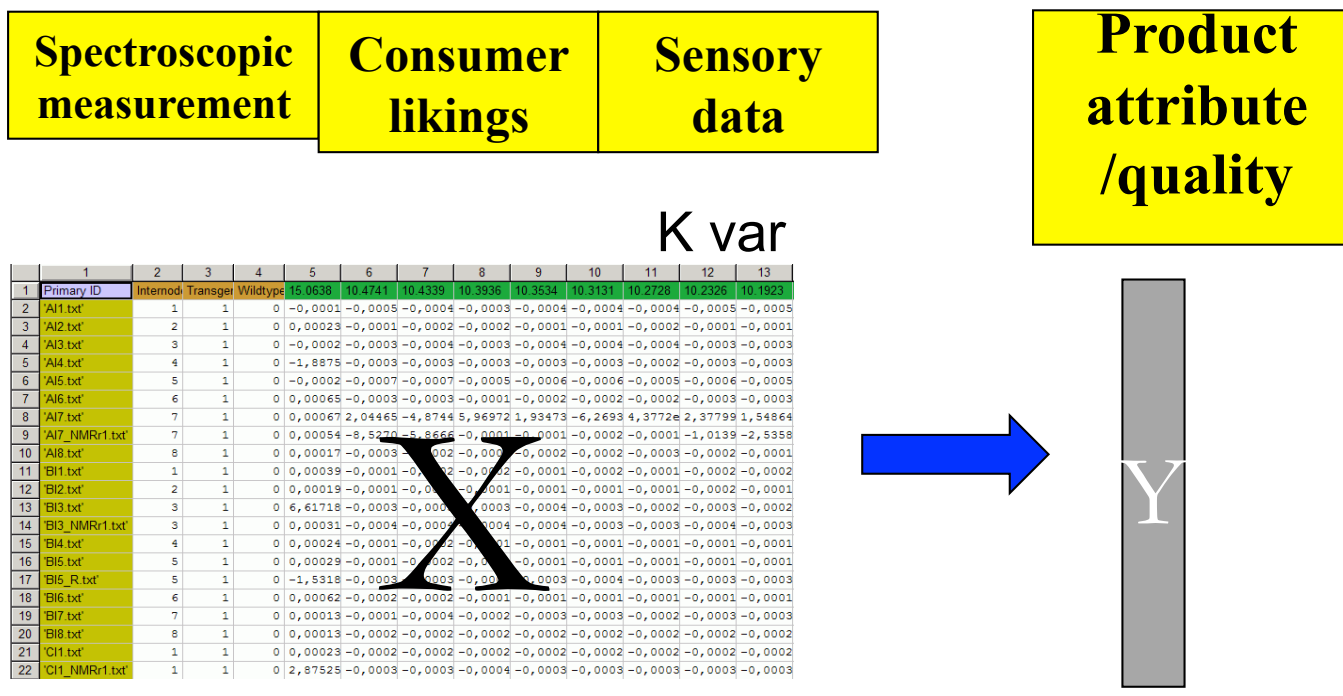
# Model the relation between two blocks of data

## Chemometrics: Multivariate calibration, MC

**Samples  
and sample characterisation**

**provide LOTS of data**

Powders, molecules, industrial process samples, plasma, tissue (leaf), ...  
Spectrometers (NIR,UV, IR, NMR, MS), chromatography, chemical descriptors,  
gene-arrays, metabolites  
highly multidimensional (1000's of variables)





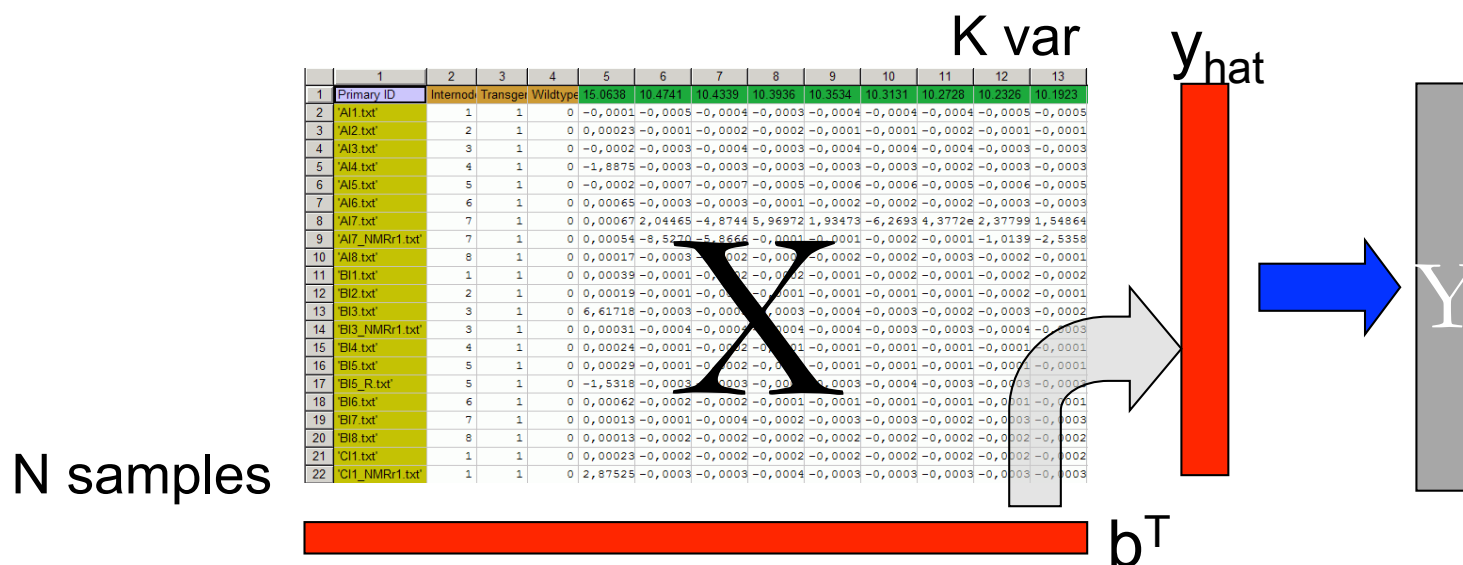
# Model the relation between two blocks of data

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highly multidimensional (1000's of variables)



Linear prediction model:

$$y = Xb + f$$

Objective: Provide good fit to estimate  $y$ , and good predictions for future samples

**Focus:** How to solve for  $b$ ?





# Many different methods to choose from

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## Linear methods

### Full rank methods

- Multiple Linear Regression (MLR)
- Stepwise MLR
- Ridge Regression
- Canonical correlation

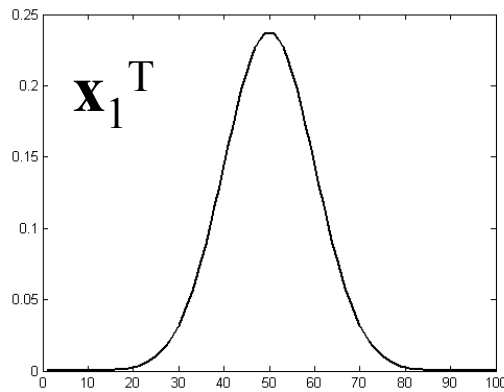
### Latent variable regression (LVR) methods

- Principal Component Regression (PCR)
- **Partial Least Squares (PLS)**
- *Orthogonal Projections to Latent Structures (OPLS)*

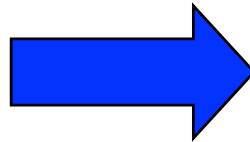
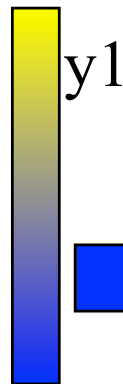
## Non-Linear methods

- Neural Networks (NN)
- Support Vector Machines (SVM)
- Regression trees

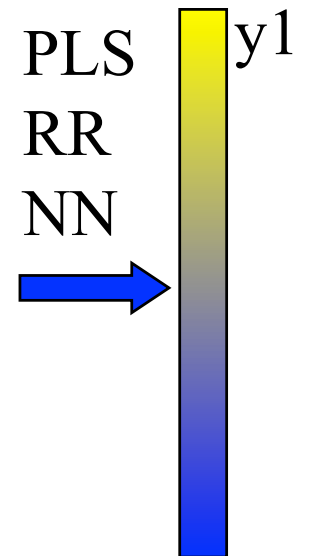
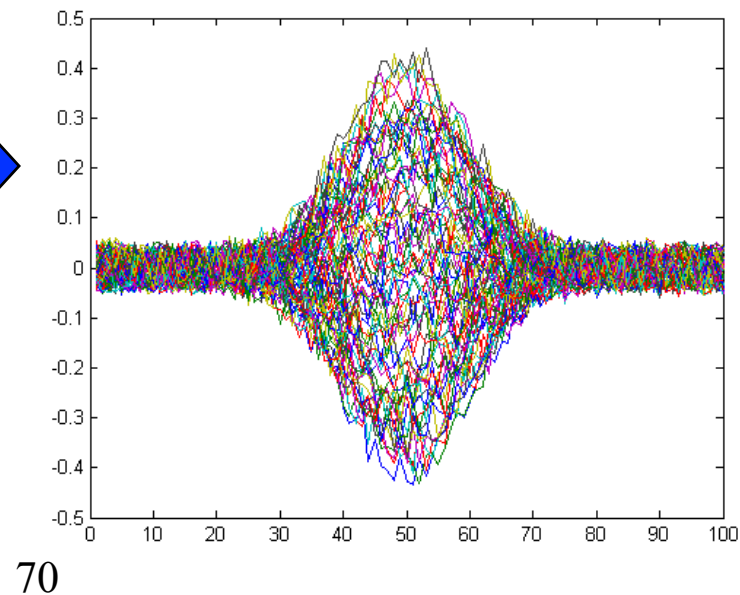
## Example: One component system



Spectral profile of  
Y-predictive component



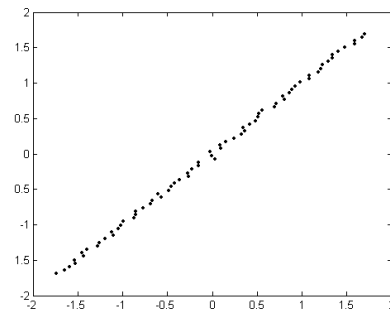
**X matrix**



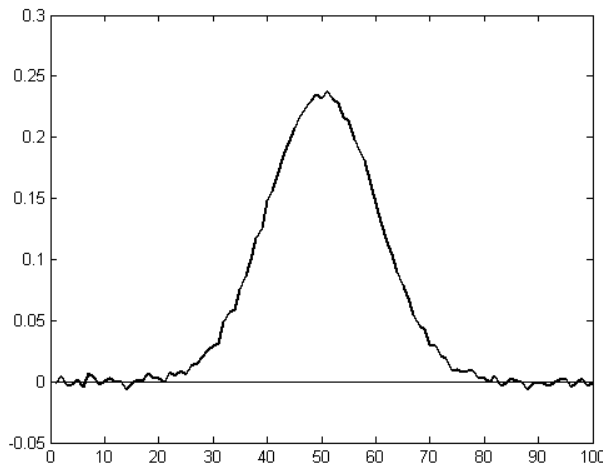
$$\mathbf{X} = \mathbf{y}_1 \mathbf{x}_1^T + \mathbf{E}$$

