

1

TREES AND HIERARCHIES



Sungahn Ko
sako@unist.ac.kr

1

Disclaimer

2

- The slides cannot be distributed, posted or used outside of this class

- Slides in this course courtesy of
 - ▣ Dr. Abish Malik (Purdue)
 - ▣ Dr. Yun Jang (Sejong Univ.)
 - ▣ Dr. Ross Maciejewski (ASU)
 - ▣ Dr. Niklas Elmqvist (UMD)
 - ▣ Dr. David Ebert (Purdue)



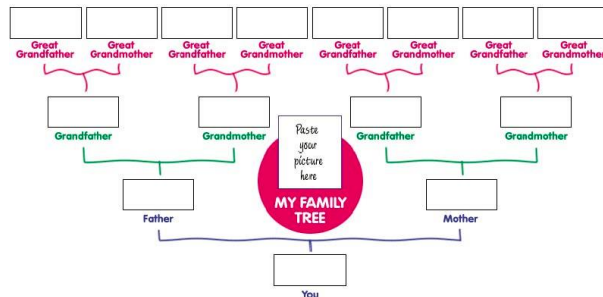
2

Hierarchies

3

Definition

- ▣ Data repository in which cases are related to subcases
- ▣ Can be thought of as imposing an ordering in which cases are parents or ancestors of other cases



Parts of this slide borrowed from John Stasko's Information Visualization Course Lecture: Hierarchies and Trees 1(Node-Link):
<http://www.cc.gatech.edu/~stasko/7450/11s/Talks/tree1.pdf>



3

Trees

4

- ▣ In the last lectures we've been discussing Graphs
- ▣ Hierarchies are often represented as trees
 - ▣ Directed
 - ▣ Acyclic
- ▣ Two main representation schemes
 - ▣ Node-link (this is similar to the graphical representations we've discussed earlier)
 - ▣ Space-Filling

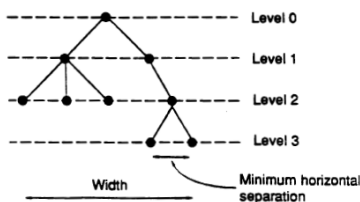


4

Rooted Trees

5

- A graph might be used to represent some hierarchy, so we often utilize a tree metaphor
- Typically, these utilize the following aesthetics
 - ▢ Vertices are placed along horizontal lines according to their level (distance from root)
 - ▢ There is a minimum separation distance between two consecutive vertices on the same level
 - ▢ The width of the drawing is as small as possible



P Eades and R Tamassia, "Algorithms for Drawing Graphs: An Annotated Bibliography," *Technical Report No. CS-89-09*, Brown University, October 1989.

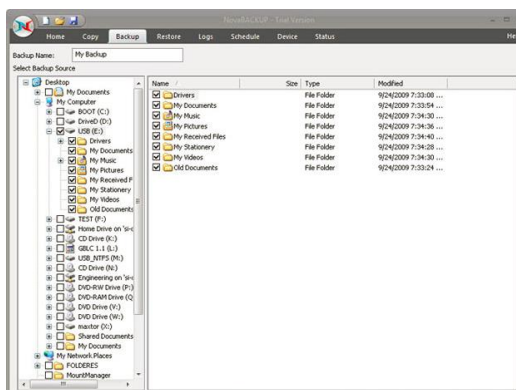
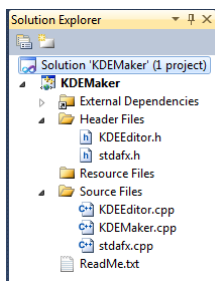


5

Using Rooted Trees

6

- What are such sorts of structures useful for?

