COMP 2012 Final Exam - Fall 2016 - HKUST

Date: December 12, 2016 (Monday)

Time Allowed: 3 hours, 12:30 - 03:30pm

Instructions:

- 1. This is a closed-book, closed-notes examination.
- 2. There are $\underline{7}$ questions on $\underline{34}$ pages (including this cover page, appendix and the four rough worksheets).
- 3. Write your answers in the space provided.
- 4. Allocate your time wisely. Show all your work to earn full credits.
- 5. All programming codes in your answers must be written in the ANSI C++ version as taught in the class.
- For programming questions, you are <u>NOT</u> allowed to define additional helper functions or structures, nor global variables unless otherwise stated. You also <u>cannot</u> use any library functions not mentioned in the questions.

Student Name	
Student ID	
Email Address	
Lecture Section	L1 (QUAN, Long) / L2 (TSOI, Desmond)
Seat Number	

For T.A.
Use Only

Problem	Topic	\mathbf{Score}
1	Type of Inheritance	/ 6
2	Polymorphism & Dynamic Binding	/ 14
3	Binary Search Tree (BST), AVL Tree & Hashing	/ 18
4	Class Template & Operator Overloading	/ 9
5	Standard Template Library (STL)	/ 8
6	Abstract Base Class, Inheritance & Polymorphism	/ 27
7	Binary Search Tree (BST)	/ 18
	Total	/ 100

Problem 1 [6 points] Type of Inheritance

There are six parts in this question. For each part, decide whether the given program is syntactically INCORRECT – that is, it will produce compilation error(s). Circle "Yes" if it will give compilation error and "No" otherwise.

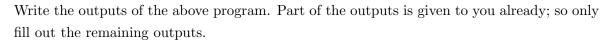
Assume the programs in the different parts are independent of each other, and "B.h" has been included in each part and is defined as follows:

```
class B { /* B.h */
 protected:
   int a;
};
             Yes / No
(a) [1 point]
   class C : public B { };
   class D : private C { public: D() : a(5) {} };
   int main() { D obj; return 0; }
(b) [1 point]
             Yes / No
   class C : public B { };
   class D : private C { public: void set(int a) { this->a = a; } };
   int main() { D obj; return 0; }
(c) [1 point]
             Yes / No
   class C : protected B { };
   class D : private C { public: void set(int a) { this->a = a; } };
   int main() { D obj; return 0; }
(d) [1 point]
            Yes / No
   class C : private B { };
   class D : public C { public: void set(int a) { this->a = a; } };
   int main() { D obj; return 0; }
(e) [1 point]
              Yes / No
   class D : public B { };
   int main() { D obj; B& ref = obj; return 0; }
(f) [1 point]
             Yes / No
   class D : protected B { };
   int main() { D obj; B& ref = obj; return 0; }
```