# Example: One component model

## PLS regression

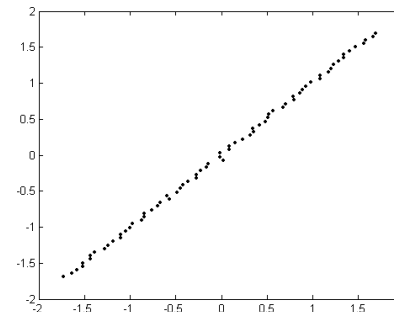


**Observed vs Predicted**

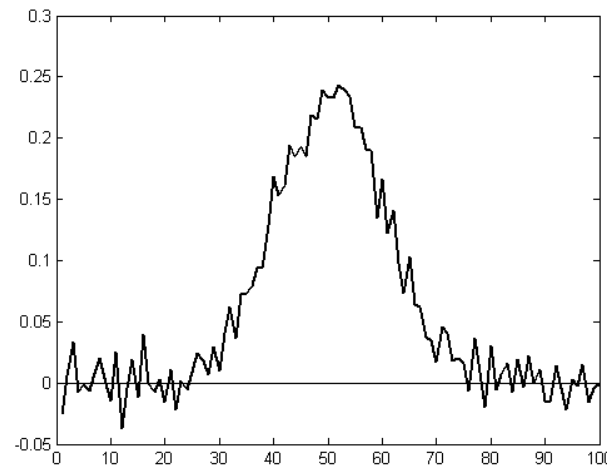


**b coefficients**

## Ridge Regression

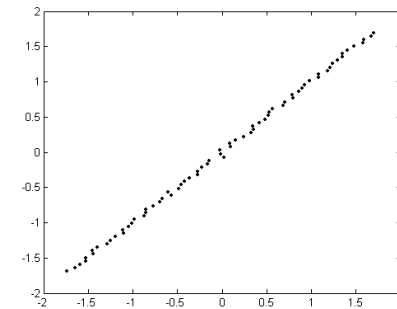


**Observed vs Predicted**

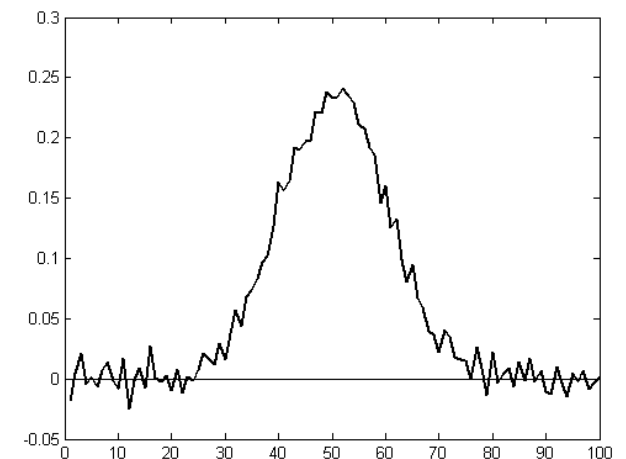


**b coefficients**

## Linear Neural Net



**Observed vs Predicted**



**b coefficients**



## ***Svante Wold's, Harald Martens et al... problem!***

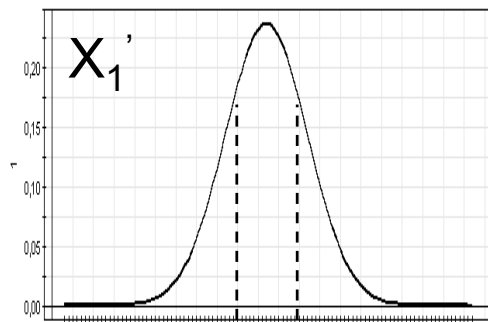
***Sensory/Consumer/Chemical / biological data are complex***

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- **Single PLS component is simply not enough!!**
- **Lots of unknown systematic variation – mostly due to poor knowledge...**
  - strong dietary, environmental, hormonal variations, etc...
  - Experimental variation, sampling, instrumental variation
  - Input material varies with supplier
- **Measured signal is the sum of many contributing factors**
  - Human urine sample (e.g. genetics, diet, gender, age, stress, disease)
  - Pharmaceutical tablet formulation (e.g. binders, fillers, active drug, lubricant)
  - Plant biotech / Pulp & paper (e.g. wood species, cellulose & lignin content, water, age)
  - In QSAR the molecular descriptor profile is a function of its chemical and biological property/activity/function

# Example: Two component system (overlap)

Spectral profile of  
Y-predictive component

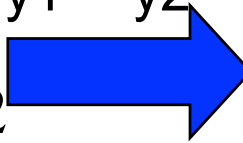


y1



$y_1 \perp y_2$

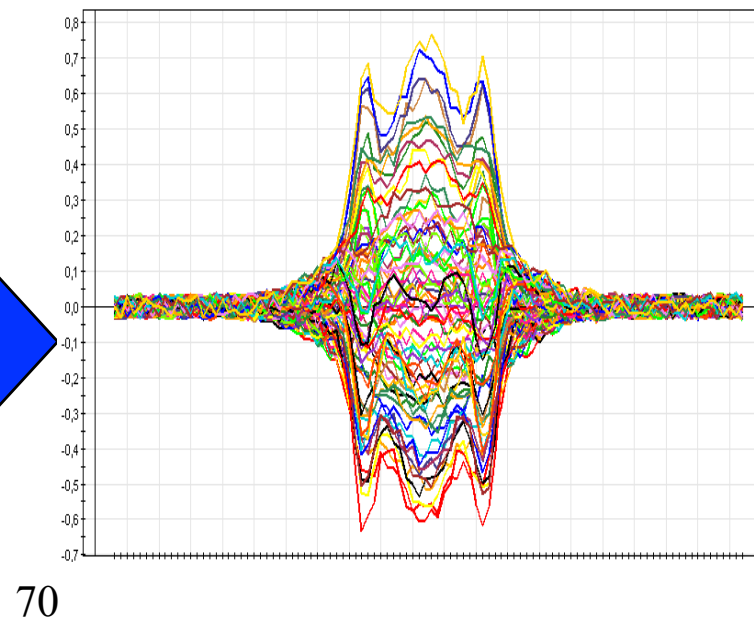
y2



Spectral profile of  
Y-Orthogonal component

X matrix

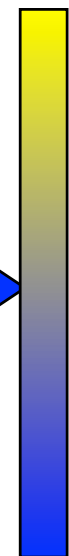
100



PLS



y1



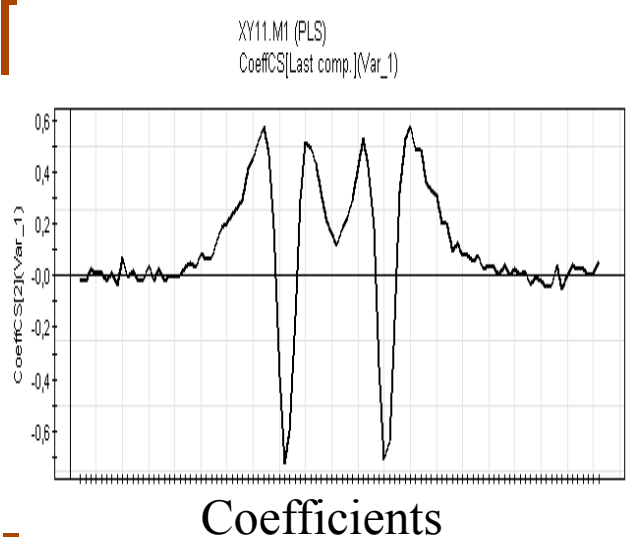
$$\mathbf{X} = \mathbf{y}_1 \mathbf{x}_1' + \mathbf{y}_2 \mathbf{x}_2' + \mathbf{E}$$

Constraint:  $y_1 \perp y_2$

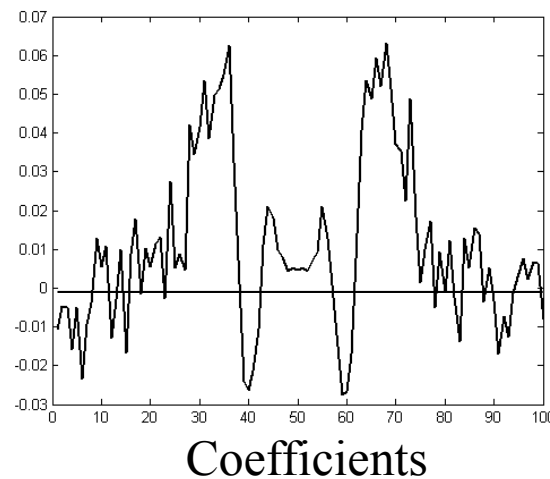
# Example: Two component system (overlap)

## Model interpretation by regression coefficient profile

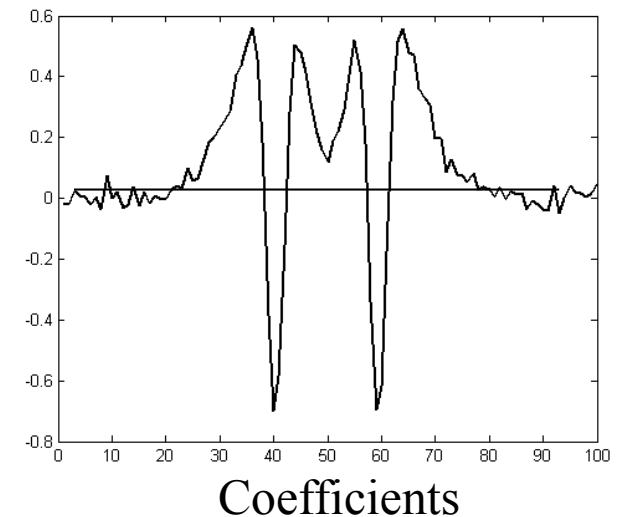
### PLS regression



### Ridge Regression



### Linear Neural Net



Negative dips observed in regression coefficients, but  
we have only positive correlation in the data?  
→ Disturbance is due to Y-Orthogonal variation

