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Kushagra, Siddharth, Harshit

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1 Combinatorial optimization

1.1 Max bipartite matchine

```
}
return false;

int BipartiteMatching(const VVI &w, VI &mr, VI &mc) {
    mr = VI(w.size(), -1);
    mc = VI(w[0].size(), -1);

int ct = 0;
    for (int i = 0; i < w.size(); i++) {
        VI seen(w[0].size());
        if (FindMatch(i, w, mr, mc, seen)) ct++;
    }
    return ct;
}
</pre>
```

2 Geometry

2.1 Convex hull

```
#include <bits/stdc++.h>
using namespace std;
#define 11 long long
#define ld long double
struct Point {
        ld x, y;
        bool operator < (const Point &p) const {</pre>
                 return x < p.x | | (x == p.x \&\& y < p.y);
} ;
ld cross(const Point &O, const Point &A, const Point &B)
        return (A.x - 0.x) * (B.y - 0.y) - (A.y - 0.y) * (B.x - 0.x);
vector<Point> convex_hull(vector<Point> P)
        int n = P.size();
        int k = 0;
        vector<Point> H(2*n);
        sort(P.begin(), P.end());
        for (int i=0; i<n; i++)</pre>
                 while (k \ge 2 \&\& cross(H[k-2], H[k-1], P[i]) \le 0) k--;
                 H[k++] = P[i];
        for (int i=n-2, t = k+1; i>=0; i--)
                 while (k \ge t \&\& cross(H[k-2], H[k-1], P[i]) \le 0) k--;
                 H[k++] = P[i];
        H.resize(k-1);
        return H;
int main()
        ios_base::sync_with_stdio(false);
        return 0;
```

