

CBSE Board
Class X Mathematics
Sample Paper 5 (Basic) – Solution

Section A

1. **Correct Option: C**

Explanation:

Prime factorisation of 196

$$196 = 2 \times 2 \times 7 \times 7 = 2^2 \times 7^2$$

Exponents of 2 and 7 are 2 and 2 respectively.

\therefore Sum of the exponents of the prime factors = 4

2. **Correct Option: C**

Explanation:

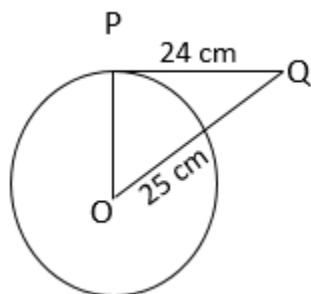
x_i	3	4	5	6	7	8	9
f_i	4	2	5	2	2	1	2

Here, the value 5 has the maximum frequency i. e. 5.

Hence, the mode is 5.

3. **Correct Option: A**

Explanation:



Here $\angle P = 90^\circ$ A tangent to a circle is perpendicular to the radius through the point of contact.

ΔPOQ is a right angled triangle.

By Pythagoras Theorem, we get

$$OQ^2 = PQ^2 + OP^2$$

$$\Rightarrow OP^2 = 25^2 - 24^2 = 49$$

$$\Rightarrow OP = 7\text{cm}$$

- 4. Correct Option: C**

Explanation:

$$\text{HCF}(26, 169) \times \text{LCM}(26, 169) = 26 \times 169$$

$$\Rightarrow 13 \times \text{LCM}(26, 169) = 4394$$

$$\Rightarrow \text{LCM}(26, 169) = 338$$

- 5. Correct Option: D**

Explanation:

$$P(A) + P(\text{not } A) = 1$$

$$\Rightarrow 0.05 + P(\text{not } A) = 1$$

$$\Rightarrow P(\text{not } A) = 1 - 0.05 = 0.95$$

- 6. Correct Option: A**

Explanation:

If the curve does not touch the x-axis, then the polynomial does not have a zero.

- 7. Correct Option: A**

Explanation:

The difference of two irrational numbers need not be an irrational number.

$$(5 + \sqrt{5}) - (1 + \sqrt{5}) = 4 \text{ (a rational number)}$$

- 8. Correct Option: C**

Explanation:

$$\begin{array}{r} \overline{)x^2-x+1} \\ \underline{-(x^2-x)} \\ 0+1 \end{array}$$

The remainder is 1.

- 9. Correct Option: D**

Explanation:

Consider $x_1 = 3, y_1 = 4, x_2 = -1, y_2 = 2, x_3 = -2, y_3 = 3$

$$\text{Area of the triangle} = \frac{1}{2} |3(2-3) - 1(3-4) - 2(4-2)|$$

$$= \frac{1}{2} |3(-1) - 1(-1) - 2 \times 2| = 3$$

10. Correct Option: A

Explanation:

$$\text{Distance Formula} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \sqrt{(0 - a)^2 + (b - 0)^2} = \sqrt{a^2 + b^2}$$

- 11.** If the distance between the points A (4, p) and B (1, 0) is 5, then the value(s) of p is/are $\boxed{\pm 4}$.

Explanation:

$$AB = 5$$

$$\therefore AB^2 = 25$$

$$\therefore (4 - 1)^2 + (p - 0)^2 = 25$$

$$\therefore 9 + p^2 = 25$$

$$\therefore p^2 = 16$$

$$\therefore p = \pm 4$$

- 12.** The cost of a table is 3 times the cost of a chair. The total cost of 4 chairs and a table is Rs. 2100, then the cost of a table is equal to Rs. 900.

Explanation:

Let the cost of the table be Rs. x and the cost of the chair be Rs. y.

$$x = 3y$$

$$x + 4y = 2100$$

$$\Rightarrow 7y = 2100$$

$$\Rightarrow y = 300$$

$$x = 3(300) = 900$$

Therefore the cost of a table is Rs. 900.

OR

The solution of a quadratic equation $x^2 + x - 2 = 0$ is equal to $x = 1, -2$.