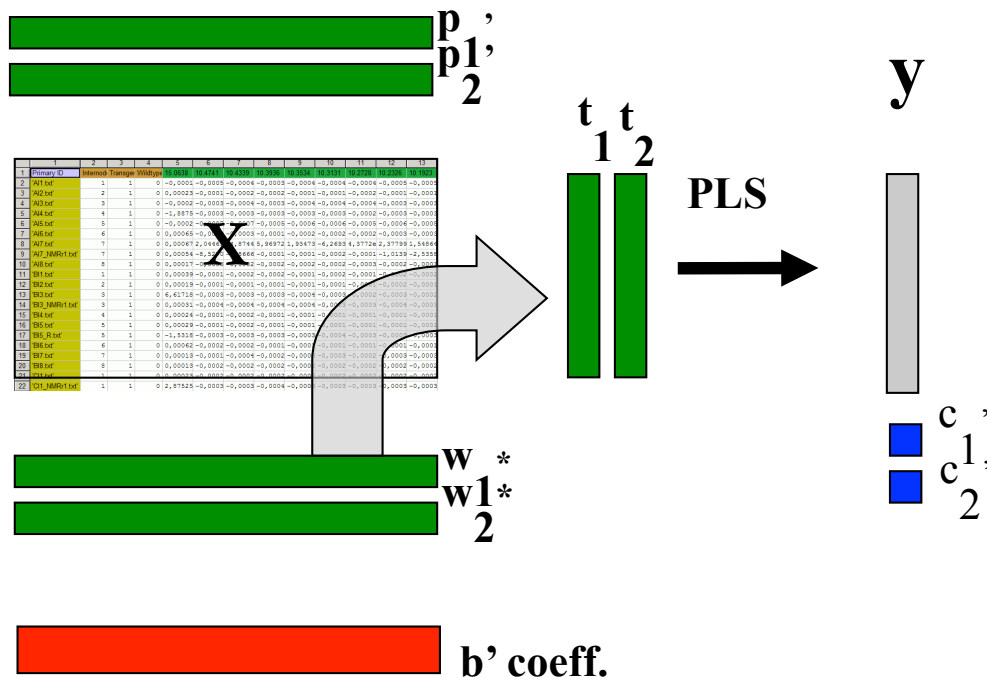


# Wold, Martens and colleagues PLS NIPALS (1982)

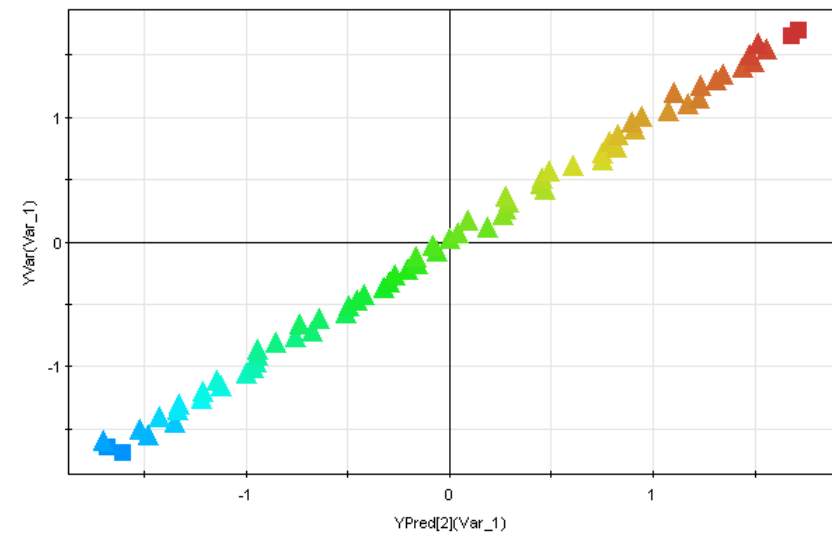
$$\mathbf{X} = \mathbf{T}\mathbf{P}' + \mathbf{E}$$

$$\mathbf{y} = \mathbf{T}\mathbf{c}' + \mathbf{f}$$

**Ability to handle unknown variation in X**  
- Success story of PLS and chemometrics



**Observed vs Predicted**

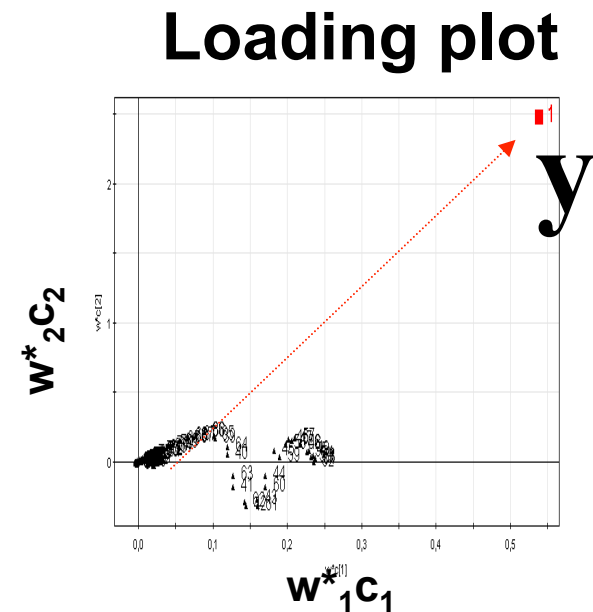
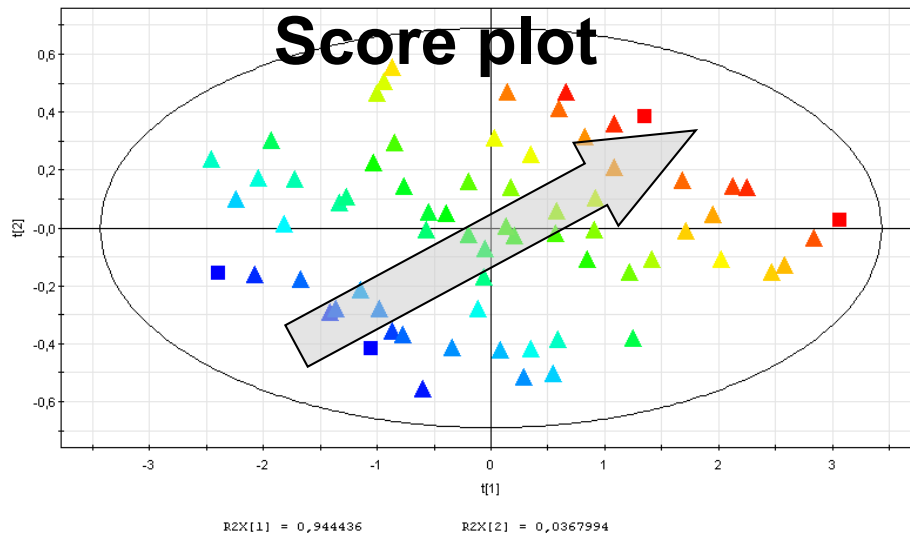


RMSEE = 0,0500342



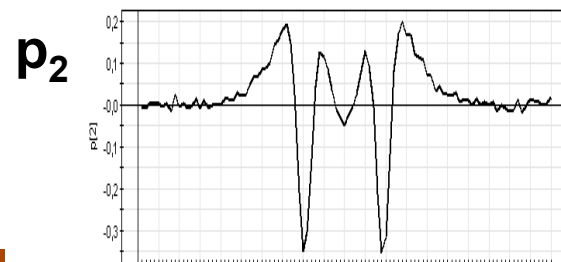
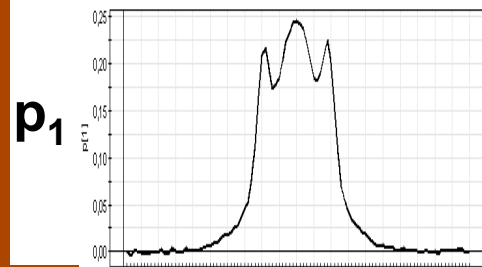
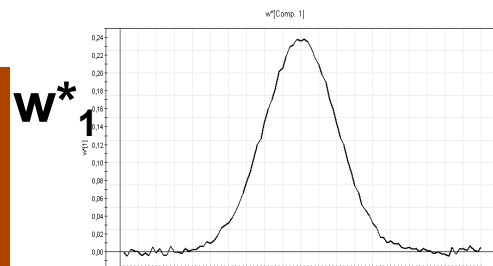
# What about interpretation of PLS model

Example: Single-Y, two component system

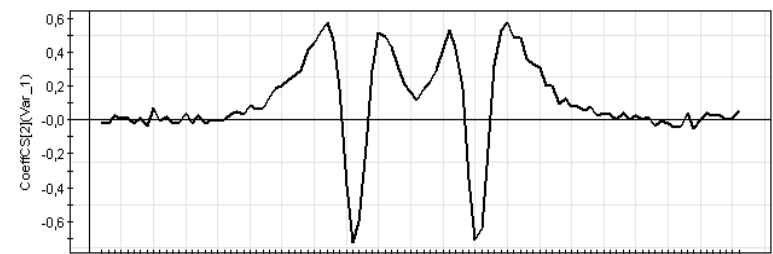


**$R^2X_{comp1}=94\%$  variation**

**$R^2X_{comp2}= 3.7\%$  variation**



**Regression coefficients, b**



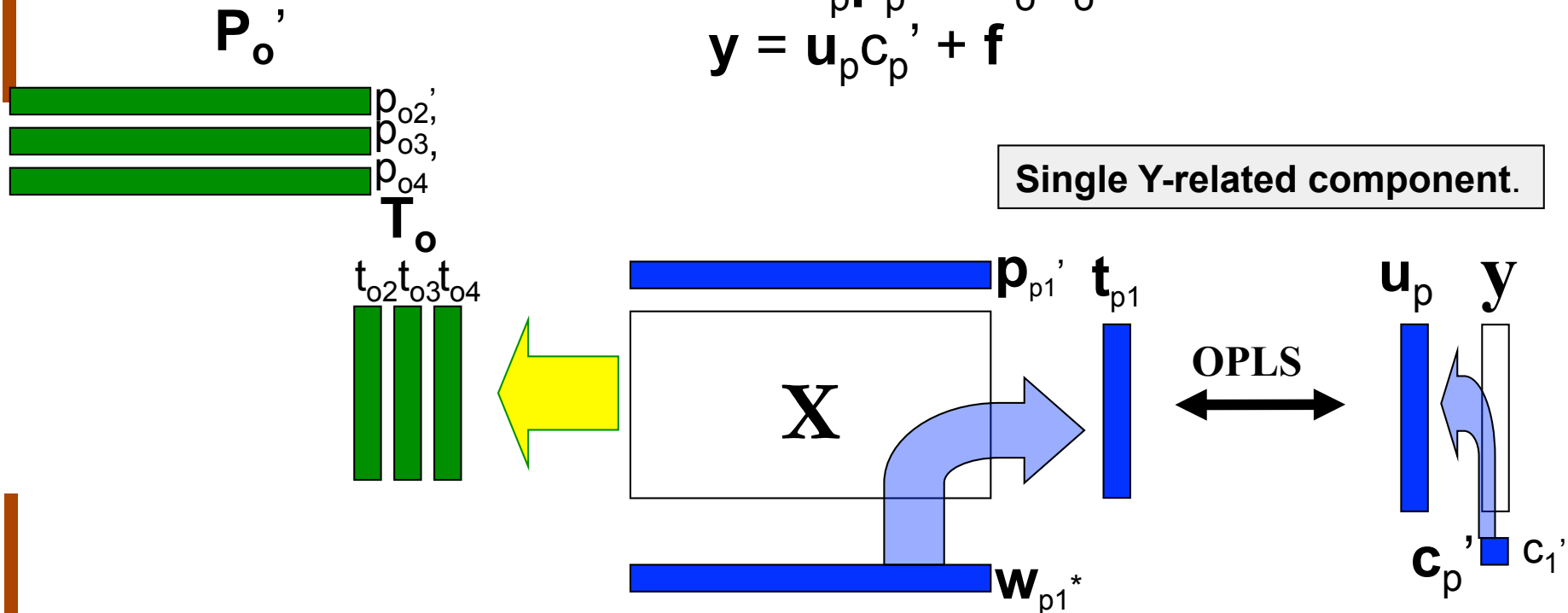


# OPLS method -Trygg & Wold (2002)

Trygg J, Wold S. J. Chemometr., 2002; **16**: 119-128

$$\mathbf{X} = \mathbf{t}_p \mathbf{p}_p' + \mathbf{T}_o \mathbf{P}_o' + \mathbf{E}$$