Problem 2 [14 points] Polymorphism and Dynamic Binding

```
#include <iostream>
using namespace std;
class Base {
    int base;
    static int count;
  public:
    Base(int b = 30): base(b) {
      count++;
      cout \ll "Base's Ctor, count = " \ll count \ll endl;
    Base(const Base& b): base(b.base) {
      count++;
      cout \ll "Base's Copy Ctor, count = " \ll count \ll endl;
    }
    virtual ∼Base() {
      count--;
      cout \ll "Base's Dtor, count = " \ll count \ll endl;
    }
    virtual void set(int b) { base = b; }
    virtual int get() const { return base; }
    void work() const { cout « "Work in Base!" « endl; }
    virtual void print() const { cout \ll "Value of base: " \ll base \ll endl; }
};
class Derived : public Base {
    static Base objBase;
    int derived;
  public:
    Derived(int d = 40): derived(d) { cout \ll "Derived's Ctor" \ll endl; }
    ~Derived() { cout ≪ "Derived's Dtor" ≪ endl; }
    void work() const {
      \mathrm{cout} \ll \text{"Work in Derived!"} \ll \mathrm{endl};
      Base::work();
      (Derived::objBase).set(50);
      (Derived::objBase).print();
    void set(int d) { derived = d; }
```

```
int get() const { return derived; }
                               void print() const {
                                              Base::print();
                                              \operatorname{cout} \ll \text{"Value of derived: } \text{"} \ll \operatorname{derived} \ll \operatorname{endl};
                               }
                               static void printStaticObjValue() {
                                               cout \ll "*** Static object's value: " \ll objBase.get() \ll " ***" \ll endl;
};
 Base Derived::objBase;
 int Base::count = 0;
 int main() {
               \operatorname{cout} \ll "--- \operatorname{Begin} \operatorname{of} \operatorname{main} --- \ll \operatorname{endl};
               Derived::printStaticObjValue();
               \operatorname{cout} \ll "----- \operatorname{Block} 1 ----- \operatorname{endl};
               Base obj1(9);
               Derived obj2(10);
                { Base obj3 = obj2; obj3.print(); }
               \operatorname{cout} \ll "----- \operatorname{Block} 2 \operatorname{-----} \ll \operatorname{endl};
               Base* objPtr = new Derived(18);
               Base& objRef = obj2;
               \operatorname{cout} \ll "----- \operatorname{Block} 3 -----\operatorname{endl};
               objPtr \rightarrow print();
               objPtr \rightarrow work();
               \operatorname{cout} \ll "----- \operatorname{Block} 4 -----\operatorname{endl};
               ((Derived*)(objPtr)) \rightarrow print();
               ((Derived*)(objPtr)) \rightarrow work();
               \operatorname{cout} \ll "----- \operatorname{Block} 5 \operatorname{-----} \ll \operatorname{endl};
               objRef.print();
               objRef.work();
               \operatorname{cout} \ll "----- \operatorname{Block} 6 \operatorname{-----} \ll \operatorname{endl};
               delete objPtr;
               \operatorname{cout} \ll "----- \operatorname{Block} 7 \operatorname{-----} \ll \operatorname{endl};
               Derived::printStaticObjValue();
               \operatorname{cout} \ll "---- \operatorname{End} \operatorname{of \ main \ } ---- = \operatorname{end} \operatorname{end} \operatorname{id} \operatorname{end} \operatorname{end} \operatorname{id} \operatorname{end} \operatorname{end} \operatorname{end} \operatorname{id} \operatorname{end} \operatorname{en
               return 0;
```





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Block	5					
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/						
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Problem 3 [18 points] Binary Search Tree (BST), AVL Tree and Hashing

(a) [6 points] Draw 5 different BSTs that can be constructed using the set of the following keys.

Also, state whether there are only 5 different BSTs that can be constructed using the given set of keys.

Answer:

(b) [8 points] Draw the AVL tree resulting from the insertion of the following keys in given order (from left to right). Show the tree after each rotation, if any.

(c) [4 points] Now, a hash table of size m=5 is used to store the same set of keys, that is

with the hash function $hash(k) = k \mod m$.

Insert the keys in the given order (from left to right) to the hash table using *sepa*rate chaining collision resolution. Assume singly linked list is used for the chains and each key is inserted to the front. Draw the resulting hash table in the space given below.

Answer:

Index	
0	
1	
2	
3	
4	

Problem 4 [9 points] Class Template and Operator Overloading

Given the program "Pair.cpp" with incomplete definition and implementation of template class 'Pair'. Complete the program by overloading the following member and non-member operator functions so that it produces the expected output given below when the program is compiled and executed.

- overload plus operator (i.e. operator+) as a member function (for adding two Pair objects)
- overload pre-increment and post-increment operator (i.e. operator++) as member functions (for adding 1 to each data member of a Pair object)
- overload insertion operator (i.e. operator<<) as non-member function (for outputting)

Write your answer in the space provided under Part (a)-(d) "ADD YOUR CODE HERE". Assumption: only numeric types will be used.