Explanation:

$$x^2 + x - 2 = 0$$

$$\Rightarrow x^2 + 2x - x - 2 = 0$$

$$\Rightarrow (x + 2)(x - 1) = 0$$

$$\Rightarrow (x + 2) = 0 \text{ or } (x - 1) = 0$$

$$\Rightarrow x = -2, 1$$

13. If $\cot A = \frac{4}{5}$, then $\frac{\sin A + \cos A}{\sin A - \cos A} = \boxed{9}$.

Explanation:

$$\frac{\sin A + \cos A}{\sin A - \cos A} = \frac{1 + \frac{\cos A}{\sin A}}{1 - \frac{\cos A}{\sin A}} = \frac{1 + \frac{4}{5}}{1 - \frac{4}{5}} = \frac{\frac{9}{5}}{\frac{1}{5}} = 9$$

14. If A and B are acute angles such that $\sin A = \cos B$, then $A + B = \underline{90^\circ}$.

Explanation:

$$\sin A = \cos B \text{ ...Given}$$

$$\therefore \sin A = \sin (90^\circ - B) \quad \dots \text{since } \sin (90^\circ - x) = \cos x$$

$$\therefore A = 90^\circ - B$$

$$\therefore A + B = 90^\circ$$

15. In an isosceles triangle ABC, $\angle C = 90^\circ$. If $AB = 8$ cm, then $AC = \underline{4\sqrt{2} \text{ cm}}$.

Explanation:

$\triangle ABC$ is an isosceles right-angled triangle.

$$AC = CB, \text{ non-opposite to } \angle C = 90^\circ$$

By Pythagoras theorem, we get

$$\Rightarrow AB^2 = AC^2 + CB^2$$

$$\Rightarrow 64 = 2AC^2$$

$$\Rightarrow AC = 4\sqrt{2} \text{ cm}$$

16. $\sin 2A = \cos 50^\circ$

$$\Rightarrow \sin 2A = \cos (90^\circ - 40^\circ)$$

$$\Rightarrow \sin 2A = \sin 40^\circ$$

$$\Rightarrow 2A = 40^\circ$$

$$\Rightarrow A = 20^\circ$$

OR

$$\begin{aligned}
& \frac{\sin 75^\circ + \cos 15^\circ}{\sin 75^\circ} \\
&= \frac{\sin 75^\circ + \sin 75^\circ}{\sin 75^\circ} \\
&= \frac{2 \sin 75^\circ}{\sin 75^\circ} \\
&= 2
\end{aligned}$$

17. Diameter of the wheel = 35 cm

$$\begin{aligned}
\text{Circumference of the wheel} &= \pi \times 35 \text{ cm} \\
&= \frac{22}{7} \times 35 = 110 \text{ cm}
\end{aligned}$$

18. The number of face cards is 12, and the total number of cards is 52.

$$\text{The probability of getting a face card is } \frac{12}{52} = \frac{3}{13}$$

$$\text{Probability of getting a non-face card} = 1 - \frac{3}{13} = \frac{10}{13}$$

19. If two triangles are similar, then their corresponding sides are proportional.

$$\frac{AB}{XY} = \frac{BC}{YZ}$$

$$\frac{11}{7} = \frac{22}{YZ}$$

$$YZ = 14 \text{ cm}$$

- 20.

$$a = 5, d = 8 - 5 = 3$$

By the n^{th} term formula,

$$a_n = a + (n - 1)d$$

$$\text{So, } a_{28} = 5 + (28 - 1)3 = 5 + 81 = 86$$

Section B

- 21.

Total number of possible outcomes of an experiment is 15.

The numbers which are divisible by 4 are 4, 8, 12 (i.e. 3).

$$\text{Required probability} = \frac{3}{15} = \frac{1}{5}$$

22.

Total number of bulbs is $5 + 6 = 11$.

Working bulbs is 6.

$$\text{Required probability} = \frac{6}{11}$$

OR

Since the first card drawn is a king.