$$\mathbf{y} = \mathbf{u}_p \mathbf{c}_p' + \mathbf{f}$$





# The concept of Orthogonal variation

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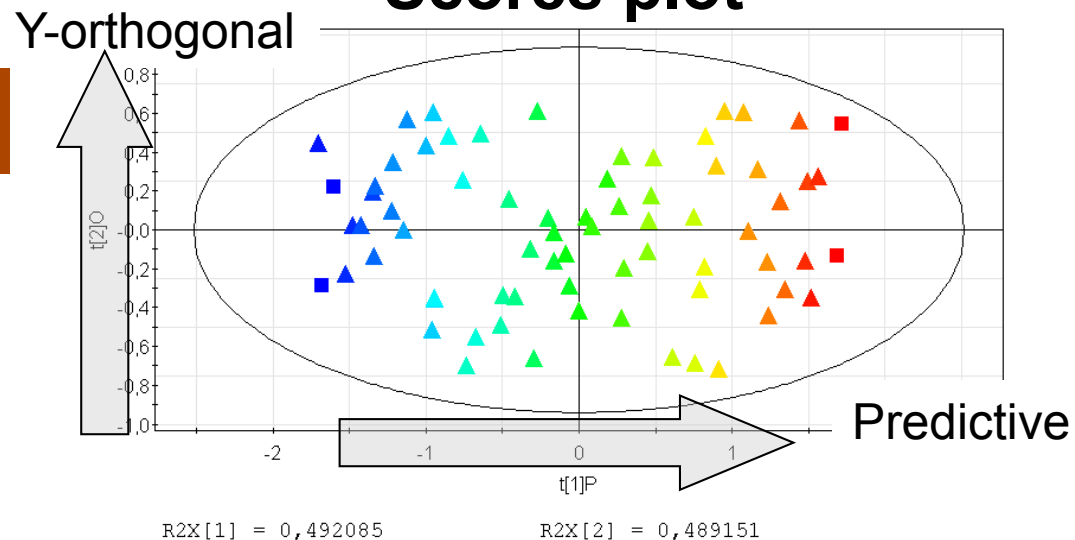
- Not all systematic variation in the X-block is related to the Y-block
- The new 'O'-methods, OPLS and O2PLS, are able to divide the systematic X-variation in two parts:
  - What in X is related to Y;                      Y-predictive variation
  - What in X is not related to Y;                      Y-orthogonal variation
- This Y-orthogonal variation is important information for the total understanding of the studied system or process
  - Gender
  - Drift
  - Unknown interferents
  - Sampling / Experimental problems
  - Non-linearities
  - Within class variation



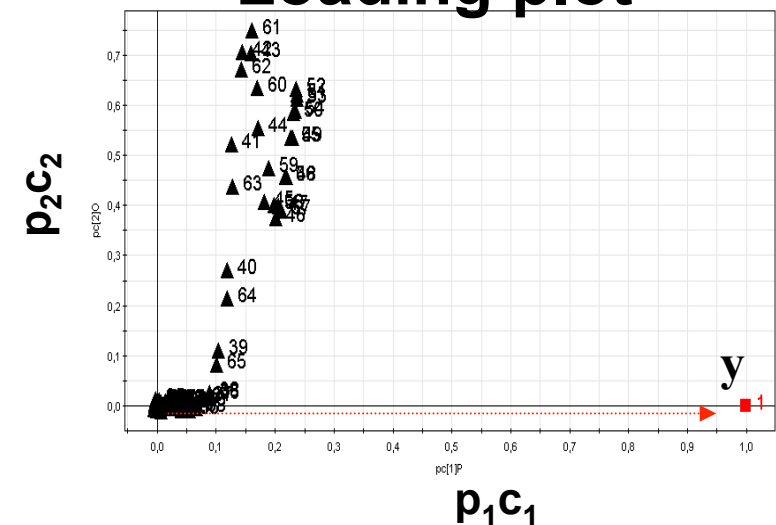
# OPLS model

Example: Single-Y, two component system

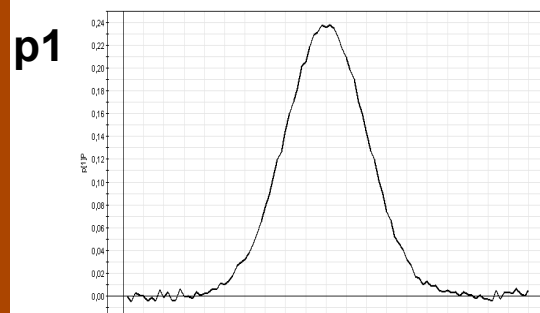
## Scores plot



## Loading plot

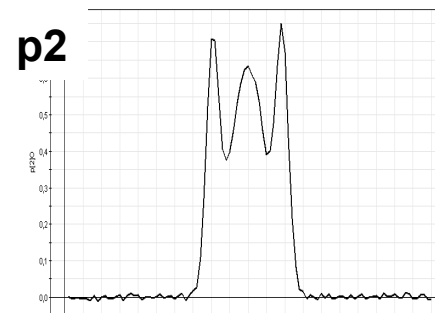


49% variation

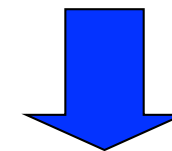


Predictive profile

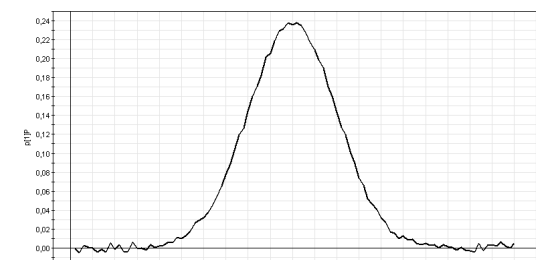
49% variation



Y-orthogonal profile



Predictive profile





## Some theoretical properties of OPLS

### Objective function:

Find  $\mathbf{t}_0$  that maximizes  
overlap with predictive score matrix  $\mathbf{T}$

$$\max(\mathbf{T}^T \mathbf{t}_{\text{osc}})^2 = \max(\mathbf{T}^T \mathbf{X} \mathbf{w}_{\text{osc}})^2$$

$$\|\mathbf{w}_{\text{osc}}\| = 1, \quad \mathbf{Y}^T \mathbf{t}_{\text{osc}} = 0$$

**Solution**  
(PLS principle)

$$\text{PCA}(\mathbf{Y}^T \mathbf{X}) = \mathbf{C} \mathbf{W}^T$$

$$\mathbf{E}_{\text{XY}} = \mathbf{X} - \mathbf{T} \mathbf{W}^T \quad \text{where } \mathbf{T} = \mathbf{X} \mathbf{W}$$

$$(\mathbf{E}_{\text{XY}}^T \mathbf{T} \mathbf{T}^T \mathbf{E}_{\text{XY}}) \mathbf{w}_{\text{osc}} = \lambda \mathbf{w}_{\text{osc}}$$



# Benefits of OPLS modeling

- ✓ **Model diagnostics:**
  - $R^2(XY)$ : How much variation in X is correlated to Y, and vice versa?
  - $R^2(X_{y0})$ : How much is not correlated to Y? (to X?)
- ✓ **Model interpretation**
  - More focussed components (plots) & easier interpretation
    - Predictive components ( $\mathbf{T}_p \mathbf{P}_p^T$ )
    - Y-orthogonal components ( $\mathbf{T}_o \mathbf{P}_o^T$ )
  - Pure profile estimation
- ✓ **Model (prediction ):**
  - Understand & correct for faults/mistakes found in Y-orthogonal components
  - e.g. experimental, sampling
- **Multi-block modeling ( $X \leftrightarrow Y$ )**
  - Integrate, compare and filter multiple data tables



# Preference mapping

understanding the descriptive sensory attributes  
that relate to consumer preferences

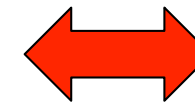
**Product attributes /  
Sensory attributes**

