

# 02-2 Data representations

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2-2 Data representa...

# DATA REPRESENTATION



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## Disclaimer

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- The slides cannot be distributed, posted or used outside of this class
- Slides in this course courtesy of
  - Dr. Abish Malik (Purdue)
  - Dr. Yun Jang (Sejong Univ.)
  - Dr. Ross Maciejewski (ASU)
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  - Dr. David Ebert (Purdue)



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## Data Models

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- Data models/representations are structured forms suitable for computer-based transformations
- These structures exist in the original data or are derivable from the original data
- Structures retain the information and knowledge content and the related context within the original data
- These structures are transformable into lower-dimensional representations for visualization and analysis



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## Data Models vs. Conceptual Models

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- Data models are mathematical abstractions
  - We can perform numerical operations, addition, subtraction, etc.
- Conceptual models are our mental constructs
  - These contain semantic structure and support reasoning
  - Think of giving directions to someone using landmarks



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## What Types of Data Models Do We Have?

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*Statistical*

### ?? Data Models

- These are data records that you deal with in excel, or typical database records
- Data records are of fixed length and well-defined
- Data is in rows and columns where each column has a domain type
- There may be a relationship defined in a schema between tables
- A database is a collection of these relations

#	A	B	C
1	Animal	Brain Weight (kg)	Body Weight (kg)
2	Mountain beaver	1.35	465
3	Cow	465	423
4	Grey wolf	36.33	119.5
5	Goat	27.66	115
6	Guinea pig	1.04	5.5
7	Diplodocus	11700	50
8	Asian elephant	2547	4603

, E.F. (1970). "A Relational Model of Data for Large Shared Data Banks". Communications of the ACM 13(6).



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## What Types of Data Models Do We Have?

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*Table*

### ?? Data Models

- This consists of variables or measurements (think of things like the census)
- Categories are factors relating to the measurements
- Observations or cases

Patient ID	Date	Chief Complaints	Location
9398	4/16/09	Ear pain	Karachi
10816	4/16/09	Stuffy nose	Lebanon
1491	4/16/09	Fever	Allepo
16237	4/16/09	Head bleed	Yemen



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## Data Types

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*Nominal*

- ??

- Data whose categories have no implied ordering
- Examples include political affiliations of a population

*Ordinal*

- ??

- Data that has a specified order, but no specified distance metric
- Examples include beverage sizes at McDonalds (Small, medium, large)

*Interval*

- ??

- Data that has measurable distances
- Examples include periods of time (second, minute, etc.) – the zero point is arbitrary

*Ratio*

- ??

- Same as interval, but include a zero point
- Examples include Celsius scale, height above sea level

SS Stevens, "On the Theory of Scales of Measurement."



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## Mapping Data

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- We need to know how to assign quantitative dimensions of our data to *aesthetic attributes*<sup>1</sup> of the data

?? Form	Surface	??	??	??
Position	Color	Direction	Tone	
Size	hue	Speed	Volume	
Shape	brightness	Acceleration	Rhythm	
polygon	saturation		Voice	
glyph	Texture			
image	pattern			
Rotation	granularity			
Resolution	orientation			
	Blur			
	Transparency			

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*Aesthetic Attributes*

*VADER*  
represent both cont. & categorical vari

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## 8 Visual Variables

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- Visualization is concerned primarily with a mapping to visual form

- [x,y]
  - Position
- [z]
  - Size (Taille)
  - Value (Valeur)
  - Color (Couleur)
  - Texture (Grain)
  - Orientation
  - Shape (Forme)

		LES VARIABLES DE L'IMAGE			12 14	
		POINTS	LIGNES	ZONES	OQ	=
XY	2 DIMENSIONS DU PLAN	x x x	/ \ / \ /	1 1 1 1 1	==	==
Z	TAILLE		/ \ / \ /	1 1 1 1 1	==	==
	VALEUR		/ \ / \ /	1 1 1 1 1	O	=
		LES VARIABLES DE SÉPARATION DES IMAGES			13	
GRAIN			/ \ / \ /	1 1 1 1 1	==	==
COULEUR			/ \ / \ /	1 1 1 1 1	==	==
ORIENTATION			/ \ / \ /	1 1 1 1 1	==	==
FORME		▲ ●	/ \ / \ /	1 1 1 1 1	==	==