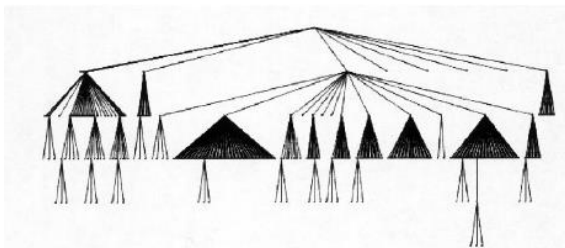


6

Top-Down Approach

7

- Width of fan-out uses up horizontal real estate very quickly
 - ▣ At level n , there are 2^n nodes
- Tree may grow very long in one branch
- Essentially you can wind up leaving a lot of screen real estate empty



Parts of this slide borrowed from John Stasko's Information Visualization Course Lecture: Hierarchies and Trees 1(Node-Link):
<http://www.cc.gatech.edu/~stasko/7450/11s/Talks/tree1.pdf>

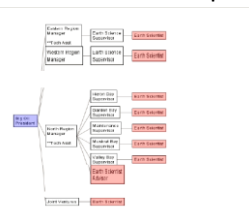
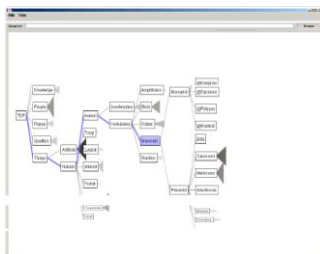


7

Space Tree

8

- Visualization techniques try to overcome some of these issues in node link tree diagrams
- *Space Tree* by Plaisant et al.
 - ▣ Dynamic rescaling of branches to best fit available screen space
 - ▣ Utilized preview icons to summarize branch topology



<https://www.jasondavies.com/wordtree/?source=c&at-in-the-hat.txt&prefix=Thing>

Plaisant, C.; Grosjean, J.; Bederson, B.B.; , "SpaceTree: supporting exploration in large node link tree, design evolution and empirical evaluation," *IEEE Symposium on Information Visualization*, pp. 57- 64, 2002

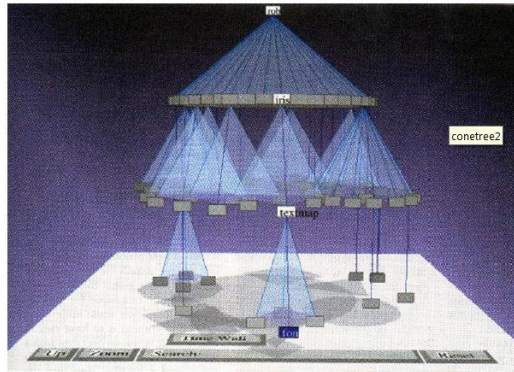


8

Cone Trees

9

- Add a third dimension for the layout
- Children of a node are laid out in a cylinder below the parent
 - ▢ Siblings live in one of the 2D planes



Robertson, G. G. Mackinlay, J. D. Card, S. K. Cone Trees: animated 3D visualizations of hierarchical information, *Proc. Human factors computing systems conference*, March 1991, 189-194.

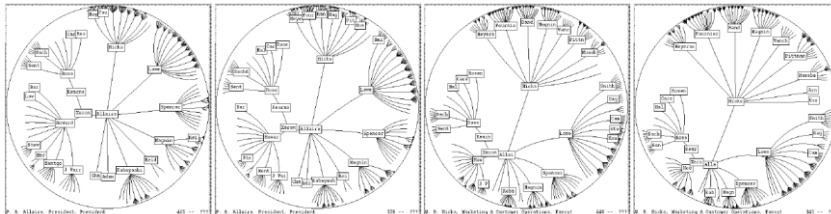


9

Hyperbolic Trees

10

- We don't have to constrain ourselves to the top-down geometry approach
- We can apply a **hyperbolic** transformation to the space
- Distance between parent and child decreases as you move farther from the center
- Children go in a wedge rather than a circle



Lamping, J., Rao, R., Pirolli; P. (1995) A focus+context technique based on hyperbolic geometry for visualizing large hierarchies *Conference proceedings on Human factors in computing systems*, 1995, 401-408

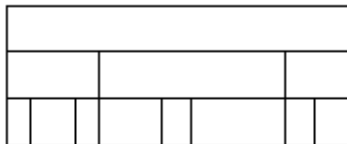


10

Space-Filling Representation

11

- Each item now occupies an area
- Children are contained under the parent



One example: "Icicle plot"

Parts of this slide borrowed from John Stasko's Information Visualization Course Lecture: Hierarchies and Trees 2(Space Filling)
<http://www.cc.gatech.edu/~stasko/7450/Notes/tree2.pdf>



11

Treemap

12

- Space filling representation developed by Johnson and Shneiderman
- Children are drawn **inside their parent**
- Alternate horizontal and vertical slicing at each successive level
- Use area to encode other variable of data items

Johnson, B. and Shneiderman, B. Treemaps: A Space-Filling Approach to the Visualization of Hierarchical Information Structures. In Proceedings of the IEEE Information Visualization '91, pages 275–282, IEEE, 1991.