**consumer  
likings**

K var

M var

Two block model



Y

**Products**

**N samples**

	1	2	3	4	5	6	7	8	9	10	11	12	13
1	Primary ID	Intermod	Transgei	Wildtype	15.0638	10.4741	10.4339	10.3936	10.3534	10.3131	10.2728	10.2326	10.1923
2	'AI1.txt'	1	1	0	-0,0001	-0,0005	-0,0004	-0,0003	-0,0004	-0,0004	-0,0004	-0,0005	-0,0005
3	'AI2.txt'	2	1	0	0,00023	-0,0001	-0,0002	-0,0002	-0,0001	-0,0001	-0,0002	-0,0001	-0,0001
4	'AI3.txt'	3	1	0	-0,0002	-0,0003	-0,0004	-0,0003	-0,0004	-0,0004	-0,0004	-0,0003	-0,0003
5	'AI4.txt'	4	1	0	-1,8875	-0,0003	-0,0003	-0,0003	-0,0003	-0,0003	-0,0002	-0,0003	-0,0003
6	'AI5.txt'	5	1	0	-0,0002	-0,0007	-0,0007	-0,0005	-0,0006	-0,0006	-0,0005	-0,0006	-0,0005
7	'AI6.txt'	6	1	0	0,00065	-0,0003	-0,0003	-0,0001	-0,0002	-0,0002	-0,0002	-0,0003	-0,0003
8	'AI7.txt'	7	1	0	0,00067	2,04465	-4,8744	5,96972	1,93473	-6,2693	4,3772e	2,37799	1,54864
9	'AI7_NMRr1.txt'	7	1	0	0,00054	-8,5270	-5,8666	-0,0001	-0,0001	-0,0002	-0,0001	-1,0139	-2,5358
10	'AI8.txt'	8	1	0	0,00017	-0,0003	-0,0002	-0,0001	-0,0002	-0,0002	-0,0003	-0,0002	-0,0001
11	'BI1.txt'	1	1	0	0,00039	-0,0001	-0,0002	-0,0002	-0,0001	-0,0002	-0,0001	-0,0002	-0,0002
12	'BI2.txt'	2	1	0	0,00019	-0,0001	-0,0001	-0,0001	-0,0001	-0,0001	-0,0001	-0,0002	-0,0001
13	'BI3.txt'	3	1	0	6,61718	-0,0003	-0,0003	-0,0003	-0,0004	-0,0003	-0,0002	-0,0003	-0,0002
14	'BI3_NMRr1.txt'	3	1	0	0,00031	-0,0004	-0,0003	-0,0004	-0,0004	-0,0003	-0,0003	-0,0004	-0,0003
15	'BI4.txt'	4	1	0	0,00024	-0,0001	-0,0002	-0,0001	-0,0001	-0,0001	-0,0001	-0,0001	-0,0001
16	'BI5.txt'	5	1	0	0,00029	-0,0001	-0,0002	-0,0001	-0,0001	-0,0001	-0,0001	-0,0001	-0,0001
17	'BI5_R.txt'	5	1	0	-1,5318	-0,0003	-0,0003	-0,0003	-0,0003	-0,0004	-0,0003	-0,0003	-0,0003
18	'BI6.txt'	6	1	0	0,00062	-0,0002	-0,0002	-0,0001	-0,0001	-0,0001	-0,0001	-0,0001	-0,0001
19	'BI7.txt'	7	1	0	0,00013	-0,0001	-0,0004	-0,0002	-0,0003	-0,0003	-0,0002	-0,0003	-0,0003
20	'BI8.txt'	8	1	0	0,00013	-0,0002	-0,0002	-0,0002	-0,0002	-0,0002	-0,0002	-0,0002	-0,0002
21	'CI1.txt'	1	1	0	0,00023	-0,0002	-0,0002	-0,0002	-0,0002	-0,0002	-0,0002	-0,0002	-0,0002
22	'CI1_NMRr1.txt'	1	1	0	2,87525	-0,0003	-0,0003	-0,0004	-0,0003	-0,0003	-0,0003	-0,0003	-0,0003

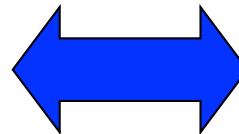
# Multi-block modeling

- Similar to multivariate calibration ( $X \rightarrow Y$ ), but extended to *both directions*
- Compare & Integrate  $X$  and  $Y$  in terms of....
  - Experimental conditions, Process step, Time (drift), Instruments, Replication, Pre-treatments, and so on...
- Understand...
  - Overlap? What is jointly related?
  - What is unique for  $X$ , for  $Y$ ?

**Product attributes /  
Sensory attributes**

**consumer  
likings**

	1	2	3	4	5	6	7	8	9	10	11	12	13
Primary ID	Internod	Transge	Wildtype	15.0636	10.4741	10.4339	10.3936	10.3534	10.3131	10.2728	10.2326	10.1923	
A11.txt	1	1	0	-0.0001	-0.0005	-0.0004	-0.0003	-0.0004	-0.0004	-0.0004	-0.0005	-0.0005	
A12.txt	2	1	0	0.00023	-0.0001	-0.0002	-0.0002	-0.0001	-0.0001	-0.0002	-0.0001	-0.0001	
A13.txt	3	1	0	-0.0002	-0.0003	-0.0004	-0.0003	-0.0004	-0.0004	-0.0004	-0.0003	-0.0003	
A14.txt	4	1	0	-1.8875	-0.0003	-0.0003	-0.0003	-0.0003	-0.0003	-0.0002	-0.0003	-0.0003	
A15.txt	5	1	0	-0.0002	-0.0007	-0.0007	-0.0005	-0.0006	-0.0006	-0.0005	-0.0006	-0.0005	
A16.txt	6	1	0	0.00065	-0.0003	-0.0003	-0.0002	-0.0002	-0.0002	-0.0002	-0.0003	-0.0003	
A17.txt	7	1	0	0.00067	2.04465	-4.8744	5.0772	1.93473	-6.2693	4.37726	2.37799	1.54864	
A17_NMR1.txt	7	1	0	0.00054	-8.5270	-5.8666	-0.0001	-0.0001	-0.0001	-0.0001	-1.0139	-2.5359	
A18.txt	8	1	0	0.00017	-0.0003	-0.0002	-0.0002	-0.0002	-0.0002	-0.0003	-0.0002	-0.0001	
B11.txt	1	1	0	0.00039	-0.0001	-0.0002	-0.0002	-0.0001	-0.0002	-0.0001	-0.0002	-0.0002	
B12.txt	2	1	0	0.00019	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	-0.0002	-0.0001	
B13.txt	3	1	0	6.41718	-0.0003	-0.0003	-0.0003	-0.0004	-0.0003	-0.0002	-0.0003	-0.0002	
B13_NMR1.txt	3	1	0	0.00031	-0.0004	-0.0004	-0.0004	-0.0004	-0.0003	-0.0003	-0.0004	-0.0003	
B14.txt	4	1	0	0.00024	-0.0001	-0.0002	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	
B15.txt	5	1	0	0.00028	-0.0001	-0.0002	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	
B15_R.txt	5	1	0	-1.5318	-0.0003	-0.0003	-0.0003	-0.0003	-0.0004	-0.0003	-0.0003	-0.0003	
B16.txt	6	1	0	0.00062	-0.0002	-0.0002	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	
B17.txt	7	1	0	0.00013	-0.0001	-0.0004	-0.0002	-0.0003	-0.0003	-0.0002	-0.0003	-0.0003	
B18.txt	8	1	0	0.00013	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	
C11.txt	1	1	0	0.00023	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	
C11_NMR1.txt	1	1	0	2.87525	-0.0003	-0.0003	-0.0004	-0.0003	-0.0003	-0.0003	-0.0003	-0.0003	



	1	2	3	4	5	6	7	8	9	10	11	12	13
Primary ID	Internod	Transge	Wildtype	15.0636	10.4741	10.4339	10.3936	10.3534	10.3131	10.2728	10.2326	10.1923	
A11.txt	1	1	0	-0.0001	-0.0005	-0.0004	-0.0003	-0.0004	-0.0004	-0.0004	-0.0005	-0.0005	
A12.txt	2	1	0	0.00023	-0.0001	-0.0002	-0.0002	-0.0001	-0.0001	-0.0002	-0.0001	-0.0001	
A13.txt	3	1	0	-0.0002	-0.0003	-0.0004	-0.0003	-0.0004	-0.0004	-0.0004	-0.0003	-0.0003	
A14.txt	4	1	0	-1.8875	-0.0003	-0.0003	-0.0003	-0.0003	-0.0003	-0.0002	-0.0003	-0.0003	
A15.txt	5	1	0	-0.0002	-0.0007	-0.0007	-0.0005	-0.0006	-0.0006	-0.0005	-0.0006	-0.0005	
A16.txt	6	1	0	0.00065	-0.0003	-0.0003	-0.0002	-0.0002	-0.0002	-0.0002	-0.0003	-0.0003	
A17.txt	7	1	0	0.00067	2.04465	-4.8744	5.0772	1.93473	-6.2693	4.37726	2.37799	1.54864	
A17_NMR1.txt	7	1	0	0.00054	-8.5270	-5.8666	-0.0001	-0.0001	-0.0001	-0.0001	-1.0139	-2.5359	
A18.txt	8	1	0	0.00017	-0.0003	-0.0002	-0.0002	-0.0002	-0.0002	-0.0003	-0.0002	-0.0001	
B11.txt	1	1	0	0.00039	-0.0001	-0.0002	-0.0002	-0.0001	-0.0002	-0.0001	-0.0002	-0.0002	
B12.txt	2	1	0	0.00019	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	-0.0002	-0.0001	
B13.txt	3	1	0	6.41718	-0.0003	-0.0003	-0.0003	-0.0004	-0.0003	-0.0002	-0.0003	-0.0002	
B13_NMR1.txt	3	1	0	0.00031	-0.0004	-0.0004	-0.0004	-0.0004	-0.0003	-0.0003	-0.0004	-0.0003	
B14.txt	4	1	0	0.00024	-0.0001	-0.0002	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	
B15.txt	5	1	0	0.00028	-0.0001	-0.0002	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	
B15_R.txt	5	1	0	-1.5318	-0.0003	-0.0003	-0.0003	-0.0003	-0.0004	-0.0003	-0.0003	-0.0003	
B16.txt	6	1	0	0.00062	-0.0002	-0.0002	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	-0.0001	
B17.txt	7	1	0	0.00013	-0.0001	-0.0004	-0.0002	-0.0003	-0.0003	-0.0002	-0.0003	-0.0003	
B18.txt	8	1	0	0.00013	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	
C11.txt	1	1	0	0.00023	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	-0.0002	
C11_NMR1.txt	1	1	0	2.87525	-0.0003	-0.0003	-0.0004	-0.0003	-0.0003	-0.0003	-0.0003	-0.0003	

# Current methods lack proper multi-block structure

- ✓ They mix all the different variations
- ✓ and/or... uni-directional models ( $X \rightarrow Y$ )
- ✓ and/or... focus on correlations only

## a.) Single-block model (e.g. PCA)

- Mixes all variation together
- No relation between blocks

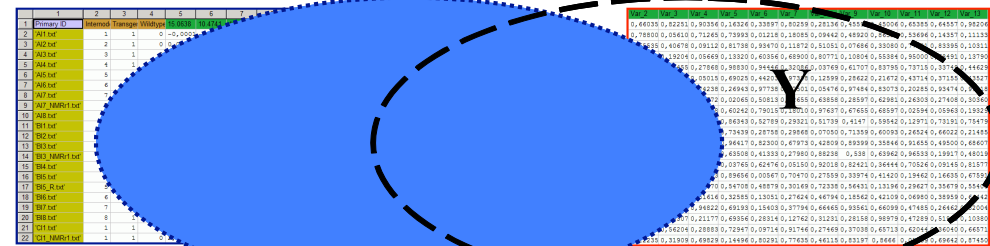
$X$       PCA       $Y$



## b.) Two-block model (e.g. PLS, PCR, MLR, RR, SVM, CC)

- Uni-directional ( $X \rightarrow Y$ ), only X-block is modelled
- Mixes all variations in X block together,
- Non-overlapping variation of no interest
  - Sometimes, the most interesting!!

