# Social network Graph Link Prediction - Facebook Challenge

In [2]:

```
#Importing Libraries
# please do go through this python notebook:
import warnings
warnings.filterwarnings("ignore")
import pandas as pd#pandas to create small dataframes
import datetime #Convert to unix time
import time #Convert to unix time
# if numpy is not installed already : pip3 install numpy
import numpy as np#Do aritmetic operations on arrays
# matplotlib: used to plot graphs
import matplotlib
import matplotlib.pylab as plt
import seaborn as sns#Plots
from matplotlib import rcParams#Size of plots
from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
import math
import pickle
import os
# to install xgboost: pip3 install xgboost
import xgboost as xgb
import warnings
import networkx as nx
import pdb
import pickle
from pandas import HDFStore, DataFrame
from pandas import read_hdf
from scipy.sparse.linalg import svds, eigs
import gc
from tqdm import tqdm
```

## 1. Reading Data

```
In [31:
```

```
if os.path.isfile('train_pos_after_eda.csv'):
train_graph=nx.read_edgelist('train_pos_after_eda.csv',delimiter=',',create_using=nx.DiGraph(),nod
etype=int)
   print(nx.info(train graph))
else:
   print("please run the FB EDA.ipynb or download the files from drive")
Name:
Type: DiGraph
Number of nodes: 1780924
Number of edges: 7550014
Average in degree: 4.2394
Average out degree: 4.2394
```

### 2. Similarity measures

#### 2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/

```
In [4]:
#for followees
def jaccard_for_followees(a,b):
    try:
       if len(set(train graph.successors(a))) == 0 | len(set(train graph.successors(b))) == 0:
           return 0
        sim = (len(set(train graph.successors(a)).intersection(set(train graph.successors(b)))))/\
(len(set(train graph.successors(a)).union(set(train graph.successors(b)))))
    except:
       return 0
    return sim
In [0]:
#one test case
print(jaccard_for_followees(273084,1505602))
0.0
In [5]:
#node 1635354 not in graph
print(jaccard_for_followees(273084,1635354))
0.0
In [6]:
#for followers
def jaccard for followers(a,b):
    try:
       if len(set(train graph.predecessors(a))) == 0 | len(set(g.predecessors(b))) == 0:
           return 0
       sim = (len(set(train graph.predecessors(a)).intersection(set(train graph.predecessors(b))))
)/\
                                (len(set(train graph.predecessors(a)).union(set(train graph.predec
ssors(b)))))
       return sim
    except:
       return 0
4
In [7]:
print(jaccard for followers(273084,470294))
0
In [8]:
#node 1635354 not in graph
print(jaccard_for_followees(669354,1635354))
0.0
2.2 Cosine distance
In [9]:
#for followees
def cosine for followees(a,b):
```

if len(set(train graph.successors(a))) == 0 | len(set(train graph.successors(b))) == 0:

```
return 0
        sim = (len(set(train_graph.successors(a)).intersection(set(train_graph.successors(b)))))/\
(math.sqrt(len(set(train graph.successors(a)))*len((set(train graph.successors(b)))))))
        return sim
    except:
        return 0
In [10]:
print(cosine_for followees(273084,1505602))
0.0
In [11]:
print(cosine for followees(273084,1635354))
0.0
In [12]:
def cosine for followers(a,b):
    try:
        if len(set(train graph.predecessors(a))) == 0 | len(set(train graph.predecessors(b))) == 0
        sim = (len(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(b))))
)/\
                                      (math.sqrt(len(set(train_graph.predecessors(a))))*(len(set(tra
n_graph.predecessors(b)))))
       return sim
    except:
        return 0
In [13]:
print(cosine for followers(2,470294))
0.0
In [14]:
print(cosine_for_followers(669354,1635354))
0
```

### 3. Ranking Measures

https://networkx.github.io/documentation/networkx-

1.10/reference/generated/networkx.algorithms.link\_analysis.pagerank\_alg.pagerank.html

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.

Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

### 3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank

```
In [15]:

if not os.path.isfile('page_rank.p'):
    pr = nx.pagerank(train_graph, alpha=0.85)
    pickle.dump(pr,open('page_rank.p','wb'))

else:
    pr = pickle.load(open('page_rank.p','rb'))

In [16]:

print('min',pr[min(pr, key=pr.get)])
    print('max',pr[max(pr, key=pr.get)])
    print('mean',float(sum(pr.values())) / len(pr))

min 1.655487615014562e-07
max 2.652608754429015e-05
mean 5.615062742682022e-07
```

In [47]:

```
#for imputing to nodes which are not there in Train data
mean_pr = float(sum(pr.values())) / len(pr)
print(mean_pr)
```

5.615062742682022e-07

### 4. Other Graph Features

### 4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
In [17]:
```

```
In [18]:
```

```
#testing
compute_shortest_path_length(77697, 826021)
```

```
Out[18]:
```

10

#### In [19]:

```
#testing
```

```
compute_shortest_path_length(669354,1635354)
Out[19]:
-1
```

### 4.2 Checking for same community

```
In [20]:
```

```
#getting weekly connected edges from graph
wcc=list(nx.weakly_connected_components(train_graph))
def belongs_to_same_wcc(a,b):
    index = []
    if train_graph.has_edge(b,a):
       return 1
    if train_graph.has_edge(a,b):
            for i in wcc:
                if a in i:
                    index= i
                    break
            if (b in index):
                train_graph.remove_edge(a,b)
                if compute_shortest_path_length(a,b) ==-1:
                    train_graph.add_edge(a,b)
                    return 0
                else:
                    train_graph.add_edge(a,b)
                    return 1
            else:
                return 0
    else:
            for i in wcc:
                if a in i:
                    index= i
                    break
            if(b in index):
                return 1
            else:
                return 0
```

```
In [21]:
```

```
belongs_to_same_wcc(861, 1659750)

Out[21]:
0

In [22]:
belongs_to_same_wcc(669354,1635354)

Out[22]:
```

#### 4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices.  $A(x,y)=\sum_{u \in N(y)}\frac{u \in N(y)}\frac{1}{\log(|N(u)|)}$ 

```
In [23]:
```

```
#adar index
def calc_adar_in(a,b):
    sum=0
    try:
    n=list(set(train graph.successors(a)).intersection(set(train graph.successors(b))))
```

```
if len(n)!=0:
            for i in n:
                sum=sum+(1/np.log10(len(list(train_graph.predecessors(i)))))
            return sum
        else:
            return 0
    except:
        return 0
In [24]:
calc_adar_in(1,189226)
Out[24]:
0
In [25]:
calc_adar_in(669354,1635354)
Out[25]:
4.4 Is persion was following back:
In [26]:
def follows_back(a,b):
    if train graph.has edge(b,a):
        return 1
    else:
        return 0
In [27]:
follows back (1, 189226)
```

```
In [27]:

follows_back(1,189226)

Out[27]:

In [28]:

follows_back(669354,1635354)

Out[28]:
```

### 4.5 Katz Centrality:

https://en.wikipedia.org/wiki/Katz\_centrality

where A is the adjacency matrix of the graph G with eigenvalues \$\$\lambda\$\$.

The parameter  $\$  controls the initial centrality and  $\$  controls \frac{1}{\lambda\_{max}}.\$\$

```
In [29]:
```

```
if not os.path.isfile('katz.p'):
    katz = nx.katz.katz_centrality(train_graph,alpha=0.005,beta=1)
    pickle.dump(katz,open('katz.p','wb'))
else:
    katz = pickle.load(open('katz.p','rb'))
In [30]:
print('min', katz[min(katz, key=katz.get)])
print('max', katz[max(katz, key=katz.get)])
print('mean',float(sum(katz.values())) / len(katz))
min 0.0007313157740577884
max 0.0033642924161174626
mean 0.0007483387364846024
In [31]:
mean katz = float(sum(katz.values())) / len(katz)
print(mean_katz)
0.0007483387364846024
```

### 4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS algorithm

```
In [32]:

if not os.path.isfile('hits.p'):
    hits = nx.hits(train_graph, max_iter=100, tol=1e-08, nstart=None, normalized=True)
    pickle.dump(hits,open('hits.p','wb'))

else:
    hits = pickle.load(open('hits.p','rb'))