12

Treemap Algorithm

13

Draw()

{

- 1) Change orientation from parent (horiz/vert)
- 2) Read all files and directories at this level
- 3) Make rectangles for each, scaled to size
- 4) Draw rectangles using appropriate size and color
- 5) For each directory
 - a) Make recursive call using its rectangle as focus

}

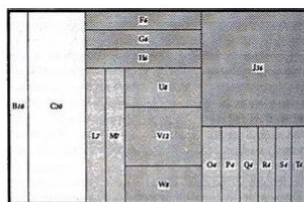
Parts of this slide borrowed from John Stasko's Information Visualization Course Lecture: Hierarchies and Trees 2(Space Filling)
<http://www.cc.gatech.edu/~stasko/7450/Notes/tree2.pdf>



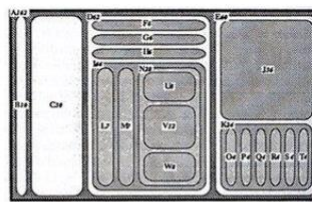
13

Nested vs. Non-Nested

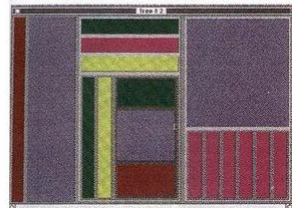
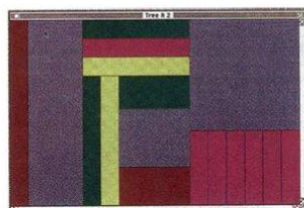
14



Non-nested Tree-Map



Nested Tree-Map



Parts of this slide borrowed from John Stasko's Information Visualization Course Lecture: Hierarchies and Trees 2(Space Filling)
<http://www.cc.gatech.edu/~stasko/7450/Notes/tree2.pdf>



14

Treemap Applications

15

- Can use the Treemap idea in a variety of domains
 - ▣ File/directory structures
 - ▣ Software diagrams
 - ▣ Sports analysis
 - ▣ Stock market data
- Examples
 - ▣ <http://www.bewitched.com/marketmap.html>
 - ▣ <https://finviz.com/map.ashx>

Parts of this slide borrowed from John Stasko's Information Visualization Course Lecture: Hierarchies and Trees 2(Space Filling)
<http://www.cc.gatech.edu/~stasko/7450/Notes/tree2.pdf>



15

Treemap Benefits

16

- Good representation of two attributes beyond node-link: color and area
- Not quite as good at representing structure
 - ▣ For example, what happens if the tree is perfectly balanced?
 - ▣ Can also get long-thin aspect ratios
 - ▣ Borders can help on small trees, but take up too much area on large, deep trees

Parts of this slide borrowed from John Stasko's Information Visualization Course Lecture: Hierarchies and Trees 2(Space Filling)
<http://www.cc.gatech.edu/~stasko/7450/Notes/tree2.pdf>

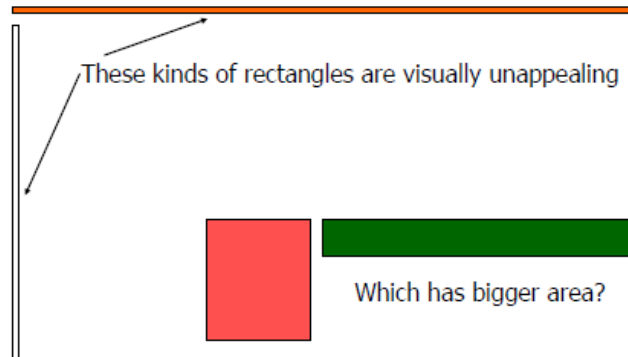


16

Aspect Ratios

17

- Here, the aspect ratio will drastically affect the visualization



Parts of this slide borrowed from John Stasko's Information Visualization Course Lecture: Hierarchies and Trees 2(Space Filling)
<http://www.cc.gatech.edu/~stasko/7450/Notes/tree2.pdf>