2.2 Miscellaneous geometry

```
// C++ routines for computational geometry.
#include <iostream>
#include <vector>
#include <cmath>
#include <cassert>
using namespace std;
double INF = 1e100;
double EPS = 1e-12;
struct PT {
  double x, y;
  PT() {}
  PT (double x, double y) : x(x), y(y) {}
  PT (const PT &p) : x(p.x), y(p.y)
  PT operator + (const PT &p)
                                 const
                                       { return PT(x+p.x, y+p.y);
  PT operator - (const PT &p)
PT operator * (double c)
                                       { return PT(x-p.x, y-p.y);
                                 const
                                         return PT(x*c,
                                 const
                                                            V*C
  PT operator / (double c)
                                 const { return PT(x/c,
                                                            y/c
                             { return p.x*q.x+p.y*q.y; }
double dot (PT p, PT q)
double dist2(PT p, PT q)
double cross(PT p, PT q)
                             { return dot(p-q,p-q); }
                           { return p.x*q.y-p.y*q.x; }
ostream & operator << (ostream & os, const PT & p) {
  os << "(" << p.x << "," << p.y << ")";
// rotate a point CCW or CW around the origin
PT RotateCCW90(PT p) { return PT(-p.y,p.x);
                       { return PT(-p.y,p.x); }
PT RotateCW90 (PT p)
                        { return PT(p.y,-p.x); }
PT RotateCCW(PT p, double t) {
  return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t));
// project point c onto line through a and b // assuming a !=\ b
PT ProjectPointLine(PT a, PT b, PT c) {
  return a + (b-a) *dot (c-a, b-a) /dot (b-a, b-a);
// project point c onto line segment through a and b
PT ProjectPointSegment (PT a, PT b, PT c) {
  double r = dot(b-a, b-a);
  if (fabs(r) < EPS) return a;</pre>
  r = dot(c-a, b-a)/r;
  if (r < 0) return a;</pre>
  if (r > 1) return b;
  return a + (b-a) *r;
// compute distance from c to segment between a and b
double DistancePointSegment(PT a, PT b, PT c) {
  return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
// compute distance between point (x,y,z) and plane ax+by+cz=d
return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
// determine if lines from a to b and c to d are parallel or collinear
bool LinesParallel(PT a, PT b, PT c, PT d) {
  return fabs(cross(b-a, c-d)) < EPS;
bool LinesCollinear(PT a, PT b, PT c, PT d) {
  return LinesParallel(a, b, c, d)
      && fabs(cross(a-b, a-c)) < EPS
```

```
&& fabs(cross(c-d, c-a)) < EPS;
}
  ^\prime determine if line segment from a to b intersects with
// line segment from c to d
bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
  if (LinesCollinear(a, b, c, d)) {
    if (dist2(a, c) < EPS || dist2(a, d) < EPS ||</pre>
      dist2(b, c) < EPS || dist2(b, d) < EPS) return true;
    if (dot(c-a, c-b) > 0 \&\& dot(d-a, d-b) > 0 \&\& dot(c-b, d-b) > 0)
      return false;
    return true;
     (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
  if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
  return true;
// compute intersection of line passing through a and b
// with line passing through c and d, assuming that unique
// intersection exists; for segment intersection, check if
  ^{\prime} segments intersect first
PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
  b=b-a; d=c-d; c=c-a;
  assert (dot (b, b) > EPS && dot (d, d) > EPS);
  return a + b*cross(c, d)/cross(b, d);
// compute center of circle given three points
PT ComputeCircleCenter(PT a, PT b, PT c) {
  b = (a+b)/2;
  c = (a + c) / 2;
  return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+RotateCW90(a-c));
// determine if point is in a possibly non-convex polygon (by William
// Randolph Franklin); returns 1 for strictly interior points, 0 for
// strictly exterior points, and 0 or 1 for the remaining points.
// Note that it is possible to convert this into an *exact* test using
// integer arithmetic by taking care of the division appropriately
// (making sure to deal with signs properly) and then by writing exact // tests for checking point on polygon boundary
bool PointInPolygon(const vector<PT> &p, PT q) {
  bool c = 0;
  for (int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1) %p.size();
    if ((p[i].y <= q.y && q.y < p[j].y ||</pre>
      p[j].y \le q.y \&\& q.y < p[i].y) \&\&
      q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y))
  return c;
// determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector<PT> &p, PT q) {
  for (int i = 0; i < p.size(); i++)</pre>
    if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q) < EPS)
      return true;
    return false;
// compute intersection of line through points a and b with
// circle centered at c with radius r > 0
vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
  vector<PT> ret;
  b = b-a;
a = a-c;
  double A = dot(b, b);
  double B = dot(a, b);
  double C = dot(a, a) - r*r;
  double D = B*B - A*C;
  if (D < -EPS) return ret;</pre>
  ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
```

```
if (D > EPS)
    ret.push_back(c+a+b*(-B-sqrt(D))/A);
  return ret;
// compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
  vector<PT> ret;
  double d = sqrt(dist2(a, b));
  if (d > r+R \mid | d+min(r, R) < max(r, R)) return ret;
  double x = (d*d-R*R+r*r)/(2*d);
  double y = sqrt(r*r-x*x);
  PT v = (b-a)/d;
  ret.push_back(a+v*x + RotateCCW90(v)*y);
  if (y > 0)
    ret.push back(a+v*x - RotateCCW90(v)*y);
  return ret;
// This code computes the area or centroid of a (possibly nonconvex)
// polygon, assuming that the coordinates are listed in a clockwise or
// counterclockwise fashion. Note that the centroid is often known as
// the "center of gravity" or "center of mass".
double ComputeSignedArea(const vector<PT> &p) {
  double area = 0;
  for(int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1) % p.size();
    area += p[i].x*p[j].y - p[j].x*p[i].y;
  return area / 2.0;
double ComputeArea(const vector<PT> &p) {
  return fabs(ComputeSignedArea(p));
PT ComputeCentroid(const vector<PT> &p) {
  PT c(0,0);
  double scale = 6.0 * ComputeSignedArea(p);
  for (int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1) % p.size();
    c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
  return c / scale;
// tests whether or not a given polygon (in CW or CCW order) is simple
bool IsSimple(const vector<PT> &p) {
  for (int i = 0; i < p.size(); i++)
    for (int k = i+1; k < p.size(); k++) {
      int j = (i+1) % p.size();
      int \bar{1} = (k+1) % p.size();
      if (i == 1 \mid | j == k) continue;
      if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
        return false;
  return true;
int main() {
  // expected: (-5,2)
  cerr << RotateCCW90(PT(2,5)) << endl;</pre>
  // expected: (5,-2)
  cerr << RotateCW90(PT(2,5)) << endl;</pre>
  // expected: (-5,2)
  cerr << RotateCCW(PT(2,5),M_PI/2) << endl;</pre>
  // expected: (5,2)
  cerr << ProjectPointLine(PT(-5,-2), PT(10,4), PT(3,7)) << endl;</pre>
  // expected: (5,2) (7.5,3) (2.5,1)
```

```
cerr << ProjectPointSegment(PT(-5,-2), PT(10,4), PT(3,7)) << " "</pre>
      << ProjectPointSegment(PT(7.5,3), PT(10,4), PT(3,7)) << " "
      << ProjectPointSegment(PT(-5,-2), PT(2.5,1), PT(3,7)) << endl;</pre>
// expected: 6.78903
cerr << DistancePointPlane(4,-4,3,2,-2,5,-8) << endl;
// expected: 1 0 1
cerr << LinesParallel(PT(1,1), PT(3,5), PT(2,1), PT(4,5)) << " "</pre>
      << LinesParallel(PT(1,1), PT(3,5), PT(2,0), PT(4,5)) << " "</pre>
      << LinesParallel(PT(1,1), PT(3,5), PT(5,9), PT(7,13)) << endl;
// expected: 0 0 1
// expected: 1 1 1 0
// expected: (1,2)
cerr << ComputeLineIntersection(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << endl;
// expected: (1,1)
cerr << ComputeCircleCenter(PT(-3,4), PT(6,1), PT(4,5)) << endl;</pre>
vector<PT> v;
v.push_back(PT(0,0));
v.push_back(PT(5,0));
v.push_back(PT(5,5));
v.push\_back(PT(0,5));
// expected: 1 1 1 0 0
cerr << PointInPolygon(v, PT(2,2)) << " "</pre>
      << PointInPolygon(v, PT(2,0)) << " "
      << PointInPolygon(v, PT(0,2)) << " "
      << PointInPolygon(v, PT(5,2)) << " "
      << PointInPolygon(v, PT(2,5)) << endl;
// expected: 0 1 1 1 1
cerr << PointOnPolygon(v, PT(2,2)) << " "</pre>
      << PointOnPolygon(v, PT(2,0)) << " "
      << PointOnPolygon(v, PT(0,2)) << " "
      << PointOnPolygon(v, PT(5,2)) << " "
      << PointOnPolygon(v, PT(2,5)) << endl;
   expected: (1,6)
                (5, 4)
                        (4,5)
                blank line
                (4,5) (5,4)
                blank line
                (4,5) (5,4)
vector<PT> u = CircleLineIntersection(PT(0,6), PT(2,6), PT(1,1), 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleLineIntersection(PT(0,9), PT(9,0), PT(1,1), 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
u = CircleCircleIntersection(PT(1,1), PT(10,10), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
u = CircleCircleIntersection(PT(1,1), PT(8,8), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 10, sqrt(2.0)/2.0);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr <math><< endl;
u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 5, sqrt(2.0)/2.0);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; <math>cerr << endl;
// area should be 5.0
// centroid should be (1.1666666, 1.166666)
PT pa[] = { PT(0,0), PT(5,0), PT(1,1), PT(0,5) };
vector<PT> p(pa, pa+4);
PT c = ComputeCentroid(p);
cerr << "Area: " << ComputeArea(p) << endl;</pre>
cerr << "Centroid: " << c << endl;</pre>
```

```
return 0;
}
```