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## Position

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- Position refers to a location in a multi-dimensional space
- Continuous variables map to densely distributed locations
- Categorical variables map to a lattice
- Positions are ordered, but the ordering may or may not have meaning in terms of what is being measured
- Sometimes, position is just a way to keep things from overlapping



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## ?? Position<sup>1</sup>

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### position

- Cleveland<sup>2</sup> rates ?? on a common scale as the **best way to represent a quantitative dimension visually**
- This reflects research findings that points or line lengths placed adjacent to a common axis enable judgments with the least bias or error
- However, this recommendation has a caveat, as it depends on how far the graphic primitive (point, line, etc.) is from a reference axis<sup>3</sup>
- If a graphic is far from an axis, the multiple steps needed to store and decode the variation can impair judgment



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## Size<sup>1</sup>

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- Bertin<sup>2</sup> defines size variation in terms of length or area
- For three dimensions we have volume
- Cleveland<sup>3</sup> ranks ?? and ?? representations among the **worst attributes** to use for **graphing data**
- Some designers assign size to only one dimension of an object
- Think of the bar chart where the width of the bar is typically constant, but the height is varied

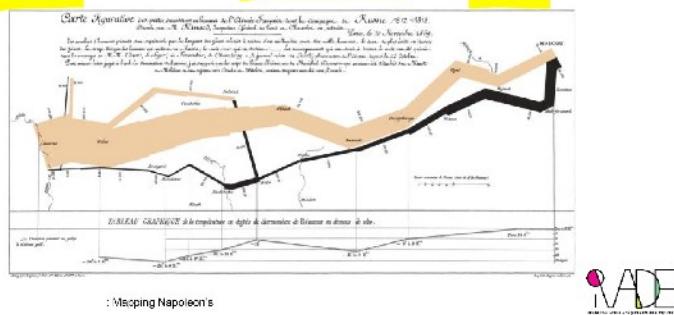


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## Size

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- Size for lines is usually equivalent to thickness
- This is less likely to induce perceptual distortion
- Size can be used to great effect with path

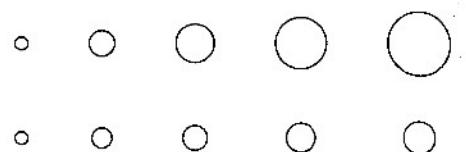


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## Size

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- For objects with rotational symmetry, we can map size to the diameter rather than area
- Representing data through area or volume should probably be confined to positively skewed data that can benefit from the perceptual equivalent of the square root transformation



Top row changes diameter from 1-5  
Bottom row changes area from 1-5

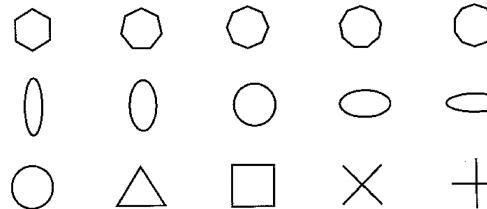


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## Shape

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- Shape refers to the shape or boundary of an object
- Examples would include map symbols
- Shape must vary without affecting size, rotation  
and other attributes

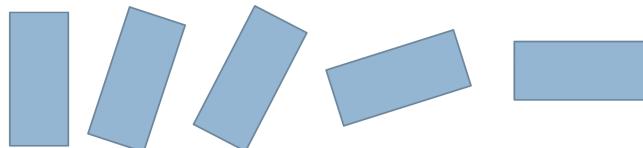


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## Rotation

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- This is the rotational angle of the graphic primitive
- Lines, areas and surfaces can only rotate if they are positionally unconstrained



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## Color

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- Color is really a psychological phenomenon
- The physical stimulus for color is light
- We see color because of the photoreceptors in our retina
- We will discuss color in-depth in a future lecture
- Use of Rainbow?