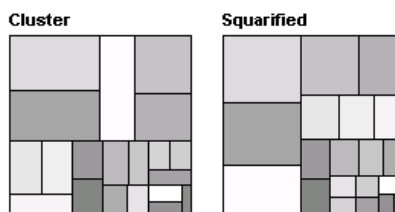


17

"Clustered and Squarified Treemaps

18

- <http://www.bewitched.com/marketmap.html>
- This treemap uses a simple recursive algorithm to reduce the overall aspect ratio
- Bruls et al. introduced the squarified treemap
 - utilized a different algorithm to also try to utilize the aspect ratio



1 -Wattenberg, M. "Visualizing the Stock Market," *Proceedings of ACM CHI 99, Extended Abstracts*, pp.188-189, 1999.
 2 -Bruls, D.M., C. Huizing, J.J. van Wijk. "Squarified Treemaps". In: W. de Leeuw, R. van Liere (eds.), *Data Visualization 2000. Proceedings of the joint Eurographics and IEEE TCVG Symposium on Visualization*, 2000, pp. 33-42.



18

Clustered and Squarified Treemaps

19

- Methods had two major drawbacks
 - ▣ Changes in the set can cause discontinuities in the layout
 - ??
 - ▣ Ordering information
 - ??

1 -Wattenberg, M. "Visualizing the Stock Market," *Proceedings of ACM CHI 99, Extended Abstracts*, pp.188-189, 1999.
 2 -Bruls, D.M., C. Huizing, J.J. van Wijk. "Squarified Treemaps". In: W. de Leeuw, R. van Liere (eds.), *Data Visualization 2000. Proceedings of the joint Eurographics and IEEE TCVG Symposium on Visualization*, 2000, pp. 33-42.



19

Ordered Treemap

20

- Shneiderman and Wattenberg introduced the ordered treemap to try and overcome these limitations
- Key insight is that it's possible to create a layout in which items that are next to each other in the given order are adjacent in the tree map
- Presented two algorithms for ordering a treemap
 - ▣ Pivot-by-size: the largest area-> most difficult to place
 - ▣ Pivot-by-middle: may create a balance layout

Ben Shneiderman, Martin Wattenberg: Ordered Treemap Layouts. INFOVIS 2001: 73-78



20

Metrics For Treemaps

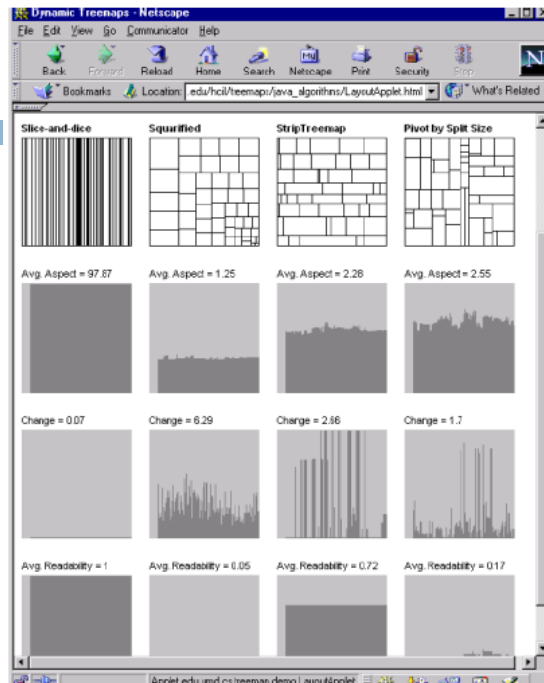
21

- In order to assess all these different treemap algorithms, we need metrics to define how “good” they are
- Use two metrics:
 - ▣ Average ?? of treemap layout
 - ▣ Layout distance change function
- Goal is to have ?? and a ?? as data is updated
- Average aspect ratio is the unweighted average
- Distance change is Euclidian distance of change in width height and corner location of rectangles