3 Numerical algorithms

3.1 Number theory (modular, Chinese remainder, linear Diophantine)

```
// This is a collection of useful code for solving problems that // involve modular linear equations. Note that all of the
// algorithms described here work on nonnegative integers.
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
typedef vector<int> VI;
typedef pair<int, int> PII;
// return a % b (positive value)
int mod(int a, int b) {
         return ((a%b) + b) % b;
// computes gcd(a,b)
int gcd(int a, int b) {
     while (b) { int t = a%b; a = b; b = t; }
     return a;
}
// computes lcm(a,b)
int lcm(int a, int b)
         return a / gcd(a, b) *b;
// (a^b) mod m via successive squaring
int powermod(int a, int b, int m)
         int ret = 1;
         while (b)
                  if (b & 1) ret = mod(ret*a, m);
                  a = mod(a*a, m);
                  b >>= 1;
         return ret;
// returns g = gcd(a, b); finds x, y such that d = ax + by
int extended_euclid(int a, int b, int &x, int &y) {
         int xx = y = 0;
         int yy = x = 1;
         while (b) {
                  int q = a / b;
                  int t = b; b = a%b; a = t;
                  t = xx; xx = x - q*xx; x = t;
                  t = yy; yy = y - q*yy; y = t;
         return a;
// finds all solutions to ax = b (mod n)
VI modular_linear_equation_solver(int a, int b, int n) {
         int x, y;
         VI ret;
         int g = extended_euclid(a, n, x, y);
         if (!(b%g)) {
                  x = mod(x*(b / g), n);
for (int i = 0; i < g; i++)
                           ret.push_back(mod(x + i*(n / g), n));
         }
```

```
return ret;
}
// computes b such that ab = 1 (mod n), returns -1 on failure
int mod_inverse(int a, int n) {
         int x, y;
int g = extended_euclid(a, n, x, y);
         if (g > 1) return -1;
         return mod(x, n);
// Chinese remainder theorem (special case): find z such that
// z % m1 = r1, z % m2 = r2. Here, z is unique modulo M = lcm(m1, m2).
// Return (z, M). On failure, M = -1.
PII chinese_remainder_theorem(int m1, int r1, int m2, int r2) {
         int s, t;
         int g = extended_euclid(m1, m2, s, t);
         if (r1%g != r2%g) return make_pair(0, -1);
         return make_pair(mod(s*r2*m1 + t*r1*m2, m1*m2) / q, m1*m2 / q);
// Chinese remainder theorem: find z such that
// z \% m[i] = r[i] for all i. Note that the solution is // unique modulo M = lcm_i (m[i]). Return (z, M). On
// failure, M = -1. Note that we do not require the a[i]'s
// to be relatively prime.
PII chinese_remainder_theorem(const VI &m, const VI &r) {
         PII ret = make_pair(r[0], m[0]);
         for (int i = 1; i < m.size(); i++) {</pre>
                  ret = chinese_remainder_theorem(ret.second, ret.first, m[i], r[i
                     ]);
                  if (ret.second == -1) break;
         return ret;
// computes x and y such that ax + by = c
// returns whether the solution exists
bool linear_diophantine(int a, int b, int c, int &x, int &y) {
         if (!a && !b)
                  if (c) return false;
                  x = 0; y = 0;
return true;
         if (!a)
                  if (c % b) return false;
                  x = 0; y = c / b; return true;
         if (!b)
                  if (c % a) return false;
                  x = c / a; y = 0;
                  return true;
         int g = gcd(a, b);
         if (c % g) return false;
x = c / g * mod_inverse(a / g, b / g);
         y = (c - a*x) / b;
         return true;
int main() {
    // expected: 2
         cout << gcd(14, 30) << endl;
         // expected: 2 -2 1
         int x, y;
int g = extended_euclid(14, 30, x, y);
cout << g << " " << x << " " << y << endl;</pre>
         // expected: 95 451
         VI sols = modular_linear_equation_solver(14, 30, 100);
```

```
for (int i = 0; i < sols.size(); i++) cout << sols[i] << " ";
    cout << endl;

// expected: 8
    cout << mod_inverse(8, 9) << endl;

// expected: 23 105
    // 11 12

PII ret = chinese_remainder_theorem(VI({ 3, 5, 7 }), VI({ 2, 3, 2 }));
    cout << ret.first << " " << ret.second << endl;
    ret = chinese_remainder_theorem(VI({ 4, 6 }), VI({ 3, 5 }));
    cout << ret.first << " " << ret.second << endl;

// expected: 5 -15
    if (!linear_diophantine(7, 2, 5, x, y)) cout << "ERROR" << endl;
    cout << x << " " << y << endl;
    return 0;
}</pre>
```

3.2 Systems of linear equations, matrix inverse, determinant

```
// Gauss-Jordan elimination with full pivoting.
  Uses:
     (1) solving systems of linear equations (AX=B)
     (2) inverting matrices (AX=I)
     (3) computing determinants of square matrices
   Running time: O(n^3)
   INPUT:
              a[][] = an nxn matrix
              b[][] = an nxm matrix
   OUTPUT:
                     = an nxm matrix (stored in b[][])
              A^{-1} = an \ nxn \ matrix \ (stored in a[][])
              returns determinant of a[][]
#include <iostream>
#include <vector>
#include <cmath>
using namespace std;
const double EPS = 1e-10;
typedef vector<int> VI;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
T GaussJordan (VVT &a, VVT &b) {
  const int n = a.size();
  const int m = b[0].size();
  VI irow(n), icol(n), ipiv(n);
  T \det = 1;
  for (int i = 0; i < n; i++) {</pre>
    int pj = -1, pk = -1;
    for (int j = 0; j < n; j++) if (!ipiv[j])</pre>
      for (int k = 0; k < n; k++) if (!ipiv[k])</pre>
        if (pj == -1 \mid | fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk = k; }
    if (fabs(a[pj][pk]) < EPS) { cerr << "Matrix is singular." << endl; exit(0);</pre>
    ipiv(pk)++;
    swap(a[pj], a[pk]);
swap(b[pj], b[pk]);
    if (pj != pk) det *= -1;
    irow[i] = pj;
    icol[i] = pk;
    T c = 1.0 / a[pk][pk];
    det *= a[pk][pk];
    a[pk][pk] = 1.0;
```

```
for (int p = 0; p < n; p++) a[pk][p] *= c;</pre>
    for (int p = 0; p < m; p++) b[pk][p] *= c;
     for (int p = 0; p < n; p++) if (p != pk) {
       c = a[p][pk];
       a[p][pk] = 0;
       for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
       for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
  }
  for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
    for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
  return det;
int main() {
  const int n = 4;
  const int m = 2;
  double A[n][n] = \{ \{1,2,3,4\}, \{1,0,1,0\}, \{5,3,2,4\}, \{6,1,4,6\} \}; double B[n][m] = \{ \{1,2\}, \{4,3\}, \{5,6\}, \{8,7\} \};
  VVT a(n), b(n);
  for (int i = 0; i < n; i++) {
    a[i] = VT(A[i], A[i] + n);
    b[i] = VT(B[i], B[i] + m);
  double det = GaussJordan(a, b);
  // expected: 60
  cout << "Determinant: " << det << endl;</pre>
  // expected: -0.233333 0.166667 0.133333 0.0666667
                  0.166667 0.166667 0.333333 -0.333333
  0.233333 0.833333 -0.133333 -0.0666667
                  0.05 - 0.75 - 0.1 0.2
  cout << "Inverse: " << endl;</pre>
  for (int i = 0; i < n; i++) {</pre>
    for (int j = 0; j < n; j++)
  cout << a[i][j] << ' ';</pre>
     cout << end1;</pre>
  }
     expected: 1.63333 1.3
                  -0.166667 0.5
                  2.36667 1.7
  //
                  -1.85 - 1.35
  cout << "Solution: " << endl;</pre>
  for (int i = 0; i < n; i++) {
  for (int j = 0; j < m; j++)
    cout << b[i][j] << ' ';</pre>
    cout << endl;</pre>
  }
```