In [33]:

print('min',hits[0][min(hits[0], key=hits[0].get)])
print('max',hits[0][max(hits[0], key=hits[0].get)])
print('mean',float(sum(hits[0].values())) / len(hits[0]))

min 0.0
max 0.004833618572939799
mean 5.615062742719634e-07
```

### 5. Featurization

### 5. 1 Reading a sample of Data from both train and test

```
In [34]:
```

```
import random
if os.path.isfile('train_after_eda.csv'):
    filename = "train_after_eda.csv"
    # you uncomment this line, if you dont know the lentgh of the file name
    # here we have hardcoded the number of lines as 15100030
    # n_train = sum(1 for line in open(filename)) #number of records in file (excludes header)
    n_train = 15100028
    s = 100000 #desired sample size
    skip_train = sorted(random.sample(range(1,n_train+1),n_train-s))
    #https://stackoverflow.com/a/22259008/4084039
```

```
In [35]:
if os.path.isfile('test after eda.csv'):
    filename = "test after eda.csv"
    # you uncomment this line, if you dont know the lentgh of the file name
    # here we have hardcoded the number of lines as 3775008
    # n test = sum(1 for line in open(filename)) #number of records in file (excludes header)
    n \text{ test} = 3775006
    s = 50000 #desired sample size
    skip_test = sorted(random.sample(range(1, n_test+1), n_test-s))
    #https://stackoverflow.com/a/22259008/4084039
In [36]:
print("Number of rows in the train data file:", n train)
print("Number of rows we are going to elimiate in train data are",len(skip train))
print("Number of rows in the test data file:", n test)
print("Number of rows we are going to elimiate in test data are", len(skip test))
Number of rows in the train data file: 15100028
Number of rows we are going to elimiate in train data are 15000028
Number of rows in the test data file: 3775006
Number of rows we are going to elimiate in test data are 3725006
In [37]:
df final train = pd.read csv('train after eda.csv', skiprows=skip train, names=['source node', 'des
tination node'])
df_final_train['indicator_link'] = pd.read_csv('train_y.csv', skiprows=skip_train, names=['indicato
r link'])
print("Our train matrix size ", df final train.shape)
df_final_train.head(2)
Our train matrix size (100001, 3)
Out[37]:
   source_node destination_node indicator_link
       273084
                    1484794
       866691
                     732537
                                    1
1
In [38]:
df final test = pd.read csv('test after eda.csv', skiprows=skip test, names=['source node', 'destin
ation node'])
df_final_test['indicator_link'] = pd.read_csv('test_y.csv', skiprows=skip_test, names=['indicator_l
print("Our test matrix size ",df_final_test.shape)
df_final_test.head(2)
Our test matrix size (50002, 3)
Out[38]:
   source_node destination_node indicator_link
0
       848424
                     301842
                                    1
      1719499
                    1546224
                                    1
```

### 5.2 Adding a set of features

we will create these each of these features for both train and test data points

```
1. jaccard_followers
```

```
2. jaccard followees
```

- 3. cosine followers
- 4. cosine\_followees
- 5. num followers s
- 6. num followees s
- 7. num followers d
- 8. num\_followees\_d
- 9. inter followers
- 10. inter followees

#### In [40]:

```
if not os.path.isfile('storage sample stage1.h5'):
    #mapping jaccrd followers to train and test data
   df_final_train['jaccard_followers'] = df_final_train.apply(lambda row:
jaccard for followers(row['source node'],row['destination node']),axis=1)
   df final test['jaccard followers'] = df final test.apply(lambda row:
jaccard_for_followers(row['source_node'],row['destination_node']),axis=1)
    #mapping jaccrd followees to train and test data
   df_final_train['jaccard_followees'] = df_final_train.apply(lambda row:
jaccard for followees(row['source node'], row['destination node']), axis=1)
   df final test['jaccard followees'] = df final test.apply(lambda row:
jaccard_for_followees(row['source_node'],row['destination_node']),axis=1)
        #mapping jaccrd followers to train and test data
   df final train['cosine followers'] = df final train.apply(lambda row:
cosine_for_followers(row['source_node'], row['destination_node']), axis=1)
   df final test['cosine followers'] = df final test.apply(lambda row:
cosine_for_followers(row['source_node'], row['destination_node']), axis=1)
    #mapping jaccrd followees to train and test data
   df final train['cosine followees'] = df final train.apply(lambda row:
cosine for followees(row['source node'],row['destination node']),axis=1)
   df final test['cosine followees'] = df final test.apply(lambda row:
cosine for followees(row['source node'],row['destination node']),axis=1)
```

#### In [41]:

```
def compute_features_stage1(df_final):
    #calculating no of followers followees for source and destination
    #calculating intersection of followers and followees for source and destination
    num_followers_s=[]
    num followees s=[]
    num followers d=[]
    num_followees_d=[]
    inter followers=[]
    inter followees=[]
    for i,row in df final.iterrows():
            s1=set(train graph.predecessors(row['source node']))
            s2=set(train graph.successors(row['source node']))
        except:
           s1 = set()
            s2 = set()
            d1=set(train_graph.predecessors(row['destination_node']))
            d2=set(train graph.successors(row['destination node']))
        except:
           d1 = set()
           d2 = set()
        num_followers_s.append(len(s1))
        num followees s.append(len(s2))
        num followers d.append(len(d1))
```

```
num_followees_d.append(len(d2))
        inter followers.append(len(s1.intersection(d1)))
        inter followees.append(len(s2.intersection(d2)))
    return num followers s, num followers d, num followees s, num followees d, inter followers, int
er followees
In [42]:
if not os.path.isfile('storage sample stage1.h5'):
    df final train['num followers s'], df final train['num followers d'], \
    df_final_train['num_followees_s'], df_final_train['num_followees_d'], \
    df_final_train['inter_followers'], df_final_train['inter_followees'] = compute_features_stage1(d
f final train)
    df final test['num followers s'], df final test['num followers d'], \
    df_final_test['num_followees_s'], df_final_test['num_followees_d'], \
    df final test['inter followers'], df final test['inter followees']=
compute features stage1(df final test)
    hdf = HDFStore('storage_sample_stage1.h5')
    hdf.put('train df', df final train, format='table', data columns=True)
    hdf.put('test_df',df_final_test, format='table', data_columns=True)
    hdf.close()
else:
    df final train = read hdf('storage sample stage1.h5', 'train df', mode='r')
    df final test = read hdf('storage sample stage1.h5', 'test df', mode='r')
```

### 5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

#### In [43]:

```
if not os.path.isfile('storage sample stage2.h5'):
   #mapping adar index on train
   df final train['adar index'] = df final train.apply(lambda row: calc adar in(row['source node']
,row['destination_node']),axis=1)
   #mapping adar index on test
   df final test['adar index'] = df final test.apply(lambda row: calc adar in(row['source node'],r
ow['destination_node']),axis=1)
   #---
   #mapping followback or not on train
   df final train['follows back'] = df final train.apply(lambda row:
follows_back(row['source_node'], row['destination_node']), axis=1)
    #mapping followback or not on test
   df final test['follows back'] = df final test.apply(lambda row: follows back(row['source node']
,row['destination node']),axis=1)
   #---
   #mapping same component of wcc or not on train
   df final train['same comp'] = df final train.apply(lambda row: belongs to same wcc(row['source
node'], row['destination node']), axis=1)
    ##mapping same component of wcc or not on train
   df final test['same comp'] = df final test.apply(lambda row: belongs to same wcc(row['source no
de'],row['destination node']),axis=1)
   #mapping shortest path on train
   df_final_train['shortest_path'] = df_final_train.apply(lambda row: compute_shortest_path_length
```