Expected output of the program:

```
Pair 1: (1,2.1)
Pair 2: (5,7.8)
Pair 3: (6,9.9)
Pair 3: (7,10.9)
Pair 3: (2,3.5)
Pair 3: (2,3.5)
Pair 3: (3,4.5)
                                                                      /* Pair.cpp */
#include <iostream>
using namespace std;
template <typename T1, typename T2>
class Pair {
  private:
    T1 firstElement;
    T2 secondElement;
  public:
    Pair() \{ \}
    Pair(const T1& e1, const T2& e2) { setElements(e1, e2); }
    T1 getFirstElement() const { return firstElement; }
    T2 getSecondElement() const { return secondElement; }
    void setElements(const T1& e1, const T2& e2) {
      firstElement = e1;
      secondElement = e2;
```

```
// Member function: plus operator, operator+
// Part (a) - ADD YOUR CODE HERE
```

```
// Member function: pre-increment operator, operator++
// Part (b) - ADD YOUR CODE HERE
```

```
// Member function: post-increment operator, operator++ 
// Part (c) - ADD YOUR CODE HERE
```

};

```
// Non-member function: insertion operator, operator<<
// Part (d) - ADD YOUR CODE HERE
```

```
int main() {
    Pair < int, double > pair1(1, 2.1), pair2(5, 7.8);
    cout « "Pair 1: " « pair1 « endl;
    cout « "Pair 2: " « pair2 « endl;
    Pair < int, double > pair3 = pair1 + pair2;
    cout « "Pair 3: " « pair3 « endl;
    ++pair3;
    cout « "Pair 3: " « pair3 « endl;
    ++pair3 = Pair < int, double > (2,3.5);
    cout « "Pair 3: " « pair3 « endl;
    cout « "Pair 3: " « pair3 « endl;
    cout « "Pair 3: " « pair3 « endl;
    cout « "Pair 3: " « pair3 « endl;
    cout « "Pair 3: " « pair3 « endl;
    cout « "Pair 3: " « pair3 « endl;
    cout « "Pair 3: " « pair3 « endl;
    cout « "Pair 3: " « pair3 » endl;
    cout « "Pair 3: " « pair3 » endl;
    cout « "Pair 3: " « pair3 » endl;
    cout »
```

For the sake of convenience, the expected output is replicated below.

```
Pair 1: (1,2.1)
Pair 2: (5,7.8)
Pair 3: (6,9.9)
Pair 3: (7,10.9)
Pair 3: (2,3.5)
Pair 3: (2,3.5)
Pair 3: (3,4.5)
```

Problem 5 [8 points] Standard Template Library (STL)

(a) [3 points] Given the following prototype of the STL function for_each

template <class InputIterator, class UnaryFunction>
UnaryFunction for_each(InputIterator first, InputIterator last, UnaryFunction f);

implement the function which applies unary function f to each container element in the range [first, last) and returns the unary function after it has been applied to each element.

Answer:

(b) [5 points] for each algorithm in STL accepts an user-defined function object or a function pointer. Implement a non-member function sqr and a function object class Sqr, both take an int reference and update the reference variable with its squared value. Write your code in the space provided under Part (b)(i) - (b)(ii) "ADD YOUR CODE HERE", so that the following program

```
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;

typedef vector<int> vi;
typedef vector<int>::iterator vii;

// Non-member function: sqr
// Part (b)(i) - ADD YOUR CODE HERE
```

```
// Function object class: Sqr
// Part (b)(ii) - ADD YOUR CODE HERE
```

```
int main() {
  int arr[] = { 52, 61, 2, 6, 41, 312 };
  vi vec1(arr, arr+6);
                                // Create a vector container with all the 6 numbers
  \operatorname{cout} \ll "---- Using function pointer ---- \ll endl;
  cout ≪ "vec1 (original values):\t";
  for(vii p = vec1.begin(); p!= vec1.end(); p++)
    cout \ll *p \ll ' \ t';
  cout \ll endl;
  for_each(vec1.begin(), vec1.end(), sqr);
                                                             // Pass function pointer
  cout \ll "vec1 (after sqr): \t";
  for(vii p = vec1.begin(); p != vec1.end(); p++)
    cout \ll *p \ll ' \ t';
  cout \ll endl;
  \operatorname{cout} \ll "---- Using function object ---- \ll endl;
  vi vec2(arr, arr+6); // Create another vector container also with the 6 numbers
  cout ≪ "vec2 (original values):\t";
  for(vii p = vec2.begin(); p != vec2.end(); p++)
    cout \ll *p \ll ' \ t';
  cout \ll endl;
  for_each(vec2.begin(), vec2.end(), Sqr());
                                                              // Pass function object
  cout \ll "vec2 (after sqr): \t";
  for(vii p = vec2.begin(); p!= vec2.end(); p++)
    cout \ll *p \ll ' \ t';
  cout \ll endl;
  return 0;
}
would produce the output below.
Output of the program:
---- Using function pointer ----
vec1 (original values): 52
                                               2
                                                        6
                                                                  41
                                                                            312
                                      61
vec1 (after sqr):
                            2704
                                      3721
                                               4
                                                        36
                                                                  1681
                                                                            97344
---- Using function object ----
vec2 (original values): 52
                                               2
                                                        6
                                                                  41
                                                                            312
                                     61
vec2 (after sqr):
                            2704
                                      3721
                                               4
                                                         36
                                                                  1681
                                                                            97344
```

Problem 6 [27 points] Abstract Base Class, Inheritance and Polymorphism

Given the definition of class 'Point'.

```
#ifndef POINT_H
                                                                               /* Point.h */
#define POINT_H
#include <cmath>
using namespace std;
class Point {
  private:
    double _x;
    double _y;
  public:
    Point(): _{x}(0), _{y}(0)\{\};
    Point(double x, double y) : _x(x), _y(y){};
    Point& operator+=(const Point& pt){
         _x += pt._x;
         _{y} += pt._{y};
         return *this;
    }
    void rotate(double angle) {
         double x = x*\cos(\text{angle}) - y*\sin(\text{angle});
         double y = x*\sin(angle) + y*\cos(angle);
         _{x} = x;
         _{-}y = y;
    double get_x() const { return _x; }
    double get_y() const { return _y; }
    void set_x(double x) \{ x = x; \}
    void set_y(double y) \{ y = y; \}
    void print() const { cout \ll "(" \ll _x \ll ", " \ll _y \ll ")"; }
};
```

#endif

your task is to implement an abstract base class called 'Shape', and two classes 'Circle' and 'Polygon' which are derived from 'Shape' by public inheritance that will work with the testing program "shape-test.cpp" and produces the given output.

```
/* shape-test.cpp */
#include <iostream>
#include <vector>
#include "Point.h"
#include "Shape.h"
#include "Circle.h"
#include "Polygon.h"
using namespace std;
void printShape(Shape* s[], int size)
  for(int i=0; i<size; i++)</pre>
     Point newCenter = s[i] \rightarrow center();
     double area = s[i] \rightarrow area();
     cout \ll "Shape " \ll i+1 \ll " - ";
     cout \ll ((typeid(*s[i]).name() == typeid(Circle).name())
                ? "Circle: ": "Polygon: ");
     cout \ll endl;
     s[i] \rightarrow print();
     cout ≪ "Center: ";
     newCenter.print();
     cout \ll endl;
     \operatorname{cout} \ll \operatorname{"Area:} \quad \operatorname{"} \ll \operatorname{area} \ll \operatorname{endl} \ll \operatorname{endl};
  }
}
```