3.3 Reduced row echelon form, matrix rank

```
// Reduced row echelon form via Gauss-Jordan elimination
// with partial pivoting. This can be used for computing
// the rank of a matrix.
//
// Running time: O(n^3)
//
// INPUT: a[][] = an nxm matrix
//
// OUTPUT: rref[][] = an nxm matrix (stored in a[][])
// returns rank of a[][]

#include <iostream>
#include <vector>
#include <cmath>
```

```
using namespace std;
const double EPSILON = 1e-10;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
int rref(VVT &a) {
  int n = a.size();
  int m = a[0].size();
  int r = 0;
  for (int c = 0; c < m \&\& r < n; c++) {
     int j = r;
for (int i = r + 1; i < n; i++)</pre>
       if (fabs(a[i][c]) > fabs(a[j][c])) j = i;
     if (fabs(a[j][c]) < EPSILON) continue;</pre>
     swap(a[j], a[r]);
     T s = 1.0 / a[r][c];
     for (int j = 0; j < m; j++) a[r][j] *= s;
for (int i = 0; i < n; i++) if (i != r) {</pre>
       T t = a[i][c];
       for (int j = 0; j < m; j++) a[i][j] -= t * a[r][j];</pre>
     <u>r</u>++;
  return r;
int main() {
  const int n = 5, m = 4;
  double A[n][m] = {
    {16, 2, 3, 13},
    },
                      8},
       5, 11, 10,
       9, 7, 6, 12},
4, 14, 15, 1},
     {13, 21,
                21,
                      13}};
  VVT a(n);
  for (int i = 0; i < n; i++)</pre>
     a[i] = VT(A[i], A[i] + m);
  int rank = rref(a);
  // expected: 3
cout << "Rank: " << rank << endl;</pre>
   // expected: 1 0 0 1
                    0
                      1 0 3
                    0 \ 0 \ 1 \ -3
                    0 0 0 3.10862e-15
                    0
                      0 0 2.22045e-15
  cout << "rref: " << endl;</pre>
  for (int i = 0; i < 5; i++) {
  for (int j = 0; j < 4; j++)
    cout << a[i][j] << ' ';</pre>
     cout << endl;</pre>
  }
```