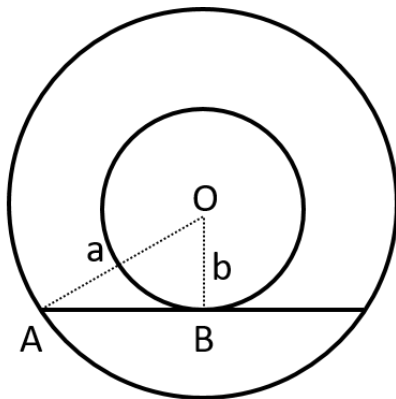
\therefore There are 4 remaining cards and there are no remaining kings.

$$n(\text{total outcomes}) = 5$$

$$n(\text{favourable outcomes}) = 0$$

$$P(\text{second card is a king}) = \frac{0}{5} = 0$$

23.



It is given that $a > b$,

AB is the tangent to the smaller circle,

$OB \perp AB$ (tangent \perp radius)

So $\triangle ABO$ is a right angled triangle

$$\therefore AO^2 = AB^2 + BO^2$$

$$\therefore AB = \sqrt{a^2 - b^2}$$

Now we know that the perpendicular drawn from the center to a chord bisects the chord.

$$\text{So, the length of chord will be } 2AB = 2\sqrt{a^2 - b^2}$$

24.

Using $(a + b)^2 = a^2 + 2ab + b^2$ & $(a - b)^2 = a^2 - 2ab + b^2$, we get

$$(\sin A + \cos A)^2 + (\sin A - \cos A)^2$$

$$= \sin^2 A + 2\sin A \cos A + \cos^2 A + \sin^2 A - 2\sin A \cos A + \cos^2 A$$

$$= 2(\sin^2 A + \cos^2 A)$$

$$= 2 \quad \dots \quad \because \sin^2 A + \cos^2 A = 1$$

OR

We know that, $\tan 30^\circ = \frac{1}{\sqrt{3}}$

$$\frac{2 \tan 30^\circ}{1 + \tan^2 30^\circ} = \frac{2 \times \frac{1}{\sqrt{3}}}{1 + \left(\frac{1}{\sqrt{3}}\right)^2} = \frac{\frac{2}{\sqrt{3}}}{1 + \frac{1}{3}} = \frac{2}{\sqrt{3}} \times \frac{3}{4} = \frac{\sqrt{3}}{2}$$

25.

Let the breadth of the rectangle be x cm.

Length of the rectangle is $2x$ cm.

Area of the rectangle = Perimeter of the rectangle

$$2x^2 = 2(x + 2x)$$

$$2x^2 = 6x$$

$$x^2 = 3x$$

$$x(x - 3) = 0$$

$x \neq 0$; hence, $x = 3$.

Therefore, breadth of the rectangle is 3 cm.

26.

Degree	Name of the polynomial	Form of the polynomial
0	Constant Polynomial	$f(x) = a$, a is a constant
1	Linear Polynomial	$f(x) = ax + b$, $a \neq 0$
2	Quadratic Polynomial	$f(x) = ax^2 + bx + c$, $a \neq 0$
3	Cubic Polynomial	$f(x) = ax^3 + bx^2 + cx + d$, $a \neq 0$

Section C

27.

Let α and β be the zeros of the polynomial $2x^3 - 4x - x^2 + 2$, where $\alpha = \sqrt{2}$ and $\beta = -\sqrt{2}$

$$\therefore \alpha + \beta = 0 \text{ and } \alpha\beta = -2$$

A polynomial whose roots are α and β is given by $x^2 - (\alpha + \beta)x + \alpha\beta$

$$= x^2 - 0 \times x - 2$$

$$= x^2 - 2$$

Divide $2x^3 - 4x - x^2 + 2$ by $x^2 - 2$

$$\begin{array}{r} \overline{2x - 1} \\ x^2 - 2 \overline{) 2x^3 - x^2 - 4x + 2} \\ \underline{2x^3 - 4x} \\ 0 - x^2 \\ \underline{- x^2 } \\ 0 \end{array}$$

$$\therefore 2x^3 - 4x - x^2 + 2 = (x^2 - 2)(2x - 1)$$

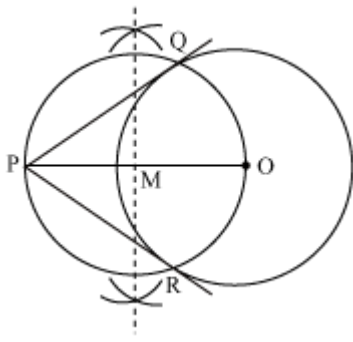
Hence, the third zero is $\frac{1}{2}$.