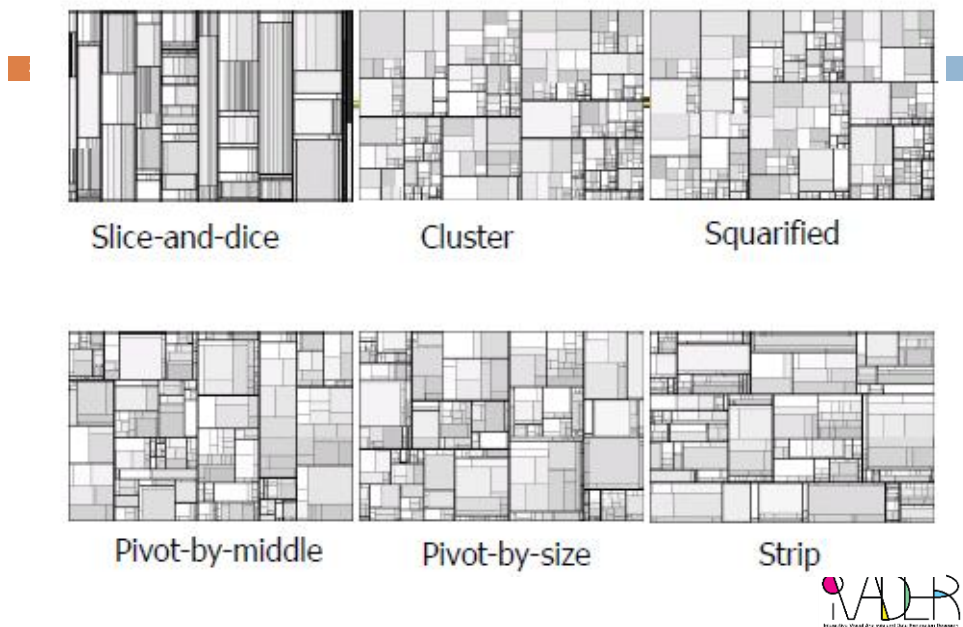


21

22



22



23

Another Problem

24

- What if nodes with zero value are very important?
- If we're mapping areas, how do we map to zero
 - ▣ Example: Stocks portfolios, I want to know what I'm not investing in because I may potentially invest

A 2 \$	C 1 \$
-----------	-----------

Classic Treemap
Preserves value proportions

A 2 \$	B 0 \$	C 1 \$
-----------	-----------	-----------

Context Treemap
Distorts value proportions to preserve identity

Parts of this slide borrowed from John Stasko's Information Visualization Course Lecture: Hierarchies and Trees 2(Space Filling)
<http://www.cc.gatech.edu/~stasko/7450/Notes/tree2.pdf>



24

Context Treemap

25

- One way to overcome this is to distort the classic treemap visualization
- Distorted treemap can show one more attribute than a classic treemap, but node area is no longer proportional to the attribute being visualized
- Several different implementation strategies for this
 1. Use a regular tree map but add some epsilon to zero value items
 - Unfortunately, as tree grows this causes things to get squished
 2. Use an exponential mapping $\text{area}(\text{node}) = 2^{\text{value}(\text{node})}$
 3. Assign some minimal screen space size to zero nodes

Christoph Csallner, Marcus Handte, Othmar Lehmann, John T. Stasko: FundExplorer: Supporting the Diversification of Mutual Fund Portfolios Using Context Treemaps. INFOVIS 2003: 203-208



25

Context Treemap

26

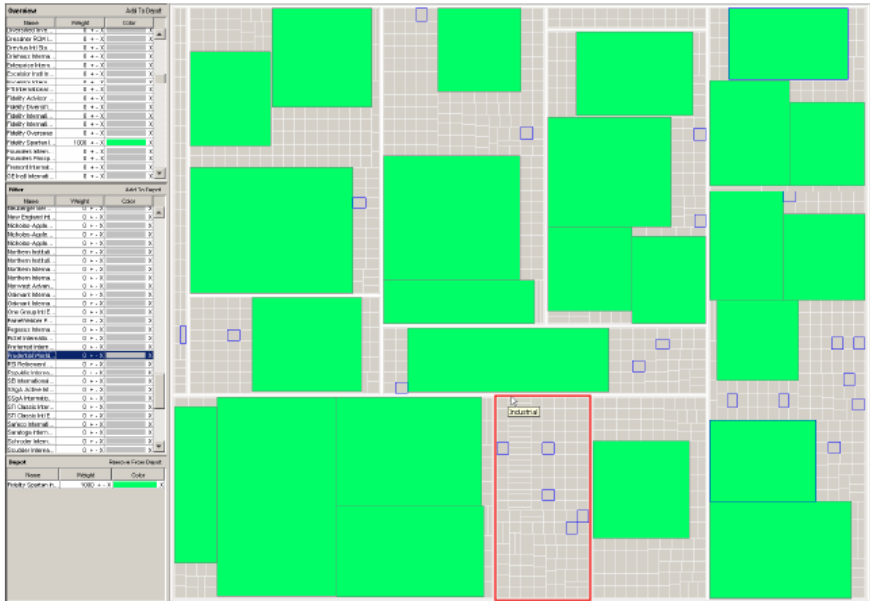
- Final solution was to calculate intermediate values
 1. Calculate the total (in this paper it was total invest money)
 - $\text{Value}(\text{total})$
 2. Create an additional total with respect to the context
 - $\text{Value}(\text{total}) * v$, where v can be modified as a **scale factor**
 3. Split context screen real estate among all empty nodes
 - $\text{Value}_c = \text{value}(\text{total}) * v / \# \text{empty}$