3.4 Fast Fourier transform

```
#include <cassert>
#include <cstdio>
#include <cmath>

struct cpx
{
    cpx(){}
    cpx(double aa):a(aa),b(0){}
    cpx(double aa, double bb):a(aa),b(bb){}
    double a;
    double b;
    double modsq(void) const
```

```
return a * a + b * b;
  cpx bar (void) const
    return cpx(a, -b);
};
cpx operator + (cpx a, cpx b)
  return cpx(a.a + b.a, a.b + b.b);
cpx operator *(cpx a, cpx b)
  return cpx(a.a * b.a - a.b * b.b, a.a * b.b + a.b * b.a);
cpx operator / (cpx a, cpx b)
  cpx r = a * b.bar();
  return cpx(r.a / b.modsq(), r.b / b.modsq());
cpx EXP (double theta)
  return cpx(cos(theta), sin(theta));
const double two_pi = 4 * acos(0);
// in:
            input array
            output array
  out:
// step:
            {SET TO 1} (used internally)
            length of the input/output {MUST BE A POWER OF 2}
  dir:
// dir: either plus or minus one (direction of the FFT) // RESULT: out[k] = \sum_{j=0}^{s} \sin_j x = 1 in[j] * exp(dir * 2pi * i * j * k /
   size)
void FFT(cpx *in, cpx *out, int step, int size, int dir)
  if(size < 1) return;</pre>
  if(size == 1)
    out[0] = in[0];
    return;
  FFT(in, out, step * 2, size / 2, dir);
FFT(in + step, out + size / 2, step * 2, size / 2, dir);
  for(int i = 0; i < size / 2; i++)
    cpx even = out[i];
    cpx odd = out[i + size / 2];
    out[i] = even + EXP(dir * two_pi * i / size) * odd;
    out[i + size / 2] = even + EXP(dir * two_pi * (i + size / 2) / size) * odd;
// Usage:
  f[0...N-1] and g[0...N-1] are numbers
// Want to compute the convolution h, defined by
// h[n] = sum \ of \ f[k]g[n-k] \ (k = 0, ..., N-1).
// Here, the index is cyclic; f[-1] = f[N-1], \ f[-2] = f[N-2], \ etc.
// Let F[0...N-1] be FFT(f), and similarly, define G and H.
// The convolution theorem says H[n] = F[n]G[n] (element-wise product).
// To compute h[] in O(N log ar{	exttt{N}}) time, do the following:
     1. Compute F and G (pass dir = 1 as the argument).
     2. Get H by element-wise multiplying F and G.
     3. Get h by taking the inverse FFT (use dir = -1 as the argument)
         and *dividing by N*. DO NOT FORGET THIS SCALING FACTOR.
int main(void)
  printf("If rows come in identical pairs, then everything works.\n");
```

```
 \begin{array}{l} {\rm cpx} \ {\rm a[8]} \ = \ \{0,\ 1,\ {\rm cpx}(1,3),\ {\rm cpx}(0,5),\ 1,\ 0,\ 2,\ 0\}; \\ {\rm cpx} \ {\rm b[8]} \ = \ \{1,\ {\rm cpx}(0,-2),\ {\rm cpx}(0,1),\ 3,\ -1,\ -3,\ 1,\ -2\}; \\ \end{array} 
cpx A[8];
cpx B[8];
FFT(a, A, 1, 8, 1);
FFT(b, B, 1, 8, 1);
for (int i = 0; i < 8; i++)
  printf("%7.21f%7.21f", A[i].a, A[i].b);
printf("\n");
for (int i = 0; i < 8; i++)
   cpx Ai(0,0);
   for (int j = 0; j < 8; j++)
     Ai = Ai + a[j] * EXP(j * i * two_pi / 8);
  printf("%7.21f%7.21f", Ai.a, Ai.b);
printf("\n");
cpx AB[8];
for(int i = 0; i < 8; i++)
   AB[i] = A[i] * B[i];</pre>
cpx aconvb[8];
FFT (AB, aconvb, 1, 8, -1);
for (int i = 0; i < 8; i++)
   aconvb[i] = aconvb[i] / 8;
for (int i = 0; i < 8; i++)
  printf("%7.21f%7.21f", aconvb[i].a, aconvb[i].b);
printf("\n");
for (int i = 0; i < 8; i++)
   cpx aconvbi(0,0);
   for (int j = 0; j < 8; j++)
     aconvbi = aconvbi + a[j] * b[(8 + i - j) % 8];
  printf("%7.21f%7.21f", aconvbi.a, aconvbi.b);
printf("\n");
return 0;
```

4 Graph algorithms

4.1 Bellman-Ford shortest paths with negative edge weights (C++)

```
// This function runs the Bellman-Ford algorithm for single source
// shortest paths with negative edge weights. The function returns
// false if a negative weight cycle is detected. Otherwise, the
// function returns true and dist[i] is the length of the shortest
// path from start to i.
//
// Running time: O(|V|^3)
//
// INPUT: start, w[i][j] = cost of edge from i to j
// OUTPUT: dist[i] = min weight path from start to i
// prev[i] = previous node on the best path from the
start node

#include <iostream>
#include <queue>
#include <cmath>
```

```
#include <vector>
using namespace std;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
typedef vector<int> VI;
typedef vector<VI> VVI;
bool BellmanFord (const VVT &w, VT &dist, VI &prev, int start) {
  int n = w.size();
  prev = VI(n, -1);
dist = VT(n, 100000000);
  dist[start] = 0;
  for (int k = 0; k < n; k++) {
    for (int i = 0; i < n; i++) {</pre>
       for (int j = 0; j < n; j++) {
  if (dist[j] > dist[i] + w[i][j]) {
           if (k == n-1) return false;
           dist[j] = dist[i] + w[i][j];
           prev[j] = i;
    }
  }
  return true;
```

4.2 Dijkstra and Floyd's algorithm (C++)

```
#include <iostream>
#include <queue>
#include <cmath>
#include <vector>
using namespace std;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
typedef vector<int> VI;
typedef vector<VI> VVI;
// This function runs Dijkstra's algorithm for single source
// shortest paths. No negative cycles allowed!
// Running time: O(|V|^2)
     INPUT:
               start, w[i][j] = cost of edge from i to j
     OUTPUT:
               dist[i] = min weight path from start to i
               prev[i] = previous node on the best path from the
                          start node
void Dijkstra (const VVT &w, VT &dist, VI &prev, int start) {
  int n = w.size();
  VI found (n);
  prev = VI(n, -1);
  dist = VT(n, 1000000000);
  dist[start] = 0;
  while (start !=-1) {
    found[start] = true;
    int best = -1;
    for (int k = 0; k < n; k++) if (!found[k]) {
   if (dist[k] > dist[start] + w[start][k]) {
        dist[k] = dist[start] + w[start][k];
        prev[k] = start;
      if (best == -1 \mid \mid dist[k] < dist[best]) best = k;
```

```
start = best;
// This function runs the Floyd-Warshall algorithm for all-pairs
// shortest paths. Also handles negative edge weights. Returns true // if a negative weight cycle is found.
// Running time: O(|V|^3)
      INPUT: w[i][j] = weight of edge from i to j
OUTPUT: w[i][j] = shortest path from i to j
prev[i][j] = node before j on the best path starting at i
bool FloydWarshall (VVT &w, VVI &prev) {
  int n = w.size();
  prev = VVI (n, VI(n, -1));
  for (int k = 0; k < n; k++) {
     for (int i = 0; i < n; i++) {</pre>
        for (int j = 0; j < n; j++) {
  if (w[i][j] > w[i][k] + w[k][j]) {
             w[i][j] = w[i][k] + w[k][j];
             prev[i][j] = k;
        }
     }
  }
   // check for negative weight cycles
  for (int i=0; i<n; i++)</pre>
     if (w[i][i] < 0) return false;</pre>
  return true;
```