28.

The steps of construction are as follows:

- a. Taking any point O on the given plane as centre draw a circle of 6 cm radius. Locate a point P, 10 cm away from O. Join OP.
- b. Bisect OP. Let M be the midpoint of PO.
- c. Taking M as centre and MO as radius, draw a circle.
- d. Let this circle intersect the circle drawn previously at points Q and R.
- e. Join PQ and PR. PQ and PR are the required tangents.

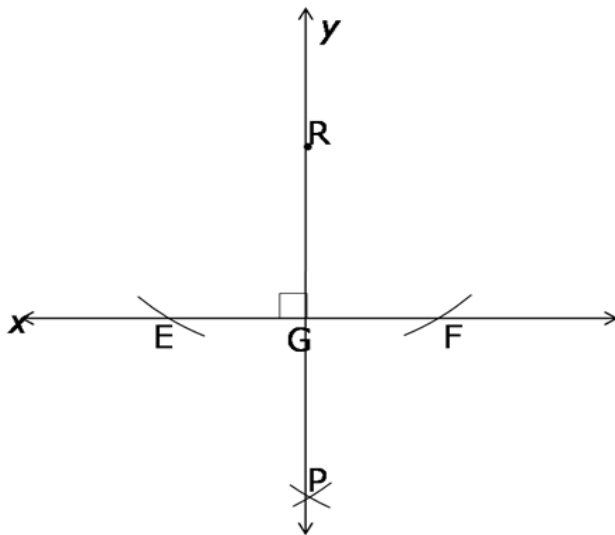
The length of tangents PQ and PR is 8 cm each.



OR

Steps of construction:

1. Draw line x . Take a point R outside the line.
2. Taking R as the centre, draw two arcs of circle cutting line x at points E and F .
3. Taking E and F as centres and the radius more than half of EF , draw two arcs one from each point intersecting each other at P below the line x and opposite to point R .
4. Draw the line y passing through points P and R .
Hence, line $y \perp$ line x passing through point R .



29.

Since the diameter of the marble is 1.4 cm, radius $r = \frac{1.4}{2} = 0.7$ cm

$$\therefore \text{Volume of a marble, } V_{\text{marble}} = \frac{4}{3} \times \pi \times r^3 = \frac{4}{3} \times \pi \times (0.7)^3 \text{ cm}^3$$

Level of water in the cylinder = H = 5.6 cm

$$\text{Radius of cylinder} = R = \frac{7}{2} = 3.5 \text{ cm}$$

\therefore Volume of the water increased in the cylinder,

$$V_{\text{water increased}} = \pi \times R^2 \times H = \pi \times (3.5)^2 \times 5.6$$

$$\text{Thus, the number of marbles} = \frac{V_{\text{water increased}}}{V_{\text{marble}}}$$

$$= \frac{\pi \times (3.5)^2 \times 5.6}{\frac{4}{3} \times \pi \times (0.7)^3}$$

$$= 3 \times 5 \times 5 \times 2$$

$$= 150$$

30.

$$\text{L.H.S} = \frac{\sin A - \sin B}{\cos A + \cos B} + \frac{\cos A - \cos B}{\sin A + \sin B}$$

$$= \frac{(\sin A - \sin B)(\sin A + \sin B) + (\cos A - \cos B)(\cos A + \cos B)}{(\cos A + \cos B)(\sin A + \sin B)}$$

$$= \frac{\sin^2 A - \sin^2 B + \cos^2 A - \cos^2 B}{(\cos A + \cos B)(\sin A + \sin B)}$$

$$= \frac{\sin^2 A + \cos^2 A - (\sin^2 B + \cos^2 B)}{(\cos A + \cos B)(\sin A + \sin B)}$$

$$= \frac{1 - 1}{(\cos A + \cos B)(\sin A + \sin B)} = 0 = \text{R. H. S}$$

Hence proved.