{

}

```
/* shape-test.cpp (continued) */
int main()
  Shape* shapes[2];
                                                                                   // For circle
  Point center(10,20);
  double radius = 5;
  shapes[0] = new Circle(center, radius);
                                                                                 // For polygon
  vector<Point> vertices;
  vertices.push_back(Point(4,10));
  vertices.push_back(Point(9,7));
  vertices.push_back(Point(11,2));
  vertices.push_back(Point(2,2));
  shapes[1] = new Polygon(vertices);
  \operatorname{cout} \ll "---- Before transformation ---- \ll endl:
  printShape(shapes, 2);
                                                            // Parameters for transformation
  Point moveAmt(2,2);
  double angle = 90;
  \operatorname{cout} \ll "---- After translating (2,2) ---- \ll endl;
  for(int i=0; i<2; i++)
    shapes[i] \rightarrow translate(moveAmt);
  printShape(shapes, 2);
  \operatorname{cout} \ll "---- After rotating 90 ---- \ll endl;
  for(int i=0; i<2; i++)</pre>
    shapes[i]\rightarrowrotate(angle);
  printShape(shapes, 2);
  for(int i=0; i<2; i++)</pre>
    delete shapes[i];
  return 0;
```

Output of the testing program:

```
---- Before transformation ----
Shape 1 - Circle:
Center: (10, 20)
Radius: 5
Center: (10, 20)
Area: 78.5398
Shape 2 - Polygon:
Vertices: (4, 10), (9, 7), (11, 2), (2, 2)
Center: (6.5, 5.25)
Area: 45.5
---- After translating (2,2) ----
Shape 1 - Circle:
Center: (12, 22)
Radius: 5
Center: (12, 22)
Area: 78.5398
Shape 2 - Polygon:
Vertices: (6, 12), (11, 9), (13, 4), (4, 4)
Center: (8.5, 7.25)
Area: 45.5
---- After rotating 90 ----
Shape 1 - Circle:
Center: (-25.0448, 0.87034)
Radius: 5
Center: (-25.0448, 0.87034)
Area: 78.5398
Shape 2 - Polygon:
Vertices: (-13.4164, -0.0129034), (-12.9748, 5.8013), (-9.40094, 9.82966), (-5.36828, 1.78369)
Center: (-10.2901, 4.35044)
Area: 45.5
```

- (a) [6 points] Define the abstract base class Shape which will be saved in the "Shape.h". The class does not have any data members but contains 5 pure virtual functions: center, area, translate, rotate and print. Use const whenever possible. The following describes each function.
 - center: Returns the center point of the shape, where the center is in type Point.
 - area: Returns the area of shape. Assume that the returned value is in double type.
 - translate: Takes a Point object which represents the amount of translation for the shape. It does not return anything.
 - rotate: Takes a double type argument which represents the angle of rotation for the shape. It does not return anything.
 - print: Prints all the data members of shape. It does not return anything.

Answer: /* File "Shape.h" */

(b) [7 points] Define and implement the class Circle which will be saved in the "Circle.h" file. The Circle class is derived from Shape and has two data members: center (type: Point) and radius (type: double). Implement all the inherited member functions and a constructor to initialize all the data members.

Note: All the member functions should be implemented inside the class definition as inline member functions.

Hint:

- Area of circle is πr^2 , where π is defined in C++ as M_PI. To use M_PI, the header file cmath should be included.
- The translation of circle is done by moving the center off the original position according to the amount of translation. Similarly, rotation of circle is done by rotating the center according to the specified angle.

Answer: /* File "Circle.h" */

(c) [14 points] Define and implement the class Polygon which will be saved in the "Polygon.h". The Polygon class is derived from Shape and has a vector of vertex points (called vertices and in type vector<Point>). As in part (b), implement all the inherited member functions and a constructor to initialize the data member, all inside the class definition as inline member functions.

Hint:

Assume you only have to deal with convex polygon, which the center and the area
of the polygon can be computed as follows:

Center =
$$\left(\frac{x_1 + x_2 + \dots + x_n}{n}, \frac{y_1 + y_2 + \dots + y_n}{n}\right)$$

Area = $\frac{1}{2} \left| (x_1 y_2 + x_2 y_3 + x_3 y_4 + \dots + x_n y_1) - (y_1 x_2 + y_2 x_3 + y_3 x_4 + \dots + y_n x_1) \right|$

where $(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)$ are the vertices of polygon and $|\cdot|$ refers to absolute value function.