4.3 Fast Dijkstra's algorithm

```
#include <bits/stdc++.h>
using namespace std;
#define INF 0x3f3f3f3f
#define 11 long long
#define pll pair<ll,
#define pb push_back
#define mp make_pair
#define F first
#define S second
const int MAX_SIZE = 1e5+10;
vector< pll > adj[MAX_SIZE];
void create_Edge(int x, int y, ll w)
         adj[x].pb(mp(y, w));
         adj[y].pb(mp(x, w));
void shortestPath(int src)
         priority_queue< pll, vector< pll >, greater< pll > > pq;
vector<ll> dist(MAX_SIZE, INF);
         pq.push(mp(0, src));
dist[src] = 0;
         while(!pq.empty())
                  int u = pq.top().S;
                  pq.pop();
                  for(auto it : adj[u])
```

4.4 Strongly connected components

```
#include<memory.h>
struct edge{int e, nxt;};
int V, E;
edge e[MAXE], er[MAXE];
int sp[MAXV], spr[MAXV];
int group_cnt, group_num[MAXV];
bool v [MAXV];
int stk[MAXV];
void fill forward(int x)
  int i;
  v[x]=true;
  for(i=sp[x];i;i=e[i].nxt) if(!v[e[i].e]) fill_forward(e[i].e);
  stk[++stk[0]]=x;
void fill_backward(int x)
  int i;
  v[x] = false;
  group_num[x]=group_cnt;
  for(i=spr[x];i;i=er[i].nxt) if(v[er[i].e]) fill_backward(er[i].e);
void add_edge(int v1, int v2) //add edge v1->v2
  e [++E].e=v2; e [E].nxt=sp [v1]; sp [v1]=E;
      E].e=v1; er[E].nxt=spr[v2]; spr[v2]=E;
void SCC()
  int i:
  stk[0]=0;
  memset(v, false, sizeof(v));
  for(i=1;i<=V;i++) if(!v[i]) fill_forward(i);</pre>
  group_cnt=0;
  for(i=stk[0];i>=1;i--) if(v[stk[i]]){group_cnt++; fill_backward(stk[i]);}
```

4.5 Eulerian path

```
} ;
const int max_vertices = ;
int num_vertices;
                                       // adjacency list
list<Edge> adj[max_vertices];
vector<int> path;
void find_path(int v)
        while (adj[v].size() > 0)
                int vn = adj[v].front().next_vertex;
                adj[vn].erase(adj[v].front().reverse_edge);
                adj[v].pop_front();
                find_path(vn);
        path.push_back(v);
void add_edge(int a, int b)
        adj[a].push_front(Edge(b));
        iter ita = adj[a].begin();
        adj[b].push_front(Edge(a));
        iter itb = adj[b].begin();
        ita->reverse_edge = itb;
        itb->reverse_edge = ita;
```

4.6 Kruskal's alternative

```
#include<bits/stdc++.h>
using namespace std;
typedef pair<int, int> iPair;
struct Graph{
    int V, E;
    vector< pair<int, iPair> > edges;
    Graph(int V, int E) {
    this->V = V;
        this->E = E;
    void addEdge(int u, int v, int w) {
        edges.push_back({w, {u, v}});
    int kruskalMST();
};
struct DisjointSets{
    int *parent, *rnk;
    int n;
    DisjointSets(int n) {
        this->n = n;
        parent = new int[n+1];
        rnk = new int[n+1];
         for (int i = 0; i <= n; i++) {
             rnk[i] = 0;
             parent[i] = i;
         }
    int find(int u) {
         if (u != parent[u])
             parent[u] = find(parent[u]);
         return parent[u];
    void merge(int x, int y) {
        x = find(x), y = find(y);
if (rnk[x] > rnk[y])
             parent[y] = x;
```

```
parent[x] = y;
            if (rnk[x] == rnk[y])
                  rnk[y]++;
};
int Graph::kruskalMST() {
      int mst_wt = 0; // Initialize result
      sort(edges.begin(), edges.end());
      DisjointSets ds(V);
      vector< pair<int, iPair> >::iterator it;
      for (it=edges.begin(); it!=edges.end(); it++){
            int u = it->second.first;
            int v = it->second.second;
            int set_u = ds.find(u);
            int set_v = ds.find(v);
            if (set_u != set_v) {
    cout << u << " - " << v << endl;</pre>
                  mst wt += it->first;
                  ds.merge(set_u, set_v);
            }
      return mst_wt;
int main(){
      int V = 9, E = 14;
Graph g(V, E);
     g.addEdge(0, 1, 4); g.addEdge(1, 2, 8); g.addEdge(1, 7, 11); g.addEdge(2, 3, 7); g.addEdge(2, 8, 2); g.addEdge(2, 5, 4); g.addEdge(3, 4, 9); g.addEdge(3, 5, 14); g.addEdge(4, 5, 10); g.addEdge(5, 6, 2); g.addEdge(6, 7, 1); g.addEdge(6, 8, 6); g.addEdge(7, 8, 7); g.addEdge(0, 7, 8); cout << "Edges of MST are \n";</pre>
      int mst_wt = g.kruskalMST();
cout << "\nWeight of MST is " << mst_wt;</pre>
      return 0;
```

4.7 Prim alternative

```
#include<bits/stdc++.h>
using namespace std;
# define INF 0x3f3f3f3f
typedef pair<int, int> iPair;
class Graph {
                // No. of vertices
    int V;
    list< pair<int, int> > *adj;
public:
    Graph(int V);
                      // Constructor
    void addEdge(int u, int v, int w);
    void primMST();
};
Graph::Graph(int V) {
    this->\overline{V} = V;
    adj = new list<iPair> [V];
void Graph::addEdge(int u, int v, int w) {
    adj[u].push_back(make_pair(v, w));
    adj[v].push_back(make_pair(u, w));
void Graph::primMST() {
    priority_queue< iPair, vector <iPair> , greater<iPair> > pq;
int src = 0; // Taking vertex 0 as source
vector<int> key(V, INF);
    vector<int> parent(V, -1);
    vector<bool> inMST(V, false);
    pq.push(make_pair(0, src));
    key[src] = 0;
```

```
while (!pq.empty())
         int u = pq.top().second;
         pq.pop();
         inMST[u] = true; // Include vertex in MST
list< pair<int, int> >::iterator i;
         for (i = adj[u].begin(); i != adj[u].end(); ++i)
              int v = (*i).first;
              int weight = (*i).second;
              if (inMST[v] == false && key[v] > weight)
                  key[v] = weight;
                  pq.push(make_pair(key[v], v));
                  parent[v] = u;
              }
         }
    for (int i = 1; i < V; ++i)
         printf("%d - %d\n", parent[i], i);
int main(){
    int V = 9;
    Graph g(V); g.addEdge(0, 1, 4); g.addEdge(0, 7, 8); g.addEdge(1, 2, 8); g.addEdge(1, 7, 11); g.addEdge(2, 3, 7);
    g.addEdge(2, 8, 2);g.addEdge(2, 5, 4);g.addEdge(3, 4, 9);g.addEdge(3, 5, 14);
    g.addEdge(4, 5, 10);
g.addEdge(5, 6, 2);g.addEdge(6, 7, 1);g.addEdge(6, 8, 6);g.addEdge(7, 8, 7);
    q.primMST();
    return 0;
}
```