$X$       PLS       $Y$

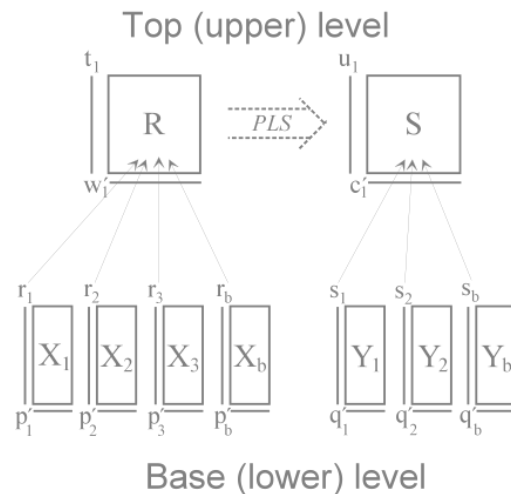




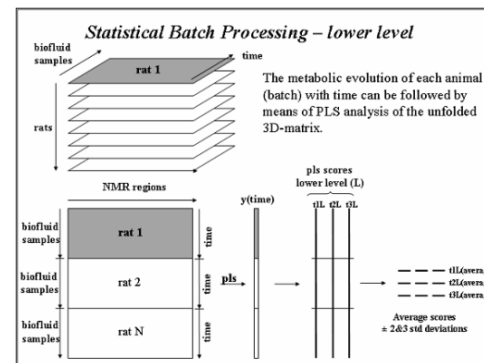
# ...including Multi-block extensions of PCA/PLS modeling

- c.) Hierarchical modeling
- d.) Batch modeling
- e.) BIF-PLS, L-PLSR (more?)

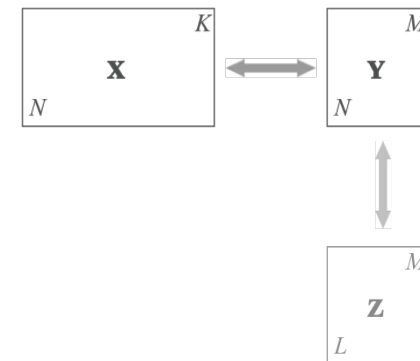
## Hierarchical modeling



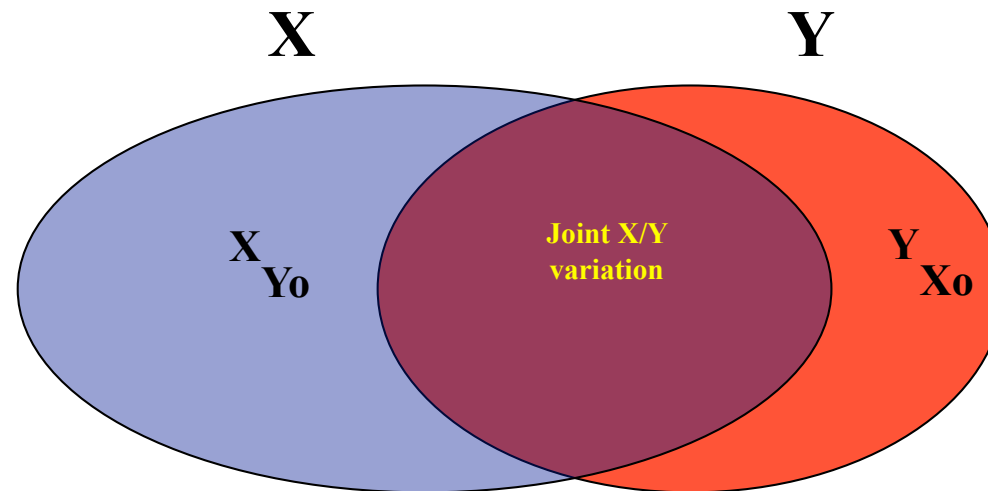
## Batch modeling



## Three block modeling (BIF-PLS, L-PLSR)



# O2PLS for multi-block modeling

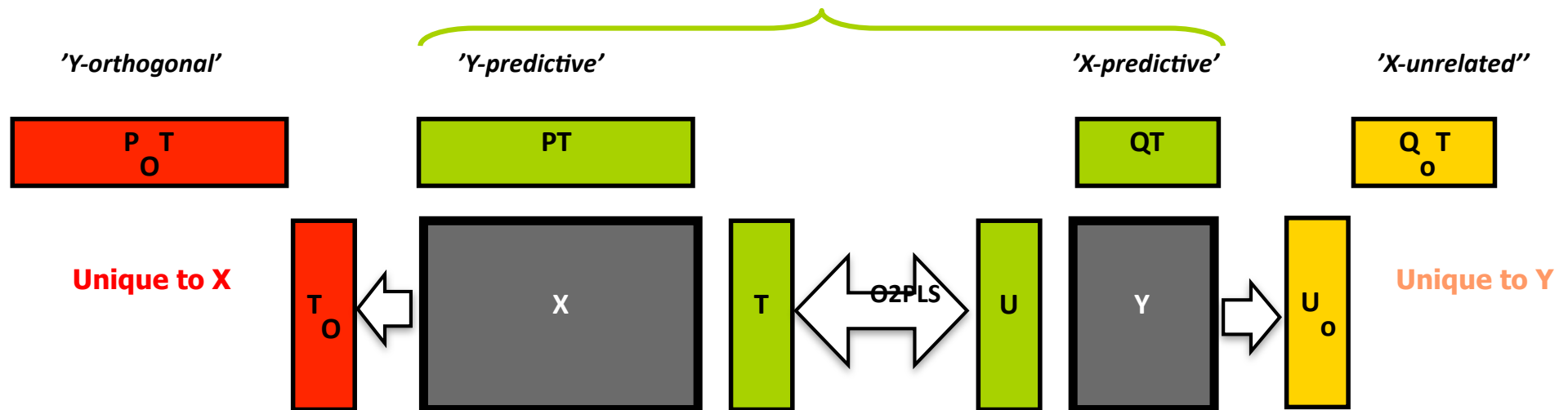


- Does not mix all different variations together
  - Separates ‘between block’ (Y-related) variation from ‘within block’ (Y-orthogonal) variation
- Only uses joint X/Y variation for modeling Y from X (and vice versa)
  - Main reason for differences in how we interpret a PLS model ( $W, W^*, P, B$ )

# The O2PLS model structure

- Separate model for joined and orthogonal variation
- Model of  $\mathbf{X}$ :  $\mathbf{X} = \mathbf{T}_p \mathbf{P}_p^T + \mathbf{T}_o \mathbf{P}_o^T + \mathbf{E}$
- Model of  $\mathbf{Y}$ :  $\mathbf{Y} = \mathbf{U}_p \mathbf{Q}_p^T + \mathbf{U}_o \mathbf{Q}_o^T + \mathbf{F}$
- O2PLS components number for  $\mathbf{X}$ - $\mathbf{Y}$  joined variation obtained by PCA of their co-variance matrix ( $\mathbf{X}^T \mathbf{Y}$ )

## X-Y Joint Variation

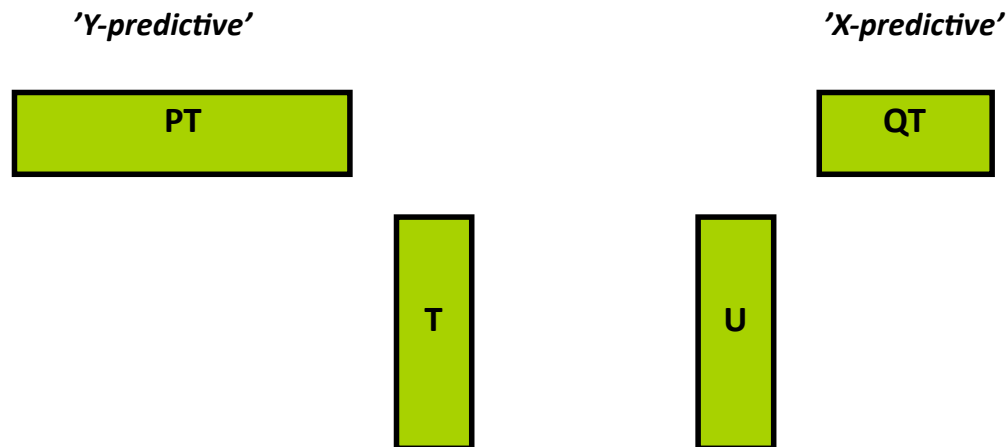


Trygg J, Wold S, O2-PLS, a two-block (X-Y) latent variable regression (LVR) method with an integral OSC filter JOURNAL OF CHEMOMETRICS 17 (1): 53-64 JAN 2003

# O2PLS - Interpretation

---

- What is the overlapping variation between  $X \leftrightarrow Y$ ?





## O2PLS - Interpretation

- Which variation is only found in **X**?

$P$   $T$   
 $O$

Unique to  
**X**

$T$   
 $O$

- What is seen in the orthogonal vectors,  $X \perp Y$ ?
  - Systematic variation in **X** that is orthogonal between **X** and **Y**
  - Look at  $T_o$  and corresponding  $P_o$



## O2PLS - Interpretation

- **Which variation is only found in Y?**

- What is seen in the unrelated vectors,  $Y \perp X$ ?
  - Systematic variation in Y that is uncorrelated between **X** and **Y**
  - Look at  $\mathbf{U}_o$  and corresponding  $\mathbf{Q}_o$

$\mathbf{Q}_o^T$

$\mathbf{U}_o$

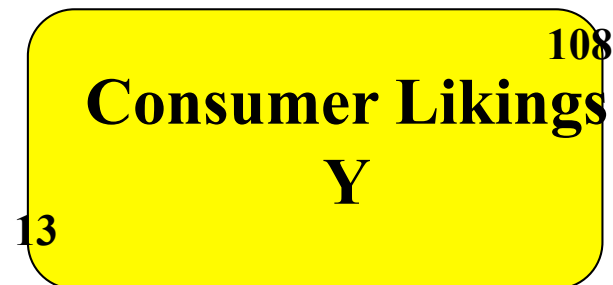
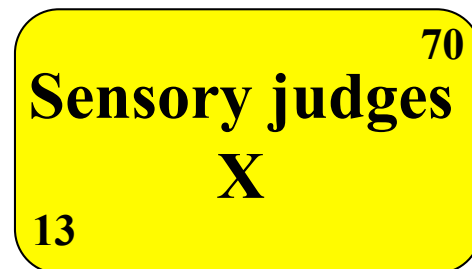
Unique to Y



# O2PLS modeling of Apples

## Preference mapping

- Sensory and preference data for a set of 13 apples
  - 70 sensory attributes (X-variables); panel averages across 12 judges
  - 108 consumer likings (Y-variables), expressed on a nine-grade scale
  - Original reference [MacFie, H., *et al.*, 1999].