```
#mapping shortest path on test
    df_final_test['shortest_path'] = df_final_test.apply(lambda row: compute_shortest_path_length(r
ow['source_node'],row['destination_node']),axis=1)

hdf = HDFStore('storage_sample_stage2.h5')
hdf.put('train_df',df_final_train, format='table', data_columns=True)
hdf.put('test_df',df_final_test, format='table', data_columns=True)
hdf.close()
else:
    df_final_train = read_hdf('storage_sample_stage2.h5', 'train_df',mode='r')
    df_final_test = read_hdf('storage_sample_stage2.h5', 'test_df',mode='r')
```

### 5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
  - · weight of incoming edges
  - · weight of outgoing edges
  - · weight of incoming edges + weight of outgoing edges
  - weight of incoming edges \* weight of outgoing edges
  - 2\*weight of incoming edges + weight of outgoing edges
  - weight of incoming edges + 2\*weight of outgoing edges
- 2. Page Ranking of source
- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities\_s of source
- 9. authorities\_s of dest

#### **Weight Features**

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

it is directed graph so calculated Weighted in and Weighted out differently

#### In [44]:

```
In [46]:
```

```
if not os.path.isfile('storage sample stage3.h5'):
    #mapping to pandas train
    df final train['weight in'] = df final train.destination node.apply(lambda x: Weight in.get(x,m
ean weight in))
    df final train['weight out'] = df final train.source node.apply(lambda x: Weight out.get(x,mean
weight out))
    #mapping to pandas test
    df final test['weight in'] = df final test.destination node.apply(lambda x: Weight in.get(x, mea
n weight in))
   df_final_test['weight_out'] = df_final_test.source_node.apply(lambda x: Weight_out.get(x,mean_w
eight_out))
    #some features engineerings on the in and out weights
    df final train['weight f1'] = df final train.weight in + df final train.weight out
    df final train['weight f2'] = df final train.weight in * df final train.weight out
    df final train['weight f3'] = (2*df final train.weight in + 1*df final train.weight out)
    df final train['weight f4'] = (1*df final train.weight in + 2*df final train.weight out)
    #some features engineerings on the in and out weights
    df_final_test['weight_f1'] = df_final_test.weight_in + df_final_test.weight_out
    df final test['weight f2'] = df final test.weight in * df final test.weight out
    df_final_test['weight_f3'] = (2*df_final_test.weight_in + 1*df_final_test.weight_out)
    df_final_test['weight_f4'] = (1*df_final_test.weight_in + 2*df_final_test.weight_out)
```

#### In [49]:

```
if not os.path.isfile('storage sample stage3.h5'):
       #page rank for source and destination in Train and Test
        #if anything not there in train graph then adding mean page rank
       df final train['page rank s'] = df final train.source node.apply(lambda x:pr.get(x,mean pr))
       df final train['page rank d'] = df final train.destination node.apply(lambda x:pr.get(x,mean pr
) )
       df final test['page rank s'] = df final test.source node.apply(lambda x:pr.get(x,mean pr))
       df_final_test['page_rank_d'] = df_final_test.destination_node.apply(lambda x:pr.get(x,mean_pr))
       #Katz centrality score for source and destination in Train and test
        #if anything not there in train graph then adding mean katz score
       df final_train['katz_s'] = df_final_train.source_node.apply(lambda x: katz.get(x,mean_katz))
       df final train['katz d'] = df final train.destination node.apply(lambda x: katz.get(x,mean katz
) )
       df final test['katz s'] = df final test.source node.apply(lambda x: katz.get(x,mean katz))
       df final test['katz d'] = df final test.destination node.apply(lambda x: katz.get(x,mean katz))
       #Hits algorithm score for source and destination in Train and test
        \#if anything not there in train graph then adding 0
       df_final_train['hubs_s'] = df_final_train.source_node.apply(lambda x: hits[0].get(x,0))
        df_final\_train['hubs\_d'] = df_final\_train.destination\_node.apply(\textbf{lambda} x: hits[0].get(x,0)) 
       df_final_test['hubs_s'] = df_final_test.source_node.apply(lambda x: hits[0].get(x,0))
        \texttt{df\_final\_test['hubs\_d']} = \texttt{df\_final\_test.destination\_node.apply(lambda x: hits[0].get(x,0))} 
        \# Hits algorithm score for source and destination in Train and Test
        #if anything not there in train graph then adding 0
       \label{lem:cource_node.apply} $$ df_final_train.source_node.apply (lambda x: hits[1].get(x,0)) $$ $$ df_final_train['authorities_s'] = df_final_train.source_node.apply (lambda x: hits[1].get(x,0)) $$ $$ df_final_train['authorities_s'] = df_final_train.source_node.apply (lambda x: hits[1].get(x,0)) $$ $$ df_final_train.source_node.apply (lambda x: hits[1].get(x,0)) $$ df_final_train.source_node.apply (lambda x: hits[
       df final train['authorities d'] = df final train.destination node.apply(lambda x: hits[1].get(x
, 0))
       df final test['authorities s'] = df final test.source node.apply(lambda x: hits[1].get(x,0))
       df final test['authorities d'] = df final test.destination node.apply(lambda x: hits[1].get(x,0)
) )
       hdf = HDFStore('storage sample stage3.h5')
       hdf.put('train df', df final train, format='table', data columns=True)
       hdf.put('test_df',df_final_test, format='table', data_columns=True)
       hdf.close()
```