 The translation of polygon is done by moving each vertex off the original position according to the amount of translation. Similarly, rotation of polygon is done by rotating each vertex according to the specified angle.

Answer: /* File "Polygon.h" */

/* part(c) continued */

Answer: /* File "Polygon.h" */

Problem 7 [18 points] Binary Search Tree (BST)

Complete the following program in the space provided under Part (a)-(d) "ADD YOUR CODE HERE". The whole program is assumed to be all written in a single source file. A sample run of the program is given below:

```
print:
        7
            6
    5
        4
3
    2
        1
findParentOf:
parent of 1 's value: 2
parent of 2 's value: 3
parent of 3 's value: -1
parent of 4 's value: 5
parent of 5 's value: 3
parent of 6 's value: 7
parent of 7 's value: 5
parent of 8 's value: -1
parent of 9 's value: -1
parent of 10 's value: -1
size:
7
findRankNItem:
rank 1 's value: 1
rank 2 's value: 2
rank 3 's value: 3
rank 4 's value: 4
rank 5 's value: 5
rank 6 's value: 6
rank 7 's value: 7
rank 8 's value: -1
rank 9 's value: -1
rank 10 's value: -1
findAllItemsLargerThanK:
6
7
```

```
#include <iostream>
#include <vector>
using namespace std;
template <typename T> struct bst_node
                                                    // A node in a binary search tree
  T value;
                                                                       // Node value.
                                                                        // Left child.
  bst_node* left;
                                                                       // Right child.
  bst_node* right;
  bst_node(const int& x) : value(x), left(NULL), right(NULL) { };
  ~bst_node() { delete left; delete right; }
};
template <typename T> class BST {
  private:
    bst\_node < T > * root;
    void insert(bst_node<T>*& node, const T& x);
    void print(bst_node<T>* node, int depth = 0) const;
    bst_node<T>* findParentOf(bst_node<T>* node, const T& v) const;
    int size(bst_node<T>* node) const;
    bst_node<T>* findRankNItem(bst_node<T>* node, const int& n) const;
    void findAllItemsLargerThanK(bst_node<T>* node, const T& k,
                                   vector<br/>bst_node<T>*>& result) const;
  public:
    BST(): root(NULL) {} // Empty BST when its root is NULL
    \sim BST() { delete root; }
    void insert(const T& x) { insert(root, x); }
    void print(int depth = 0) const { print(root, depth); }
    bst_node<T>* findParentOf(const T& v) const { return findParentOf(root, v); }
    int size() const { return size(root); }
    bst_node<T>* findRankNItem(const T& n) const {
      return findRankNItem(root, n);
    void findAllItemsLargerThanK(const T& k,
                                   vector<br/>bst_node<T>*>& result) const {
      findAllItemsLargerThanK(root, k, result);
};
```

```
// Insert an item and preserve the BST property
template <typename T>
void BST<T>::insert(bst_node<T>*& node, const T& x)
  if(node == NULL)
    node = new bst\_node < T > (x);
  else if(x < node \rightarrow value)
    insert(node \rightarrow left, x);
  else if (x > node \rightarrow value)
    insert(node \rightarrow right, x);
  else
                                                            // x == root > value; do nothing
}
// Print the BST
template <typename T>
void BST<T>::print(bst_node<T>* node, int depth) const
                                                                                  // Base case
  if(node == NULL)
    return;
  print(node \rightarrow right, depth+1);
                                                                   // Recursion: right subtree
  for(int j = 0; j < depth; j++)
                                                                       // Print the node value
    cout \ll ' \ t';
  cout \ll node \rightarrow value \ll endl;
  print(node \rightarrow left, depth+1);
                                                                     // Recursion: left subtree
```

- /* Part (a) [6 points] ADD YOUR CODE HERE
- * Implement the member function
- $*\ bst_node < T > *\ findParentOf(bst_node < T > *\ node,\ const\ T \ensuremath{\mathcal{C}}\ v)\ const$
- * Return the pointer that points to the parent node of the node that has the value of v.
- * Return NULL if no node has the value of v.
- * Return NULL if root is NULL.
- * You CANNOT use stacks.
- * You CANNOT use recursion.