$$\text{value}'(\text{node}) = \begin{cases} \text{value}_c & \text{if } \text{value}(\text{node}) = 0 \\ \text{value}(\text{node}) & \text{otherwise} \end{cases}$$

Christoph Csallner, Marcus Handte, Othmar Lehmann, John T. Stasko: FundExplorer: Supporting the Diversification of Mutual Fund Portfolios Using Context Treemaps. INFOVIS 2003: 203-208



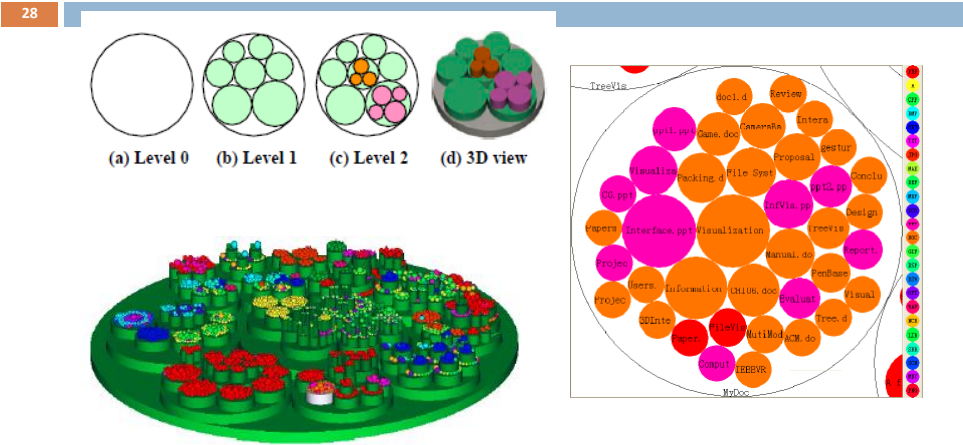
26



Christoph Csallner, Marcus Handte, Othmar Lehmann, John T. Stasko: FundExplorer: Supporting the Diversification of Mutual Fund Portfolios Using Context Treemaps. INFOVIS 2003: 203-208

27

Circle Packing



Weixin Wang, Hui Wang, Guozhong Dai, and Hongan Wang. 2006. Visualization of large hierarchical data by circle packing. In *Proceedings of the SIGCHI conference on Human Factors in computing systems (CHI '06)*, pg. 517-520.

28

Applications

29

- <http://www.cs.umd.edu/hcil/treemap-history/index.shtml>



29

Readings

30

- Required Reading:
 - B. Johnson and B. Shneiderman, "Tree-maps: A Space Filling Approach to the Visualization of Hierarchical Information Structures", Proc. of Vis '91, Oct. 1991, pp. 284-291.
 - B. Bederson, B. Shneiderman, and M. Wattenberg, Ordered and Quantum Treemaps: Making Effective Use of 2D Space to Display Hierarchies, *ACM Trans. on Graphics*, Vol. 21, No. 4, Oct. 2002, pp. 833-854.
 - **Perceptual Guidelines for Creating Rectangular Treemaps**, Nicholas Kong, Jeffrey Heer and Maneesh Agrawala. *IEEE Transactions on Visualization and Computer Graphics (Proc. InfoVis'10)*, Oct 2010.



30