OR

i.

$$\tan 1^\circ \tan 2^\circ \tan 3^\circ \dots \tan 89^\circ$$

$$= (\tan 1^\circ \tan 89^\circ) (\tan 2^\circ \tan 88^\circ) (\tan 3^\circ \tan 87^\circ) \dots \tan 45^\circ$$

$$= (\cot 89^\circ \tan 89^\circ) (\cot 88^\circ \tan 88^\circ) (\cot 87^\circ \tan 87^\circ) \dots \times 1$$

$$\because \tan (90 - x) = \cot x \text{ and } \tan 45^\circ = 1$$

$$= 1 \times 1 \times 1 \dots \times 1$$

$$= 1$$

ii.

$$\sin^2 45^\circ - \tan^2 60^\circ + \cos^2 90^\circ$$

$$= \left(\frac{1}{\sqrt{2}} \right)^2 - (\sqrt{3})^2 + 0$$

$$= \frac{1}{2} - 3$$

$$= \frac{-5}{2}$$

31. In the given pair, $963 > 657$, thus let $963 = a$ and $657 = b$.

Now by applying Euclid's division algorithm $a = bq + r$, we get

$$963 = 657 \times 1 + 306$$

$$657 = 306 \times 2 + 45$$

$$306 = 45 \times 6 + 36$$

$$45 = 36 \times 1 + \underline{9}$$

$$36 = 9 \times 4 + 0$$

Since in the above equation we get $r = 0$; therefore, 9 is the HCF of the given pair 963 and 657.

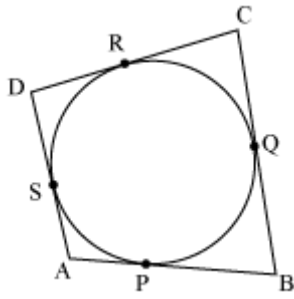
OR

$$\frac{129}{2^2 \times 5^7} = \frac{129}{312500}$$

$$\begin{array}{r} \\ 312500 \overline{) 1290000.00} \\ \underline{-1250000} \\ 400000 \\ \underline{-312500} \\ 875000 \\ \underline{-625000} \\ 2500000 \\ \underline{-2500000} \\ 0000 \end{array}$$

$$\text{Hence, } \frac{129}{2^2 \times 5^7} = 0.0004128$$

32.



It can be observed that:

$$DR = DS \quad (\text{tangents from point D})$$

$$CR = CQ \quad (\text{tangents from point C})$$

$$BP = BQ \quad (\text{tangents from point B})$$

$$AP = AS \quad (\text{tangents from point A})$$

Adding the above four equations,

$$DR + CR + BP + AP = DS + CQ + BQ + AS$$

$$(DR + CR) + (BP + AP) = (DS + AS) + (CQ + BQ)$$

$$CD + AB = AD + BC$$

33.

$$\text{i. } AB = \sqrt{(6-3)^2 + (7-4)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$BC = \sqrt{(9-6)^2 + (4-7)^2} = \sqrt{9+9} = \sqrt{18} = 3\sqrt{2}$$

$$AC = \sqrt{(9-3)^2 + (4-4)^2} = \sqrt{36} = 6$$

$$\text{Since, } AB = BC = 3\sqrt{2}$$

Therefore, the three students A, B and C forms an isosceles triangle.

ii.

$$\begin{aligned} \text{Area of a } \Delta ABC &= \frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)| \\ &= \frac{1}{2} \times |3(7-4) + 6(4-4) + 9(4-7)| \\ &= \frac{1}{2} \times |3 \times 3 + 0 + 9 \times -3| \\ &= \frac{1}{2} \times |-18| \\ &= 9 \end{aligned}$$

34.

$$0.2x + 0.3y = 1.3 \quad \dots (i)$$

$$0.4x + 0.5y = 2.3 \quad \dots (ii)$$

From equation (i), we obtain:

$$x = \frac{1.3 - 0.3y}{0.2} \quad \dots (iii)$$

Substituting this value in equation (ii), we obtain:

$$0.4 \left(\frac{1.3 - 0.3y}{0.2} \right) + 0.5y = 2.3$$

$$2.6 - 0.6y + 0.5y = 2.3$$

$$2.6 - 2.3 = 0.1y$$

$$0.3 = 0.1y$$

$$y = 3$$

Substituting the value of y in equation (iii), we obtain:

$$x = \frac{1.3 - 0.3 \times 3}{0.2} = \frac{1.3 - 0.9}{0.2} = \frac{0.4}{0.2} = 2$$

$$\therefore x = 2, y = 3$$

Section D

35.