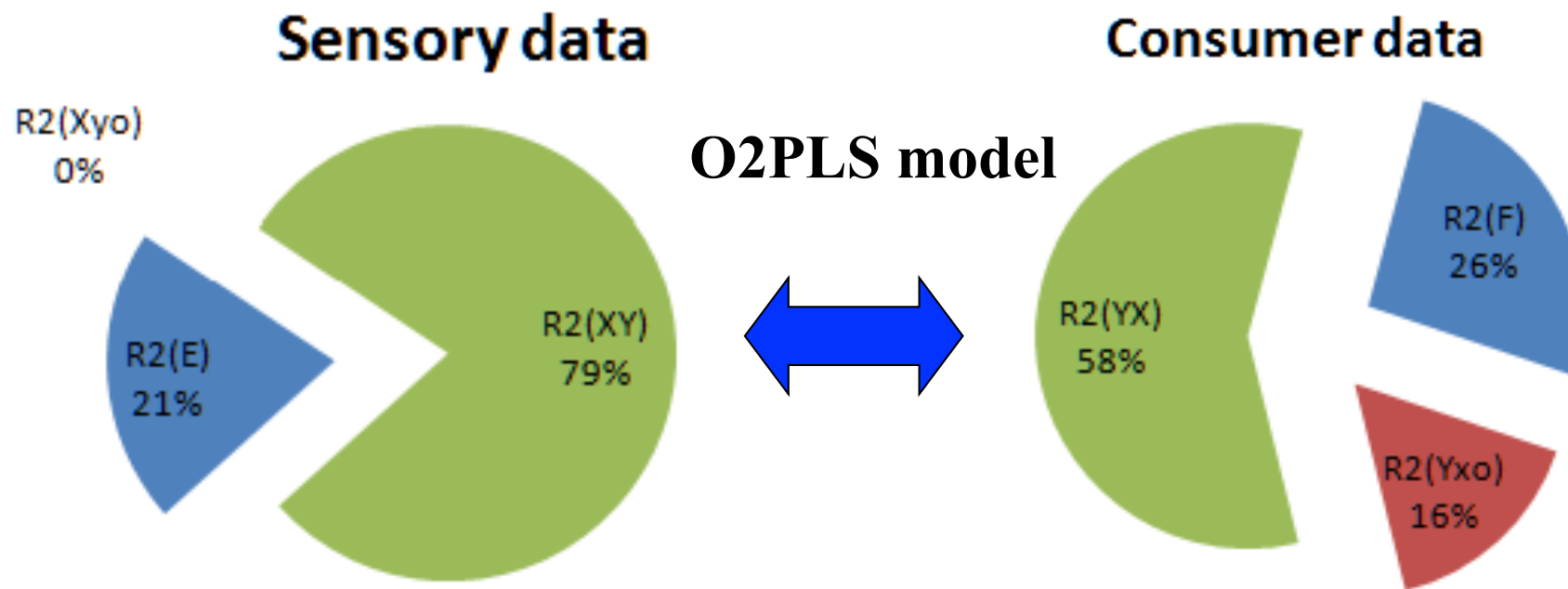


- Group formation among sensory attributes
  - 1\_ is a "First Bite" attribute,
  - E\_ is an "External Appearance" attribute,
  - EA\_ is "External Aroma",
  - A\_ is "Astringent aftertaste",
  - F\_ is "Flavor",
  - I\_ is "Internal Appearance",
  - T\_ is "Texture"

# O2PLS modeling of Apples

## Preference mapping

- O2PLS analysis results in a 4 + 0 + 2 model
  - Joint information;  $R^2X = 0.79$ ;  $R^2Y = 0.56$
  - Y-orthogonal (uncorrelated to the judges); ---
  - X-orthogonal (uncorrelated to the consumers);  $R^2Y_{X\text{-orth}} = 0.16$



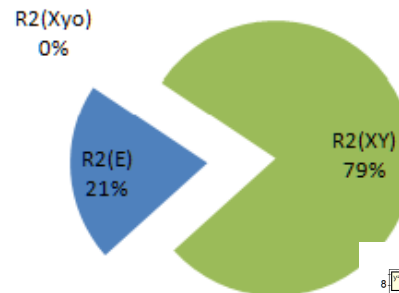




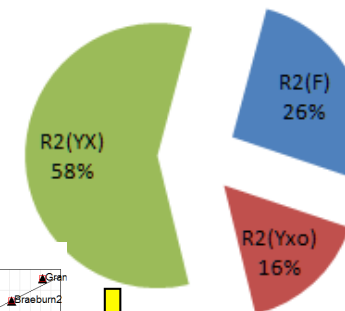
# O2PLS modeling in Preference mapping

## Joint variation (overlapping)

### Sensory data

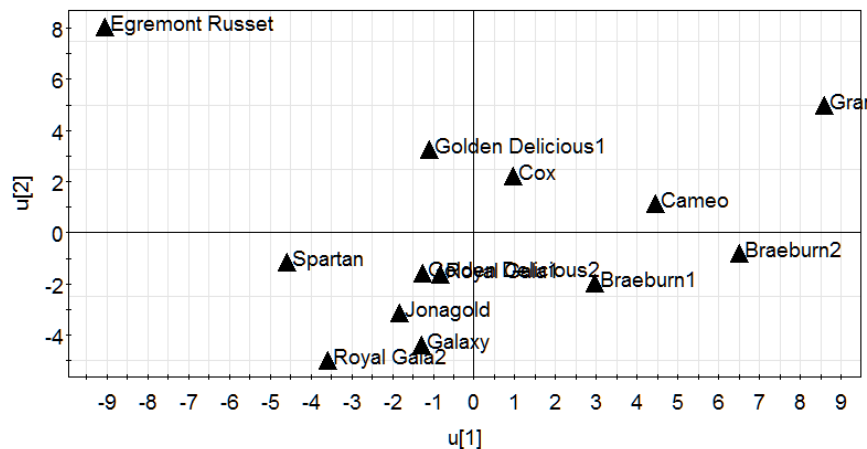


### Consumer data



### Sensory data plot Score plot ( $t_1-t_2$ )

SensCons.M4 (OPLS/O2PLS), Sensory vs Preference  
t[Comp. 1]/u[Comp. 2]



R2X[1] = 0,329641 R2X[2] = 0,208404

### Consumer data plot Score plot ( $t_1-t_2$ )

SensCons.M4 (OPLS/O2PLS), Sensory vs Preference  
t[Comp. 1]/t[Comp. 2]



X[1] = 0,329641

R2X[2] = 0,208404

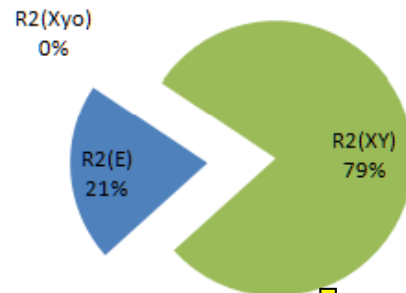
Ellipse: Hotell:



# O2PLS modeling in Preference mapping

## Joint variation (overlapping)

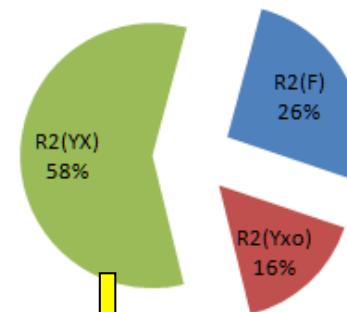
**Sensory data**



**Joint variation (79%)**

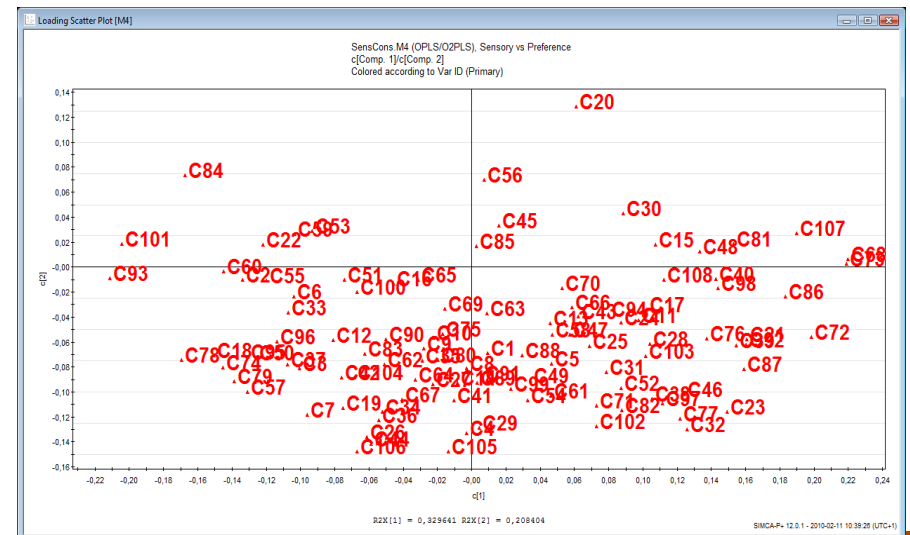
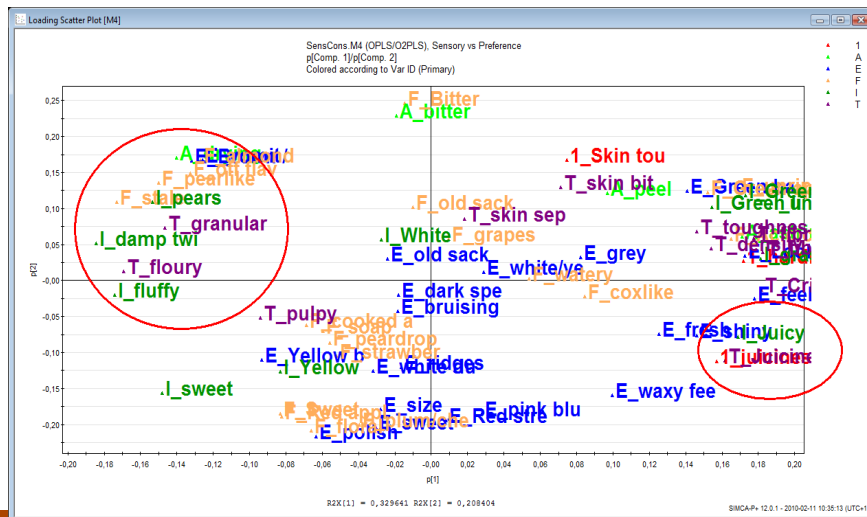
**Loading plot ( $p_1$ - $p_2$ )**

**Consumer data**



**Joint variation (58%)**

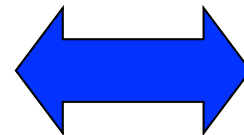
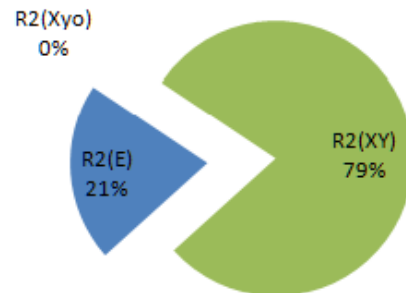
**Loading plot ( $q_1$ - $q_2$ )**