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## Texture

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- Texture includes pattern, granularity, and orientation
- Granularity is the repetition of a pattern per unit of area
- Orientation is the angle of the pattern
- Textures can be described in a variety of ways
  - **Fourier transform** – decomposes a grid of brightness values into sums of trigonometric components
  - This decomposition is orientation dependent
  - **Auto-correlogram** – characterize the spatial moments of a texture

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## Texture

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- Texture alone can be a basis for perception
- Two gray areas that have the same overall level of brightness can be discriminated if their texture is different



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## Texture

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- **Granularity** – Changing the size or resolution of patterns in a texture changes the granularity
  - Less grainy patterns (those with low-frequency spatial components) are more difficult to resolve
- **Pattern** – Patterns make use of increasing degrees of randomness to encode data

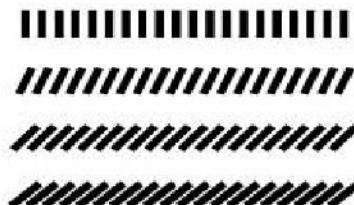


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## Texture

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- **Orientation** – Variation in texture orientation can introduce visual illusions (making lines not seem parallel) and is typically avoided as an encoding in textures



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	Point	Line	Area	Surface
Form				
Size	• • •	=====	□ □ □	~~~~~
Shape	● ■ ▲	=====	△○□	~~~~~
Rotation	▲ ▾ ▷	=====	□□□	~~~~~
Color				
Brightness	● ● ○	=====	■ ■ ■	~~~~~
Hue	● ● ○	=====	■ ■ ■	~~~~~
Saturation	● ● ○	=====	■ ■ ■	~~~~~
Texture				
Granularity	Φ Φ Φ	=====	■■■■■	~~~~~
Pattern	Φ Φ Φ	=====	■■■■■	~~~~~
Orientation	Φ Φ Φ	=====	■■■■■	~~~~~
Optics				
Blur	● ● ●	=====	■■■■■	~~~~~
Transparency	● ● ●	=====	■■■■■	~~~~~



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## Groups of Representation

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- Bertin describes four groups of representations
- *Diagrams* – correspondences are between a single component (think of things like a bar chart or a line graph)
- *Networks* – correspondences between different components are linked together
- *Maps* – correspondences between components are arranged according to geography
- *Symbols* – correspondences between components is linked to a symbol or a shape



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## Taxonomy by Data Type<sup>1</sup>

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- 1D (sets and sequences)
  - Temporal
  - 2D (maps)
  - 3D (shapes)
  - nD (relational)
  - Trees (hierarchies)
  - Networks (graphs)
  - Text and Documents<sup>2</sup>
- 
- Hanrahan's "From Data to Image" lecture: <http://graphics.stanford.edu/courses/cs448/>



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## Types of Graphic Representation

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IMPOSITION	TYPES OF IMPOSITION					
		ARRANGEMENT	RECTILINEAR	CIRCULAR	ORTHOGONAL	POLAR
DIAGRAMS						
NETWORKS						
MAPS						
SYMBOLS						

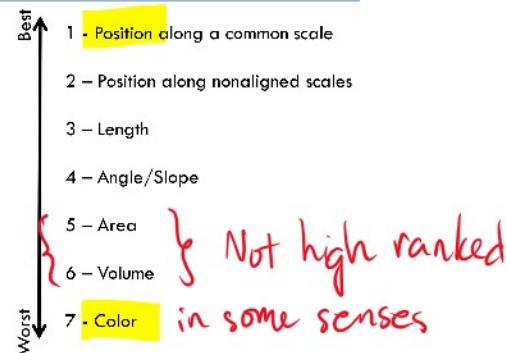


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## Cleveland's Hierarchy<sup>1</sup>

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- Cleveland evaluated elements when isolated
- Tasks were restricted to magnitude and ratio comparisons
- Research indicates this hierarchy may be best in pre-attentive stages or when focusing only on portions of a graphic<sup>2,3,4</sup>



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