Let the base of the right triangle be x cm.

Its altitude = $(x - 7)$ cm

From pythagoras theorem,

$$\text{Base}^2 + \text{Altitude}^2 = \text{Hypotenuse}^2$$

$$\therefore x^2 + (x - 7)^2 = 13^2$$

$$\Rightarrow x^2 + x^2 + 49 - 14x = 169$$

$$\Rightarrow 2x^2 - 14x - 120 = 0$$

$$\Rightarrow x^2 - 7x - 60 = 0$$

$$\Rightarrow x^2 - 12x + 5x - 60 = 0$$

$$\Rightarrow x(x - 12) + 5(x - 12) = 0$$

$$\Rightarrow (x - 12)(x + 5) = 0$$

Either $x - 12 = 0$ or $x + 5 = 0$, i.e., $x = 12$ or $x = -5$

Since sides are positive, x can only be 12.

Therefore, the base of the given triangle is 12 cm and the altitude of this triangle will be $(12 - 7)$ cm = 5 cm.

36. The sum of the first n terms of an AP is given by

$$S_n = \frac{n}{2}[2a + (n - 1)d]$$

$$S_{12} = \frac{12}{2}[2a + (12 - 1)d] = 12a + 66d \quad \dots (i)$$

$$S_8 = \frac{8}{2}[2a + (8 - 1)d] = 8a + 28d \quad \dots (ii)$$

$$S_4 = \frac{4}{2}[2a + (4 - 1)d] = 4a + 6d \quad \dots (iii)$$

To prove that $S_{12} = 3(S_8 - S_4)$

$$\text{RHS} = 3(S_8 - S_4)$$

$$= 3[(8a + 28d) - (4a + 6d)] \quad \dots \text{from (ii) and (iii)}$$

$$= 3(4a + 22d)$$

$$= 12a + 66d$$

$$= S_{12} \quad \dots \text{from (i)}$$

$$= \text{LHS}$$

Hence proved.

OR

11, 8, 5, 2, ...

First term (a) = 11

Common difference (d) = $a_n - (a_{n-1}) = 8 - 11 = -3$

Suppose that -150 is the n^{th} term of the given AP.

$$\Rightarrow a_n = -150$$

$$\Rightarrow a + (n - 1)d = -150$$

$$\Rightarrow 11 + (n - 1)(-3) = -150$$

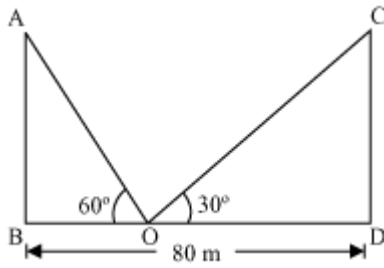
$$\Rightarrow 11 - 3n + 3 = -150$$

$$\Rightarrow -3n = -150 - 14$$

$$\Rightarrow n = \frac{-164}{-3} = \frac{164}{3}$$

Since n is not a natural number, therefore -150 is not a term of the given AP.

37.



Let AB and CD be the poles and O is the point on the road.

In $\triangle ABO$,

$$\frac{AB}{BO} = \tan 60^\circ$$

$$\frac{AB}{BO} = \sqrt{3}$$

$$BO = \frac{AB}{\sqrt{3}} \quad \dots (i)$$

In $\triangle CDO$,

$$\frac{CD}{DO} = \tan 30^\circ$$

$$\frac{CD}{80 - BO} = \frac{1}{\sqrt{3}}$$

$$CD\sqrt{3} = 80 - BO$$

$$CD\sqrt{3} = 80 - \frac{AB}{\sqrt{3}} \quad [\text{From (i)}]$$

$$CD\sqrt{3} + \frac{AB}{\sqrt{3}} = 80$$

$$CD \left[\sqrt{3} + \frac{1}{\sqrt{3}} \right] = 80 \quad (\text{Since, } AB = CD)$$