5 Data structures

5.1 Suffix array

```
// Suffix array construction in O(L log^2 L) time. Routine for // computing the length of the longest common prefix of any two
// suffixes in O(log L) time.
   INPUT:
            string s
            array \ suffix[] \ such that \ suffix[i] = index \ (from 0 to L-1)
   OUTPUT:
            of substring s[i...L-1] in the list of sorted suffixes.
            That is, if we take the inverse of the permutation suffix[],
            we get the actual suffix array.
#include <vector>
#include <iostream>
#include <string>
using namespace std;
struct SuffixArray {
  const int L;
  string s;
  vector<vector<int> > P;
  vector<pair<int,int>,int> > M;
  SuffixArray(const string &s) : L(s.length()), s(s), P(1, vector<int>(L, 0)), M(
     L) {
    for (int i = 0; i < L; i++) P[0][i] = int(s[i]);</pre>
    for (int skip = 1, level = 1; skip < L; skip \star= 2, level++) {
      P.push_back(vector<int>(L, 0));
      for (int i = 0; i < L; i++)
        sort(M.begin(), M.end());
      for (int i = 0; i < L; i++)
```

```
P[level][M[i].second] = (i > 0 && M[i].first == M[i-1].first) ? P[level][
           M[i-1].second] : i;
  }
  vector<int> GetSuffixArray() { return P.back(); }
  // returns the length of the longest common prefix of s[i...L-1] and s[j...L-1]
  int LongestCommonPrefix(int i, int j) {
    int len = 0;
    if (i == j) return L - i;
    for (int k = P.size() - 1; k \ge 0 && i < L && j < L; k--) {
      if (P[k][i] == P[k][j]) {
        i += 1 << k;
        i += 1 << k;
        len += 1 << k;
      }
    return len;
};
  BEGIN CUT
^{\prime}/ The following code solves UVA problem 11512: GATTACA.
#define TESTING
#ifdef TESTING
int main() {
  int T;
  cin >>
  for (int caseno = 0; caseno < T; caseno++) {</pre>
    string s;
    cin > \bar{s};
    SuffixArray array(s);
    vector<int> v = array.GetSuffixArray();
    int bestlen = -1, bestpos = -1, bestcount = 0;
    for (int i = 0; i < s.length(); i++) {</pre>
      int len = 0, count = 0;
      for (int j = i+1; j < s.length(); j++)</pre>
        int l = array.LongestCommonPrefix(i, j);
        if (l >= len) {
          if (1 > len) count = 2; else count++;
          len = 1;
        }
      if (len > bestlen || len == bestlen && s.substr(bestpos, bestlen) > s.
        substr(i, len)) {
bestlen = len;
        bestcount = count;
        bestpos = i;
    if (bestlen == 0) {
      cout << "No repetitions found!" << endl;</pre>
    } else {
      cout << s.substr(bestpos, bestlen) << " " << bestcount << endl;</pre>
  }
}
#else
// END CUT
int main() {
  // bobocel is the O'th suffix
      obocel is the 5'th suffix
       bocel is the 1'st suffix
        ocel
             is the 6'th suffix
         cel is the 2'nd suffix
          el is the 3'rd suffix
           1 is the 4'th suffix
  SuffixArray suffix("bobocel");
  vector<int> v = suffix.GetSuffixArray();
  // Expected output: 0 5 1 6 2 3 4
```

```
for (int i = 0; i < v.size(); i++) cout << v[i] << " ";
cout << endl;
cout << suffix.LongestCommonPrefix(0, 2) << endl;
}
// BEGIN CUT
#endif
// END CUT</pre>
```

5.2 Binary Indexed Tree

```
#include <iostream>
using namespace std;
#define LOGSZ 17
int tree[(1<<LOGSZ)+1];</pre>
int N = (1 << LOGSZ);
// add v to value at x
void set(int x, int v) {
  while (x \le N) {
    tree[x] += v;
    x += (x \& -x);
  }
// get cumulative sum up to and including x
int get(int x) {
  int res = 0;
  while(x) {
  res += tree[x];
    x = (x \& -x);
  return res;
// get largest value with cumulative sum less than or equal to x; // for smallest, pass x-1 and add 1 to result
int getind(int x) {
  int idx = 0, mask = N;
  while (mask && idx < N) {</pre>
    int t = idx + mask;
     if(x >= tree[t]) {
       idx = t;
       x -= tree[t];
    mask >>= 1;
  }
  return idx;
```

5.3 Union-find set

```
#include <iostream>
#include <vector>
using namespace std;
int find(vector<int> &C, int x) { return (C[x] == x) ? x : C[x] = find(C, C[x]);
}
void merge(vector<int> &C, int x, int y) { C[find(C, x)] = find(C, y); }
int main()
{
    int n = 5;
    vector<int> C(n);
    for (int i = 0; i < n; i++) C[i] = i;
    merge(C, 0, 2);
    merge(C, 1, 0);
    merge(C, 3, 4);
    for (int i = 0; i < n; i++) cout << i << " " << find(C, i) << endl;
    return 0;</pre>
```

.