*/

```
/*\ Part\ (b)\ [3\ points]\ ADD\ YOUR\ CODE\ HERE
```

- * Implement the member function int size(bst_node< T>* node) const
- * Return the size (i.e. number of nodes) of the whole BST.
- * You MUST use recursion.

*/

```
/* Part (c) [5 points] ADD YOUR CODE HERE * Implement the member function
```

- $*\ bst_node < T > *\ findRankNItem(bst_node < T > *\ node,\ const\ int \@ifnext{$\@mode}$ in the matching of the const of the matching of the const of the cons$
- * Return the pointer that points to the rank n node;
- * The node with the smallest value is of rank 1,
- * the node with the second smallest value is of rank 2, and so on.
- * You MUST use recursion.

*/

```
/* Part (d) [4 points] ADD YOUR CODE HERE

* Implement the member function

* void findAllItemsLargerThanK(bst_node<T>* node, const T& k,

* vector<bst_node<T>*>& result)

* Find all the nodes that have their values being larger than k

* and add them to the result vector and make sure the nodes in the vector are sorted

* ascendingly according to their values.

* Assume the given vector is empty initially.

* You MUST use recursion.
```

{

}

```
int main()
  BST<int> bst;
  bst.insert(3);
  bst.insert(5);
  bst.insert(7);
  bst.insert(2);
  bst.insert(4);
  bst.insert(6);
  bst.insert(1);
  cout \ll "print:" \ll endl;
  bst.print();
  cout ≪ endl ≪ "findParentOf:" ≪ endl;
  for(int i=1; i<=10; i++) {</pre>
    cout \ll "parent of " \ll i \ll " 's value: " \ll
       (bst.findParentOf(i) == NULL?-1:bst.findParentOf(i) \rightarrow value) \ll endl;
  }
  \operatorname{cout} \ll \operatorname{endl} \ll \text{"size:"} \ll \operatorname{endl};
  cout \ll bst.size() \ll endl;
  cout \ll endl \ll "findRankNItem:" \ll endl;
  for(int i=1; i<=10; i++) {</pre>
    \mathrm{cout} \ll "rank " \ll i \ll " 's value: " \ll
       (bst.findRankNItem(i) == NULL?-1:bst.findRankNItem(i) \rightarrow value) \ll endl;
  }
  cout \ll endl \ll "findAllItemsLargerThanK:" \ll endl;
  vector<br/>bst_node<int>*> result;
  bst.findAllItemsLargerThanK(4, result);
  for(unsigned int i=0; i<result.size(); i++)</pre>
     cout \ll result[i] \rightarrow value \ll endl;
  return 0;
```

Appendix

STL Sequence Container: Vector

template <class T, class Alloc = allocator<T> > class vector;

Defined in the standard header **vector**.

Description:

Vectors are sequence containers representing arrays that can change in size. Just like arrays, vectors use contiguous storage locations for their elements, which means that their elements can also be accessed using offsets on regular pointers to its elements, and just as efficiently as in arrays. But unlike arrays, their size can change dynamically, with their storage being handled automatically by the container.

The member functions in the vector<T> container class where T is the type of data stored in the vector are listed as follows:

Member function	Description
vector()	Constructor
iterator begin()	Returns an iterator pointing to the first element
const_iterator begin() const	in the vector. If the vector object is const-qualified,
	the function returns a const_iterator.
	Otherwise, it returns iterator.
iterator end()	Returns an iterator referring to the past-the-end
const_iterator end() const	element in the vector container. If the vector object
	is const-qualified, the function returns a const_iterator.
	Otherwise, it returns iterator.
void push_back(const T& val)	Adds a new element, val, at the end of the vector,
	after its current last element. The content of val is
	copied (or moved) to the new element.
size_type size() const	Returns the size of the vector

Useful Function in cmath

double fabs(double x);

• Returns the absolute value of x.