$$CD \left(\frac{3 + 1}{\sqrt{3}} \right) = 80$$

$$CD = 20\sqrt{3}$$

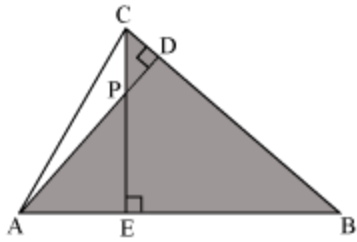
$$BO = \frac{AB}{\sqrt{3}} = \frac{CD}{\sqrt{3}} = \frac{20\sqrt{3}}{\sqrt{3}} = 20 \text{ m}$$

$$DO = BD - BO = 80 \text{ m} - 20 \text{ m} = 60 \text{ m}$$

Thus, the height of the poles is $20\sqrt{3}$ m and the point between the poles is 20m and 60 m far from these poles.

38.

(i)



In $\triangle ABD$ and $\triangle CBE$

$$\angle ADB = \angle CEB = 90^\circ$$

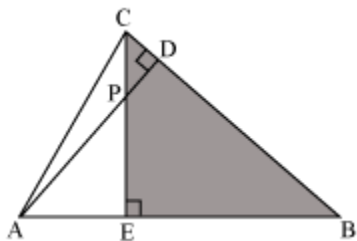
$$\angle ABD = \angle CBE \text{ (common angle)}$$

$$\angle DAB = \angle ECB \text{ (remaining angle)}$$

Therefore by AAA rule

$$\triangle ABD \sim \triangle CBE$$

(ii)



In $\triangle PDC$ and $\triangle BEC$

$$\angle PDC = \angle BEC = 90^\circ$$

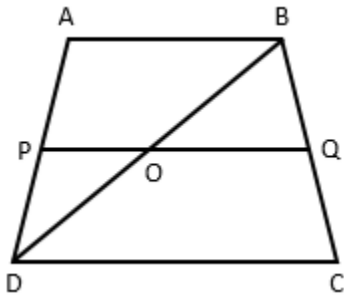
$$\angle PCD = \angle BCE \text{ (common angle)}$$

$$\angle CPD = \angle CBE$$

Therefore by AAA rule

$$\triangle PDC \sim \triangle BEC$$

OR



$AB \parallel DC$ and $PQ \parallel DC$

Hence, $AB \parallel PQ \parallel DC$

In $\triangle ABD$,

$PQ \parallel AB$

$\therefore PO \parallel AB$

$$\frac{DP}{PA} = \frac{DO}{OB} \dots (i) \because \text{BPT}$$

In $\triangle BDC$,

$PQ \parallel DC$

$\therefore OQ \parallel DC$

$$\frac{DO}{OB} = \frac{CQ}{QB} \dots (ii) \because \text{BPT}$$

$$\frac{DP}{PA} = \frac{CQ}{QB} \text{ from (i) and (ii)}$$

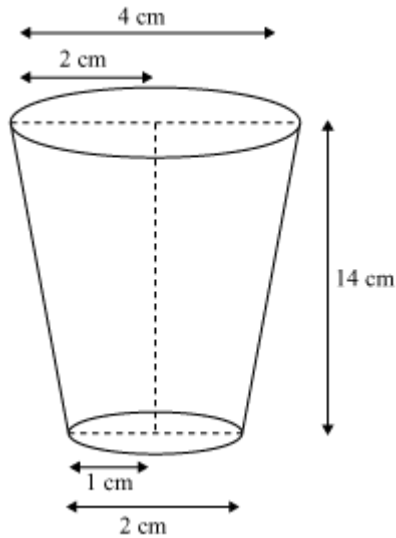
$PD = 18 \text{ cm}$, $BQ = 35 \text{ cm}$ and $QC = 15 \text{ cm}$

$$\therefore \frac{18}{PA} = \frac{15}{35}$$

$$\therefore PA = \frac{18 \times 35}{15}$$

$$\therefore PA = 42 \text{ cm.}$$

39.



$$\text{Radius } (r_1) \text{ of upper base of glass} = \frac{4}{2} = 2 \text{ cm}$$