```
else:
    df_final_train = read_hdf('storage_sample_stage3.h5', 'train_df',mode='r')
    df_final_test = read_hdf('storage_sample_stage3.h5', 'test_df',mode='r')
```

### 5.5 Adding new set of features

we will create these each of these features for both train and test data points

```
1. SVD features for both source and destination
In [50]:
def svd(x, S):
        z = sadj dict[x]
        return S[z]
    except:
       return [0,0,0,0,0,0]
In [51]:
#for svd features to get feature vector creating a dict node val and inedx in svd vector
sadj col = sorted(train graph.nodes())
sadj_dict = { val:idx for idx,val in enumerate(sadj_col)}
In [52]:
Adj = nx.adjacency matrix(train graph, nodelist=sorted(train graph.nodes())).asfptype()
In [53]:
U, s, V = svds(Adj, k = 6)
print('Adjacency matrix Shape', Adj.shape)
print('U Shape',U.shape)
print('V Shape', V.shape)
print('s Shape',s.shape)
Adjacency matrix Shape (1780924, 1780924)
U Shape (1780924, 6)
V Shape (6, 1780924)
s Shape (6,)
In [67]:
if not os.path.isfile('storage sample stage4.h5'):
    df_final_train[['svd_u_s_1', 'svd_u_s_2','svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 'svd_u_s_6']] =
    df final train.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
    df final train[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4', 'svd u d 5','svd u d 6']] =
    df final train.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
    df_final_train[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6',]]
    df_final_train.source_node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
    df final train[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5','svd v d 6']] =
    df final train.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
```

#### **SVD DOT Feature**

### In [80]:

```
if not os.path.isfile('storage sample stage5.h5'):
              Source_svd=df_final_train.apply(lambda x: list([x['svd_u_s_1'],
                                                                                                                                               x['svd_u_s_2'],
                                                                                                                                                x['svd u s 3'],
                                                                                                                                                x['svd u s 4'],
                                                                                                                                                x['svd u s 5'],
                                                                                                                                                x['svd u s 6'],
                                                                                                                                                x['svd_v_s_1'],
                                                                                                                                                x['svd v s 2'],
                                                                                                                                                 x['svd v s 3'],
                                                                                                                                                x['svd v s 4'],
                                                                                                                                                x['svd v s 5'],x['svd v s 6']]),axis=1)
              Destination svd=df final train.apply(lambda x: list([x['svd u d 1'],
                                                                                                                                                x['svd_u_d_2'],
                                                                                                                                                x['svd u d 3'],
                                                                                                                                                x['svd u d 4'],
                                                                                                                                                x['svd u d_5'],
                                                                                                                                                x['svd u d 6'],
                                                                                                                                                x['svd_v_d_1'],
                                                                                                                                                x['svd_v_d_2'],
                                                                                                                                                x['svd v d 3'],
                                                                                                                                                x['svd v d_4'],
                                                                                                                                                x['svd v d 5'],x['svd v d 6']]),axis=1)
              \label{lem:control_solution} Source\_test\_svd=df\_final\_test.apply(\textbf{lambda}\ x:\ list([x['svd_u\ s\ 1'],
                                                                                                                                                x['svd u s 2'],
                                                                                                                                                x['svd u s 3'],
                                                                                                                                                x['svd_u_s_4'],
                                                                                                                                                x['svd u s 5'],
                                                                                                                                                x['svd_u_s_6'],
                                                                                                                                                x['svd_v_s_1'],
                                                                                                                                                x['svd v s 2'],
                                                                                                                                                x['svd_v_s_3'],
                                                                                                                                                x['svd_v_s_4'],
                                                                                                                                                x['svd_v_s_5'],x['svd_v_s_6']]),axis=1)
              \label{lem:decomposition} Destination\_test\_svd=df\_final\_test.apply(\textbf{lambda} \ x: \ list([x['svd\_u\_d\_1'], list([x['svd\_u], list([x['s
```