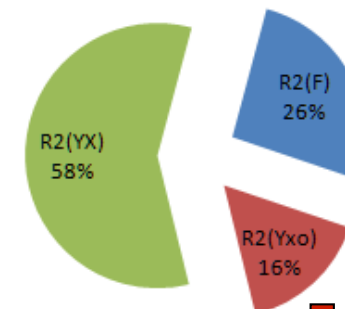
# O2PLS modeling in Preference mapping

## Unique variation in Y (uncorrelated)

### Sensory data

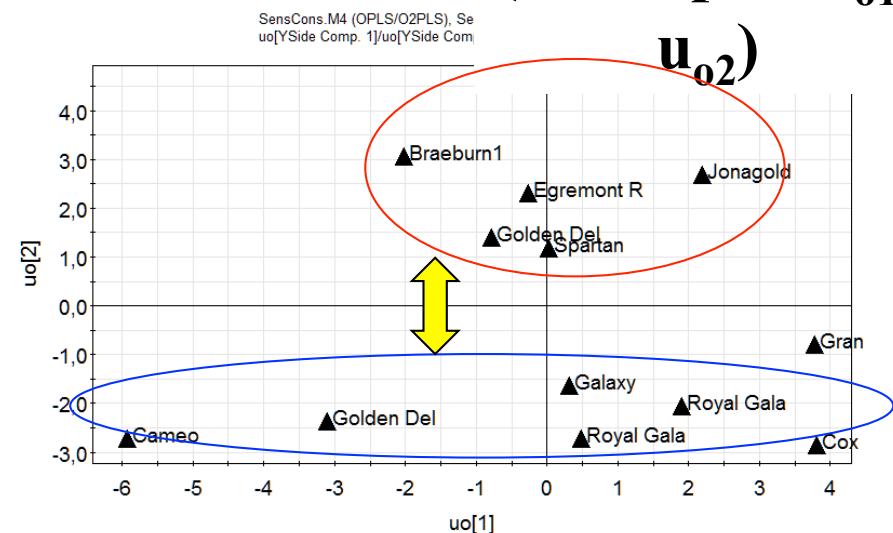


### Consumer data



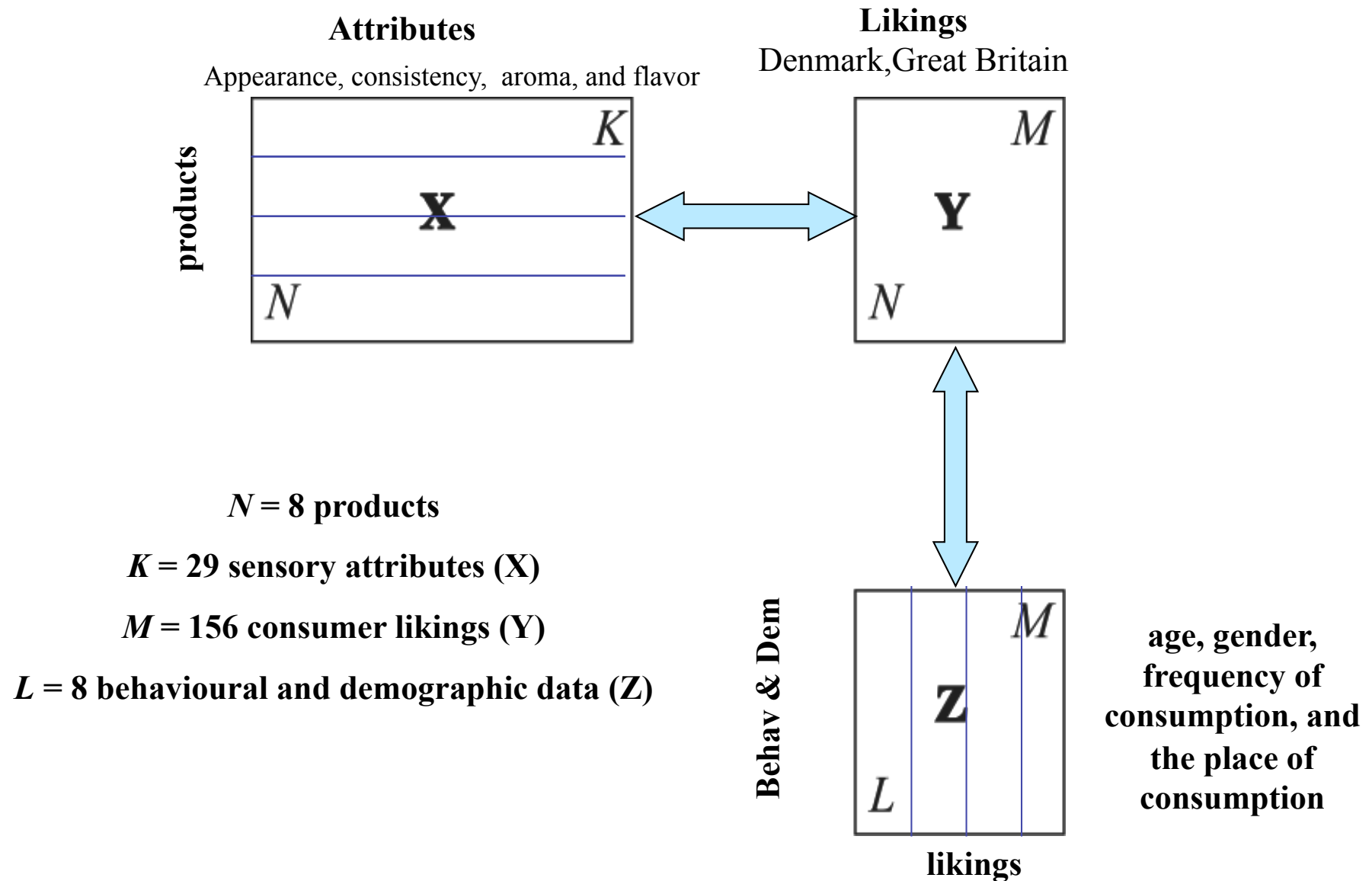
Unique variation in Y  
Apples plot  
(Score plot  $u_{o1}$ -

**Unique variation  
in Y (16%)**  
Consumers discriminate  
Between two groups of apples  
Not picked up by Sensory data

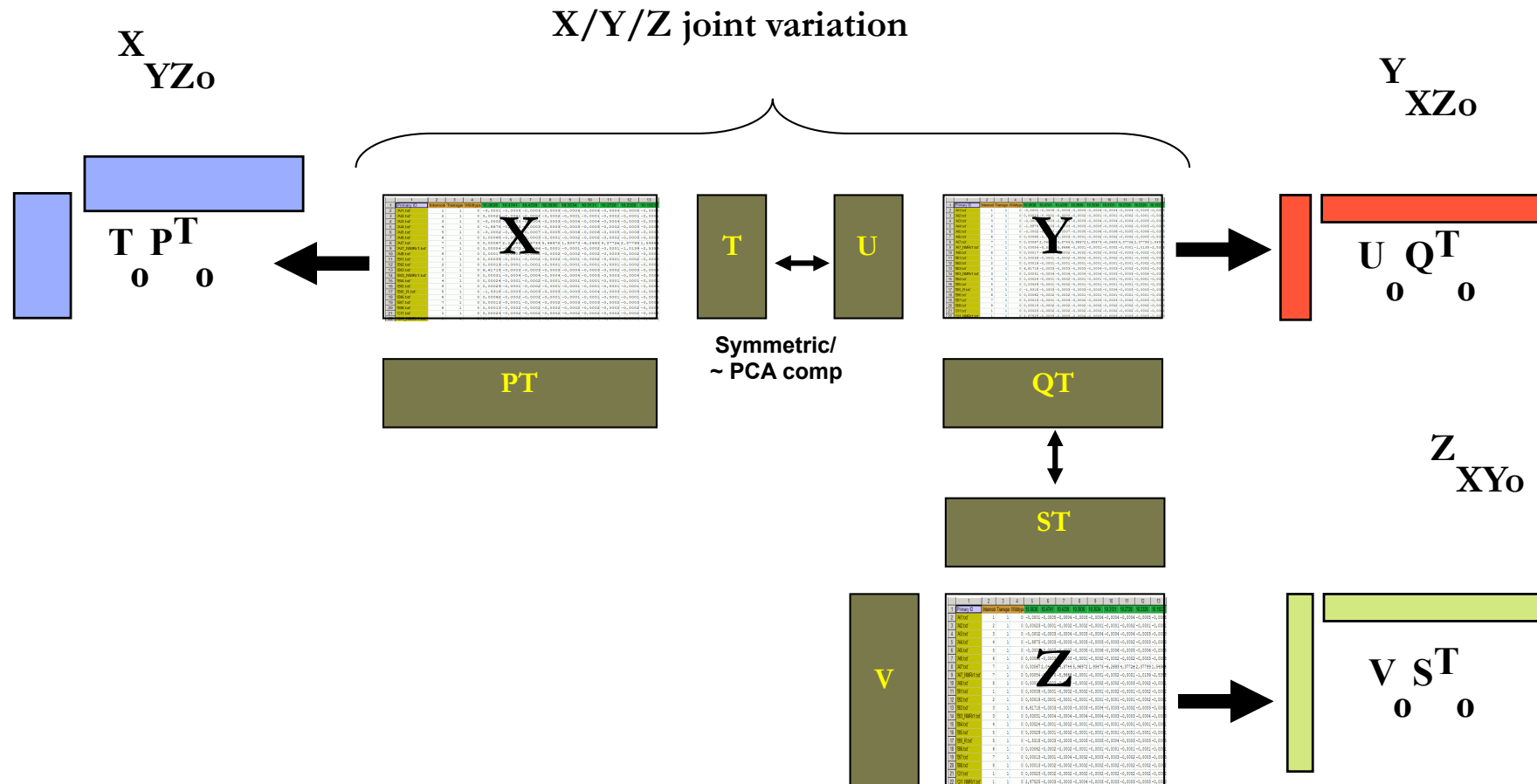




# Preference mapping using 3 block extension of O2PLS



# Structure of the extended O2PLS model





## Concluding remarks

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- OPLS and O2PLS are the only methods that have a multi-focus
  - Analyzes the correlation
  - analyzes the Orthogonal variation i.e. the uncorrelated, unique structure in a comprehensive way.
- Predictive component
  - What is related between blocks
- Uncorrelated structure, orthogonal variation
  - What is NOT related between blocks



# Acknowledgements

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Swedish Foundation for Strategic Research (SSF)  
Swedish Research Council  
FORMAS FuncFibre  
Knut & Alice Wallenberg Foundation  
GlaxoSmithKline  
AstraZeneca  
MKS Umetrics

*Chemometrics group, Umeå University*

M. Bylesjö  
S. Wiklund  
H. Stenlund  
P. Jonsson  
H. Antti  
M. Hedenström  
M. Sjöström

*Umeå Plant Science Center, Umeå Univ*

T. Moritz  
A. Johansson  
D. Eriksson  
A. Sjödin  
B Sundberg  
G. Sandberg

*Bergen University*

Olav Kvalheim

*Acure Pharma*

T. Lundstedt

*Umetrics AB, Sweden*

E. Johansson  
S. Wold  
L. Eriksson

*AstraZeneca*

O. Berntsson  
M Josefsson  
S Folestad  
J Gottfries

*GlaxoSmithKline*

R Escott  
C Airau  
T Thurston

*SweTreeTechnologies*

M Hertzberg  
K Johansson  
A Karlsson