5.4 Lowest common ancestor

```
const int max_nodes, log_max_nodes;
int num_nodes, log_num_nodes, root;
vector<int> children[max_nodes];
                                          // children[i] contains the children of
   node i
// A[i][j] is the 2^j-th ancestor of node
int L[max_nodes];
                                          // L[i] is the distance between node i
   and the root
// floor of the binary logarithm of n
int lb (unsigned int n)
    if(n==0)
        return -1;
    int p = 0;
    if (n >= 1 << 16)
                     \{ n >>= 16; p += 16; 
    if (n >= 1 << 8)
                    \{ n >>= 8; p +=
                                       8;
    if (n >= 1 << 4) { n >>=
                              4; p +=
                                        4; }
    if (n >= 1 << 2) { n >>=
                              2; p +=
                                        2; }
    if (n >= 1<< 1) {
    return p;
void DFS(int i, int 1)
    L[i] = 1;
    for(int j = 0; j < children[i].size(); j++)</pre>
        DFS(children[i][j], l+1);
int LCA(int p, int q)
    // ensure node p is at least as deep as node q
    if(L[p] < L[q])
        swap(p, q);
    // "binary search" for the ancestor of node {
m p} situated on the same level as {
m q}
    for(int i = log_num_nodes; i >= 0; i--)
        if(L[p] - (1 << i)) >= L[q])
            p = A[p][i];
    if(p == q)
        return p;
    // "binary search" for the LCA
    for (int i = log_num_nodes; i >= 0; i--)
   if (A[p][i] != -1 && A[p][i] != A[q][i])
            p = A[p][i];
            q = A[q][i];
    return A[p][0];
int main(int argc,char* argv[])
    // read num_nodes, the total number of nodes
    log_num_nodes=lb(num_nodes);
    for(int i = 0; i < num_nodes; i++)</pre>
        int p;
        // read p, the parent of node i or -1 if node i is the root
        A[i][0] = p;
        if (p != -1)
            children[p].push_back(i);
        else
```

5.5 Sparse Table

```
#include <bits/stdc++.h>
using namespace std;
#define 11 long long
const int MAX_SIZE = 1e5+10;
const int K = 16;
const int ZERO = 0; //define zero according to F
11 arr[MAX_SIZE];
11 Table[MAX_SIZE][K+1];
ll F(ll a, ll b)
{
         return max(a, b);
void buildTable(int n)
         for (int i=0; i<n; i++)</pre>
                  Table[i][0] = arr[i];
         for (int j = 1; j \le K; j++)
                  for (int i=0; i<= n - (1<<j); i++)</pre>
                           Table[i][j] = F(Table[i][j-1], Table[i + (1 << (j-1))][j]
                              -1]);
         }
11 query(int 1, int r)
         11 \text{ answer} = ZERO;
         for (int j=K; j>=0; j--)
                  if (1 + (1 << \dot{\uparrow}) - 1
                                      \leq r
                           answer = F(answer, Table[1][j]);
                  1 += (1 << j);
         }
int main()
         return 0;
```

6 Miscellaneous

6.1 Longest increasing subsequence

```
// Given a list of numbers of length n, this routine extracts a
// longest increasing subsequence.
  Running time: O(n log n)
     INPUT: a vector of integers
     OUTPUT: a vector containing the longest increasing subsequence
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
typedef vector<int> VI;
typedef pair<int, int> PII;
typedef vector<PII> VPII;
#define STRICTLY_INCREASNG
VI LongestIncreasingSubsequence(VI v) {
  VPII best;
  VI dad(v.size(), -1);
  for (int i = 0; i < v.size(); i++) {</pre>
#ifdef STRICTLY_INCREASNG
    PII item = make_pair(v[i], 0);
VPII::iterator it = lower_bound(best.begin(), best.end(), item);
    item.second = i;
    PII item = make_pair(v[i], i);
    VPII::iterator it = upper_bound(best.begin(), best.end(), item);
#endif
    if (it == best.end())
      dad[i] = (best.size() == 0 ? -1 : best.back().second);
      best.push_back(item);
    } else {
      dad[i] = dad[it->second];
      *it = item;
  }
  VI ret;
  for (int i = best.back().second; i >= 0; i = dad[i])
    ret.push_back(v[i]);
  reverse(ret.begin(), ret.end());
  return ret;
```

6.2 Vimrc file

```
set autoindent
set smartindent
set cindent
set shiftwidth=4
set tabstop=4
set autoread
set cmdheight=1
set number
set splitright
set splitbelow
set makeprg=g++\ -std=c++14\ %\ -o\ out
map <F8>:!./out < input > output <ENTER><ENTER>
map <F7< :make \ | cope 8 \ | wincmd J <ENTER><ENTER>
```

```
map <C-Right> <C-W><Right>
map <C-Left> <C-W><Left>
map <C-Up> <C-W><Up>
map <C-Down> <C-W><Down>
only
40vsp input
20vsp output
wincmd w
```

6.3 Topological sort (C++)

```
This function uses performs a non-recursive topological sort.
// Running time: O(|V|^2). If you use adjacency lists (vector<map<int> >),
                   the running time is reduced to O(|E|).
     INPUT:
                w[i][j] = 1 if i should come before j, 0 otherwise
                a permutation of 0, \ldots, n-1 (stored in a vector)
     OUTPUT:
                which represents an ordering of the nodes which
                is consistent with w
// If no ordering is possible, false is returned.
#include <iostream>
#include <queue>
#include <cmath>
#include <vector>
using namespace std;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
typedef vector<int> VI;
typedef vector<VI> VVI;
bool TopologicalSort (const VVI &w, VI &order) {
  int n = w.size();
  VI parents (n);
  queue<int> q;
  order.clear();
  for (int i = 0; i < n; i++) {</pre>
    for (int j = 0; j < n; j++)
  if (w[j][i]) parents[i]++;
  if (parents[i] == 0) q.push (i);</pre>
  while (q.size() > 0) {
    int i = q.front();
    q.pop();
    order.push_back (i);
    for (int j = 0; j < n; j++) if (w[i][j]) {
  parents[j]--;</pre>
       if (parents[j] == 0) q.push (j);
  return (order.size() == n);
```