```
x['svd u d 2'],
                                        x['svd u d 3'],
                                        x['svd_u_d_4'],
                                        x['svd u d 5'],
                                        x['svd u d 6'],
                                        x['svd_v_d_1'],
                                        x['svd v d 2'],
                                        x['svd v d 3'],
                                        x['svd_v_d_4'],
                                        x['svd_v_d_5'],x['svd_v_d_6']]),axis=1)
   train_svd_dot=[]
   for i in range(0,len(Source svd)):
       train_svd_dot.append(np.dot(Source_svd[i], Destination_svd[i]))
   test svd dot=[]
   for i in range(0,len(Source test svd)):
       test_svd_dot.append(np.dot(Source_test_svd[i],Destination_test_svd[i]))
   df_final_train['Svd_dot']=train_svd_dot
   df final test['Svd dot']=test svd dot
   hdf = HDFStore('storage sample_stage5.h5')
   hdf.put('train df', df final train, format='table', data columns=True)
   hdf.put('test_df',df_final_test, format='table', data_columns=True)
   hdf.close()
else:
   df_final_train = read_hdf('storage_sample_stage5.h5', 'train_df',mode='r')
   df_final_test = read_hdf('storage_sample_stage5.h5', 'test df',mode='r')
```

#### **Preferential Attachment Feature**

```
In [88]:
```

```
if not os.path.isfile('storage sample stage6.h5'):
    df final train['Pref attach followers']=df final train['num followers s']*df final train['num f
ollowers d'1
    df final train['Pref attach followees']=df final train['num followees s']*df final train['num f
ollowees_d']
df final test['Pref attach followers']=df final test['num followers s']*df final test['num follower
df_final_test['Pref_attach_followees']=df_final_test['num_followees_s']*df_final_test['num_followee
s_d']
    hdf = HDFStore('storage sample stage6.h5')
    hdf.put('train_df',df_final_train, format='table', data_columns=True)
    hdf.put('test df',df final test, format='table', data columns=True)
    hdf.close()
else:
    df final train = read hdf('storage sample stage6.h5', 'train df',mode='r')
    df final test = read hdf('storage sample stage6.h5', 'test df',mode='r')
4
```

#### In [89]:

```
# prepared and stored the data from machine learning models
# pelase check the FB_Models.ipynb
df_final_train.head()
```

#### Out[89]:

|   | source_node | destination_node | indicator_link | jaccard_followers | jaccard_followees | cosine_followers | cosine_followees | num_followe |
|---|-------------|------------------|----------------|-------------------|-------------------|------------------|------------------|-------------|
| 0 | 273084      | 1484794          | 1              | 0                 | 0.055556          | 0.096225         | 0.129099         |             |
| 1 | 866691      | 732537           | 1              | 0                 | 0.000000          | 0.000000         | 0.000000         |             |
| 2 | 201819      | 886117           | 1              | 0                 | 0.021739          | 0.013176         | 0.069007         |             |
| 3 | 1218356     | 498085           | 1              | 0                 | 0.122807          | 0.043470         | 0.225924         |             |

| 4 source node destination node               | indicator_link | jaccard_followers | jaccard_followees | cosine_followers | cosine_followees | num_followe |
|--|----------------|-------------------|-------------------|------------------|------------------|-------------|
|  |                |                   |                   |                  |                  |             |
| 5 rows × 58 columns                          |                |                   |                   |                  |                  |             |
| <u>(                                    </u> |                |                   |                   |                  |                  | <u>)</u>    |
| In [ ]:                                      |                |                   |                   |                  |                  |             |
|  |                |                   |                   |                  |                  |             |
|  |                |                   |                   |                  |                  |             |