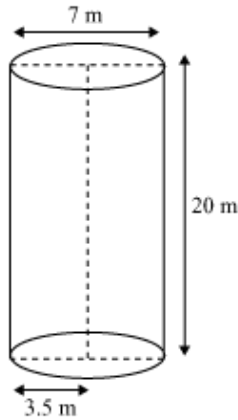
$$\text{Radius } (r_2) \text{ of lower base of glass} = \frac{2}{2} = 1 \text{ cm}$$

Capacity of glass = Volume of frustum of a cone

$$\begin{aligned} &= \frac{1}{3} \pi h (r_1^2 + r_2^2 + r_1 r_2) \\ &= \frac{1}{3} \pi h [(2)^2 + (1)^2 + (2)(1)] \\ &= \frac{1}{3} \times \frac{22}{7} \times 14 [4 + 1 + 2] \\ &= \frac{308}{3} = 102 \frac{2}{3} \text{ cm}^3 \end{aligned}$$

So, the capacity of the glass is $102 \frac{2}{3} \text{ cm}^3$.

OR



The shape of well will be cylindrical.

Depth (h) of well = 20m and Radius (r) of circular end of well = $\frac{7}{2}$ m

Area of platform = length \times breadth = 22×14 m².

Volume of soil dug from well will be equal to the volume of soil scattered on platform.

Volume of soil from well = volume of soil used to make such platform

$$\pi \times r^2 \times h = \text{Area of platform} \times \text{Height of platform}$$

$$\pi \times \left(\frac{7}{2}\right)^2 \times 20 = 22 \times 14 \times h$$

$$\therefore h = \frac{22}{7} \times \frac{49}{4} \times \frac{20}{22 \times 14} = \frac{5}{2} \text{ m}$$

$$\therefore \text{Height of the platform} = 2.5 \text{ m}$$

So, height of such platform will be 2.5m.

40.

Monthly consumption (in units)	Number of consumers
65 – 85	4
85 – 105	5
105 – 125	13
125 – 145	20
145 – 165	14
165 – 185	8
185 – 205	4

We may find class marks by using the relation

$$\text{Class mark} = \frac{\text{Upper class limit} + \text{lower class limit}}{2}$$

Taking 135 as assumed mean (a) we may find d_i , u_i , $f_i u_i$, according to step deviation method as following

Monthly consumption (in units)	Number of consumers (f_i)	x_i class mark	$d_i = x_i - 135$	$u_i = \frac{d_i}{20}$	$f_i u_i$
65 – 85	4	75	– 60	– 3	– 12
85 – 105	5	95	– 40	– 2	– 10
105 – 125	13	115	– 20	– 1	– 13
125 – 145	20	135	0	0	0
145 – 165	14	155	20	1	14
165 – 185	8	175	40	2	16
185 – 205	4	195	60	3	12
Total	68				7

From the table we may observe that

$$\sum f_i u_i = 7$$

$$\sum f_i = 68$$

$$\text{Class size } (h) = 20$$

$$\begin{aligned} \text{Mean } \bar{x} &= a + \left(\frac{\sum f_i u_i}{\sum f_i} \right) \times h \\ &= 135 + \frac{7}{68} \times 20 \\ &= 135 + \frac{140}{68} \\ &= 137.058 \end{aligned}$$

Now from table it is clear that maximum class frequency is 20 belonging to class interval 125 – 145.

Modal class = 125 – 145

Lower limit (l) of modal class = 125

Class size (h) = 20

Frequency (f_1) of modal class = 20

Frequency (f_0) of class preceding modal class = 13

Frequency (f_2) of class succeeding the modal class = 14

$$\begin{aligned}\text{Mode} &= l + \left(\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right) \times h \\ &= 125 + \left[\frac{20 - 13}{2(20) - 13 - 14} \right] \times 20 \\ &= 125 + \frac{7}{13} \times 20 \\ &= 125 + \frac{140}{13} = 135.76\end{aligned}$$

We know that

3 median = mode + 2 mean

$$= 135.76 + 2 (137.058)$$

$$= 135.76 + 274.116$$

$$= 409.876$$

Median = 136.625

So median, mode and mean of the given data are 136.625, 135.76 and 137.05 respectively.